

Rules for integrands of the form $(d + e x^r)^q (a + b \operatorname{Log}[c x^n])^p$

1: $\int (d + e x^r)^q (a + b \operatorname{Log}[c x^n]) dx$ when $q \in \mathbb{Z}^+$

▪ **Derivation: Integration by parts**

▪ **Basis:** $\partial_x (a + b \operatorname{Log}[c x^n]) = \frac{bn}{x}$

▪ **Rule:** If $q \in \mathbb{Z}^+$, let $u \rightarrow \int (d + e x^r)^q dx$, then

$$\int (d + e x^r)^q (a + b \operatorname{Log}[c x^n]) dx \rightarrow u (a + b \operatorname{Log}[c x^n]) - bn \int \frac{u}{x} dx$$

▪ **Program code:**

```
Int[(d_+e_.*x_^r_)^q.*(a_+b_.*Log[c_.*x_^n_.]),x_Symbol] :=
  With[{u=IntHide[(d+e*x^r)^q,x]},
    u*(a+b*Log[c*x^n]) - b*n*Int[SimplifyIntegrand[u/x,x],x] /;
  FreeQ[{a,b,c,d,e,n,r},x] && IGtQ[q,0]
```

```
Int[(d_+e_.*x_^r_)^q.*(a_+b_.*Log[c_.*x_^n_.]),x_Symbol] :=
  With[{u=IntHide[(d+e*x^r)^q,x]},
    Dist[(a+b*Log[c*x^n]),u] - b*n*Int[SimplifyIntegrand[u/x,x],x] /;
  FreeQ[{a,b,c,d,e,n,r},x] && IGtQ[q,0]
```

2: $\int (d + e x^r)^q (a + b \operatorname{Log}[c x^n]) dx$ when $r (q + 1) + 1 = 0$

▪ **Derivation: Integration by parts**

▪ **Basis:** If $r (q + 1) + 1 = 0$, then $(d + e x^r)^q = \partial_x \frac{x (d + e x^r)^{q+1}}{d}$

▪ **Rule:** If $r (q + 1) + 1 = 0$, then

$$\int (d + e x^r)^q (a + b \operatorname{Log}[c x^n]) dx \rightarrow \frac{x (d + e x^r)^{q+1} (a + b \operatorname{Log}[c x^n])}{d} - \frac{bn}{d} \int (d + e x^r)^{q+1} dx$$

▪ **Program code:**

```
Int[(d_+e_.*x_^r_)^q.*(a_+b_.*Log[c_.*x_^n_.]),x_Symbol] :=
  x*(d+e*x^r)^(q+1)*(a+b*Log[c*x^n])/d - b*n/d*Int[(d+e*x^r)^(q+1),x] /;
  FreeQ[{a,b,c,d,e,n,q,r},x] && EqQ[r*(q+1)+1,0]
```

$$\mathbf{x:} \int \frac{(a + b \operatorname{Log}[c x^n])^p}{d + e x^r} dx \text{ when } p \in \mathbb{Z}^+ \wedge r \in \mathbb{Z}^+$$

Derivation: Algebraic expansion

$$\mathbf{Basis:} \frac{x^m}{d+e x^r} = \frac{x^{m-r}}{e} - \frac{d x^{m-r}}{e(d+e x^r)}$$

Note: This rule produces antiderivatives in terms of $\operatorname{PolyLog}\left[k, -\frac{d}{e x^r}\right]$

Rule: If $p \in \mathbb{Z}^+ \wedge r \in \mathbb{Z}^+$, then

$$\int \frac{(a + b \operatorname{Log}[c x^n])^p}{d + e x^r} dx \rightarrow \frac{1}{e} \int \frac{(a + b \operatorname{Log}[c x^n])^p}{x^r} dx - \frac{d}{e} \int \frac{(a + b \operatorname{Log}[c x^n])^p}{x^r (d + e x^r)} dx$$

Program code:

```
(* Int[(a_.+b_.*Log[c_.*x_^n_.])^p_./(d_.+e_.*x_^r_.),x_Symbol] :=
  1/e*Int[(a+b*Log[c*x^n])^p/x^r,x] -
  d/e*Int[(a+b*Log[c*x^n])^p/(x^r*(d+e*x^r)),x] /;
FreeQ[{a,b,c,d,e,n,r},x] && IGtQ[p,0] && IGtQ[r,0] *)
```

$$3. \int (d + e x)^q (a + b \operatorname{Log}[c x^n])^p dx$$

$$1. \int (d + e x)^q (a + b \operatorname{Log}[c x^n])^p dx \text{ when } p > 0$$

$$1. \int \frac{(a + b \operatorname{Log}[c x^n])^p}{d + e x} dx \text{ when } p \in \mathbb{Z}^+$$

$$1. \int \frac{a + b \operatorname{Log}[c x]}{d + e x} dx \text{ when } -\frac{c d}{e} > 0$$

$$\mathbf{1:} \int \frac{\operatorname{Log}[c x]}{d + e x} dx \text{ when } e + c d = 0$$

Rule: If $e + c d = 0$, then

$$\int \frac{\operatorname{Log}[c x]}{d + e x} dx \rightarrow -\frac{1}{e} \operatorname{PolyLog}[2, 1 - c x]$$

Program code:

```
Int[Log[c_.*x_]/(d_.+e_.*x_),x_Symbol] :=
  -1/e*PolyLog[2,1-c*x] /;
FreeQ[{c,d,e},x] && EqQ[e+c*d,0]
```

$$2: \int \frac{a + b \operatorname{Log}[c x]}{d + e x} dx \text{ when } -\frac{cd}{e} > 0$$

Derivation: Algebraic expansion

- **Basis:** If $-\frac{cd}{e} > 0$, then $\operatorname{Log}[c x] = \operatorname{Log}\left[-\frac{cd}{e}\right] + \operatorname{Log}\left[-\frac{ex}{d}\right]$

Note: Resulting integrand is of the form required by the above rule.

- **Rule:** If $-\frac{cd}{e} > 0$, then

$$\int \frac{a + b \operatorname{Log}[c x]}{d + e x} dx \rightarrow \frac{(a + b \operatorname{Log}\left[-\frac{cd}{e}\right]) \operatorname{Log}[d + e x]}{e} + b \int \frac{\operatorname{Log}\left[-\frac{ex}{d}\right]}{d + e x} dx$$

Program code:

```
Int[(a_.+b_.*Log[c_.*x_])/(d_+e_.*x_),x_Symbol] :=
  (a+b*Log[-c*d/e])*Log[d+e*x]/e + b*Int[Log[-e*x/d]/(d+e*x),x] /;
FreeQ[{a,b,c,d,e},x] && GtQ[-c*d/e,0]
```

$$2: \int \frac{(a + b \operatorname{Log}[c x^n])^p}{d + e x} dx \text{ when } p \in \mathbb{Z}^+$$

Derivation: Integration by parts

- **Basis:** $\frac{1}{d+ex} = \frac{1}{e} \partial_x \operatorname{Log}\left[1 + \frac{ex}{d}\right]$

- **Basis:** $\partial_x (a + b \operatorname{Log}[c x^n])^p = \frac{b n p (a + b \operatorname{Log}[c x^n])^{p-1}}{x}$

Rule: If $p \in \mathbb{Z}^+$, then

$$\int \frac{(a + b \operatorname{Log}[c x^n])^p}{d + e x} dx \rightarrow \frac{\operatorname{Log}\left[1 + \frac{ex}{d}\right] (a + b \operatorname{Log}[c x^n])^p}{e} - \frac{b n p}{e} \int \frac{\operatorname{Log}\left[1 + \frac{ex}{d}\right] (a + b \operatorname{Log}[c x^n])^{p-1}}{x} dx$$

Program code:

```
Int[(a_.+b_.*Log[c_.*x_^n_.])^p_/(d_+e_.*x_),x_Symbol] :=
  Log[1+e*x/d]*(a+b*Log[c*x^n])^p/e - b*n*p/e*Int[Log[1+e*x/d]*(a+b*Log[c*x^n])^(p-1)/x,x] /;
FreeQ[{a,b,c,d,e,n},x] && IGtQ[p,0]
```

$$2: \int \frac{(a + b \operatorname{Log}[c x^n])^p}{(d + e x)^2} dx \text{ when } p > 0$$

Derivation: Integration by parts

$$\text{Basis: } \frac{1}{(d+e x)^2} = \partial_x \frac{x}{d+e x}$$

$$\text{Basis: } \partial_x (a + b \operatorname{Log}[c x^n])^p = \frac{b n p (a+b \operatorname{Log}[c x^n])^{p-1}}{x}$$

Rule: If $p > 0$, then

$$\int \frac{(a + b \operatorname{Log}[c x^n])^p}{(d + e x)^2} dx \rightarrow \frac{x (a + b \operatorname{Log}[c x^n])^p}{d (d + e x)} - \frac{b n p}{d} \int \frac{(a + b \operatorname{Log}[c x^n])^{p-1}}{d + e x} dx$$

Program code:

```
Int[(a_.+b_.*Log[c_*x_^n_.])^p_./.(d+e_*x_)^2,x_Symbol] :=
  x*(a+b*Log[c*x^n])^p/(d*(d+e*x)) - b*n*p/d*Int[(a+b*Log[c*x^n])^(p-1)/(d+e*x),x] /;
FreeQ[{a,b,c,d,e,n,p},x] && GtQ[p,0]
```

$$3: \int (d + e x)^q (a + b \operatorname{Log}[c x^n])^p dx \text{ when } p > 0 \wedge q \neq -1$$

Reference: G&R 2.728.1, CRC 501, A&S 4.1.50'

Derivation: Integration by parts

$$\text{Basis: } \partial_x (a + b \operatorname{Log}[c x^n])^p = \frac{b n p (a+b \operatorname{Log}[c x^n])^{p-1}}{x}$$

Rule: If $p > 0 \wedge q \neq -1$, then

$$\int (d + e x)^q (a + b \operatorname{Log}[c x^n])^p dx \rightarrow \frac{(d + e x)^{q+1} (a + b \operatorname{Log}[c x^n])^p}{e (q + 1)} - \frac{b n p}{e (q + 1)} \int \frac{(d + e x)^{q+1} (a + b \operatorname{Log}[c x^n])^{p-1}}{x} dx$$

Program code:

```
Int[(d+e_*x_)^q_.*(a_.+b_.*Log[c_*x_^n_.])^p_,x_Symbol] :=
  (d+e*x)^(q+1)*(a+b*Log[c*x^n])^p/(e*(q+1)) - b*n*p/(e*(q+1))*Int[((d+e*x)^(q+1)*(a+b*Log[c*x^n])^(p-1))/x,x] /;
FreeQ[{a,b,c,d,e,n,p,q},x] && GtQ[p,0] && NeQ[q,-1] && (EqQ[p,1] || IntegersQ[2*p,2*q] && Not[IGtQ[q,0]] || EqQ[p,2] && NeQ[q,1])
```

$$2: \int (d + e x)^q (a + b \operatorname{Log}[c x^n])^p dx \text{ when } p < -1 \wedge q > 0$$

Rule: If $p < -1 \wedge q > 0$, then

$$\int (d+e x)^q (a+b \log(c x^n))^p dx \rightarrow \frac{x (d+e x)^q (a+b \log(c x^n))^{p+1}}{b n (p+1)} + \frac{d q}{b n (p+1)} \int (d+e x)^{q-1} (a+b \log(c x^n))^{p+1} dx - \frac{q+1}{b n (p+1)} \int (d+e x)^q (a+b \log(c x^n))^{p+1} dx$$

Program code:

```
Int[(d+_e*_x_)^q.*(a+_b_*Log[c*_x_^n_])^p_,x_Symbol] :=
  x*(d+e*x)^q*(a+b*Log[c*x^n])^(p+1)/(b*n*(p+1)) +
  d*q/(b*n*(p+1))*Int[(d+e*x)^(q-1)*(a+b*Log[c*x^n])^(p+1),x] -
  (q+1)/(b*n*(p+1))*Int[(d+e*x)^q*(a+b*Log[c*x^n])^(p+1),x] /;
FreeQ[{a,b,c,d,e,n},x] && LtQ[p,-1] && GtQ[q,0]
```

4. $\int (d+e x^2)^q (a+b \log(c x^n)) dx$

1: $\int (d+e x^2)^q (a+b \log(c x^n)) dx$ when $q > 0$

Rule: If $q > 0$, then

$$\int (d+e x^2)^q (a+b \log(c x^n)) dx \rightarrow \frac{x (d+e x^2)^q (a+b \log(c x^n))}{2 q+1} - \frac{b n}{2 q+1} \int (d+e x^2)^q dx + \frac{2 d q}{2 q+1} \int (d+e x^2)^{q-1} (a+b \log(c x^n)) dx$$

Program code:

```
Int[(d+_e*_x_^2)^q.*(a+_b_*Log[c*_x_^n_]),x_Symbol] :=
  x*(d+e*x^2)^q*(a+b*Log[c*x^n])/(2*q+1) -
  b*n/(2*q+1)*Int[(d+e*x^2)^q,x] +
  2*d*q/(2*q+1)*Int[(d+e*x^2)^(q-1)*(a+b*Log[c*x^n]),x] /;
FreeQ[{a,b,c,d,e,n},x] && GtQ[q,0]
```

2. $\int (d+e x^2)^q (a+b \log(c x^n)) dx$ when $q < -1$

$$1: \int \frac{a+b \log(c x^n)}{(d+e x^2)^{3/2}} dx$$

Rule:

$$\int \frac{a+b \log(c x^n)}{(d+e x^2)^{3/2}} dx \rightarrow \frac{x(a+b \log(c x^n))}{d \sqrt{d+e x^2}} - \frac{b n}{d} \int \frac{1}{\sqrt{d+e x^2}} dx$$

Program code:

```
Int[(a_.+b_.*Log[c.*x^n_.])/(d+.e.*x^2)^(3/2),x_Symbol] :=
  x*(a+b*Log[c*x^n])/(d*Sqrt[d+e*x^2]) - b*n/d*Int[1/Sqrt[d+e*x^2],x] /;
FreeQ[{a,b,c,d,e,n},x]
```

2: $\int (d+e x^2)^q (a+b \log(c x^n)) dx$ when $q < -1$

Rule: If $q < -1$, then

$$\int (d+e x^2)^q (a+b \log(c x^n)) dx \rightarrow -\frac{x(d+e x^2)^{q+1}(a+b \log(c x^n))}{2d(q+1)} + \frac{b n}{2d(q+1)} \int (d+e x^2)^{q+1} dx + \frac{2q+3}{2d(q+1)} \int (d+e x^2)^{q+1} (a+b \log(c x^n)) dx$$

Program code:

```
Int[(d+.e.*x^2)^q*(a_.+b_.*Log[c.*x^n_.]),x_Symbol] :=
  -x*(d+e*x^2)^(q+1)*(a+b*Log[c*x^n])/(2*d*(q+1)) +
  b*n/(2*d*(q+1))*Int[(d+e*x^2)^(q+1),x] +
  (2*q+3)/(2*d*(q+1))*Int[(d+e*x^2)^(q+1)*(a+b*Log[c*x^n]),x] /;
FreeQ[{a,b,c,d,e,n},x] && LtQ[q,-1]
```

$$3: \int \frac{a+b \log(c x^n)}{d+e x^2} dx$$

Derivation: Integration by parts

- Basis: $\partial_x (a+b \log(c x^n)) = \frac{b n}{x}$
- Rule: Let $u \rightarrow \int \frac{1}{d+e x^2} dx$, then

$$\int \frac{a + b \operatorname{Log}[c x^n]}{d + e x^2} dx \rightarrow u (a + b \operatorname{Log}[c x^n]) - b n \int \frac{u}{x} dx$$

Program code:

```
Int[(a_.+b_.*Log[c_.*x_^n_.])/(d_+e_.*x_^2),x_Symbol] :=
  With[{u=IntHide[1/(d+e*x^2),x]},
    u*(a+b*Log[c*x^n]) - b*n*Int[u/x,x] /;
  FreeQ[{a,b,c,d,e,n},x]
```

$$4. \int \frac{a + b \operatorname{Log}[c x^n]}{\sqrt{d + e x^2}} dx$$

$$1. \int \frac{a + b \operatorname{Log}[c x^n]}{\sqrt{d + e x^2}} dx \text{ when } d > 0$$

$$1: \int \frac{a + b \operatorname{Log}[c x^n]}{\sqrt{d + e x^2}} dx \text{ when } d > 0 \wedge e > 0$$

Derivation: Integration by parts

■ **Basis:** If $d > 0$, then $\frac{1}{\sqrt{d+e x^2}} = \partial_x \frac{\operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{\sqrt{e}}$

Rule: If $d > 0 \wedge e > 0$, then

$$\int \frac{a + b \operatorname{Log}[c x^n]}{\sqrt{d + e x^2}} dx \rightarrow \frac{\operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{\sqrt{e}} - \frac{b n}{\sqrt{e}} \int \frac{\operatorname{ArcSinh}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right]}{x} dx$$

Program code:

```
Int[(a_.+b_.*Log[c_.*x_^n_.])/Sqrt[d_+e_.*x_^2],x_Symbol] :=
  ArcSinh[Rt[e,2]*x/Sqrt[d]]*(a+b*Log[c*x^n])/Rt[e,2] - b*n/Rt[e,2]*Int[ArcSinh[Rt[e,2]*x/Sqrt[d]]/x,x] /;
  FreeQ[{a,b,c,d,e,n},x] && GtQ[d,0] && PosQ[e]
```

$$2: \int \frac{a + b \operatorname{Log}[c x^n]}{\sqrt{d + e x^2}} dx \text{ when } d > 0 \wedge e \neq 0$$

Derivation: Integration by parts

■ **Basis:** If $d > 0$, then $\frac{1}{\sqrt{d+e x^2}} = \partial_x \frac{\operatorname{ArcSin}\left[\frac{\sqrt{-e} x}{\sqrt{d}}\right]}{\sqrt{-e}}$

Rule: If $d > 0 \wedge e \neq 0$, then

$$\int \frac{a + b \operatorname{Log}[c x^n]}{\sqrt{d + e x^2}} dx \rightarrow \frac{\operatorname{ArcSin}\left[\frac{\sqrt{-e} x}{\sqrt{d}}\right] (a + b \operatorname{Log}[c x^n])}{\sqrt{-e}} - \frac{b n}{\sqrt{-e}} \int \frac{\operatorname{ArcSin}\left[\frac{\sqrt{-e} x}{\sqrt{d}}\right]}{x} dx$$

Program code:

```
Int[(a_.+b_.*Log[c_.*x^n_.])/Sqrt[d_+e_.*x^2],x_Symbol] :=
  ArcSin[Rt[-e,2]*x/Sqrt[d]]*(a+b*Log[c*x^n])/Rt[-e,2] - b*n/Rt[-e,2]*Int[ArcSin[Rt[-e,2]*x/Sqrt[d]]/x,x] /;
FreeQ[{a,b,c,d,e,n},x] && GtQ[d,0] && NegQ[e]
```

$$2: \int \frac{a + b \operatorname{Log}[c x^n]}{\sqrt{d + e x^2}} dx \text{ when } d \neq 0$$

Derivation: Piecewise constant extraction

■ **Basis:** $\partial_x \frac{\sqrt{1 + \frac{e}{d} x^2}}{\sqrt{d + e x^2}} = 0$

Rule: If $d \neq 0$, then

$$\int \frac{a + b \operatorname{Log}[c x^n]}{\sqrt{d + e x^2}} dx \rightarrow \frac{\sqrt{1 + \frac{e}{d} x^2}}{\sqrt{d + e x^2}} \int \frac{a + b \operatorname{Log}[c x^n]}{\sqrt{1 + \frac{e}{d} x^2}} dx$$

Program code:

```
Int[(a_.+b_.*Log[c_.*x^n_.])/Sqrt[d_+e_.*x^2],x_Symbol] :=
  Sqrt[1+e/d*x^2]/Sqrt[d+e*x^2]*Int[(a+b*Log[c*x^n])/Sqrt[1+e/d*x^2],x] /;
FreeQ[{a,b,c,d,e,n},x] && Not[GtQ[d,0]]
```



```
Int[(a_+b_.*Log[c_.*x_^n_.])/(Sqrt[d1_+e1_.*x_]*Sqrt[d2_+e2_.*x_]),x_Symbol] :=
  Sqrt[1+e1*e2/(d1*d2)*x^2]/(Sqrt[d1+e1*x]*Sqrt[d2+e2*x])*Int[(a+b*Log[c*x^n])/Sqrt[1+e1*e2/(d1*d2)*x^2],x] /;
FreeQ[{a,b,c,d1,e1,d2,e2,n},x] && EqQ[d2*e1+d1*e2,0]
```

5: $\int (d+e x^r)^q (a+b \log(c x^n)) dx$ when $2q \in \mathbb{Z} \wedge r \in \mathbb{Z}$

Derivation: Integration by parts

Basis: $\partial_x (a+b \log(c x^n)) = \frac{bn}{x}$

Note: If $q - \frac{1}{2} \in \mathbb{Z}$, then the terms of $\int (d+e x^r)^q dx$ will be algebraic functions or constants times an inverse function.

Rule: If $2q \in \mathbb{Z} \wedge r \in \mathbb{Z}$, let $u \rightarrow \int (d+e x^r)^q dx$, then

$$\int (d+e x^r)^q (a+b \log(c x^n)) dx \rightarrow u (a+b \log(c x^n)) - bn \int \frac{u}{x} dx$$

Program code:

```
Int[(d_+e_.*x_^r_)^q_.*(a_+b_.*Log[c_.*x_^n_.]),x_Symbol] :=
  With[{u=IntHide[(d+e*x^r)^q,x]},
  Dist[(a+b*Log[c*x^n]),u,x] - b*n*Int[SimplifyIntegrand[u/x,x],x] /;
  EqQ[r,1] && IntegerQ[q-1/2] || EqQ[r,2] && EqQ[q,-1] || InverseFunctionFreeQ[u,x] /;
  FreeQ[{a,b,c,d,e,n,q,r},x] && IntegerQ[2*q] && IntegerQ[r]
```

6: $\int (d+e x^r)^q (a+b \log(c x^n))^p dx$ when $q \in \mathbb{Z} \wedge (q > 0 \vee p \in \mathbb{Z}^+ \wedge r \in \mathbb{Z})$

Derivation: Algebraic expansion

Rule: If $q \in \mathbb{Z} \wedge (q > 0 \vee p \in \mathbb{Z}^+ \wedge r \in \mathbb{Z})$, then

$$\int (d+e x^r)^q (a+b \log(c x^n))^p dx \rightarrow \int (a+b \log(c x^n))^p \text{ExpandIntegrand}[(d+e x^r)^q, x] dx$$

Program code:

```
Int[(d_+e_.*x_^r_)^q_.*(a_+b_.*Log[c_.*x_^n_.])^p_,x_Symbol] :=
  With[{u=ExpandIntegrand[(a+b*Log[c*x^n])^p,(d+e*x^r)^q,x]},
  Int[u,x] /;
  SumQ[u] /;
  FreeQ[{a,b,c,d,e,n,p,q,r},x] && IntegerQ[q] && (GtQ[q,0] || IGtQ[p,0] && IntegerQ[r])
```

U: $\int (d + e x^r)^q (a + b \operatorname{Log}[c x^n])^p dx$

▪ **Rule:**

$$\int (d + e x^r)^q (a + b \operatorname{Log}[c x^n])^p dx \rightarrow \int (d + e x^r)^q (a + b \operatorname{Log}[c x^n])^p dx$$

▪ **Program code:**

```
Int[(d_+e_*x_^r_)^q.*(a_+b_*Log[c_*x_^n_])^p_,x_Symbol] :=
  Unintegrable[(d+e*x^r)^q*(a+b*Log[c*x^n])^p,x] /;
  FreeQ[{a,b,c,d,e,n,p,q,r},x]
```

N: $\int u^q (a + b \operatorname{Log}[c x^n])^p dx$ when $u = d + e x^r$

▪ **Derivation: Algebraic normalization**

▪ **Rule: If $u = d + e x^r$, then**

$$\int u^q (a + b \operatorname{Log}[c x^n])^p dx \rightarrow \int (d + e x)^q (a + b \operatorname{Log}[c x^n])^p dx$$

▪ **Program code:**

```
Int[u^q.*(a_+b_*Log[c_*x_^n_])^p_,x_Symbol] :=
  Int[ExpandToSum[u,x]^q*(a+b*Log[c*x^n])^p,x] /;
  FreeQ[{a,b,c,n,p,q},x] && BinomialQ[u,x] && Not[BinomialMatchQ[u,x]]
```