

# Mathematica 11.3 Integration Test Results

## on the problems in the test-suite directory "5 Inverse trig functions\5.1 Inverse sine"

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Test results for the 227 problems in "5.1.2 (d x)^m (a+b arcsin(c x))^n.m"

Problem 121: Unable to integrate problem.

$$\int (b x)^m \operatorname{ArcSin}[a x]^2 dx$$

Optimal (type 5, 150 leaves, 2 steps):

$$\frac{(b x)^{1+m} \operatorname{ArcSin}[a x]^2}{b (1+m)} - \frac{2 a (b x)^{2+m} \operatorname{ArcSin}[a x] \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2+m}{2}, \frac{4+m}{2}, a^2 x^2\right]}{b^2 (1+m) (2+m)} + \\ \frac{2 a^2 (b x)^{3+m} \operatorname{HypergeometricPFQ}\left[\left\{1, \frac{3}{2} + \frac{m}{2}, \frac{3}{2} + \frac{m}{2}\right\}, \left\{2 + \frac{m}{2}, \frac{5}{2} + \frac{m}{2}\right\}, a^2 x^2\right]}{b^3 (1+m) (2+m) (3+m)}$$

Result (type 9, 143 leaves):

$$\frac{1}{(1+m) (2+m)} 2^{-2-m} x (b x)^m \left( 2^{2+m} \operatorname{ArcSin}[a x] \left( (2+m) \operatorname{ArcSin}[a x] - 2 a x \sqrt{1-a^2 x^2} \operatorname{Hypergeometric2F1}\left[1, \frac{3+m}{2}, \frac{4+m}{2}, a^2 x^2\right] \right) + \right. \\ \left. a^2 (2+m) \sqrt{\pi} x^2 \operatorname{Gamma}[2+m] \operatorname{HypergeometricPFQRegularized}\left[\left\{1, \frac{3+m}{2}, \frac{3+m}{2}\right\}, \left\{\frac{4+m}{2}, \frac{5+m}{2}\right\}, a^2 x^2\right] \right)$$

Problem 157: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^3}{x^2} dx$$

Optimal (type 4, 137 leaves, 9 steps):

$$-\frac{(a + b \operatorname{ArcSin}[c x])^3}{x} - 6 b c (a + b \operatorname{ArcSin}[c x])^2 \operatorname{ArcTanh}[e^{i \operatorname{ArcSin}[c x]}] + 6 i b^2 c (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c x]}] - \\ 6 i b^2 c (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c x]}] - 6 b^3 c \operatorname{PolyLog}[3, -e^{i \operatorname{ArcSin}[c x]}] + 6 b^3 c \operatorname{PolyLog}[3, e^{i \operatorname{ArcSin}[c x]}]$$

Result (type 4, 283 leaves):

$$-\frac{a^3}{x} - \frac{3 a^2 b \operatorname{ArcSin}[c x]}{x} + 3 a^2 b c \operatorname{Log}[x] - 3 a^2 b c \operatorname{Log}\left[1 + \sqrt{1 - c^2 x^2}\right] + 3 a b^2 c \\ \left(-\operatorname{ArcSin}[c x] \left(\frac{\operatorname{ArcSin}[c x]}{c x} - 2 \operatorname{Log}\left[1 - e^{i \operatorname{ArcSin}[c x]}\right] + 2 \operatorname{Log}\left[1 + e^{i \operatorname{ArcSin}[c x]}\right]\right) + 2 i \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c x]}] - 2 i \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c x]}]\right) + \\ b^3 c \left(-\frac{\operatorname{ArcSin}[c x]^3}{c x} + 3 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 - e^{i \operatorname{ArcSin}[c x]}\right] - 3 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + e^{i \operatorname{ArcSin}[c x]}\right] + 6 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c x]}] - \right. \\ \left. 6 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c x]}] - 6 \operatorname{PolyLog}[3, -e^{i \operatorname{ArcSin}[c x]}] + 6 \operatorname{PolyLog}[3, e^{i \operatorname{ArcSin}[c x]}]\right)$$

Problem 203: Result unnecessarily involves imaginary or complex numbers.

$$\int (d x)^{5/2} (a + b \operatorname{ArcSin}[c x]) dx$$

Optimal (type 4, 120 leaves, 5 steps):

$$\frac{20 b d^2 \sqrt{d x} \sqrt{1 - c^2 x^2}}{147 c^3} + \frac{4 b (d x)^{5/2} \sqrt{1 - c^2 x^2}}{49 c} + \frac{2 (d x)^{7/2} (a + b \operatorname{ArcSin}[c x])}{7 d} - \frac{20 b d^{5/2} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{c} \sqrt{d x}}{\sqrt{d}}\right], -1\right]}{147 c^{7/2}}$$

Result (type 4, 159 leaves):

$$\frac{1}{147 c^3 \sqrt{1 - c^2 x^2}} 2 d^2 \sqrt{d x} \left(10 b - 4 b c^2 x^2 - 6 b c^4 x^4 + 21 a c^3 x^3 \sqrt{1 - c^2 x^2} + \right. \\ \left. 21 b c^3 x^3 \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] + 10 i b \sqrt{-\frac{1}{c}} c \sqrt{1 - \frac{1}{c^2 x^2}} \sqrt{x} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{1}{c}}}{\sqrt{x}}\right], -1\right]\right)$$

Problem 204: Result unnecessarily involves imaginary or complex numbers.

$$\int (d x)^{3/2} (a + b \operatorname{ArcSin}[c x]) dx$$

Optimal (type 4, 124 leaves, 7 steps):

$$\frac{4 b (d x)^{3/2} \sqrt{1 - c^2 x^2}}{25 c} + \frac{2 (d x)^{5/2} (a + b \operatorname{ArcSin}[c x])}{5 d} - \frac{12 b d^{3/2} \operatorname{EllipticE}[\operatorname{ArcSin}\left[\frac{\sqrt{c} \sqrt{d x}}{\sqrt{d}}\right], -1]}{25 c^{5/2}} + \frac{12 b d^{3/2} \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\sqrt{c} \sqrt{d x}}{\sqrt{d}}\right], -1]}{25 c^{5/2}}$$

Result (type 4, 107 leaves):

$$\frac{1}{25 c^2 \sqrt{-c x}} 2 d \sqrt{d x} \\ \left( c x \sqrt{-c x} \left( 5 a c x + 2 b \sqrt{1 - c^2 x^2} + 5 b c x \operatorname{ArcSin}[c x] \right) + 6 i b \operatorname{EllipticE}[i \operatorname{ArcSinh}[\sqrt{-c x}], -1] - 6 i b \operatorname{EllipticF}[i \operatorname{ArcSinh}[\sqrt{-c x}], -1] \right)$$

Problem 205: Result unnecessarily involves imaginary or complex numbers.

$$\int \sqrt{d x} (a + b \operatorname{ArcSin}[c x]) dx$$

Optimal (type 4, 88 leaves, 4 steps):

$$\frac{4 b \sqrt{d x} \sqrt{1 - c^2 x^2}}{9 c} + \frac{2 (d x)^{3/2} (a + b \operatorname{ArcSin}[c x])}{3 d} - \frac{4 b \sqrt{d} \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\sqrt{c} \sqrt{d x}}{\sqrt{d}}\right], -1]}{9 c^{3/2}}$$

Result (type 4, 113 leaves):

$$\frac{2}{9} \sqrt{d x} \left( 3 a x + \frac{2 b \sqrt{1 - c^2 x^2}}{c} + 3 b x \operatorname{ArcSin}[c x] + \frac{2 i b \sqrt{-\frac{1}{c}} \sqrt{1 - \frac{1}{c^2 x^2}} \sqrt{x} \operatorname{EllipticF}[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{1}{c}}}{\sqrt{x}}\right], -1]}{\sqrt{1 - c^2 x^2}} \right)$$

Problem 206: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{\sqrt{d x}} dx$$

Optimal (type 4, 89 leaves, 6 steps):

$$\frac{2 \sqrt{d x} (a + b \operatorname{ArcSin}[c x])}{d} - \frac{4 b \operatorname{EllipticE}[\operatorname{ArcSin}\left[\frac{\sqrt{c} \sqrt{d x}}{\sqrt{d}}\right], -1]}{\sqrt{c} \sqrt{d}} + \frac{4 b \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\sqrt{c} \sqrt{d x}}{\sqrt{d}}\right], -1]}{\sqrt{c} \sqrt{d}}$$

Result (type 4, 76 leaves):

$$\frac{1}{\sqrt{-c x} \sqrt{d x}} 2 x \left( \sqrt{-c x} (a + b \operatorname{ArcSin}[c x]) + 2 i b \operatorname{EllipticE}[\pm \operatorname{ArcSinh}[\sqrt{-c x}], -1] - 2 i b \operatorname{EllipticF}[\pm \operatorname{ArcSinh}[\sqrt{-c x}], -1] \right)$$

**Problem 207:** Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{(d x)^{3/2}} dx$$

Optimal (type 4, 55 leaves, 3 steps):

$$-\frac{2 (a + b \operatorname{ArcSin}[c x])}{d \sqrt{d x}} + \frac{4 b \sqrt{c} \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\sqrt{c} \sqrt{d x}}{\sqrt{d}}\right], -1]}{d^{3/2}}$$

Result (type 4, 91 leaves):

$$\frac{2 x \left( -a - b \operatorname{ArcSin}[c x] + \frac{2 i b c \sqrt{1 - \frac{1}{c^2 x^2}} x^{3/2} \operatorname{EllipticF}[\pm i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{1}{c}}}{\sqrt{x}}\right], -1]}{\sqrt{\frac{1}{c}} \sqrt{1 - c^2 x^2}} \right)}{(d x)^{3/2}}$$

**Problem 208:** Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{(d x)^{5/2}} dx$$

Optimal (type 4, 125 leaves, 7 steps):

$$-\frac{4 b c \sqrt{1 - c^2 x^2}}{3 d^2 \sqrt{d x}} - \frac{2 (a + b \operatorname{ArcSin}[c x])}{3 d (d x)^{3/2}} - \frac{4 b c^{3/2} \operatorname{EllipticE}[\operatorname{ArcSin}\left[\frac{\sqrt{c} \sqrt{d x}}{\sqrt{d}}\right], -1]}{3 d^{5/2}} + \frac{4 b c^{3/2} \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\sqrt{c} \sqrt{d x}}{\sqrt{d}}\right], -1]}{3 d^{5/2}}$$

Result (type 4, 110 leaves):

$$\begin{aligned} & \frac{1}{3 \sqrt{-c x} (d x)^{5/2}} \\ & x \left( -2 \sqrt{-c x} \left( a + 2 b c x \sqrt{1 - c^2 x^2} + b \operatorname{ArcSin}[c x] \right) + 4 i b c^2 x^2 \operatorname{EllipticE}[\pm \operatorname{ArcSinh}[\sqrt{-c x}], -1] - 4 i b c^2 x^2 \operatorname{EllipticF}[\pm \operatorname{ArcSinh}[\sqrt{-c x}], -1] \right) \end{aligned}$$

### Problem 209: Result more than twice size of optimal antiderivative.

$$\int (\mathrm{d}x)^{5/2} (a + b \operatorname{ArcSin}[cx])^2 \mathrm{d}x$$

Optimal (type 5, 109 leaves, 2 steps):

$$\frac{2 (\mathrm{d}x)^{7/2} (a + b \operatorname{ArcSin}[cx])^2}{7 \mathrm{d}} - \frac{8 b c (\mathrm{d}x)^{9/2} (a + b \operatorname{ArcSin}[cx]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{9}{4}, \frac{13}{4}, c^2 x^2\right]}{63 \mathrm{d}^2} + \\ \frac{16 b^2 c^2 (\mathrm{d}x)^{11/2} \operatorname{HypergeometricPFQ}\left[\left\{1, \frac{11}{4}, \frac{11}{4}\right\}, \left\{\frac{13}{4}, \frac{15}{4}\right\}, c^2 x^2\right]}{693 \mathrm{d}^3}$$

Result (type 5, 269 leaves):

$$\frac{1}{6174} (\mathrm{d}x)^{5/2} \left( 1764 a^2 x + 3528 a b x \operatorname{ArcSin}[cx] - \right. \\ \left. \frac{336 a b x \left( \sqrt{c x} (-5 + 2 c^2 x^2 + 3 c^4 x^4) - 5 c \sqrt{1 - \frac{1}{c^2 x^2}} x \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{1}{\sqrt{c x}}\right], -1\right] \right)}{(c x)^{7/2} \sqrt{1 - c^2 x^2}} + \frac{1}{c^3 x^2 \operatorname{Gamma}\left[\frac{5}{4}\right] \operatorname{Gamma}\left[\frac{7}{4}\right]} \right. \\ \left. b^2 \left( 210 \sqrt{2} c \pi x \operatorname{HypergeometricPFQ}\left[\left\{\frac{3}{4}, \frac{3}{4}, 1\right\}, \left\{\frac{5}{4}, \frac{7}{4}\right\}, c^2 x^2\right] + 4 \operatorname{Gamma}\left[\frac{5}{4}\right] \operatorname{Gamma}\left[\frac{7}{4}\right] \left( -334 c x + 441 c^3 x^3 \operatorname{ArcSin}[cx]^2 + 21 \operatorname{ArcSin}[cx] \right. \right. \right. \\ \left. \left. \left. \left( 23 \sqrt{1 - c^2 x^2} - 3 \operatorname{Cos}[3 \operatorname{ArcSin}[cx]] \right) - 420 \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[cx] \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{5}{4}, c^2 x^2\right] + 18 \operatorname{Sin}[3 \operatorname{ArcSin}[cx]] \right) \right) \right)$$

### Problem 211: Result more than twice size of optimal antiderivative.

$$\int \sqrt{\mathrm{d}x} (a + b \operatorname{ArcSin}[cx])^2 \mathrm{d}x$$

Optimal (type 5, 109 leaves, 2 steps):

$$\frac{2 (d x)^{3/2} (a + b \operatorname{ArcSin}[c x])^2}{3 d} - \frac{8 b c (d x)^{5/2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{5}{4}, \frac{9}{4}, c^2 x^2\right]}{15 d^2} + \\ \frac{16 b^2 c^2 (d x)^{7/2} \operatorname{HypergeometricPFQ}\left[\left\{1, \frac{7}{4}, \frac{7}{4}\right\}, \left\{\frac{9}{4}, \frac{11}{4}\right\}, c^2 x^2\right]}{105 d^3}$$

Result (type 5, 228 leaves):

$$\frac{1}{27} \sqrt{d x} \left( \begin{array}{l} 18 a^2 x + 36 a b x \operatorname{ArcSin}[c x] + \frac{24 b^2 \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x]}{c} + \\ 24 a b x \left( -\sqrt{c x} + (c x)^{5/2} - c \sqrt{1 - \frac{1}{c^2 x^2}} x \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{1}{\sqrt{c x}}\right], -1\right] \right) - \\ 2 b^2 x (-8 + 9 \operatorname{ArcSin}[c x]^2) - \frac{(c x)^{3/2} \sqrt{1 - c^2 x^2}}{(c x)^{3/2} \sqrt{1 - c^2 x^2}} - \\ \frac{24 b^2 \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{5}{4}, c^2 x^2\right]}{c} + \frac{3 \sqrt{2} b^2 \pi x \operatorname{HypergeometricPFQ}\left[\left\{\frac{3}{4}, \frac{3}{4}, 1\right\}, \left\{\frac{5}{4}, \frac{7}{4}\right\}, c^2 x^2\right]}{\Gamma\left[\frac{5}{4}\right] \Gamma\left[\frac{7}{4}\right]} \end{array} \right)$$

Problem 214: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^2}{(d x)^{5/2}} d x$$

Optimal (type 5, 109 leaves, 2 steps):

$$\frac{2 (a + b \operatorname{ArcSin}[c x])^2}{3 d (d x)^{3/2}} - \frac{8 b c (a + b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, c^2 x^2\right]}{3 d^2 \sqrt{d x}} + \\ \frac{16 b^2 c^2 \sqrt{d x} \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{4}, 1\right\}, \left\{\frac{3}{4}, \frac{5}{4}\right\}, c^2 x^2\right]}{3 d^3}$$

Result (type 5, 242 leaves):

$$\frac{1}{36 \left(d x\right)^{5/2} \text{Gamma}\left[\frac{7}{4}\right] \text{Gamma}\left[\frac{9}{4}\right]} \\ x \left(-8 \text{Gamma}\left[\frac{7}{4}\right] \text{Gamma}\left[\frac{9}{4}\right] \left(3 a^2-24 b^2 c^2 x^2+12 a b c x \sqrt{1-c^2 x^2}+6 a b \text{ArcSin}[c x]+12 b^2 c x \sqrt{1-c^2 x^2} \text{ArcSin}[c x]+\right.\right. \\ \left.3 b^2 \text{ArcSin}[c x]^2+12 a b (c x)^{3/2} \text{EllipticE}[\text{ArcSin}[\sqrt{c x}],-1]-12 a b (c x)^{3/2} \text{EllipticF}[\text{ArcSin}[\sqrt{c x}],-1]\right.+ \\ \left.4 b^2 c^3 x^3 \sqrt{1-c^2 x^2} \text{ArcSin}[c x] \text{Hypergeometric2F1}\left[1,\frac{5}{4},\frac{7}{4},c^2 x^2\right]\right)+3 \sqrt{2} b^2 c^4 \pi x^4 \text{HypergeometricPFQ}\left[\left\{1,\frac{5}{4},\frac{5}{4}\right\},\left\{\frac{7}{4},\frac{9}{4}\right\},c^2 x^2\right]\right)$$

Problem 216: Attempted integration timed out after 120 seconds.

$$\int \sqrt{d x} (a + b \text{ArcSin}[c x])^3 dx$$

Optimal (type 9, 66 leaves, 1 step) :

$$\frac{2 (d x)^{3/2} (a + b \text{ArcSin}[c x])^3}{3 d} - \frac{2 b c \text{Unintegrable}\left[\frac{(d x)^{3/2} (a+b \text{ArcSin}[c x])^2}{\sqrt{1-c^2 x^2}}, x\right]}{d}$$

Result (type 1, 1 leaves) :

???

Test results for the 703 problems in "5.1.4 (f x)^m (d+e x^2)^p (a+b arcsin(c x))^n.m"

Problem 29: Result more than twice size of optimal antiderivative.

$$\int \frac{x^3 (a + b \text{ArcSin}[c x])}{d - c^2 d x^2} dx$$

Optimal (type 4, 144 leaves, 8 steps) :

$$-\frac{b x \sqrt{1-c^2 x^2}}{4 c^3 d}+\frac{b \text{ArcSin}[c x]}{4 c^4 d}-\frac{x^2 (a+b \text{ArcSin}[c x])}{2 c^2 d}+ \\ \frac{\frac{i}{2} (a+b \text{ArcSin}[c x])^2}{2 b c^4 d}-\frac{(a+b \text{ArcSin}[c x]) \log \left[1+e^{2 i \text{ArcSin}[c x]}\right]}{c^4 d}+\frac{\frac{i}{2} b \text{PolyLog}\left[2,-e^{2 i \text{ArcSin}[c x]}\right]}{2 c^4 d}$$

Result (type 4, 294 leaves) :

$$\begin{aligned}
& -\frac{1}{4 c^4 d} \left( 2 a c^2 x^2 + b c x \sqrt{1 - c^2 x^2} - b \operatorname{ArcSin}[c x] + 4 i b \pi \operatorname{ArcSin}[c x] + 2 b c^2 x^2 \operatorname{ArcSin}[c x] - 2 i b \operatorname{ArcSin}[c x]^2 + \right. \\
& 8 b \pi \operatorname{Log}\left[1 + e^{-i \operatorname{ArcSin}[c x]}\right] + 2 b \pi \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[c x]}\right] + 4 b \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[c x]}\right] - 2 b \pi \operatorname{Log}\left[1 + i e^{i \operatorname{ArcSin}[c x]}\right] + \\
& 4 b \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + i e^{i \operatorname{ArcSin}[c x]}\right] + 2 a \operatorname{Log}\left[1 - c^2 x^2\right] - 8 b \pi \operatorname{Log}\left[\cos\left(\frac{1}{2} \operatorname{ArcSin}[c x]\right)\right] + 2 b \pi \operatorname{Log}\left[-\cos\left(\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right)\right] - \\
& \left. 2 b \pi \operatorname{Log}\left[\sin\left(\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right)\right] - 4 i b \operatorname{PolyLog}\left[2, -i e^{i \operatorname{ArcSin}[c x]}\right] - 4 i b \operatorname{PolyLog}\left[2, i e^{i \operatorname{ArcSin}[c x]}\right] \right)
\end{aligned}$$

**Problem 31:** Result more than twice size of optimal antiderivative.

$$\int \frac{x (a + b \operatorname{ArcSin}[c x])}{d - c^2 d x^2} dx$$

Optimal (type 4, 82 leaves, 5 steps):

$$\frac{\frac{i (a + b \operatorname{ArcSin}[c x])^2}{2 b c^2 d} - \frac{(a + b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 + e^{2 i \operatorname{ArcSin}[c x]}\right]}{c^2 d} + \frac{i b \operatorname{PolyLog}\left[2, -e^{2 i \operatorname{ArcSin}[c x]}\right]}{2 c^2 d}}{2 c^2 d}$$

Result (type 4, 244 leaves):

$$\begin{aligned}
& -\frac{1}{2 c^2 d} \left( 2 i b \pi \operatorname{ArcSin}[c x] - i b \operatorname{ArcSin}[c x]^2 + 4 b \pi \operatorname{Log}\left[1 + e^{-i \operatorname{ArcSin}[c x]}\right] + b \pi \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[c x]}\right] + \right. \\
& 2 b \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[c x]}\right] - b \pi \operatorname{Log}\left[1 + i e^{i \operatorname{ArcSin}[c x]}\right] + 2 b \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + i e^{i \operatorname{ArcSin}[c x]}\right] + \\
& a \operatorname{Log}\left[1 - c^2 x^2\right] - 4 b \pi \operatorname{Log}\left[\cos\left(\frac{1}{2} \operatorname{ArcSin}[c x]\right)\right] + b \pi \operatorname{Log}\left[-\cos\left(\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right)\right] - \\
& \left. b \pi \operatorname{Log}\left[\sin\left(\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right)\right] - 2 i b \operatorname{PolyLog}\left[2, -i e^{i \operatorname{ArcSin}[c x]}\right] - 2 i b \operatorname{PolyLog}\left[2, i e^{i \operatorname{ArcSin}[c x]}\right] \right)
\end{aligned}$$

**Problem 32:** Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{d - c^2 d x^2} dx$$

Optimal (type 4, 84 leaves, 6 steps):

$$-\frac{\frac{2 i (a + b \operatorname{ArcSin}[c x]) \operatorname{ArcTan}\left[e^{i \operatorname{ArcSin}[c x]}\right]}{c d} + \frac{i b \operatorname{PolyLog}\left[2, -i e^{i \operatorname{ArcSin}[c x]}\right]}{c d} - \frac{i b \operatorname{PolyLog}\left[2, i e^{i \operatorname{ArcSin}[c x]}\right]}{c d}}{c d}$$

Result (type 4, 207 leaves):

$$\frac{1}{2 c d} \left( -\frac{i b \pi \operatorname{ArcSin}[c x] + b \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + 2 b \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + b \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}]}{d} - \right.$$

$$2 b \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - a \operatorname{Log}[1 - c x] + a \operatorname{Log}[1 + c x] - b \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] -$$

$$\left. b \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] + 2 i b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] - 2 i b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] \right)$$

### Problem 33: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{x (d - c^2 d x^2)} dx$$

Optimal (type 4, 71 leaves, 7 steps):

$$-\frac{2 (a + b \operatorname{ArcSin}[c x]) \operatorname{ArcTanh}[e^{2 i \operatorname{ArcSin}[c x]}]}{d} + \frac{i b \operatorname{PolyLog}[2, -e^{2 i \operatorname{ArcSin}[c x]}]}{2 d} - \frac{i b \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}[c x]}]}{2 d}$$

Result (type 4, 274 leaves):

$$-\frac{1}{2 d} \left( 2 i b \pi \operatorname{ArcSin}[c x] + 4 b \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] + b \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + 2 b \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - \right.$$

$$b \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + 2 b \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - 2 b \operatorname{ArcSin}[c x] \operatorname{Log}[1 - e^{2 i \operatorname{ArcSin}[c x]}] - 2 a \operatorname{Log}[x] +$$

$$a \operatorname{Log}[1 - c^2 x^2] - 4 b \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + b \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] - b \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] -$$

$$\left. 2 i b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] - 2 i b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] + i b \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}[c x]}] \right)$$

### Problem 34: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{x^2 (d - c^2 d x^2)} dx$$

Optimal (type 4, 116 leaves, 10 steps):

$$-\frac{a + b \operatorname{ArcSin}[c x]}{d x} - \frac{2 i c (a + b \operatorname{ArcSin}[c x]) \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[c x]}]}{d} -$$

$$\frac{b c \operatorname{ArcTanh}[\sqrt{1 - c^2 x^2}]}{d} + \frac{i b c \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{d} - \frac{i b c \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{d}$$

Result (type 4, 268 leaves):

$$\begin{aligned}
& -\frac{1}{2 dx} \left( 2a + 2b \operatorname{ArcSin}[cx] + i b c \pi x \operatorname{ArcSin}[cx] - b c \pi x \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] - \right. \\
& \quad 2 b c x \operatorname{ArcSin}[cx] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] - b c \pi x \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] + 2 b c x \operatorname{ArcSin}[cx] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] - \\
& \quad 2 b c x \operatorname{Log}[x] + a c x \operatorname{Log}[1 - cx] - a c x \operatorname{Log}[1 + cx] + 2 b c x \operatorname{Log}[1 + \sqrt{1 - c^2 x^2}] + b c \pi x \operatorname{Log}[-\operatorname{Cos}\left[\frac{1}{4}(\pi + 2 \operatorname{ArcSin}[cx])\right]] + \\
& \quad b c \pi x \operatorname{Log}[\operatorname{Sin}\left[\frac{1}{4}(\pi + 2 \operatorname{ArcSin}[cx])\right]] - 2 i b c x \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[cx]}] + 2 i b c x \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[cx]}] \Big)
\end{aligned}$$

**Problem 35:** Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcSin}[cx]}{x^3 (d - c^2 d x^2)} dx$$

Optimal (type 4, 124 leaves, 9 steps):

$$\begin{aligned}
& -\frac{b c \sqrt{1 - c^2 x^2}}{2 dx} - \frac{a + b \operatorname{ArcSin}[cx]}{2 dx^2} - \frac{2 c^2 (a + b \operatorname{ArcSin}[cx]) \operatorname{ArcTanh}[e^{2i \operatorname{ArcSin}[cx]}]}{d} + \\
& \quad \frac{i b c^2 \operatorname{PolyLog}[2, -e^{2i \operatorname{ArcSin}[cx]}]}{2 d} - \frac{i b c^2 \operatorname{PolyLog}[2, e^{2i \operatorname{ArcSin}[cx]}]}{2 d}
\end{aligned}$$

Result (type 4, 392 leaves):

$$\begin{aligned}
& -\frac{1}{2 dx^2} \left( a + b c x \sqrt{1 - c^2 x^2} + b \operatorname{ArcSin}[cx] + 2 i b c^2 \pi x^2 \operatorname{ArcSin}[cx] + 4 b c^2 \pi x^2 \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[cx]}] + \right. \\
& \quad b c^2 \pi x^2 \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] + 2 b c^2 x^2 \operatorname{ArcSin}[cx] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] - b c^2 \pi x^2 \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] + \\
& \quad 2 b c^2 x^2 \operatorname{ArcSin}[cx] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] - 2 b c^2 x^2 \operatorname{ArcSin}[cx] \operatorname{Log}[1 - e^{2i \operatorname{ArcSin}[cx]}] - 2 a c^2 x^2 \operatorname{Log}[x] + a c^2 x^2 \operatorname{Log}[1 - c^2 x^2] - \\
& \quad 4 b c^2 \pi x^2 \operatorname{Log}[\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] + b c^2 \pi x^2 \operatorname{Log}[-\operatorname{Cos}\left[\frac{1}{4}(\pi + 2 \operatorname{ArcSin}[cx])\right]] - b c^2 \pi x^2 \operatorname{Log}[\operatorname{Sin}\left[\frac{1}{4}(\pi + 2 \operatorname{ArcSin}[cx])\right]] - \\
& \quad \left. 2 i b c^2 x^2 \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[cx]}] - 2 i b c^2 x^2 \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[cx]}] + i b c^2 x^2 \operatorname{PolyLog}[2, e^{2i \operatorname{ArcSin}[cx]}] \right)
\end{aligned}$$

**Problem 36:** Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcSin}[cx]}{x^4 (d - c^2 d x^2)} dx$$

Optimal (type 4, 173 leaves, 15 steps):

$$\begin{aligned}
& -\frac{b c \sqrt{1 - c^2 x^2}}{6 dx^2} - \frac{a + b \operatorname{ArcSin}[cx]}{3 dx^3} - \frac{c^2 (a + b \operatorname{ArcSin}[cx])}{dx} - \frac{2 i c^3 (a + b \operatorname{ArcSin}[cx]) \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[cx]}]}{d} - \\
& \quad \frac{7 b c^3 \operatorname{ArcTanh}[\sqrt{1 - c^2 x^2}]}{6 d} + \frac{i b c^3 \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[cx]}]}{d} - \frac{i b c^3 \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[cx]}]}{d}
\end{aligned}$$

Result (type 4, 363 leaves):

$$\begin{aligned}
 & -\frac{1}{6 d x^3} \left( 2 a + 6 a c^2 x^2 + b c x \sqrt{1 - c^2 x^2} + 2 b \operatorname{ArcSin}[c x] + 6 b c^2 x^2 \operatorname{ArcSin}[c x] + 3 i b c^3 \pi x^3 \operatorname{ArcSin}[c x] - 3 b c^3 \pi x^3 \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - \right. \\
 & \quad 6 b c^3 x^3 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - 3 b c^3 \pi x^3 \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + 6 b c^3 x^3 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - \\
 & \quad 7 b c^3 x^3 \operatorname{Log}[x] + 3 a c^3 x^3 \operatorname{Log}[1 - c x] - 3 a c^3 x^3 \operatorname{Log}[1 + c x] + 7 b c^3 x^3 \operatorname{Log}[1 + \sqrt{1 - c^2 x^2}] + 3 b c^3 \pi x^3 \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] + \\
 & \quad \left. 3 b c^3 \pi x^3 \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] - 6 i b c^3 x^3 \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] + 6 i b c^3 x^3 \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] \right)
 \end{aligned}$$

Problem 38: Result more than twice size of optimal antiderivative.

$$\int \frac{x^3 (a + b \operatorname{ArcSin}[c x])}{(d - c^2 d x^2)^2} dx$$

Optimal (type 4, 155 leaves, 8 steps):

$$\begin{aligned}
 & -\frac{b x}{2 c^3 d^2 \sqrt{1 - c^2 x^2}} + \frac{b \operatorname{ArcSin}[c x]}{2 c^4 d^2} + \frac{x^2 (a + b \operatorname{ArcSin}[c x])}{2 c^2 d^2 (1 - c^2 x^2)} - \\
 & \frac{\frac{i}{2} (a + b \operatorname{ArcSin}[c x])^2}{2 b c^4 d^2} + \frac{(a + b \operatorname{ArcSin}[c x]) \operatorname{Log}[1 + e^{2 i \operatorname{ArcSin}[c x]}]}{c^4 d^2} - \frac{\frac{i}{2} b \operatorname{PolyLog}[2, -e^{2 i \operatorname{ArcSin}[c x]}]}{2 c^4 d^2}
 \end{aligned}$$

Result (type 4, 334 leaves):

$$\begin{aligned}
 & \frac{1}{4 c^4 d^2} \left( \frac{b \sqrt{1 - c^2 x^2}}{-1 + c x} + \frac{b \sqrt{1 - c^2 x^2}}{1 + c x} - \frac{2 a}{-1 + c^2 x^2} + 4 i b \pi \operatorname{ArcSin}[c x] + \frac{b \operatorname{ArcSin}[c x]}{1 - c x} + \frac{b \operatorname{ArcSin}[c x]}{1 + c x} - 2 i b \operatorname{ArcSin}[c x]^2 + \right. \\
 & \quad 8 b \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] + 2 b \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + 4 b \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - 2 b \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + \\
 & \quad 4 b \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + 2 a \operatorname{Log}[1 - c^2 x^2] - 8 b \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + 2 b \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] - \\
 & \quad \left. 2 b \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] - 4 i b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] - 4 i b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] \right)
 \end{aligned}$$

Problem 39: Result more than twice size of optimal antiderivative.

$$\int \frac{x^2 (a + b \operatorname{ArcSin}[c x])}{(d - c^2 d x^2)^2} dx$$

Optimal (type 4, 144 leaves, 8 steps):

$$\begin{aligned}
& -\frac{b}{2 c^3 d^2 \sqrt{1 - c^2 x^2}} + \frac{x (a + b \operatorname{ArcSin}[c x])}{2 c^2 d^2 (1 - c^2 x^2)} + \\
& \frac{\frac{i}{2} (a + b \operatorname{ArcSin}[c x]) \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[c x]}] - \frac{i}{2} b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{c^3 d^2} + \frac{\frac{i}{2} b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{2 c^3 d^2}
\end{aligned}$$

Result (type 4, 463 leaves):

$$\begin{aligned}
& -\frac{a x}{2 c^2 d^2 (-1 + c^2 x^2)} + \frac{a \operatorname{Log}[1 - c x]}{4 c^3 d^2} - \frac{a \operatorname{Log}[1 + c x]}{4 c^3 d^2} + \\
& \frac{1}{d^2} b \left( \frac{\sqrt{1 - c^2 x^2} - \operatorname{ArcSin}[c x]}{4 c^3 (-1 + c x)} - \frac{\sqrt{1 - c^2 x^2} + \operatorname{ArcSin}[c x]}{4 c^2 (c + c^2 x)} + \frac{1}{4 c^2} \left( \frac{3 i \pi \operatorname{ArcSin}[c x]}{2 c} - \frac{i \operatorname{ArcSin}[c x]^2}{2 c} + \right. \right. \\
& \frac{2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}]}{c} - \frac{\pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}]}{c} + \frac{2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}]}{c} - \frac{2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]]}{c} + \\
& \left. \left. \frac{\pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]}{c} - \frac{2 i \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{c} \right) - \frac{1}{4 c^2} \right. \\
& \left( \frac{\frac{i}{2} \pi \operatorname{ArcSin}[c x]}{2 c} - \frac{\frac{i}{2} \operatorname{ArcSin}[c x]^2}{2 c} + \frac{2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}]}{c} + \frac{\pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}]}{c} + \frac{2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}]}{c} - \right. \\
& \left. \left. \frac{2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]]}{c} - \frac{\pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]}{c} - \frac{2 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{c} \right) \right)
\end{aligned}$$

Problem 41: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{(d - c^2 d x^2)^2} dx$$

Optimal (type 4, 141 leaves, 8 steps):

$$\begin{aligned}
& -\frac{b}{2 c d^2 \sqrt{1 - c^2 x^2}} + \frac{x (a + b \operatorname{ArcSin}[c x])}{2 d^2 (1 - c^2 x^2)} - \\
& \frac{\frac{i}{2} (a + b \operatorname{ArcSin}[c x]) \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[c x]}] + \frac{i}{2} b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{c d^2} - \frac{\frac{i}{2} b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{2 c d^2}
\end{aligned}$$

Result (type 4, 334 leaves):

$$\begin{aligned}
& - \frac{1}{4 d^2} \left( \frac{b \sqrt{1 - c^2 x^2}}{c - c^2 x} + \frac{b \sqrt{1 - c^2 x^2}}{c + c^2 x} + \frac{2 a x}{-1 + c^2 x^2} + \frac{i b \pi \operatorname{ArcSin}[c x]}{c} + \frac{b \operatorname{ArcSin}[c x]}{c (-1 + c x)} + \right. \\
& \frac{b \operatorname{ArcSin}[c x]}{c + c^2 x} - \frac{b \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}]}{c} - \frac{2 b \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}]}{c} - \frac{b \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}]}{c} + \\
& \frac{2 b \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}]}{c} + \frac{a \operatorname{Log}[1 - c x]}{c} - \frac{a \operatorname{Log}[1 + c x]}{c} + \frac{b \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]}{c} + \\
& \left. \frac{b \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]}{c} - \frac{2 i b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{c} + \frac{2 i b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{c} \right)
\end{aligned}$$

**Problem 42:** Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{x (d - c^2 d x^2)^2} dx$$

Optimal (type 4, 122 leaves, 9 steps):

$$\begin{aligned}
& - \frac{b c x}{2 d^2 \sqrt{1 - c^2 x^2}} + \frac{a + b \operatorname{ArcSin}[c x]}{2 d^2 (1 - c^2 x^2)} - \frac{2 (a + b \operatorname{ArcSin}[c x]) \operatorname{ArcTanh}[e^{2 i \operatorname{ArcSin}[c x]}]}{d^2} + \frac{i b \operatorname{PolyLog}[2, -e^{2 i \operatorname{ArcSin}[c x]}]}{2 d^2} - \frac{i b \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}[c x]}]}{2 d^2}
\end{aligned}$$

Result (type 4, 364 leaves):

$$\begin{aligned}
& \frac{1}{4 d^2} \left( \frac{b \sqrt{1 - c^2 x^2}}{-1 + c x} + \frac{b \sqrt{1 - c^2 x^2}}{1 + c x} - \frac{2 a}{-1 + c^2 x^2} - 4 i b \pi \operatorname{ArcSin}[c x] + \frac{b \operatorname{ArcSin}[c x]}{1 - c x} + \frac{b \operatorname{ArcSin}[c x]}{1 + c x} - 8 b \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] - \right. \\
& 2 b \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - 4 b \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + 2 b \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - 4 b \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + \\
& 4 b \operatorname{ArcSin}[c x] \operatorname{Log}[1 - e^{2 i \operatorname{ArcSin}[c x]}] + 4 a \operatorname{Log}[x] - 2 a \operatorname{Log}[1 - c^2 x^2] + 8 b \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - 2 b \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] + \\
& \left. 2 b \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] + 4 i b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] + 4 i b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] - 2 i b \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}[c x]}] \right)
\end{aligned}$$

**Problem 44:** Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{x^3 (d - c^2 d x^2)^2} dx$$

Optimal (type 4, 159 leaves, 12 steps):

$$\begin{aligned}
& -\frac{b c}{2 d^2 x \sqrt{1 - c^2 x^2}} + \frac{c^2 (a + b \operatorname{ArcSin}[c x])}{d^2 (1 - c^2 x^2)} - \frac{a + b \operatorname{ArcSin}[c x]}{2 d^2 x^2 (1 - c^2 x^2)} - \\
& \frac{4 c^2 (a + b \operatorname{ArcSin}[c x]) \operatorname{ArcTanh}[e^{2 i \operatorname{ArcSin}[c x]}]}{d^2} + \frac{i b c^2 \operatorname{PolyLog}[2, -e^{2 i \operatorname{ArcSin}[c x]}]}{d^2} - \frac{i b c^2 \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}[c x]}]}{d^2}
\end{aligned}$$

Result (type 4, 461 leaves):

$$\begin{aligned}
& \frac{1}{4 d^2} \left( -\frac{2 a}{x^2} - \frac{2 b c \sqrt{1 - c^2 x^2}}{x} + \frac{b c^2 \sqrt{1 - c^2 x^2}}{-1 + c x} + \frac{b c^2 \sqrt{1 - c^2 x^2}}{1 + c x} - \frac{2 a c^2}{-1 + c^2 x^2} - 8 i b c^2 \pi \operatorname{ArcSin}[c x] - \frac{2 b \operatorname{ArcSin}[c x]}{x^2} + \frac{b c^2 \operatorname{ArcSin}[c x]}{1 - c x} + \right. \\
& \frac{b c^2 \operatorname{ArcSin}[c x]}{1 + c x} - 16 b c^2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] - 4 b c^2 \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - 8 b c^2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + \\
& 4 b c^2 \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - 8 b c^2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + 8 b c^2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - e^{2 i \operatorname{ArcSin}[c x]}] + 8 a c^2 \operatorname{Log}[x] - \\
& 4 a c^2 \operatorname{Log}[1 - c^2 x^2] + 16 b c^2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - 4 b c^2 \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] + 4 b c^2 \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] + \\
& \left. 8 i b c^2 \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] + 8 i b c^2 \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] - 4 i b c^2 \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}[c x]}] \right)
\end{aligned}$$

Problem 46: Result more than twice size of optimal antiderivative.

$$\int \frac{x^4 (a + b \operatorname{ArcSin}[c x])}{(d - c^2 d x^2)^3} dx$$

Optimal (type 4, 204 leaves, 12 steps):

$$\begin{aligned}
& -\frac{b}{12 c^5 d^3 (1 - c^2 x^2)^{3/2}} + \frac{5 b}{8 c^5 d^3 \sqrt{1 - c^2 x^2}} + \frac{x^3 (a + b \operatorname{ArcSin}[c x])}{4 c^2 d^3 (1 - c^2 x^2)^2} - \frac{3 x (a + b \operatorname{ArcSin}[c x])}{8 c^4 d^3 (1 - c^2 x^2)} - \\
& \frac{3 i (a + b \operatorname{ArcSin}[c x]) \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[c x]}]}{4 c^5 d^3} + \frac{3 i b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{8 c^5 d^3} - \frac{3 i b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{8 c^5 d^3}
\end{aligned}$$

Result (type 4, 445 leaves):

$$\begin{aligned}
& \frac{1}{48 c^5 d^3} \left( -\frac{2 b \sqrt{1 - c^2 x^2}}{(-1 + c x)^2} + \frac{b c x \sqrt{1 - c^2 x^2}}{(-1 + c x)^2} - \frac{15 b \sqrt{1 - c^2 x^2}}{-1 + c x} - \frac{2 b \sqrt{1 - c^2 x^2}}{(1 + c x)^2} - \frac{b c x \sqrt{1 - c^2 x^2}}{(1 + c x)^2} + \right. \\
& \frac{15 b \sqrt{1 - c^2 x^2}}{1 + c x} + \frac{12 a c x}{(-1 + c^2 x^2)^2} + \frac{30 a c x}{-1 + c^2 x^2} - 9 i b \pi \operatorname{ArcSin}[c x] + \frac{3 b \operatorname{ArcSin}[c x]}{(-1 + c x)^2} + \frac{15 b \operatorname{ArcSin}[c x]}{-1 + c x} - \frac{3 b \operatorname{ArcSin}[c x]}{(1 + c x)^2} + \\
& \frac{15 b \operatorname{ArcSin}[c x]}{1 + c x} + 9 b \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + 18 b \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + 9 b \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - \\
& 18 b \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - 9 a \operatorname{Log}[1 - c x] + 9 a \operatorname{Log}[1 + c x] - 9 b \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] - \\
& 9 b \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] + 18 i b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] - 18 i b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] \Big)
\end{aligned}$$

**Problem 48: Result more than twice size of optimal antiderivative.**

$$\int \frac{x^2 (a + b \operatorname{ArcSin}[c x])}{(d - c^2 d x^2)^3} dx$$

Optimal (type 4, 202 leaves, 10 steps):

$$\begin{aligned}
& -\frac{b}{12 c^3 d^3 (1 - c^2 x^2)^{3/2}} + \frac{b}{8 c^3 d^3 \sqrt{1 - c^2 x^2}} + \frac{x (a + b \operatorname{ArcSin}[c x])}{4 c^2 d^3 (1 - c^2 x^2)^2} - \frac{x (a + b \operatorname{ArcSin}[c x])}{8 c^2 d^3 (1 - c^2 x^2)} + \\
& \frac{\frac{i}{4} (a + b \operatorname{ArcSin}[c x]) \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[c x]}]}{4 c^3 d^3} - \frac{\frac{i}{4} b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{8 c^3 d^3} + \frac{\frac{i}{4} b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{8 c^3 d^3}
\end{aligned}$$

Result (type 4, 445 leaves):

$$\begin{aligned}
& \frac{1}{48 c^3 d^3} \left( -\frac{2 b \sqrt{1 - c^2 x^2}}{(-1 + c x)^2} + \frac{b c x \sqrt{1 - c^2 x^2}}{(-1 + c x)^2} - \frac{3 b \sqrt{1 - c^2 x^2}}{-1 + c x} - \frac{2 b \sqrt{1 - c^2 x^2}}{(1 + c x)^2} - \frac{b c x \sqrt{1 - c^2 x^2}}{(1 + c x)^2} + \right. \\
& \frac{3 b \sqrt{1 - c^2 x^2}}{1 + c x} + \frac{12 a c x}{(-1 + c^2 x^2)^2} + \frac{6 a c x}{-1 + c^2 x^2} + 3 i b \pi \operatorname{ArcSin}[c x] + \frac{3 b \operatorname{ArcSin}[c x]}{(-1 + c x)^2} + \frac{3 b \operatorname{ArcSin}[c x]}{-1 + c x} - \frac{3 b \operatorname{ArcSin}[c x]}{(1 + c x)^2} + \\
& \frac{3 b \operatorname{ArcSin}[c x]}{1 + c x} - 3 b \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - 6 b \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - 3 b \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + \\
& 6 b \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + 3 a \operatorname{Log}[1 - c x] - 3 a \operatorname{Log}[1 + c x] + 3 b \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] + \\
& 3 b \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] - 6 i b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] + 6 i b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] \Big)
\end{aligned}$$

### Problem 50: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcSin}[cx]}{(d - c^2 dx^2)^3} dx$$

Optimal (type 4, 196 leaves, 10 steps):

$$\begin{aligned} & -\frac{b}{12 c d^3 (1 - c^2 x^2)^{3/2}} - \frac{3 b}{8 c d^3 \sqrt{1 - c^2 x^2}} + \frac{x (a + b \operatorname{ArcSin}[cx])}{4 d^3 (1 - c^2 x^2)^2} + \frac{3 x (a + b \operatorname{ArcSin}[cx])}{8 d^3 (1 - c^2 x^2)} - \\ & \frac{3 i (a + b \operatorname{ArcSin}[cx]) \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[cx]}]}{4 c d^3} + \frac{3 i b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[cx]}]}{8 c d^3} - \frac{3 i b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[cx]}]}{8 c d^3} \end{aligned}$$

Result (type 4, 501 leaves):

$$\begin{aligned} & -\frac{1}{16 d^3} \left( \frac{2 b \sqrt{1 - c^2 x^2}}{3 c (-1 + c x)^2} - \frac{b x \sqrt{1 - c^2 x^2}}{3 (-1 + c x)^2} + \frac{2 b \sqrt{1 - c^2 x^2}}{3 c (1 + c x)^2} + \frac{b x \sqrt{1 - c^2 x^2}}{3 (1 + c x)^2} + \frac{3 b \sqrt{1 - c^2 x^2}}{c - c^2 x} + \right. \\ & \frac{3 b \sqrt{1 - c^2 x^2}}{c + c^2 x} - \frac{4 a x}{(-1 + c^2 x^2)^2} + \frac{6 a x}{-1 + c^2 x^2} + \frac{3 i b \pi \operatorname{ArcSin}[cx]}{c} - \frac{b \operatorname{ArcSin}[cx]}{c (-1 + c x)^2} + \frac{b \operatorname{ArcSin}[cx]}{c (1 + c x)^2} - \frac{3 b \operatorname{ArcSin}[cx]}{c - c^2 x} + \\ & \frac{3 b \operatorname{ArcSin}[cx]}{c + c^2 x} - \frac{3 b \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}]}{c} - \frac{6 b \operatorname{ArcSin}[cx] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}]}{c} - \frac{3 b \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}]}{c} + \\ & \frac{6 b \operatorname{ArcSin}[cx] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}]}{c} + \frac{3 a \operatorname{Log}[1 - c x]}{c} - \frac{3 a \operatorname{Log}[1 + c x]}{c} + \frac{3 b \pi \operatorname{Log}[-\operatorname{Cos}[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])]]}{c} + \\ & \left. \frac{3 b \pi \operatorname{Log}[\operatorname{Sin}[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])]]}{c} - \frac{6 i b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[cx]}]}{c} + \frac{6 i b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[cx]}]}{c} \right) \end{aligned}$$

### Problem 51: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcSin}[cx]}{x (d - c^2 dx^2)^3} dx$$

Optimal (type 4, 173 leaves, 12 steps):

$$\begin{aligned} & -\frac{b c x}{12 d^3 (1 - c^2 x^2)^{3/2}} - \frac{2 b c x}{3 d^3 \sqrt{1 - c^2 x^2}} + \frac{a + b \operatorname{ArcSin}[cx]}{4 d^3 (1 - c^2 x^2)^2} + \frac{a + b \operatorname{ArcSin}[cx]}{2 d^3 (1 - c^2 x^2)} - \\ & \frac{2 (a + b \operatorname{ArcSin}[cx]) \operatorname{ArcTanh}[e^{2 i \operatorname{ArcSin}[cx]}]}{d^3} + \frac{i b \operatorname{PolyLog}[2, -e^{2 i \operatorname{ArcSin}[cx]}]}{2 d^3} - \frac{i b \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}[cx]}]}{2 d^3} \end{aligned}$$

Result (type 4, 524 leaves):

$$\begin{aligned}
& \frac{1}{4 d^3} \left( -\frac{b \sqrt{1 - c^2 x^2}}{6 (-1 + c x)^2} + \frac{b c x \sqrt{1 - c^2 x^2}}{12 (-1 + c x)^2} + \frac{b \sqrt{1 - c^2 x^2}}{6 (1 + c x)^2} + \frac{b c x \sqrt{1 - c^2 x^2}}{12 (1 + c x)^2} + \frac{5 b \sqrt{1 - c^2 x^2}}{-4 + 4 c x} + \frac{5 b \sqrt{1 - c^2 x^2}}{4 + 4 c x} + \frac{a}{(-1 + c^2 x^2)^2} - \frac{2 a}{-1 + c^2 x^2} - \right. \\
& 4 i b \pi \operatorname{ArcSin}[c x] + \frac{5 b \operatorname{ArcSin}[c x]}{4 - 4 c x} + \frac{b \operatorname{ArcSin}[c x]}{4 (-1 + c x)^2} + \frac{b \operatorname{ArcSin}[c x]}{4 (1 + c x)^2} + \frac{5 b \operatorname{ArcSin}[c x]}{4 + 4 c x} - 8 b \pi \log[1 + e^{-i \operatorname{ArcSin}[c x]}] - \\
& 2 b \pi \log[1 - i e^{i \operatorname{ArcSin}[c x]}] - 4 b \operatorname{ArcSin}[c x] \log[1 - i e^{i \operatorname{ArcSin}[c x]}] + 2 b \pi \log[1 + i e^{i \operatorname{ArcSin}[c x]}] - 4 b \operatorname{ArcSin}[c x] \log[1 + i e^{i \operatorname{ArcSin}[c x]}] + \\
& 4 b \operatorname{ArcSin}[c x] \log[1 - e^{2 i \operatorname{ArcSin}[c x]}] + 4 a \log[x] - 2 a \log[1 - c^2 x^2] + 8 b \pi \log[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - 2 b \pi \log[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] + \\
& \left. 2 b \pi \log[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] + 4 i b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] + 4 i b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] - 2 i b \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}[c x]}] \right)
\end{aligned}$$

Problem 52: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{x^2 (d - c^2 d x^2)^3} dx$$

Optimal (type 4, 242 leaves, 16 steps):

$$\begin{aligned}
& -\frac{b c}{12 d^3 (1 - c^2 x^2)^{3/2}} - \frac{7 b c}{8 d^3 \sqrt{1 - c^2 x^2}} - \frac{a + b \operatorname{ArcSin}[c x]}{d^3 x (1 - c^2 x^2)^2} + \\
& \frac{5 c^2 x (a + b \operatorname{ArcSin}[c x])}{4 d^3 (1 - c^2 x^2)^2} + \frac{15 c^2 x (a + b \operatorname{ArcSin}[c x])}{8 d^3 (1 - c^2 x^2)} - \frac{15 i c (a + b \operatorname{ArcSin}[c x]) \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[c x]}]}{4 d^3} - \\
& \frac{b c \operatorname{ArcTanh}[\sqrt{1 - c^2 x^2}]}{d^3} + \frac{15 i b c \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{8 d^3} - \frac{15 i b c \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{8 d^3}
\end{aligned}$$

Result (type 4, 520 leaves):

$$\begin{aligned}
& -\frac{1}{16 d^3} \left( \frac{16 a}{x} + \frac{2 b c \sqrt{1 - c^2 x^2}}{3 (-1 + c x)^2} - \frac{b c^2 x \sqrt{1 - c^2 x^2}}{3 (-1 + c x)^2} - \frac{7 b c \sqrt{1 - c^2 x^2}}{-1 + c x} + \frac{2 b c \sqrt{1 - c^2 x^2}}{3 (1 + c x)^2} + \right. \\
& \frac{b c^2 x \sqrt{1 - c^2 x^2}}{3 (1 + c x)^2} + \frac{7 b c \sqrt{1 - c^2 x^2}}{1 + c x} - \frac{4 a c^2 x}{(-1 + c^2 x^2)^2} + \frac{14 a c^2 x}{-1 + c^2 x^2} + 15 i b c \pi \operatorname{ArcSin}[c x] + \frac{16 b \operatorname{ArcSin}[c x]}{x} - \\
& \frac{b c \operatorname{ArcSin}[c x]}{(-1 + c x)^2} + \frac{7 b c \operatorname{ArcSin}[c x]}{-1 + c x} + \frac{b c \operatorname{ArcSin}[c x]}{(1 + c x)^2} + \frac{7 b c \operatorname{ArcSin}[c x]}{1 + c x} - 15 b c \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - \\
& 30 b c \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - 15 b c \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + 30 b c \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - \\
& 16 b c \operatorname{Log}[x] + 15 a c \operatorname{Log}[1 - c x] - 15 a c \operatorname{Log}[1 + c x] + 16 b c \operatorname{Log}[1 + \sqrt{1 - c^2 x^2}] + 15 b c \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] + \\
& \left. 15 b c \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] - 30 i b c \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] + 30 i b c \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] \right)
\end{aligned}$$

Problem 53: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{x^3 (d - c^2 d x^2)^3} dx$$

Optimal (type 4, 248 leaves, 16 steps):

$$\begin{aligned}
& -\frac{b c}{2 d^3 x (1 - c^2 x^2)^{3/2}} + \frac{5 b c^3 x}{12 d^3 (1 - c^2 x^2)^{3/2}} - \frac{2 b c^3 x}{3 d^3 \sqrt{1 - c^2 x^2}} + \frac{3 c^2 (a + b \operatorname{ArcSin}[c x])}{4 d^3 (1 - c^2 x^2)^2} - \frac{a + b \operatorname{ArcSin}[c x]}{2 d^3 x^2 (1 - c^2 x^2)^2} + \frac{3 c^2 (a + b \operatorname{ArcSin}[c x])}{2 d^3 (1 - c^2 x^2)} - \\
& \frac{6 c^2 (a + b \operatorname{ArcSin}[c x]) \operatorname{ArcTanh}[e^{2 i \operatorname{ArcSin}[c x]}]}{d^3} + \frac{3 i b c^2 \operatorname{PolyLog}[2, -e^{2 i \operatorname{ArcSin}[c x]}]}{2 d^3} - \frac{3 i b c^2 \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}[c x]}]}{2 d^3}
\end{aligned}$$

Result (type 4, 568 leaves):

$$\begin{aligned}
& \frac{1}{4 d^3} \left( -\frac{2 a}{x^2} + \frac{a c^2}{(-1 + c^2 x^2)^2} - \frac{4 a c^2}{-1 + c^2 x^2} + \frac{9 b c^2 (\sqrt{1 - c^2 x^2} - \text{ArcSin}[c x])}{-4 + 4 c x} + \frac{9 b c^2 (\sqrt{1 - c^2 x^2} + \text{ArcSin}[c x])}{4 + 4 c x} - \right. \\
& \left. \frac{2 b (c x \sqrt{1 - c^2 x^2} + \text{ArcSin}[c x])}{x^2} + \frac{b c^2 ((-2 + c x) \sqrt{1 - c^2 x^2} + 3 \text{ArcSin}[c x])}{12 (-1 + c x)^2} + \frac{b c^2 ((2 + c x) \sqrt{1 - c^2 x^2} + 3 \text{ArcSin}[c x])}{12 (1 + c x)^2} + \right. \\
& 12 a c^2 \text{Log}[x] - 6 a c^2 \text{Log}[1 - c^2 x^2] + 3 b c^2 \left( \frac{i \text{ArcSin}[c x]^2 + \text{ArcSin}[c x] (-3 i \pi - 4 \text{Log}[1 + e^{i \text{ArcSin}[c x]}])}{2} \right) + \\
& 2 \pi \left( -2 \text{Log}[1 + e^{-i \text{ArcSin}[c x]}] + \text{Log}[1 + e^{i \text{ArcSin}[c x]}] + 2 \text{Log}[\text{Cos}[\frac{1}{2} \text{ArcSin}[c x]]] - \text{Log}[-\text{Cos}[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])]] \right) + \\
& 4 i \text{PolyLog}[2, -\frac{i e^{i \text{ArcSin}[c x]}}{2}] + 3 b c^2 \left( \frac{i \text{ArcSin}[c x]^2 + \text{ArcSin}[c x] (-i \pi - 4 \text{Log}[1 - e^{i \text{ArcSin}[c x]}])}{2} \right) + \\
& 2 \pi \left( -2 \text{Log}[1 + e^{-i \text{ArcSin}[c x]}] - \text{Log}[1 - e^{i \text{ArcSin}[c x]}] + 2 \text{Log}[\text{Cos}[\frac{1}{2} \text{ArcSin}[c x]]] + \text{Log}[\text{Sin}[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])]] \right) + \\
& \left. 4 i \text{PolyLog}[2, \frac{i e^{i \text{ArcSin}[c x]}}{2}] + 12 b c^2 \left( \text{ArcSin}[c x] \text{Log}[1 - e^{2 i \text{ArcSin}[c x]}] - \frac{1}{2} i (\text{ArcSin}[c x]^2 + \text{PolyLog}[2, e^{2 i \text{ArcSin}[c x]}]) \right) \right)
\end{aligned}$$

**Problem 119: Result unnecessarily involves higher level functions.**

$$\int \frac{x^5 (a + b \text{ArcSin}[c x])}{(d - c^2 d x^2)^{3/2}} dx$$

Optimal (type 3, 221 leaves, 5 steps):

$$\begin{aligned}
& -\frac{5 b x \sqrt{d - c^2 d x^2}}{3 c^5 d^2 \sqrt{1 - c^2 x^2}} - \frac{b x^3 \sqrt{d - c^2 d x^2}}{9 c^3 d^2 \sqrt{1 - c^2 x^2}} + \frac{a + b \text{ArcSin}[c x]}{c^6 d \sqrt{d - c^2 d x^2}} + \\
& \frac{2 \sqrt{d - c^2 d x^2} (a + b \text{ArcSin}[c x])}{c^6 d^2} - \frac{(d - c^2 d x^2)^{3/2} (a + b \text{ArcSin}[c x])}{3 c^6 d^3} - \frac{b \sqrt{d - c^2 d x^2} \text{ArcTanh}[c x]}{c^6 d^2 \sqrt{1 - c^2 x^2}}
\end{aligned}$$

Result (type 4, 166 leaves):

$$\begin{aligned}
& \frac{1}{9 c^6 \sqrt{-c^2} d^2 (-1 + c^2 x^2)} \sqrt{d - c^2 d x^2} \left( \sqrt{-c^2} \left( b c x \sqrt{1 - c^2 x^2} (15 + c^2 x^2) + 3 a (-8 + 4 c^2 x^2 + c^4 x^4) + 3 b (-8 + 4 c^2 x^2 + c^4 x^4) \text{ArcSin}[c x] \right) - \right. \\
& \left. 9 i b c \sqrt{1 - c^2 x^2} \text{EllipticF}\left[i \text{ArcSinh}[\sqrt{-c^2} x], 1\right] \right)
\end{aligned}$$

### Problem 121: Result unnecessarily involves higher level functions.

$$\int \frac{x^3 (a + b \operatorname{ArcSin}[c x])}{(d - c^2 d x^2)^{3/2}} dx$$

Optimal (type 3, 142 leaves, 4 steps):

$$-\frac{b x \sqrt{d - c^2 d x^2}}{c^3 d^2 \sqrt{1 - c^2 x^2}} + \frac{a + b \operatorname{ArcSin}[c x]}{c^4 d \sqrt{d - c^2 d x^2}} + \frac{\sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])}{c^4 d^2} - \frac{b \sqrt{d - c^2 d x^2} \operatorname{ArcTanh}[c x]}{c^4 d^2 \sqrt{1 - c^2 x^2}}$$

Result (type 4, 136 leaves):

$$\frac{1}{c^4 \sqrt{-c^2} d^2 (-1 + c^2 x^2)} \\ \sqrt{d - c^2 d x^2} \left( \sqrt{-c^2} \left( -2 a + a c^2 x^2 + b c x \sqrt{1 - c^2 x^2} + b (-2 + c^2 x^2) \operatorname{ArcSin}[c x] \right) - i b c \sqrt{1 - c^2 x^2} \operatorname{EllipticF}[i \operatorname{ArcSinh}[\sqrt{-c^2} x], 1] \right)$$

### Problem 123: Result unnecessarily involves higher level functions.

$$\int \frac{x (a + b \operatorname{ArcSin}[c x])}{(d - c^2 d x^2)^{3/2}} dx$$

Optimal (type 3, 73 leaves, 2 steps):

$$\frac{a + b \operatorname{ArcSin}[c x]}{c^2 d \sqrt{d - c^2 d x^2}} - \frac{b \sqrt{1 - c^2 x^2} \operatorname{ArcTanh}[c x]}{c^2 d \sqrt{d - c^2 d x^2}}$$

Result (type 4, 96 leaves):

$$\frac{\sqrt{d - c^2 d x^2} \left( \sqrt{-c^2} (a + b \operatorname{ArcSin}[c x]) + i b c \sqrt{1 - c^2 x^2} \operatorname{EllipticF}[i \operatorname{ArcSinh}[\sqrt{-c^2} x], 1] \right)}{(-c^2)^{3/2} d^2 (-1 + c^2 x^2)}$$

### Problem 130: Result unnecessarily involves higher level functions.

$$\int \frac{x^5 (a + b \operatorname{ArcSin}[c x])}{(d - c^2 d x^2)^{5/2}} dx$$

Optimal (type 3, 219 leaves, 5 steps):

$$\begin{aligned}
& - \frac{b x \sqrt{d - c^2 d x^2}}{6 c^5 d^3 (1 - c^2 x^2)^{3/2}} + \frac{b x \sqrt{d - c^2 d x^2}}{c^5 d^3 \sqrt{1 - c^2 x^2}} + \frac{a + b \operatorname{ArcSin}[c x]}{3 c^6 d (d - c^2 d x^2)^{3/2}} - \\
& \frac{2 (a + b \operatorname{ArcSin}[c x])}{c^6 d^2 \sqrt{d - c^2 d x^2}} - \frac{\sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])}{c^6 d^3} + \frac{11 b \sqrt{d - c^2 d x^2} \operatorname{ArcTanh}[c x]}{6 c^6 d^3 \sqrt{1 - c^2 x^2}}
\end{aligned}$$

Result (type 4, 169 leaves) :

$$\left( \sqrt{d - c^2 d x^2} \left( \sqrt{-c^2} \left( b c x \sqrt{1 - c^2 x^2} (-5 + 6 c^2 x^2) + 2 a (8 - 12 c^2 x^2 + 3 c^4 x^4) + 2 b (8 - 12 c^2 x^2 + 3 c^4 x^4) \operatorname{ArcSin}[c x] \right) + \right. \right. \\
\left. \left. 11 \pm b c (1 - c^2 x^2)^{3/2} \operatorname{EllipticF}[\pm \operatorname{ArcSinh}[\sqrt{-c^2} x], 1] \right) \right) / \left( 6 c^4 (-c^2)^{3/2} d^3 (-1 + c^2 x^2)^2 \right)$$

Problem 132: Result unnecessarily involves higher level functions.

$$\int \frac{x^3 (a + b \operatorname{ArcSin}[c x])}{(d - c^2 d x^2)^{5/2}} dx$$

Optimal (type 3, 150 leaves, 4 steps) :

$$- \frac{b x \sqrt{d - c^2 d x^2}}{6 c^3 d^3 (1 - c^2 x^2)^{3/2}} + \frac{a + b \operatorname{ArcSin}[c x]}{3 c^4 d (d - c^2 d x^2)^{3/2}} - \frac{a + b \operatorname{ArcSin}[c x]}{c^4 d^2 \sqrt{d - c^2 d x^2}} + \frac{5 b \sqrt{d - c^2 d x^2} \operatorname{ArcTanh}[c x]}{6 c^4 d^3 \sqrt{1 - c^2 x^2}}$$

Result (type 4, 143 leaves) :

$$\left( \sqrt{d - c^2 d x^2} \left( \sqrt{-c^2} \left( -4 a + 6 a c^2 x^2 - b c x \sqrt{1 - c^2 x^2} + 2 b (-2 + 3 c^2 x^2) \operatorname{ArcSin}[c x] \right) - 5 \pm b c (1 - c^2 x^2)^{3/2} \operatorname{EllipticF}[\pm \operatorname{ArcSinh}[\sqrt{-c^2} x], 1] \right) \right) / \left( 6 c^4 \sqrt{-c^2} d^3 (-1 + c^2 x^2)^2 \right)$$

Problem 134: Result unnecessarily involves higher level functions.

$$\int \frac{x (a + b \operatorname{ArcSin}[c x])}{(d - c^2 d x^2)^{5/2}} dx$$

Optimal (type 3, 119 leaves, 3 steps) :

$$- \frac{b x}{6 c d^2 \sqrt{1 - c^2 x^2} \sqrt{d - c^2 d x^2}} + \frac{a + b \operatorname{ArcSin}[c x]}{3 c^2 d (d - c^2 d x^2)^{3/2}} - \frac{b \sqrt{1 - c^2 x^2} \operatorname{ArcTanh}[c x]}{6 c^2 d^2 \sqrt{d - c^2 d x^2}}$$

Result (type 4, 121 leaves) :

$$-\left( \left( \sqrt{d - c^2 d x^2} \left( \sqrt{-c^2} \left( 2 a - b c x \sqrt{1 - c^2 x^2} + 2 b \operatorname{ArcSin}[c x] \right) + i b c (1 - c^2 x^2)^{3/2} \operatorname{EllipticF}[i \operatorname{ArcSinh}[\sqrt{-c^2} x], 1] \right) \right) / \right. \\ \left. \left( 6 (-c^2)^{3/2} d^3 (-1 + c^2 x^2)^2 \right) \right)$$

**Problem 141:** Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(f x)^{3/2} (a + b \operatorname{ArcSin}[c x])}{\sqrt{1 - c^2 x^2}} dx$$

Optimal (type 5, 79 leaves, 1 step):

$$\frac{2 (f x)^{5/2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{5}{4}, \frac{9}{4}, c^2 x^2\right]}{5 f} - \frac{4 b c (f x)^{7/2} \operatorname{HypergeometricPFQ}\left[\{1, \frac{7}{4}, \frac{7}{4}\}, \{\frac{9}{4}, \frac{11}{4}\}, c^2 x^2\right]}{35 f^2}$$

Result (type 5, 233 leaves):

$$\frac{1}{36 c^2 \sqrt{1 - c^2 x^2} \operatorname{Gamma}\left[\frac{5}{4}\right] \operatorname{Gamma}\left[\frac{7}{4}\right]} f \sqrt{f x} \left( \begin{array}{l} 8 \operatorname{Gamma}\left[\frac{5}{4}\right] \operatorname{Gamma}\left[\frac{7}{4}\right] \\ \\ \left( -3 a + 3 a c^2 x^2 + 2 b c x \sqrt{1 - c^2 x^2} - 3 b \operatorname{ArcSin}[c x] + 3 b c^2 x^2 \operatorname{ArcSin}[c x] + \frac{3 i a \sqrt{1 - \frac{1}{c^2 x^2}} \sqrt{x} \operatorname{EllipticF}[i \operatorname{ArcSinh}[\frac{\sqrt{-\frac{1}{c}}}{\sqrt{x}}], -1]}{\sqrt{-\frac{1}{c}}} - \right. \\ \left. 3 b \left(-1 + c^2 x^2\right) \operatorname{ArcSin}[c x] \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{5}{4}, c^2 x^2\right] \right) - 3 b c \pi x \sqrt{2 - 2 c^2 x^2} \operatorname{HypergeometricPFQ}\left[\{\frac{3}{4}, \frac{3}{4}, 1\}, \{\frac{5}{4}, \frac{7}{4}\}, c^2 x^2\right] \right)$$

**Problem 142:** Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(f x)^{3/2} (a + b \operatorname{ArcSin}[c x])}{\sqrt{d - c^2 d x^2}} dx$$

Optimal (type 5, 137 leaves, 1 step):

$$\frac{2 (f x)^{5/2} \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{5}{4}, \frac{9}{4}, c^2 x^2\right]}{5 f \sqrt{d - c^2 d x^2}} - \frac{4 b c (f x)^{7/2} \sqrt{1 - c^2 x^2} \operatorname{HypergeometricPFQ}\left[\{1, \frac{7}{4}, \frac{7}{4}\}, \{\frac{9}{4}, \frac{11}{4}\}, c^2 x^2\right]}{35 f^2 \sqrt{d - c^2 d x^2}}$$

Result (type 5, 234 leaves):

$$\begin{aligned} & \frac{1}{36 c^2 \sqrt{d - c^2 d x^2} \Gamma\left[\frac{5}{4}\right] \Gamma\left[\frac{7}{4}\right]} f \sqrt{f x} \left( 8 \Gamma\left[\frac{5}{4}\right] \Gamma\left[\frac{7}{4}\right] \right. \\ & \left( -3 a + 3 a c^2 x^2 + 2 b c x \sqrt{1 - c^2 x^2} - 3 b \operatorname{ArcSin}[c x] + 3 b c^2 x^2 \operatorname{ArcSin}[c x] + \frac{3 i a \sqrt{1 - \frac{1}{c^2 x^2}} \sqrt{x} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{1}{c}}}{\sqrt{x}}\right], -1\right]}{\sqrt{-\frac{1}{c}}} - \right. \\ & \left. 3 b \left(-1 + c^2 x^2\right) \operatorname{ArcSin}[c x] \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{5}{4}, c^2 x^2\right] \right) - 3 b c \pi x \sqrt{2 - 2 c^2 x^2} \operatorname{HypergeometricPFQ}\left[\left\{\frac{3}{4}, \frac{3}{4}, 1\right\}, \left\{\frac{5}{4}, \frac{7}{4}\right\}, c^2 x^2\right] \end{aligned}$$

Problem 149: Unable to integrate problem.

$$\int x^m (d - c^2 d x^2)^{5/2} (a + b \operatorname{ArcSin}[c x]) dx$$

Optimal (type 5, 635 leaves, 9 steps):

$$\begin{aligned}
& - \frac{15 b c d^2 x^{2+m} \sqrt{d - c^2 d x^2}}{(2+m)^2 (4+m) (6+m) \sqrt{1 - c^2 x^2}} - \frac{5 b c d^2 x^{2+m} \sqrt{d - c^2 d x^2}}{(6+m) (8+6m+m^2) \sqrt{1 - c^2 x^2}} - \frac{b c d^2 x^{2+m} \sqrt{d - c^2 d x^2}}{(12+8m+m^2) \sqrt{1 - c^2 x^2}} + \frac{5 b c^3 d^2 x^{4+m} \sqrt{d - c^2 d x^2}}{(4+m)^2 (6+m) \sqrt{1 - c^2 x^2}} + \\
& \frac{2 b c^3 d^2 x^{4+m} \sqrt{d - c^2 d x^2}}{(4+m) (6+m) \sqrt{1 - c^2 x^2}} - \frac{b c^5 d^2 x^{6+m} \sqrt{d - c^2 d x^2}}{(6+m)^2 \sqrt{1 - c^2 x^2}} + \frac{15 d^2 x^{1+m} \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])}{(6+m) (8+6m+m^2)} + \frac{5 d x^{1+m} (d - c^2 d x^2)^{3/2} (a + b \operatorname{ArcSin}[c x])}{(4+m) (6+m)} + \\
& \frac{x^{1+m} (d - c^2 d x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])}{6+m} + \frac{15 d^2 x^{1+m} \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, c^2 x^2\right]}{(6+m) (8+14m+7m^2+m^3) \sqrt{1 - c^2 x^2}} - \\
& \frac{15 b c d^2 x^{2+m} \sqrt{d - c^2 d x^2} \operatorname{HypergeometricPFQ}\left[\left\{1, 1+\frac{m}{2}, 1+\frac{m}{2}\right\}, \left\{\frac{3}{2}+\frac{m}{2}, 2+\frac{m}{2}\right\}, c^2 x^2\right]}{(1+m) (2+m)^2 (4+m) (6+m) \sqrt{1 - c^2 x^2}}
\end{aligned}$$

Result (type 8, 29 leaves):

$$\int x^m (d - c^2 d x^2)^{5/2} (a + b \operatorname{ArcSin}[c x]) dx$$

**Problem 150:** Unable to integrate problem.

$$\int x^m (d - c^2 d x^2)^{3/2} (a + b \operatorname{ArcSin}[c x]) dx$$

Optimal (type 5, 399 leaves, 6 steps):

$$\begin{aligned}
& - \frac{3 b c d x^{2+m} \sqrt{d - c^2 d x^2}}{(2+m)^2 (4+m) \sqrt{1 - c^2 x^2}} - \frac{b c d x^{2+m} \sqrt{d - c^2 d x^2}}{(8+6m+m^2) \sqrt{1 - c^2 x^2}} + \frac{b c^3 d x^{4+m} \sqrt{d - c^2 d x^2}}{(4+m)^2 \sqrt{1 - c^2 x^2}} + \frac{3 d x^{1+m} \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])}{8+6m+m^2} + \\
& \frac{x^{1+m} (d - c^2 d x^2)^{3/2} (a + b \operatorname{ArcSin}[c x])}{4+m} + \frac{3 d x^{1+m} \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, c^2 x^2\right]}{(8+14m+7m^2+m^3) \sqrt{1 - c^2 x^2}} - \\
& \frac{3 b c d x^{2+m} \sqrt{d - c^2 d x^2} \operatorname{HypergeometricPFQ}\left[\left\{1, 1+\frac{m}{2}, 1+\frac{m}{2}\right\}, \left\{\frac{3}{2}+\frac{m}{2}, 2+\frac{m}{2}\right\}, c^2 x^2\right]}{(1+m) (2+m)^2 (4+m) \sqrt{1 - c^2 x^2}}
\end{aligned}$$

Result (type 8, 29 leaves):

$$\int x^m (d - c^2 d x^2)^{3/2} (a + b \operatorname{ArcSin}[c x]) dx$$

**Problem 151:** Unable to integrate problem.

$$\int x^m \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x]) dx$$

Optimal (type 5, 245 leaves, 3 steps):

$$\begin{aligned} & \frac{b c x^{2+m} \sqrt{d - c^2 d x^2}}{(2+m)^2 \sqrt{1 - c^2 x^2}} + \frac{x^{1+m} \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])}{2+m} + \frac{x^{1+m} \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, c^2 x^2\right]}{(2+3m+m^2) \sqrt{1 - c^2 x^2}} - \\ & \frac{b c x^{2+m} \sqrt{d - c^2 d x^2} \operatorname{HypergeometricPFQ}\left[\{1, 1+\frac{m}{2}, 1+\frac{m}{2}\}, \{\frac{3}{2}+\frac{m}{2}, 2+\frac{m}{2}\}, c^2 x^2\right]}{(1+m) (2+m)^2 \sqrt{1 - c^2 x^2}} \end{aligned}$$

Result (type 8, 29 leaves):

$$\int x^m \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x]) dx$$

Problem 152: Unable to integrate problem.

$$\int \frac{x^m (a + b \operatorname{ArcSin}[c x])}{\sqrt{d - c^2 d x^2}} dx$$

Optimal (type 5, 163 leaves, 1 step):

$$\begin{aligned} & \frac{x^{1+m} \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, c^2 x^2\right]}{(1+m) \sqrt{d - c^2 d x^2}} - \\ & \frac{b c x^{2+m} \sqrt{1 - c^2 x^2} \operatorname{HypergeometricPFQ}\left[\{1, 1+\frac{m}{2}, 1+\frac{m}{2}\}, \{\frac{3}{2}+\frac{m}{2}, 2+\frac{m}{2}\}, c^2 x^2\right]}{(2+3m+m^2) \sqrt{d - c^2 d x^2}} \end{aligned}$$

Result (type 9, 181 leaves):

$$\begin{aligned} & \frac{1}{(1+m) \sqrt{d - c^2 d x^2}} \\ & 2^{-2-m} x^{1+m} \sqrt{1 - c^2 x^2} \left( 2^{2+m} \left( a \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, c^2 x^2\right] + b \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] \operatorname{Hypergeometric2F1}\left[1, \frac{2+m}{2}, \frac{3+m}{2}, c^2 x^2\right] \right) - \right. \\ & \left. b c (1+m) \sqrt{\pi} x \operatorname{Gamma}[1+m] \operatorname{HypergeometricPFQRegularized}\left[\{1, \frac{2+m}{2}, \frac{2+m}{2}\}, \{\frac{3+m}{2}, \frac{4+m}{2}\}, c^2 x^2\right] \right) \end{aligned}$$

Problem 153: Unable to integrate problem.

$$\int \frac{x^m (a + b \operatorname{ArcSin}[c x])}{(d - c^2 d x^2)^{3/2}} dx$$

Optimal (type 5, 272 leaves, 3 steps):

$$\frac{x^{1+m} (a + b \operatorname{ArcSin}[c x])}{d \sqrt{d - c^2 d x^2}} - \frac{m x^{1+m} \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, c^2 x^2\right]}{d (1+m) \sqrt{d - c^2 d x^2}} -$$

$$\frac{b c x^{2+m} \sqrt{1 - c^2 x^2} \operatorname{Hypergeometric2F1}\left[1, \frac{2+m}{2}, \frac{4+m}{2}, c^2 x^2\right]}{d (2+m) \sqrt{d - c^2 d x^2}} + \frac{b c m x^{2+m} \sqrt{1 - c^2 x^2} \operatorname{HypergeometricPFQ}\left[\{1, 1+\frac{m}{2}, 1+\frac{m}{2}\}, \{\frac{3}{2}+\frac{m}{2}, 2+\frac{m}{2}\}, c^2 x^2\right]}{d (2+3m+m^2) \sqrt{d - c^2 d x^2}}$$

Result (type 8, 29 leaves):

$$\int \frac{x^m (a + b \operatorname{ArcSin}[c x])}{(d - c^2 d x^2)^{3/2}} dx$$

Problem 154: Unable to integrate problem.

$$\int \frac{x^m (a + b \operatorname{ArcSin}[c x])}{(d - c^2 d x^2)^{5/2}} dx$$

Optimal (type 5, 408 leaves, 5 steps):

$$\frac{x^{1+m} (a + b \operatorname{ArcSin}[c x])}{3 d (d - c^2 d x^2)^{3/2}} + \frac{(2-m) x^{1+m} (a + b \operatorname{ArcSin}[c x])}{3 d^2 \sqrt{d - c^2 d x^2}} - \frac{(2-m) m x^{1+m} \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, c^2 x^2\right]}{3 d^2 (1+m) \sqrt{d - c^2 d x^2}}$$

$$\frac{b c (2-m) x^{2+m} \sqrt{1 - c^2 x^2} \operatorname{Hypergeometric2F1}\left[1, \frac{2+m}{2}, \frac{4+m}{2}, c^2 x^2\right]}{3 d^2 (2+m) \sqrt{d - c^2 d x^2}} - \frac{b c x^{2+m} \sqrt{1 - c^2 x^2} \operatorname{Hypergeometric2F1}\left[2, \frac{2+m}{2}, \frac{4+m}{2}, c^2 x^2\right]}{3 d^2 (2+m) \sqrt{d - c^2 d x^2}} +$$

$$\frac{b c (2-m) m x^{2+m} \sqrt{1 - c^2 x^2} \operatorname{HypergeometricPFQ}\left[\{1, 1+\frac{m}{2}, 1+\frac{m}{2}\}, \{\frac{3}{2}+\frac{m}{2}, 2+\frac{m}{2}\}, c^2 x^2\right]}{3 d^2 (2+3m+m^2) \sqrt{d - c^2 d x^2}}$$

Result (type 8, 29 leaves):

$$\int \frac{x^m (a + b \operatorname{ArcSin}[c x])}{(d - c^2 d x^2)^{5/2}} dx$$

Problem 155: Unable to integrate problem.

$$\int \frac{x^m \operatorname{ArcSin}[a x]}{\sqrt{1 - a^2 x^2}} dx$$

Optimal (type 5, 100 leaves, 1 step):

$$\frac{x^{1+m} \operatorname{ArcSin}[ax] \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, a^2 x^2\right]}{1+m} - \frac{a x^{2+m} \operatorname{HypergeometricPFQ}\left[\{1, 1+\frac{m}{2}, 1+\frac{m}{2}\}, \{\frac{3}{2}+\frac{m}{2}, 2+\frac{m}{2}\}, a^2 x^2\right]}{2+3m+m^2}$$

Result (type 9, 117 leaves):

$$\frac{1}{2} x^{1+m} \left( \frac{2 \sqrt{1-a^2 x^2} \operatorname{ArcSin}[ax] \operatorname{Hypergeometric2F1}\left[1, 1+\frac{m}{2}, \frac{3+m}{2}, a^2 x^2\right]}{1+m} - 2^{-1-m} a \sqrt{\pi} x \operatorname{Gamma}\left[1+m\right] \operatorname{HypergeometricPFQRegularized}\left[\{1, 1+\frac{m}{2}, 1+\frac{m}{2}\}, \{\frac{3+m}{2}, 2+\frac{m}{2}\}, a^2 x^2\right] \right)$$

Problem 184: Result more than twice size of optimal antiderivative.

$$\int \frac{x^3 (a + b \operatorname{ArcSin}[cx])^2}{d - c^2 d x^2} dx$$

Optimal (type 4, 210 leaves, 10 steps):

$$\begin{aligned} & \frac{b^2 x^2}{4 c^2 d} - \frac{b x \sqrt{1-c^2 x^2} (a + b \operatorname{ArcSin}[c x])}{2 c^3 d} + \frac{(a + b \operatorname{ArcSin}[c x])^2}{4 c^4 d} - \frac{x^2 (a + b \operatorname{ArcSin}[c x])^2}{2 c^2 d} + \frac{i (a + b \operatorname{ArcSin}[c x])^3}{3 b c^4 d} - \\ & \frac{(a + b \operatorname{ArcSin}[c x])^2 \operatorname{Log}\left[1 + e^{2i \operatorname{ArcSin}[c x]}\right]}{c^4 d} + \frac{i b (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}\left[2, -e^{2i \operatorname{ArcSin}[c x]}\right]}{c^4 d} - \frac{b^2 \operatorname{PolyLog}\left[3, -e^{2i \operatorname{ArcSin}[c x]}\right]}{2 c^4 d} \end{aligned}$$

Result (type 4, 441 leaves):

$$\begin{aligned} & -\frac{1}{24 c^4 d} \left( 12 a^2 c^2 x^2 + 12 a b c x \sqrt{1-c^2 x^2} - 12 a b \operatorname{ArcSin}[c x] + 48 i a b \pi \operatorname{ArcSin}[c x] + 24 a b c^2 x^2 \operatorname{ArcSin}[c x] - \right. \\ & 24 i a b \operatorname{ArcSin}[c x]^2 - 8 i b^2 \operatorname{ArcSin}[c x]^3 + 3 b^2 \operatorname{Cos}[2 \operatorname{ArcSin}[c x]] - 6 b^2 \operatorname{ArcSin}[c x]^2 \operatorname{Cos}[2 \operatorname{ArcSin}[c x]] + \\ & 96 a b \pi \operatorname{Log}\left[1 + e^{-i \operatorname{ArcSin}[c x]}\right] + 24 a b \pi \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[c x]}\right] + 48 a b \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[c x]}\right] - \\ & 24 a b \pi \operatorname{Log}\left[1 + i e^{i \operatorname{ArcSin}[c x]}\right] + 48 a b \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + i e^{i \operatorname{ArcSin}[c x]}\right] + 24 b^2 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + e^{2i \operatorname{ArcSin}[c x]}\right] + \\ & 12 a^2 \operatorname{Log}\left[1 - c^2 x^2\right] - 96 a b \pi \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right] + 24 a b \pi \operatorname{Log}\left[-\operatorname{Cos}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]\right] - \\ & 24 a b \pi \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]\right] - 48 i a b \operatorname{PolyLog}\left[2, -i e^{i \operatorname{ArcSin}[c x]}\right] - 48 i a b \operatorname{PolyLog}\left[2, i e^{i \operatorname{ArcSin}[c x]}\right] - \\ & \left. 24 i b^2 \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, -e^{2i \operatorname{ArcSin}[c x]}\right] + 12 b^2 \operatorname{PolyLog}\left[3, -e^{2i \operatorname{ArcSin}[c x]}\right] + 6 b^2 \operatorname{ArcSin}[c x] \operatorname{Sin}[2 \operatorname{ArcSin}[c x]] \right) \end{aligned}$$

Problem 186: Result more than twice size of optimal antiderivative.

$$\int \frac{x (a + b \operatorname{ArcSin}[c x])^2}{d - c^2 d x^2} dx$$

Optimal (type 4, 117 leaves, 6 steps):

$$\frac{\frac{i}{3} (a + b \operatorname{ArcSin}[cx])^3 - \frac{(a + b \operatorname{ArcSin}[cx])^2 \operatorname{Log}[1 + e^{2i \operatorname{ArcSin}[cx]}]}{c^2 d} + \frac{i b (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, -e^{2i \operatorname{ArcSin}[cx]}]}{c^2 d} - \frac{b^2 \operatorname{PolyLog}[3, -e^{2i \operatorname{ArcSin}[cx]}]}{2 c^2 d}}$$

Result (type 4, 342 leaves):

$$\begin{aligned} & \frac{1}{6 c^2 d} \left( -12 i a b \pi \operatorname{ArcSin}[cx] + 6 i a b \operatorname{ArcSin}[cx]^2 + 2 i b^2 \operatorname{ArcSin}[cx]^3 - 24 a b \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[cx]}] - \right. \\ & 6 a b \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] - 12 a b \operatorname{ArcSin}[cx] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] + 6 a b \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] - \\ & 12 a b \operatorname{ArcSin}[cx] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] - 6 b^2 \operatorname{ArcSin}[cx]^2 \operatorname{Log}[1 + e^{2i \operatorname{ArcSin}[cx]}] - 3 a^2 \operatorname{Log}[1 - c^2 x^2] + 24 a b \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[cx]]] - \\ & 6 a b \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])]]) + 6 a b \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])]]) + 12 i a b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[cx]}] + \\ & \left. 12 i a b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[cx]}] + 6 i b^2 \operatorname{ArcSin}[cx] \operatorname{PolyLog}[2, -e^{2i \operatorname{ArcSin}[cx]}] - 3 b^2 \operatorname{PolyLog}[3, -e^{2i \operatorname{ArcSin}[cx]}] \right) \end{aligned}$$

**Problem 187:** Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[cx])^2}{d - c^2 d x^2} dx$$

Optimal (type 4, 156 leaves, 8 steps):

$$\begin{aligned} & -\frac{2 i (a + b \operatorname{ArcSin}[cx])^2 \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[cx]}]}{c d} + \frac{2 i b (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[cx]}]}{c d} - \\ & \frac{2 i b (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[cx]}]}{c d} - \frac{2 b^2 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[cx]}]}{c d} + \frac{2 b^2 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[cx]}]}{c d} \end{aligned}$$

Result (type 4, 334 leaves):

$$\begin{aligned} & \frac{1}{2 c d} \left( -2 i a b \pi \operatorname{ArcSin}[cx] + 2 a b \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] + 4 a b \operatorname{ArcSin}[cx] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] + \right. \\ & 2 b^2 \operatorname{ArcSin}[cx]^2 \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] + 2 a b \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] - 4 a b \operatorname{ArcSin}[cx] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] - \\ & 2 b^2 \operatorname{ArcSin}[cx]^2 \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] - a^2 \operatorname{Log}[1 - c x] + a^2 \operatorname{Log}[1 + c x] - 2 a b \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])]]) - \\ & 2 a b \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])]]) + 4 i b (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[cx]}] - \\ & \left. 4 i b (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[cx]}] - 4 b^2 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[cx]}] + 4 b^2 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[cx]}] \right) \end{aligned}$$

### Problem 188: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[cx])^2}{x(d - c^2 d x^2)} dx$$

Optimal (type 4, 131 leaves, 9 steps):

$$\begin{aligned} & \frac{2 (a + b \operatorname{ArcSin}[cx])^2 \operatorname{ArcTanh}[e^{2i \operatorname{ArcSin}[cx]}]}{d} + \frac{i b (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, -e^{2i \operatorname{ArcSin}[cx]}]}{d} - \\ & \frac{i b (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, e^{2i \operatorname{ArcSin}[cx]}]}{d} - \frac{b^2 \operatorname{PolyLog}[3, -e^{2i \operatorname{ArcSin}[cx]}]}{2d} + \frac{b^2 \operatorname{PolyLog}[3, e^{2i \operatorname{ArcSin}[cx]}]}{2d} \end{aligned}$$

Result (type 4, 453 leaves):

$$\begin{aligned} & \frac{1}{24d} \left( -\frac{1}{2} b^2 \pi^3 - 48 \frac{1}{2} a b \pi \operatorname{ArcSin}[cx] + 16 \frac{1}{2} b^2 \operatorname{ArcSin}[cx]^3 - 96 a b \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[cx]}] - \right. \\ & 24 a b \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] - 48 a b \operatorname{ArcSin}[cx] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] + 24 a b \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] - \\ & 48 a b \operatorname{ArcSin}[cx] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] + 24 b^2 \operatorname{ArcSin}[cx]^2 \operatorname{Log}[1 - e^{-2i \operatorname{ArcSin}[cx]}] + 48 a b \operatorname{ArcSin}[cx] \operatorname{Log}[1 - e^{2i \operatorname{ArcSin}[cx]}] - \\ & 24 b^2 \operatorname{ArcSin}[cx]^2 \operatorname{Log}[1 + e^{2i \operatorname{ArcSin}[cx]}] + 24 a^2 \operatorname{Log}[cx] - 12 a^2 \operatorname{Log}[1 - c^2 x^2] + 96 a b \pi \operatorname{Log}[\operatorname{Cos}\left(\frac{1}{2} \operatorname{ArcSin}[cx]\right)] - \\ & 24 a b \pi \operatorname{Log}[-\operatorname{Cos}\left(\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right)] + 24 a b \pi \operatorname{Log}[\operatorname{Sin}\left(\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right)] + 48 \frac{1}{2} a b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[cx]}] + \\ & 48 \frac{1}{2} a b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[cx]}] + 24 \frac{1}{2} b^2 \operatorname{ArcSin}[cx] \operatorname{PolyLog}[2, e^{-2i \operatorname{ArcSin}[cx]}] + 24 \frac{1}{2} b^2 \operatorname{ArcSin}[cx] \operatorname{PolyLog}[2, -e^{2i \operatorname{ArcSin}[cx]}] - \\ & \left. 24 \frac{1}{2} a b \operatorname{PolyLog}[2, e^{2i \operatorname{ArcSin}[cx]}] + 12 b^2 \operatorname{PolyLog}[3, e^{-2i \operatorname{ArcSin}[cx]}] - 12 b^2 \operatorname{PolyLog}[3, -e^{2i \operatorname{ArcSin}[cx]}] \right) \end{aligned}$$

### Problem 189: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[cx])^2}{x^2(d - c^2 d x^2)} dx$$

Optimal (type 4, 238 leaves, 15 steps):

$$\begin{aligned} & \frac{(a + b \operatorname{ArcSin}[cx])^2}{d x} - \frac{2 i c (a + b \operatorname{ArcSin}[cx])^2 \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[cx]}]}{d} - \frac{4 b c (a + b \operatorname{ArcSin}[cx]) \operatorname{ArcTanh}[e^{i \operatorname{ArcSin}[cx]}]}{d} + \\ & \frac{2 i b^2 c \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[cx]}]}{d} + \frac{2 i b c (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[cx]}]}{d} - \frac{2 i b c (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[cx]}]}{d} - \\ & \frac{2 i b^2 c \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[cx]}]}{d} - \frac{2 b^2 c \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[cx]}]}{d} + \frac{2 b^2 c \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[cx]}]}{d} \end{aligned}$$

Result (type 4, 537 leaves):

$$\begin{aligned}
& -\frac{1}{2 d x} \\
& \left( 2 a^2 + 4 a b \operatorname{ArcSin}[c x] + 2 i a b c \pi x \operatorname{ArcSin}[c x] + 2 b^2 \operatorname{ArcSin}[c x]^2 - 4 b^2 c x \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - e^{i \operatorname{ArcSin}[c x]}\right] - 2 a b c \pi x \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[c x]}\right] - \right. \\
& \quad 4 a b c x \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[c x]}\right] - 2 b^2 c x \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[c x]}\right] - 2 a b c \pi x \operatorname{Log}\left[1 + i e^{i \operatorname{ArcSin}[c x]}\right] + \\
& \quad 4 a b c x \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + i e^{i \operatorname{ArcSin}[c x]}\right] + 2 b^2 c x \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + i e^{i \operatorname{ArcSin}[c x]}\right] + 4 b^2 c x \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + e^{i \operatorname{ArcSin}[c x]}\right] - \\
& \quad 4 a b c x \operatorname{Log}[c x] + a^2 c x \operatorname{Log}[1 - c x] - a^2 c x \operatorname{Log}[1 + c x] + 4 a b c x \operatorname{Log}\left[1 + \sqrt{1 - c^2 x^2}\right] + 2 a b c \pi x \operatorname{Log}\left[-\cos\left(\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right)\right] + \\
& \quad 2 a b c \pi x \operatorname{Log}\left[\sin\left(\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right)\right] - 4 i b^2 c x \operatorname{PolyLog}\left[2, -e^{i \operatorname{ArcSin}[c x]}\right] - 4 i b c x (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}\left[2, -i e^{i \operatorname{ArcSin}[c x]}\right] + \\
& \quad 4 i a b c x \operatorname{PolyLog}\left[2, i e^{i \operatorname{ArcSin}[c x]}\right] + 4 i b^2 c x \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, i e^{i \operatorname{ArcSin}[c x]}\right] + \\
& \quad \left. 4 i b^2 c x \operatorname{PolyLog}\left[2, e^{i \operatorname{ArcSin}[c x]}\right] + 4 b^2 c x \operatorname{PolyLog}\left[3, -i e^{i \operatorname{ArcSin}[c x]}\right] - 4 b^2 c x \operatorname{PolyLog}\left[3, i e^{i \operatorname{ArcSin}[c x]}\right] \right)
\end{aligned}$$

**Problem 190:** Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^2}{x^3 (d - c^2 d x^2)} dx$$

Optimal (type 4, 210 leaves, 12 steps) :

$$\begin{aligned}
& \frac{b c \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])}{d x} - \frac{(a + b \operatorname{ArcSin}[c x])^2}{2 d x^2} - \\
& \frac{2 c^2 (a + b \operatorname{ArcSin}[c x])^2 \operatorname{ArcTanh}\left[e^{2 i \operatorname{ArcSin}[c x]}\right]}{d} + \frac{b^2 c^2 \operatorname{Log}[x]}{d} + \frac{i b c^2 (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}\left[2, -e^{2 i \operatorname{ArcSin}[c x]}\right]}{d} - \\
& \frac{i b c^2 (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}\left[2, e^{2 i \operatorname{ArcSin}[c x]}\right]}{d} - \frac{b^2 c^2 \operatorname{PolyLog}\left[3, -e^{2 i \operatorname{ArcSin}[c x]}\right]}{2 d} + \frac{b^2 c^2 \operatorname{PolyLog}\left[3, e^{2 i \operatorname{ArcSin}[c x]}\right]}{2 d}
\end{aligned}$$

Result (type 4, 614 leaves) :

$$\begin{aligned}
& -\frac{1}{2d} \left( \frac{1}{12} \pm b^2 c^2 \pi^3 + \frac{a^2}{x^2} + \frac{2ab\sqrt{1-c^2x^2}}{x} + 4 \pm abc^2 \pi \operatorname{ArcSin}[cx] + \frac{2ab \operatorname{ArcSin}[cx]}{x^2} + \frac{2b^2 c \sqrt{1-c^2x^2} \operatorname{ArcSin}[cx]}{x} + \frac{b^2 \operatorname{ArcSin}[cx]^2}{x^2} - \right. \\
& \quad \frac{4}{3} \pm b^2 c^2 \operatorname{ArcSin}[cx]^3 + 8abc^2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[cx]}] + 2abc^2 \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] + 4abc^2 \operatorname{ArcSin}[cx] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] - \\
& \quad 2abc^2 \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] + 4abc^2 \operatorname{ArcSin}[cx] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] - 2b^2 c^2 \operatorname{ArcSin}[cx]^2 \operatorname{Log}[1 - e^{-2i \operatorname{ArcSin}[cx]}] - \\
& \quad 4abc^2 \operatorname{ArcSin}[cx] \operatorname{Log}[1 - e^{2i \operatorname{ArcSin}[cx]}] + 2b^2 c^2 \operatorname{ArcSin}[cx]^2 \operatorname{Log}[1 + e^{2i \operatorname{ArcSin}[cx]}] - 2a^2 c^2 \operatorname{Log}[x] - 2b^2 c^2 \operatorname{Log}[cx] + \\
& \quad a^2 c^2 \operatorname{Log}[1 - c^2 x^2] - 8abc^2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[cx]]] + 2abc^2 \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])]] - \\
& \quad 2abc^2 \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])]] - 4 \pm abc^2 \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[cx]}] - 4 \pm abc^2 \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[cx]}] - \\
& \quad 2 \pm b^2 c^2 \operatorname{ArcSin}[cx] \operatorname{PolyLog}[2, e^{-2i \operatorname{ArcSin}[cx]}] - 2 \pm b^2 c^2 \operatorname{ArcSin}[cx] \operatorname{PolyLog}[2, -e^{2i \operatorname{ArcSin}[cx]}] + \\
& \quad \left. 2 \pm abc^2 \operatorname{PolyLog}[2, e^{2i \operatorname{ArcSin}[cx]}] - b^2 c^2 \operatorname{PolyLog}[3, e^{-2i \operatorname{ArcSin}[cx]}] + b^2 c^2 \operatorname{PolyLog}[3, -e^{2i \operatorname{ArcSin}[cx]}] \right)
\end{aligned}$$

**Problem 191:** Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[cx])^2}{x^4 (d - c^2 d x^2)} dx$$

Optimal (type 4, 333 leaves, 24 steps):

$$\begin{aligned}
& \frac{b^2 c^2}{3dx} - \frac{bc\sqrt{1-c^2x^2}(a+b\operatorname{ArcSin}[cx])}{3dx^2} - \frac{(a+b\operatorname{ArcSin}[cx])^2}{3dx^3} - \frac{c^2(a+b\operatorname{ArcSin}[cx])^2}{dx} - \\
& \frac{2\pm c^3(a+b\operatorname{ArcSin}[cx])^2 \operatorname{ArcTan}[e^{i\operatorname{ArcSin}[cx]}]}{d} - \frac{14b^3(a+b\operatorname{ArcSin}[cx]) \operatorname{ArcTanh}[e^{i\operatorname{ArcSin}[cx]}]}{3d} + \frac{7\pm b^2 c^3 \operatorname{PolyLog}[2, -e^{i\operatorname{ArcSin}[cx]}]}{3d} + \\
& \frac{2\pm b^3(a+b\operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, -i e^{i\operatorname{ArcSin}[cx]}]}{d} - \frac{2\pm b^3(a+b\operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, i e^{i\operatorname{ArcSin}[cx]}]}{d} - \\
& \frac{7\pm b^2 c^3 \operatorname{PolyLog}[2, e^{i\operatorname{ArcSin}[cx]}]}{3d} - \frac{2b^2 c^3 \operatorname{PolyLog}[3, -i e^{i\operatorname{ArcSin}[cx]}]}{d} + \frac{2b^2 c^3 \operatorname{PolyLog}[3, i e^{i\operatorname{ArcSin}[cx]}]}{d}
\end{aligned}$$

Result (type 4, 868 leaves):

$$\begin{aligned}
& - \frac{a^2}{3 d x^3} - \frac{a^2 c^2}{d x} - \frac{a^2 c^3 \operatorname{Log}[1 - c x]}{2 d} + \frac{a^2 c^3 \operatorname{Log}[1 + c x]}{2 d} - \\
& \frac{1}{d} \frac{2 a b}{6 x^2} \left( \frac{c \sqrt{1 - c^2 x^2}}{6 x^2} + \frac{\operatorname{ArcSin}[c x]}{3 x^3} - \frac{1}{6} c^3 \operatorname{Log}[x] + \frac{1}{6} c^3 \operatorname{Log}[1 + \sqrt{1 - c^2 x^2}] - c^2 \left( - \frac{\operatorname{ArcSin}[c x]}{x} + c \operatorname{Log}[x] - c \operatorname{Log}[1 + \sqrt{1 - c^2 x^2}] \right) + \right. \\
& \frac{1}{2} \frac{c^4}{c} \left( \frac{3 i \pi \operatorname{ArcSin}[c x]}{2 c} - \frac{i \operatorname{ArcSin}[c x]^2}{2 c} + \frac{2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}]}{c} - \frac{\pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}]}{c} + \frac{2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}]}{c} - \right. \\
& \frac{2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]]}{c} + \frac{\pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]}{c} - \frac{2 i \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{c} \Big) - \\
& \frac{1}{2} \frac{c^4}{c} \left( \frac{i \pi \operatorname{ArcSin}[c x]}{2 c} - \frac{i \operatorname{ArcSin}[c x]^2}{2 c} + \frac{2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}]}{c} + \frac{\pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}]}{c} + \frac{2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}]}{c} - \right. \\
& \left. \frac{2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]]}{c} - \frac{\pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]}{c} - \frac{2 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{c} \right) - \\
& \frac{1}{24 d} b^2 c^3 \left( 4 \operatorname{Cot}[\frac{1}{2} \operatorname{ArcSin}[c x]] + 14 \operatorname{ArcSin}[c x]^2 \operatorname{Cot}[\frac{1}{2} \operatorname{ArcSin}[c x]] + 2 \operatorname{ArcSin}[c x] \operatorname{Csc}[\frac{1}{2} \operatorname{ArcSin}[c x]]^2 + \right. \\
& \frac{1}{2} c x \operatorname{ArcSin}[c x]^2 \operatorname{Csc}[\frac{1}{2} \operatorname{ArcSin}[c x]]^4 - 56 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - e^{i \operatorname{ArcSin}[c x]}] - 24 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + \\
& 24 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + 56 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + e^{i \operatorname{ArcSin}[c x]}] - 56 i \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c x]}] - \\
& 48 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] + 48 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] + 56 i \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c x]}] + \\
& 48 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[c x]}] - 48 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[c x]}] - 2 \operatorname{ArcSin}[c x] \operatorname{Sec}[\frac{1}{2} \operatorname{ArcSin}[c x]]^2 + \\
& \left. \frac{8 \operatorname{ArcSin}[c x]^2 \operatorname{Sin}[\frac{1}{2} \operatorname{ArcSin}[c x]]^4}{c^3 x^3} + 4 \operatorname{Tan}[\frac{1}{2} \operatorname{ArcSin}[c x]] + 14 \operatorname{ArcSin}[c x]^2 \operatorname{Tan}[\frac{1}{2} \operatorname{ArcSin}[c x]] \right)
\end{aligned}$$

**Problem 192: Result more than twice size of optimal antiderivative.**

$$\int \frac{x^4 (a + b \operatorname{ArcSin}[c x])^2}{(d - c^2 d x^2)^2} dx$$

Optimal (type 4, 300 leaves, 15 steps):

$$\begin{aligned}
& -\frac{2 b^2 x}{c^4 d^2} - \frac{b (a + b \operatorname{ArcSin}[c x])}{c^5 d^2 \sqrt{1 - c^2 x^2}} + \frac{2 b \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])}{c^5 d^2} + \frac{3 x (a + b \operatorname{ArcSin}[c x])^2}{2 c^4 d^2} + \frac{x^3 (a + b \operatorname{ArcSin}[c x])^2}{2 c^2 d^2 (1 - c^2 x^2)} + \\
& \frac{3 i (a + b \operatorname{ArcSin}[c x])^2 \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[c x]}]}{c^5 d^2} + \frac{b^2 \operatorname{ArcTanh}[c x]}{c^5 d^2} - \frac{3 i b (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{c^5 d^2} + \\
& \frac{3 i b (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{c^5 d^2} + \frac{3 b^2 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[c x]}]}{c^5 d^2} - \frac{3 b^2 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[c x]}]}{c^5 d^2}
\end{aligned}$$

Result (type 4, 1081 leaves):

$$\begin{aligned}
& \frac{a^2 x}{c^4 d^2} - \frac{a^2 x}{2 c^4 d^2 (-1 + c^2 x^2)} + \frac{3 a^2 \operatorname{Log}[1 - c x]}{4 c^5 d^2} - \frac{3 a^2 \operatorname{Log}[1 + c x]}{4 c^5 d^2} + \\
& \frac{1}{d^2} 2 a b \left( \frac{\sqrt{1 - c^2 x^2} - \operatorname{ArcSin}[c x]}{4 c^5 (-1 + c x)} - \frac{\sqrt{1 - c^2 x^2} + \operatorname{ArcSin}[c x]}{4 c^4 (c + c^2 x)} + \frac{\sqrt{1 - c^2 x^2} + c x \operatorname{ArcSin}[c x]}{c^5} + \frac{1}{4 c^4} \right. \\
& 3 \left( \frac{3 i \pi \operatorname{ArcSin}[c x]}{2 c} - \frac{i \operatorname{ArcSin}[c x]^2}{2 c} + \frac{2 \pi \operatorname{Log}[1 + e^{-i} \operatorname{ArcSin}[c x]]}{c} - \frac{\pi \operatorname{Log}[1 + i e^i \operatorname{ArcSin}[c x]]}{c} + \frac{2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^i \operatorname{ArcSin}[c x]]}{c} - \right. \\
& \frac{2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]]}{c} + \frac{\pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]}{c} - \frac{2 i \operatorname{PolyLog}[2, -i e^i \operatorname{ArcSin}[c x]]}{c} \Big) - \frac{1}{4 c^4} \\
& 3 \left( \frac{i \pi \operatorname{ArcSin}[c x]}{2 c} - \frac{i \operatorname{ArcSin}[c x]^2}{2 c} + \frac{2 \pi \operatorname{Log}[1 + e^{-i} \operatorname{ArcSin}[c x]]}{c} + \frac{\pi \operatorname{Log}[1 - i e^i \operatorname{ArcSin}[c x]]}{c} + \frac{2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^i \operatorname{ArcSin}[c x]]}{c} - \right. \\
& \frac{2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]]}{c} - \frac{\pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]}{c} - \frac{2 i \operatorname{PolyLog}[2, i e^i \operatorname{ArcSin}[c x]]}{c} \Big) + \\
& \frac{1}{c^5 d^2} b^2 \left( \frac{\operatorname{ArcSin}[c x] + \frac{c x (2 (-1 + \operatorname{ArcSin}[c x]^2) + (-2 + \operatorname{ArcSin}[c x]^2) \cos[2 \operatorname{ArcSin}[c x]])}{\sqrt{1 - c^2 x^2}} + \frac{\operatorname{ArcSin}[c x] \cos[3 \operatorname{ArcSin}[c x]]}{\sqrt{1 - c^2 x^2}}}{2 \sqrt{1 - c^2 x^2}} + \right. \\
& \frac{1}{2} \left( -3 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 - i e^i \operatorname{ArcSin}[c x]] + 3 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 + i e^i \operatorname{ArcSin}[c x]] - \right. \\
& 3 \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[\left(-\frac{1}{2} - \frac{i}{2}\right) e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} (-i + e^i \operatorname{ArcSin}[c x])\right] + 3 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} (-i + e^i \operatorname{ArcSin}[c x])\right] - \\
& 3 \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} ((1 + i) + (1 - i) e^i \operatorname{ArcSin}[c x])\right] - 3 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} ((1 + i) + (1 - i) e^i \operatorname{ArcSin}[c x])\right] - \\
& 2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \operatorname{Sin}[\frac{1}{2} \operatorname{ArcSin}[c x]] - 3 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \operatorname{Sin}[\frac{1}{2} \operatorname{ArcSin}[c x]] + \\
& 3 \pi \operatorname{ArcSin}[c x] \operatorname{Log}[-\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \operatorname{Sin}[\frac{1}{2} \operatorname{ArcSin}[c x]] + 2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \operatorname{Sin}[\frac{1}{2} \operatorname{ArcSin}[c x]] + 3 \pi \operatorname{ArcSin}[c x] \\
& \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \operatorname{Sin}[\frac{1}{2} \operatorname{ArcSin}[c x]] + 3 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \operatorname{Sin}[\frac{1}{2} \operatorname{ArcSin}[c x]] - 6 i \operatorname{ArcSin}[c x] \\
& \operatorname{PolyLog}[2, -i e^i \operatorname{ArcSin}[c x]] + 6 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, i e^i \operatorname{ArcSin}[c x]] + 6 \operatorname{PolyLog}[3, -i e^i \operatorname{ArcSin}[c x]] - 6 \operatorname{PolyLog}[3, i e^i \operatorname{ArcSin}[c x]] \Big) \Big)
\end{aligned}$$

Problem 193: Result more than twice size of optimal antiderivative.

$$\int \frac{x^3 (a + b \operatorname{ArcSin}[c x])^2}{(d - c^2 d x^2)^2} dx$$

Optimal (type 4, 227 leaves, 10 steps):

$$\begin{aligned} & \frac{b x (a + b \operatorname{ArcSin}[c x])}{c^3 d^2 \sqrt{1 - c^2 x^2}} + \frac{(a + b \operatorname{ArcSin}[c x])^2}{2 c^4 d^2} + \frac{x^2 (a + b \operatorname{ArcSin}[c x])^2}{2 c^2 d^2 (1 - c^2 x^2)} - \frac{i (a + b \operatorname{ArcSin}[c x])^3}{3 b c^4 d^2} + \frac{(a + b \operatorname{ArcSin}[c x])^2 \operatorname{Log}[1 + e^{2i \operatorname{ArcSin}[c x]}]}{c^4 d^2} - \\ & \frac{b^2 \operatorname{Log}[1 - c^2 x^2]}{2 c^4 d^2} - \frac{i b (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, -e^{2i \operatorname{ArcSin}[c x]}]}{c^4 d^2} + \frac{b^2 \operatorname{PolyLog}[3, -e^{2i \operatorname{ArcSin}[c x]}]}{2 c^4 d^2} \end{aligned}$$

Result (type 4, 502 leaves):

$$\begin{aligned} & \frac{1}{6 c^4 d^2} \left( \frac{3 a b \sqrt{1 - c^2 x^2}}{-1 + c x} + \frac{3 a b \sqrt{1 - c^2 x^2}}{1 + c x} - \frac{3 a^2}{-1 + c^2 x^2} + 12 i a b \pi \operatorname{ArcSin}[c x] - \frac{3 a b \operatorname{ArcSin}[c x]}{-1 + c x} + \frac{3 a b \operatorname{ArcSin}[c x]}{1 + c x} - \frac{6 b^2 c x \operatorname{ArcSin}[c x]}{\sqrt{1 - c^2 x^2}} - \right. \\ & 6 i a b \operatorname{ArcSin}[c x]^2 + \frac{3 b^2 \operatorname{ArcSin}[c x]^2}{1 - c^2 x^2} - 2 i b^2 \operatorname{ArcSin}[c x]^3 + 24 a b \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] + 6 a b \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + \\ & 12 a b \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - 6 a b \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + 12 a b \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + \\ & 6 b^2 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 + e^{2i \operatorname{ArcSin}[c x]}] + 3 a^2 \operatorname{Log}[1 - c^2 x^2] - 3 b^2 \operatorname{Log}[1 - c^2 x^2] - 24 a b \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \\ & 6 a b \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]) - 6 a b \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]) - 12 i a b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] - \\ & \left. 12 i a b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] - 6 i b^2 \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, -e^{2i \operatorname{ArcSin}[c x]}] + 3 b^2 \operatorname{PolyLog}[3, -e^{2i \operatorname{ArcSin}[c x]}] \right) \end{aligned}$$

Problem 194: Result more than twice size of optimal antiderivative.

$$\int \frac{x^2 (a + b \operatorname{ArcSin}[c x])^2}{(d - c^2 d x^2)^2} dx$$

Optimal (type 4, 233 leaves, 11 steps):

$$\begin{aligned}
& - \frac{b(a + b \operatorname{ArcSin}[cx])}{c^3 d^2 \sqrt{1 - c^2 x^2}} + \frac{x(a + b \operatorname{ArcSin}[cx])^2}{2 c^2 d^2 (1 - c^2 x^2)} + \frac{i (a + b \operatorname{ArcSin}[cx])^2 \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[cx]}]}{c^3 d^2} + \\
& \frac{b^2 \operatorname{ArcTanh}[cx]}{c^3 d^2} - \frac{i b (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[cx]}]}{c^3 d^2} + \\
& \frac{i b (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[cx]}]}{c^3 d^2} + \frac{b^2 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[cx]}]}{c^3 d^2} - \frac{b^2 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[cx]}]}{c^3 d^2}
\end{aligned}$$

Result (type 4, 839 leaves):

$$\begin{aligned}
& - \frac{1}{4 c^3 d^2} \left( - \frac{2 a b \sqrt{1 - c^2 x^2}}{-1 + c x} + \frac{2 a b \sqrt{1 - c^2 x^2}}{1 + c x} + \frac{2 a^2 c x}{-1 + c^2 x^2} - 2 i a b \pi \operatorname{ArcSin}[cx] + \frac{2 a b \operatorname{ArcSin}[cx]}{-1 + c x} + \frac{2 a b \operatorname{ArcSin}[cx]}{1 + c x} + \frac{4 b^2 \operatorname{ArcSin}[cx]}{\sqrt{1 - c^2 x^2}} + \right. \\
& \frac{2 b^2 c x \operatorname{ArcSin}[cx]^2}{-1 + c^2 x^2} + 2 a b \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] + 4 a b \operatorname{ArcSin}[cx] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] + 2 b^2 \operatorname{ArcSin}[cx]^2 \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] + \\
& 2 a b \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] - 4 a b \operatorname{ArcSin}[cx] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] - 2 b^2 \operatorname{ArcSin}[cx]^2 \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] + \\
& 2 b^2 \pi \operatorname{ArcSin}[cx] \operatorname{Log}\left[\left(-\frac{1}{2} - \frac{i}{2}\right) e^{-\frac{1}{2} i \operatorname{ArcSin}[cx]} (-i + e^{i \operatorname{ArcSin}[cx]})\right] - 2 b^2 \operatorname{ArcSin}[cx]^2 \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) e^{-\frac{1}{2} i \operatorname{ArcSin}[cx]} (-i + e^{i \operatorname{ArcSin}[cx]})\right] + \\
& 2 b^2 \pi \operatorname{ArcSin}[cx] \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[cx]} ((1 + i) + (1 - i) e^{i \operatorname{ArcSin}[cx]})\right] + 2 b^2 \operatorname{ArcSin}[cx]^2 \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[cx]} ((1 + i) + (1 - i) e^{i \operatorname{ArcSin}[cx]})\right] - \\
& a^2 \operatorname{Log}[1 - c x] + a^2 \operatorname{Log}[1 + c x] - 2 a b \pi \operatorname{Log}[-\operatorname{Cos}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right]] + \\
& 4 b^2 \operatorname{Log}[\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] - \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] + 2 b^2 \operatorname{ArcSin}[cx]^2 \operatorname{Log}[\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] - \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] - \\
& 2 b^2 \pi \operatorname{ArcSin}[cx] \operatorname{Log}[-\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] + \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] - 4 b^2 \operatorname{Log}[\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] + \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] - \\
& 2 b^2 \pi \operatorname{ArcSin}[cx] \operatorname{Log}[\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] + \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] - 2 b^2 \operatorname{ArcSin}[cx]^2 \operatorname{Log}[\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] + \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] - \\
& 2 a b \pi \operatorname{Log}[\operatorname{Sin}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right]] + 4 i b (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[cx]}] - \\
& \left. 4 i b (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[cx]}] - 4 b^2 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[cx]}] + 4 b^2 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[cx]}] \right)
\end{aligned}$$

Problem 196: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[cx])^2}{(d - c^2 d x^2)^2} dx$$

Optimal (type 4, 230 leaves, 11 steps):

$$\begin{aligned}
& -\frac{b(a+b \operatorname{ArcSin}[cx])}{c d^2 \sqrt{1-c^2 x^2}} + \frac{x(a+b \operatorname{ArcSin}[cx])^2}{2 d^2 (1-c^2 x^2)} - \frac{i(a+b \operatorname{ArcSin}[cx])^2 \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[cx]}]}{c d^2} + \\
& \frac{b^2 \operatorname{ArcTanh}[cx]}{c d^2} + \frac{i b(a+b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[cx]}]}{c d^2} - \\
& \frac{i b(a+b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[cx]}]}{c d^2} - \frac{b^2 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[cx]}]}{c d^2} + \frac{b^2 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[cx]}]}{c d^2}
\end{aligned}$$

Result (type 4, 810 leaves):

$$\begin{aligned}
& \frac{1}{4 d^2} \left( -\frac{2 a^2 x}{-1+c^2 x^2} - \frac{a^2 \operatorname{Log}[1-cx]}{c} + \frac{a^2 \operatorname{Log}[1+cx]}{c} + \right. \\
& \frac{1}{c} 2 a b \left( \frac{\sqrt{1-c^2 x^2}}{-1+cx} - \frac{\sqrt{1-c^2 x^2}}{1+cx} - \frac{i \pi \operatorname{ArcSin}[cx]}{1-cx} + \frac{\operatorname{ArcSin}[cx]}{1-cx} - \frac{\operatorname{ArcSin}[cx]}{1+cx} + \pi \operatorname{Log}[1-i e^{i \operatorname{ArcSin}[cx]}] + 2 \operatorname{ArcSin}[cx] \operatorname{Log}[1-i e^{i \operatorname{ArcSin}[cx]}] + \right. \\
& \pi \operatorname{Log}[1+i e^{i \operatorname{ArcSin}[cx]}] - 2 \operatorname{ArcSin}[cx] \operatorname{Log}[1+i e^{i \operatorname{ArcSin}[cx]}] - \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])]] - \\
& \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])]] + 2 i \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[cx]}] - 2 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[cx]}] \Big) + \\
& \frac{1}{c} 2 b^2 \left( -\frac{2 \operatorname{ArcSin}[cx]}{\sqrt{1-c^2 x^2}} + \frac{c x \operatorname{ArcSin}[cx]^2}{1-c^2 x^2} + \operatorname{ArcSin}[cx]^2 \operatorname{Log}[1-i e^{i \operatorname{ArcSin}[cx]}] - \operatorname{ArcSin}[cx]^2 \operatorname{Log}[1+i e^{i \operatorname{ArcSin}[cx]}] + \right. \\
& \pi \operatorname{ArcSin}[cx] \operatorname{Log}\left[ \left( -\frac{1}{2} - \frac{i}{2} \right) e^{-\frac{1}{2} i \operatorname{ArcSin}[cx]} (-i + e^{i \operatorname{ArcSin}[cx]}) \right] - \operatorname{ArcSin}[cx]^2 \operatorname{Log}\left[ \left( \frac{1}{2} + \frac{i}{2} \right) e^{-\frac{1}{2} i \operatorname{ArcSin}[cx]} (-i + e^{i \operatorname{ArcSin}[cx]}) \right] + \\
& \pi \operatorname{ArcSin}[cx] \operatorname{Log}\left[ \frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[cx]} ((1+i) + (1-i) e^{i \operatorname{ArcSin}[cx]}) \right] + \\
& \operatorname{ArcSin}[cx]^2 \operatorname{Log}\left[ \frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[cx]} ((1+i) + (1-i) e^{i \operatorname{ArcSin}[cx]}) \right] - 2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[cx]] - \sin[\frac{1}{2} \operatorname{ArcSin}[cx]]] + \\
& \operatorname{ArcSin}[cx]^2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[cx]] - \sin[\frac{1}{2} \operatorname{ArcSin}[cx]]] - \pi \operatorname{ArcSin}[cx] \operatorname{Log}[-\cos[\frac{1}{2} \operatorname{ArcSin}[cx]] + \sin[\frac{1}{2} \operatorname{ArcSin}[cx]]] + \\
& 2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[cx]] + \sin[\frac{1}{2} \operatorname{ArcSin}[cx]]] - \pi \operatorname{ArcSin}[cx] \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[cx]] + \sin[\frac{1}{2} \operatorname{ArcSin}[cx]]] - \\
& \operatorname{ArcSin}[cx]^2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[cx]] + \sin[\frac{1}{2} \operatorname{ArcSin}[cx]]] + 2 i \operatorname{ArcSin}[cx] \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[cx]}] - \\
& \left. 2 i \operatorname{ArcSin}[cx] \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[cx]}] - 2 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[cx]}] + 2 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[cx]}] \right)
\end{aligned}$$

### Problem 197: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[cx])^2}{x (d - c^2 dx^2)^2} dx$$

Optimal (type 4, 211 leaves, 12 steps):

$$\begin{aligned} & -\frac{b c x (a + b \operatorname{ArcSin}[cx])}{d^2 \sqrt{1 - c^2 x^2}} + \frac{(a + b \operatorname{ArcSin}[cx])^2}{2 d^2 (1 - c^2 x^2)} - \frac{2 (a + b \operatorname{ArcSin}[cx])^2 \operatorname{ArcTanh}[e^{2 i \operatorname{ArcSin}[cx]}]}{d^2} - \\ & \frac{b^2 \operatorname{Log}[1 - c^2 x^2]}{2 d^2} + \frac{i b (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, -e^{2 i \operatorname{ArcSin}[cx]}]}{d^2} - \\ & \frac{i b (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}[cx]}]}{d^2} - \frac{b^2 \operatorname{PolyLog}[3, -e^{2 i \operatorname{ArcSin}[cx]}]}{2 d^2} + \frac{b^2 \operatorname{PolyLog}[3, e^{2 i \operatorname{ArcSin}[cx]}]}{2 d^2} \end{aligned}$$

Result (type 4, 612 leaves):

$$\begin{aligned} & \frac{1}{2 d^2} \left( -\frac{1}{12} i b^2 \pi^3 + \frac{a^2}{1 - c^2 x^2} + \frac{a b \sqrt{1 - c^2 x^2}}{-1 + c x} + \frac{a b \sqrt{1 - c^2 x^2}}{1 + c x} - 4 i a b \pi \operatorname{ArcSin}[c x] + \frac{a b \operatorname{ArcSin}[c x]}{1 - c x} + \frac{a b \operatorname{ArcSin}[c x]}{1 + c x} - \frac{2 b^2 c x \operatorname{ArcSin}[c x]}{\sqrt{1 - c^2 x^2}} + \right. \\ & \frac{b^2 \operatorname{ArcSin}[c x]^2}{1 - c^2 x^2} + \frac{4}{3} i b^2 \operatorname{ArcSin}[c x]^3 - 8 a b \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] - 2 a b \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - 4 a b \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + \\ & 2 a b \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - 4 a b \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + 2 b^2 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 - e^{-2 i \operatorname{ArcSin}[c x]}] + \\ & 4 a b \operatorname{ArcSin}[c x] \operatorname{Log}[1 - e^{2 i \operatorname{ArcSin}[c x]}] - 2 b^2 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 + e^{2 i \operatorname{ArcSin}[c x]}] + 2 a^2 \operatorname{Log}[c x] - a^2 \operatorname{Log}[1 - c^2 x^2] - b^2 \operatorname{Log}[1 - c^2 x^2] + \\ & 8 a b \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - 2 a b \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]) + 2 a b \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]) + \\ & 4 i a b \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] + 4 i a b \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] + 2 i b^2 \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, e^{-2 i \operatorname{ArcSin}[c x]}] + \\ & \left. 2 i b^2 \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, -e^{2 i \operatorname{ArcSin}[c x]}] - 2 i a b \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}[c x]}] + b^2 \operatorname{PolyLog}[3, e^{-2 i \operatorname{ArcSin}[c x]}] - b^2 \operatorname{PolyLog}[3, -e^{2 i \operatorname{ArcSin}[c x]}] \right) \end{aligned}$$

### Problem 198: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[cx])^2}{x^2 (d - c^2 dx^2)^2} dx$$

Optimal (type 4, 324 leaves, 20 steps):

$$\begin{aligned}
& - \frac{b c (a + b \operatorname{ArcSin}[c x])}{d^2 \sqrt{1 - c^2 x^2}} - \frac{(a + b \operatorname{ArcSin}[c x])^2}{d^2 (1 - c^2 x^2)} + \frac{3 c^2 x (a + b \operatorname{ArcSin}[c x])^2}{2 d^2 (1 - c^2 x^2)} - \frac{3 i c (a + b \operatorname{ArcSin}[c x])^2 \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[c x]}]}{d^2} \\
& + \frac{4 b c (a + b \operatorname{ArcSin}[c x]) \operatorname{ArcTanh}[e^{i \operatorname{ArcSin}[c x]}]}{d^2} + \frac{b^2 c \operatorname{ArcTanh}[c x]}{d^2} + \frac{2 i b^2 c \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c x]}]}{d^2} + \\
& \frac{3 i b c (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{d^2} - \frac{3 i b c (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{d^2} - \\
& \frac{2 i b^2 c \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c x]}]}{d^2} - \frac{3 b^2 c \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[c x]}]}{d^2} + \frac{3 b^2 c \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[c x]}]}{d^2}
\end{aligned}$$

Result (type 4, 1175 leaves) :

$$\begin{aligned}
& -\frac{a^2}{d^2 x} - \frac{a^2 c^2 x}{2 d^2 (-1 + c^2 x^2)} - \frac{3 a^2 c \operatorname{Log}[1 - c x]}{4 d^2} + \frac{3 a^2 c \operatorname{Log}[1 + c x]}{4 d^2} + \\
& \frac{1}{d^2} \frac{2 a b c}{2} \left( \frac{\sqrt{1 - c^2 x^2} - \operatorname{ArcSin}[c x]}{4 (-1 + c x)} - \frac{\operatorname{ArcSin}[c x]}{c x} - \frac{\sqrt{1 - c^2 x^2} + \operatorname{ArcSin}[c x]}{4 (1 + c x)} + \operatorname{Log}[c x] - \operatorname{Log}[1 + \sqrt{1 - c^2 x^2}] \right) - \\
& \frac{3}{4} \left( \frac{3}{2} \frac{i \pi \operatorname{ArcSin}[c x]}{2} - \frac{1}{2} i \operatorname{ArcSin}[c x]^2 + 2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] - \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + 2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - \right. \\
& 2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] - 2 i \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] \Big) + \\
& \frac{3}{4} \left( \frac{1}{2} \frac{i \pi \operatorname{ArcSin}[c x]}{2} - \frac{1}{2} i \operatorname{ArcSin}[c x]^2 + 2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] + \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + 2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - \right. \\
& 2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] - 2 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] \Big) + \\
& \frac{1}{4 d^2} b^2 c \left( -4 \operatorname{ArcSin}[c x] - 2 \operatorname{ArcSin}[c x]^2 \operatorname{Cot}[\frac{1}{2} \operatorname{ArcSin}[c x]] + 8 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - e^{i \operatorname{ArcSin}[c x]}] + 6 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - \right. \\
& 6 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + 6 \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[\left(-\frac{1}{2} - \frac{i}{2}\right) e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} (-i + e^{i \operatorname{ArcSin}[c x]})\right] - \\
& 6 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} (-i + e^{i \operatorname{ArcSin}[c x]})\right] - 8 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + e^{i \operatorname{ArcSin}[c x]}] + \\
& 6 \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} ((1 + i) + (1 - i) e^{i \operatorname{ArcSin}[c x]})\right] + 6 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} ((1 + i) + (1 - i) e^{i \operatorname{ArcSin}[c x]})\right] - \\
& 4 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] + 6 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] - \\
& 6 \pi \operatorname{ArcSin}[c x] \operatorname{Log}[-\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] + 4 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \\
& 6 \pi \operatorname{ArcSin}[c x] \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] - 6 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \\
& 8 i \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c x]}] + 12 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] - 12 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] - \\
& 8 i \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c x]}] - 12 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[c x]}] + 12 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[c x]}] + \\
& \frac{\operatorname{ArcSin}[c x]^2}{\left(\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]\right)^2} - \frac{4 \operatorname{ArcSin}[c x] \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]}{\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]} - \\
& \frac{\operatorname{ArcSin}[c x]^2}{\left(\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]\right)^2} + \frac{4 \operatorname{ArcSin}[c x] \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]}{\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]} - 2 \operatorname{ArcSin}[c x]^2 \operatorname{Tan}[\frac{1}{2} \operatorname{ArcSin}[c x]]
\end{aligned}$$

### Problem 199: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[cx])^2}{x^3 (d - c^2 d x^2)^2} dx$$

Optimal (type 4, 270 leaves, 17 steps):

$$\begin{aligned} & \frac{b c (a + b \operatorname{ArcSin}[cx])}{d^2 x \sqrt{1 - c^2 x^2}} + \frac{c^2 (a + b \operatorname{ArcSin}[cx])^2}{d^2 (1 - c^2 x^2)} - \frac{(a + b \operatorname{ArcSin}[cx])^2}{2 d^2 x^2 (1 - c^2 x^2)} - \frac{4 c^2 (a + b \operatorname{ArcSin}[cx])^2 \operatorname{ArcTanh}[e^{2i \operatorname{ArcSin}[cx]}]}{d^2} + \\ & \frac{b^2 c^2 \operatorname{Log}[x]}{d^2} - \frac{b^2 c^2 \operatorname{Log}[1 - c^2 x^2]}{2 d^2} + \frac{2 i b c^2 (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, -e^{2i \operatorname{ArcSin}[cx]}]}{d^2} - \\ & \frac{2 i b c^2 (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[2, e^{2i \operatorname{ArcSin}[cx]}]}{d^2} - \frac{b^2 c^2 \operatorname{PolyLog}[3, -e^{2i \operatorname{ArcSin}[cx]}]}{d^2} + \frac{b^2 c^2 \operatorname{PolyLog}[3, e^{2i \operatorname{ArcSin}[cx]}]}{d^2} \end{aligned}$$

Result (type 4, 759 leaves):

$$\begin{aligned} & \frac{1}{2 d^2} \left( -\frac{a^2}{x^2} + \frac{a^2 c^2}{1 - c^2 x^2} - \frac{2 a b c \sqrt{1 - c^2 x^2}}{x} + \frac{a b c^2 \sqrt{1 - c^2 x^2}}{-1 + c x} + \frac{a b c^2 \sqrt{1 - c^2 x^2}}{1 + c x} - 8 i a b c^2 \pi \operatorname{ArcSin}[cx] - \frac{2 a b \operatorname{ArcSin}[cx]}{x^2} + \right. \\ & \frac{a b c^2 \operatorname{ArcSin}[cx]}{1 - c x} + \frac{a b c^2 \operatorname{ArcSin}[cx]}{1 + c x} - \frac{2 b^2 c^3 x \operatorname{ArcSin}[cx]}{\sqrt{1 - c^2 x^2}} - \frac{2 b^2 c \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[cx]}{x} - \frac{b^2 \operatorname{ArcSin}[cx]^2}{x^2} + \frac{b^2 c^2 \operatorname{ArcSin}[cx]^2}{1 - c^2 x^2} - \\ & 16 a b c^2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[cx]}] - 4 a b c^2 \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] - 8 a b c^2 \operatorname{ArcSin}[cx] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[cx]}] + 4 a b c^2 \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] - \\ & 8 a b c^2 \operatorname{ArcSin}[cx] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[cx]}] + 8 a b c^2 \operatorname{ArcSin}[cx] \operatorname{Log}[1 - e^{2i \operatorname{ArcSin}[cx]}] + 4 b^2 c^2 \operatorname{ArcSin}[cx]^2 \operatorname{Log}[1 - e^{2i \operatorname{ArcSin}[cx]}] - \\ & 4 b^2 c^2 \operatorname{ArcSin}[cx]^2 \operatorname{Log}[1 + e^{2i \operatorname{ArcSin}[cx]}] + 4 a^2 c^2 \operatorname{Log}[x] + 2 b^2 c^2 \operatorname{Log}\left[\frac{c x}{\sqrt{1 - c^2 x^2}}\right] - 2 a^2 c^2 \operatorname{Log}[1 - c^2 x^2] + 16 a b c^2 \pi \operatorname{Log}[\cos\left(\frac{1}{2} \operatorname{ArcSin}[cx]\right)] - \\ & 4 a b c^2 \pi \operatorname{Log}[-\cos\left(\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right)] + 4 a b c^2 \pi \operatorname{Log}[\sin\left(\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right)] + 8 i a b c^2 \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[cx]}] + \\ & 8 i a b c^2 \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[cx]}] + 4 i b^2 c^2 \operatorname{ArcSin}[cx] \operatorname{PolyLog}[2, -e^{2i \operatorname{ArcSin}[cx]}] - 4 i a b c^2 \operatorname{PolyLog}[2, e^{2i \operatorname{ArcSin}[cx]}] - \\ & \left. 4 i b^2 c^2 \operatorname{ArcSin}[cx] \operatorname{PolyLog}[2, e^{2i \operatorname{ArcSin}[cx]}] - 2 b^2 c^2 \operatorname{PolyLog}[3, -e^{2i \operatorname{ArcSin}[cx]}] + 2 b^2 c^2 \operatorname{PolyLog}[3, e^{2i \operatorname{ArcSin}[cx]}] \right) \end{aligned}$$

### Problem 200: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[cx])^2}{x^4 (d - c^2 d x^2)^2} dx$$

Optimal (type 4, 439 leaves, 32 steps):

$$\begin{aligned}
& -\frac{b^2 c^2}{3 d^2 x} - \frac{2 b c^3 (a + b \operatorname{ArcSin}[c x])}{3 d^2 \sqrt{1 - c^2 x^2}} - \frac{b c (a + b \operatorname{ArcSin}[c x])}{3 d^2 x^2 \sqrt{1 - c^2 x^2}} - \frac{(a + b \operatorname{ArcSin}[c x])^2}{3 d^2 x^3 (1 - c^2 x^2)} - \\
& \frac{5 c^2 (a + b \operatorname{ArcSin}[c x])^2}{3 d^2 x (1 - c^2 x^2)} + \frac{5 c^4 x (a + b \operatorname{ArcSin}[c x])^2}{2 d^2 (1 - c^2 x^2)} - \frac{5 i c^3 (a + b \operatorname{ArcSin}[c x])^2 \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[c x]}]}{d^2} - \\
& \frac{26 b c^3 (a + b \operatorname{ArcSin}[c x]) \operatorname{ArcTanh}[e^{i \operatorname{ArcSin}[c x]}]}{3 d^2} + \frac{b^2 c^3 \operatorname{ArcTanh}[c x]}{d^2} + \frac{13 i b^2 c^3 \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c x]}]}{3 d^2} + \\
& \frac{5 i b c^3 (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{d^2} - \frac{5 i b c^3 (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{d^2} - \\
& \frac{13 i b^2 c^3 \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c x]}]}{3 d^2} - \frac{5 b^2 c^3 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[c x]}]}{d^2} + \frac{5 b^2 c^3 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[c x]}]}{d^2}
\end{aligned}$$

Result (type 4, 1541 leaves):

$$\begin{aligned}
& -\frac{a^2}{3 d^2 x^3} - \frac{2 a^2 c^2}{d^2 x} - \frac{a^2 c^4 x}{2 d^2 (-1 + c^2 x^2)} - \frac{5 a^2 c^3 \operatorname{Log}[1 - c x]}{4 d^2} + \frac{5 a^2 c^3 \operatorname{Log}[1 + c x]}{4 d^2} + \\
& \frac{1}{d^2} \frac{2 a b}{2} \left( -\frac{c \sqrt{1 - c^2 x^2}}{6 x^2} + \frac{c^3 (\sqrt{1 - c^2 x^2} - \operatorname{ArcSin}[c x])}{4 (-1 + c x)} - \frac{\operatorname{ArcSin}[c x]}{3 x^3} - \frac{c^4 (\sqrt{1 - c^2 x^2} + \operatorname{ArcSin}[c x])}{4 (c + c^2 x)} + \right. \\
& \frac{1}{6} c^3 \operatorname{Log}[x] - \frac{1}{6} c^3 \operatorname{Log}[1 + \sqrt{1 - c^2 x^2}] + 2 c^2 \left( -\frac{\operatorname{ArcSin}[c x]}{x} + c \operatorname{Log}[x] - c \operatorname{Log}[1 + \sqrt{1 - c^2 x^2}] \right) - \\
& \frac{5}{4} c^4 \left( \frac{3 i \pi \operatorname{ArcSin}[c x]}{2 c} - \frac{i \operatorname{ArcSin}[c x]^2}{2 c} + \frac{2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}]}{c} - \frac{\pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}]}{c} + \frac{2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}]}{c} - \right. \\
& \left. \frac{2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]]}{c} + \frac{\pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]}{c} - \frac{2 i \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{c} \right) + \\
& \frac{5}{4} c^4 \left( \frac{i \pi \operatorname{ArcSin}[c x]}{2 c} - \frac{i \operatorname{ArcSin}[c x]^2}{2 c} + \frac{2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}]}{c} + \frac{\pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}]}{c} + \frac{2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}]}{c} - \right. \\
& \left. \frac{2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]]}{c} - \frac{\pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]}{c} - \frac{2 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{c} \right) + \\
& \frac{1}{d^2} b^2 c^3 \left( \frac{5}{6} \operatorname{ArcSin}[c x]^3 + \frac{1}{12} \left( -2 \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - 13 \operatorname{ArcSin}[c x]^2 \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) \operatorname{Csc}[\frac{1}{2} \operatorname{ArcSin}[c x]] - \right. \\
& \left. \frac{1}{12} \operatorname{ArcSin}[c x] \operatorname{Csc}[\frac{1}{2} \operatorname{ArcSin}[c x]]^2 - \frac{1}{24} \operatorname{ArcSin}[c x]^2 \operatorname{Cot}[\frac{1}{2} \operatorname{ArcSin}[c x]] \operatorname{Csc}[\frac{1}{2} \operatorname{ArcSin}[c x]]^2 + \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{-26}{3} \left( \frac{1}{8} \operatorname{ArcSin}[c x]^2 - \frac{1}{2} \operatorname{ArcSin}[c x] \operatorname{Log}[1 + e^{i \operatorname{ArcSin}[c x]}] + \frac{1}{2} \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c x]}] \right) + \\
& \frac{26}{3} \left( \frac{1}{2} \operatorname{ArcSin}[c x] \operatorname{Log}[1 - e^{i \operatorname{ArcSin}[c x]}] - \frac{1}{2} i \left( \frac{1}{4} \operatorname{ArcSin}[c x]^2 + \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c x]}] \right) \right) + \\
& \frac{1}{6} \left( -6 \operatorname{ArcSin}[c x] - 5 \operatorname{ArcSin}[c x]^3 + 15 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - \right. \\
& \quad 15 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + 15 \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left(-\frac{1}{2} - \frac{i}{2}\right) e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} (-i + e^{i \operatorname{ArcSin}[c x]}) - \\
& \quad 15 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left(\frac{1}{2} + \frac{i}{2}\right) e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} (-i + e^{i \operatorname{ArcSin}[c x]}) + 15 \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} ((1+i) + (1-i) e^{i \operatorname{ArcSin}[c x]})\right] + \\
& \quad 15 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} ((1+i) + (1-i) e^{i \operatorname{ArcSin}[c x]})\right] - 6 \operatorname{Log}[\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]] + \\
& \quad 15 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]] - 15 \pi \operatorname{ArcSin}[c x] \operatorname{Log}[-\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]] + \\
& \quad 6 \operatorname{Log}[\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]] - 15 \pi \operatorname{ArcSin}[c x] \operatorname{Log}[\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]] - \\
& \quad 15 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]] + 30 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] - \\
& \quad 30 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] - 30 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[c x]}] + 30 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[c x]}] \Big) + \\
& \frac{1}{12} \operatorname{ArcSin}[c x] \operatorname{Sec}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]^2 + \frac{\operatorname{ArcSin}[c x]^2}{4 (\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right])^2} - \frac{\operatorname{ArcSin}[c x] \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]}{\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]} - \\
& \frac{\operatorname{ArcSin}[c x]^2}{4 (\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right])^2} + \frac{\operatorname{ArcSin}[c x] \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]}{\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]} + \\
& \frac{1}{12} \operatorname{Sec}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \left( -2 \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - 13 \operatorname{ArcSin}[c x]^2 \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) - \\
& \frac{1}{24} \operatorname{ArcSin}[c x]^2 \operatorname{Sec}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]^2 \operatorname{Tan}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]
\end{aligned}$$

Problem 201: Result more than twice size of optimal antiderivative.

$$\int \frac{x^4 (a + b \operatorname{ArcSin}[c x])^2}{(d - c^2 d x^2)^3} dx$$

Optimal (type 4, 343 leaves, 16 steps):

$$\begin{aligned}
& \frac{b^2 x}{12 c^4 d^3 (1 - c^2 x^2)} - \frac{b (a + b \operatorname{ArcSin}[c x])}{6 c^5 d^3 (1 - c^2 x^2)^{3/2}} + \frac{5 b (a + b \operatorname{ArcSin}[c x])}{4 c^5 d^3 \sqrt{1 - c^2 x^2}} + \frac{x^3 (a + b \operatorname{ArcSin}[c x])^2}{4 c^2 d^3 (1 - c^2 x^2)^2} - \frac{3 x (a + b \operatorname{ArcSin}[c x])^2}{8 c^4 d^3 (1 - c^2 x^2)} - \\
& \frac{3 i (a + b \operatorname{ArcSin}[c x])^2 \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[c x]}]}{4 c^5 d^3} - \frac{7 b^2 \operatorname{ArcTanh}[c x]}{6 c^5 d^3} + \frac{3 i b (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{4 c^5 d^3} - \\
& \frac{3 i b (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{4 c^5 d^3} - \frac{3 b^2 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[c x]}]}{4 c^5 d^3} + \frac{3 b^2 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[c x]}]}{4 c^5 d^3}
\end{aligned}$$

Result (type 4, 1148 leaves):

$$\begin{aligned}
& \frac{a^2 x}{4 c^4 d^3 (-1 + c^2 x^2)^2} + \frac{5 a^2 x}{8 c^4 d^3 (-1 + c^2 x^2)} - \frac{3 a^2 \operatorname{Log}[1 - c x]}{16 c^5 d^3} + \frac{3 a^2 \operatorname{Log}[1 + c x]}{16 c^5 d^3} - \\
& \frac{1}{d^3} \frac{2 a b}{48 c^5 (-1 + c x)^2} \left( \frac{(2 - c x) \sqrt{1 - c^2 x^2} - 3 \operatorname{ArcSin}[c x]}{16 c^5 (-1 + c x)} + \frac{5 (\sqrt{1 - c^2 x^2} - \operatorname{ArcSin}[c x])}{16 c^5 (-1 + c x)} - \frac{5 (\sqrt{1 - c^2 x^2} + \operatorname{ArcSin}[c x])}{16 c^4 (c + c^2 x)} + \frac{(2 + c x) \sqrt{1 - c^2 x^2} + 3 \operatorname{ArcSin}[c x]}{48 c^5 (1 + c x)^2} + \right. \\
& \frac{1}{16 c^4} \frac{3}{2} \left( \frac{3 \frac{i \pi}{2} \operatorname{ArcSin}[c x]}{2 c} - \frac{\frac{i}{2} \operatorname{ArcSin}[c x]^2}{2 c} + \frac{2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}]}{c} - \frac{\pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}]}{c} + \frac{2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}]}{c} - \right. \\
& \frac{2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]]}{c} + \frac{\pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]}{c} - \frac{2 i \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{c} \Big) - \frac{1}{16 c^4} \\
& 3 \left( \frac{\frac{i \pi}{2} \operatorname{ArcSin}[c x]}{2 c} - \frac{\frac{i}{2} \operatorname{ArcSin}[c x]^2}{2 c} + \frac{2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}]}{c} + \frac{\pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}]}{c} + \frac{2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}]}{c} - \right. \\
& \left. \frac{2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]]}{c} - \frac{\pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]}{c} - \frac{2 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{c} \right) - \\
& \frac{1}{c^5 d^3} b^2 \left( \frac{1}{24} \left( -9 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + 9 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - \right. \right. \\
& 9 \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[\left(-\frac{1}{2} - \frac{i}{2}\right) e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} (-i + e^{i \operatorname{ArcSin}[c x]})\right] + 9 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} (-i + e^{i \operatorname{ArcSin}[c x]})\right] - \\
& 9 \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} ((1+i) + (1-i) e^{i \operatorname{ArcSin}[c x]})\right] - 9 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} ((1+i) + (1-i) e^{i \operatorname{ArcSin}[c x]})\right] - \\
& 28 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] - 9 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] + \\
& 9 \pi \operatorname{ArcSin}[c x] \operatorname{Log}[-\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] + 28 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] + \\
& 9 \pi \operatorname{ArcSin}[c x] \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] + 9 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] - \\
& 18 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] + 18 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] + \\
& 18 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[c x]}] - 18 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[c x]}] \Big) - \frac{1}{96 (1 - c^2 x^2)^2} \left( 2 c x + 74 \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] + \right. \\
& \left. 9 c x \operatorname{ArcSin}[c x]^2 + 30 \operatorname{ArcSin}[c x] \cos[3 \operatorname{ArcSin}[c x]] + 2 \sin[3 \operatorname{ArcSin}[c x]] - 15 \operatorname{ArcSin}[c x]^2 \sin[3 \operatorname{ArcSin}[c x]] \right)
\end{aligned}$$

### Problem 203: Result more than twice size of optimal antiderivative.

$$\int \frac{x^2 (a + b \operatorname{ArcSin}[c x])^2}{(d - c^2 d x^2)^3} dx$$

Optimal (type 4, 341 leaves, 15 steps):

$$\begin{aligned} & \frac{b^2 x}{12 c^2 d^3 (1 - c^2 x^2)} - \frac{b (a + b \operatorname{ArcSin}[c x])}{6 c^3 d^3 (1 - c^2 x^2)^{3/2}} + \frac{b (a + b \operatorname{ArcSin}[c x])}{4 c^3 d^3 \sqrt{1 - c^2 x^2}} + \frac{x (a + b \operatorname{ArcSin}[c x])^2}{4 c^2 d^3 (1 - c^2 x^2)^2} - \frac{x (a + b \operatorname{ArcSin}[c x])^2}{8 c^2 d^3 (1 - c^2 x^2)} + \\ & \frac{\frac{i}{4} (a + b \operatorname{ArcSin}[c x])^2 \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[c x]}]}{4 c^3 d^3} - \frac{b^2 \operatorname{ArcTanh}[c x]}{6 c^3 d^3} - \frac{\frac{i}{4} b (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, -\frac{i}{4} e^{i \operatorname{ArcSin}[c x]}]}{4 c^3 d^3} + \\ & \frac{\frac{i}{4} b (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, \frac{i}{4} e^{i \operatorname{ArcSin}[c x]}]}{4 c^3 d^3} + \frac{b^2 \operatorname{PolyLog}[3, -\frac{i}{4} e^{i \operatorname{ArcSin}[c x]}]}{4 c^3 d^3} - \frac{b^2 \operatorname{PolyLog}[3, \frac{i}{4} e^{i \operatorname{ArcSin}[c x]}]}{4 c^3 d^3} \end{aligned}$$

Result (type 4, 1082 leaves):

$$\begin{aligned}
& \frac{a^2 x}{4 c^2 d^3 (-1 + c^2 x^2)^2} + \frac{a^2 x}{8 c^2 d^3 (-1 + c^2 x^2)} + \frac{a^2 \operatorname{Log}[1 - c x]}{16 c^3 d^3} - \frac{a^2 \operatorname{Log}[1 + c x]}{16 c^3 d^3} - \\
& \frac{1}{c^3 d^3} 2 a b \left( \frac{\sqrt{1 - c^2 x^2} - \operatorname{ArcSin}[c x]}{16 (-1 + c x)} - \frac{\sqrt{1 - c^2 x^2} + \operatorname{ArcSin}[c x]}{16 (1 + c x)} - \frac{(-2 + c x) \sqrt{1 - c^2 x^2} + 3 \operatorname{ArcSin}[c x]}{48 (-1 + c x)^2} + \frac{(2 + c x) \sqrt{1 - c^2 x^2} + 3 \operatorname{ArcSin}[c x]}{48 (1 + c x)^2} + \right. \\
& \frac{1}{16} \left( -\frac{3}{2} i \pi \operatorname{ArcSin}[c x] + \frac{1}{2} i \operatorname{ArcSin}[c x]^2 - 2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] + \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - 2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + \right. \\
& 2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] + 2 i \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] \Big) + \\
& \frac{1}{16} \left( \frac{1}{2} i \pi \operatorname{ArcSin}[c x] - \frac{1}{2} i \operatorname{ArcSin}[c x]^2 + 2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] + \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + 2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - \right. \\
& \left. 2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] - 2 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] \right) - \\
& \frac{1}{c^3 d^3} b^2 \left( \frac{1}{24} \left( 3 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - 3 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + \right. \right. \\
& 3 \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[\left(-\frac{1}{2} - \frac{i}{2}\right) e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} (-i + e^{i \operatorname{ArcSin}[c x]})\right] - 3 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} (-i + e^{i \operatorname{ArcSin}[c x]})\right] + \\
& 3 \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} ((1+i) + (1-i) e^{i \operatorname{ArcSin}[c x]})\right] + 3 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} ((1+i) + (1-i) e^{i \operatorname{ArcSin}[c x]})\right] - \\
& 4 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] + 3 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] - \\
& 3 \pi \operatorname{ArcSin}[c x] \operatorname{Log}[-\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] + 4 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] - 3 \pi \operatorname{ArcSin}[c x] \\
& \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] - 3 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] + 6 i \operatorname{ArcSin}[c x] \\
& \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] - 6 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] - 6 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[c x]}] + 6 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[c x]}] \Big) - \\
& \frac{1}{96 (1 - c^2 x^2)^2} \left( 2 c x + 2 \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] + 21 c x \operatorname{ArcSin}[c x]^2 + 6 \operatorname{ArcSin}[c x] \cos[3 \operatorname{ArcSin}[c x]] + \right. \\
& \left. 2 \sin[3 \operatorname{ArcSin}[c x]] - 3 \operatorname{ArcSin}[c x]^2 \sin[3 \operatorname{ArcSin}[c x]] \right)
\end{aligned}$$

**Problem 205:** Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^2}{(d - c^2 d x^2)^3} dx$$

Optimal (type 4, 332 leaves, 15 steps):

$$\begin{aligned} & \frac{b^2 x}{12 d^3 (1 - c^2 x^2)} - \frac{b (a + b \operatorname{ArcSin}[c x])}{6 c d^3 (1 - c^2 x^2)^{3/2}} - \frac{3 b (a + b \operatorname{ArcSin}[c x])}{4 c d^3 \sqrt{1 - c^2 x^2}} + \frac{x (a + b \operatorname{ArcSin}[c x])^2}{4 d^3 (1 - c^2 x^2)^2} + \frac{3 x (a + b \operatorname{ArcSin}[c x])^2}{8 d^3 (1 - c^2 x^2)} - \\ & \frac{3 i (a + b \operatorname{ArcSin}[c x])^2 \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[c x]}]}{4 c d^3} + \frac{5 b^2 \operatorname{ArcTanh}[c x]}{6 c d^3} + \frac{3 i b (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{4 c d^3} - \\ & \frac{3 i b (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{4 c d^3} - \frac{3 b^2 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[c x]}]}{4 c d^3} + \frac{3 b^2 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[c x]}]}{4 c d^3} \end{aligned}$$

Result (type 4, 1069 leaves):

$$\begin{aligned}
& \frac{a^2 x}{4 d^3 (-1 + c^2 x^2)^2} - \frac{3 a^2 x}{8 d^3 (-1 + c^2 x^2)} - \frac{3 a^2 \operatorname{Log}[1 - c x]}{16 c d^3} + \frac{3 a^2 \operatorname{Log}[1 + c x]}{16 c d^3} - \frac{1}{c d^3} 2 a b \\
& \left( -\frac{3 (\sqrt{1 - c^2 x^2} - \operatorname{ArcSin}[c x])}{16 (-1 + c x)} + \frac{3 (\sqrt{1 - c^2 x^2} + \operatorname{ArcSin}[c x])}{16 (1 + c x)} - \frac{(-2 + c x) \sqrt{1 - c^2 x^2} + 3 \operatorname{ArcSin}[c x]}{48 (-1 + c x)^2} + \frac{(2 + c x) \sqrt{1 - c^2 x^2} + 3 \operatorname{ArcSin}[c x]}{48 (1 + c x)^2} + \right. \\
& \frac{3}{16} \left( \frac{3}{2} i \pi \operatorname{ArcSin}[c x] - \frac{1}{2} i \operatorname{ArcSin}[c x]^2 + 2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] - \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + 2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - \right. \\
& 2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]) - 2 i \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] \Big) - \\
& \frac{3}{16} \left( \frac{1}{2} i \pi \operatorname{ArcSin}[c x] - \frac{1}{2} i \operatorname{ArcSin}[c x]^2 + 2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] + \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + 2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - \right. \\
& 2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]) - 2 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] \Big) \Big) - \\
& \frac{1}{c d^3} b^2 \left( -\frac{1}{48 (1 - c^2 x^2)^2} \left( -35 \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] + c x (2 + 21 \operatorname{ArcSin}[c x]^2 + (2 + 9 \operatorname{ArcSin}[c x]^2) \cos[2 \operatorname{ArcSin}[c x]]) - \right. \right. \\
& 9 \operatorname{ArcSin}[c x] \cos[3 \operatorname{ArcSin}[c x]] \Big) + \frac{1}{24} \left( -9 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + \right. \\
& 9 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - 9 \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[\left(-\frac{1}{2} - \frac{i}{2}\right) e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} (-i + e^{i \operatorname{ArcSin}[c x]})\right] + \\
& 9 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} (-i + e^{i \operatorname{ArcSin}[c x]})\right] - 9 \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} ((1 + i) + (1 - i) e^{i \operatorname{ArcSin}[c x]})\right] - \\
& 9 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} ((1 + i) + (1 - i) e^{i \operatorname{ArcSin}[c x]})\right] + 20 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \\
& 9 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] + 9 \pi \operatorname{ArcSin}[c x] \operatorname{Log}[-\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \\
& 20 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] + 9 \pi \operatorname{ArcSin}[c x] \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \\
& 9 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] - 18 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] + \\
& 18 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] + 18 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[c x]}] - 18 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[c x]}] \Big) \Big)
\end{aligned}$$

**Problem 206: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^2}{x (d - c^2 d x^2)^3} dx$$

Optimal (type 4, 296 leaves, 17 steps):

$$\begin{aligned} & \frac{b^2}{12 d^3 (1 - c^2 x^2)} - \frac{b c x (a + b \operatorname{ArcSin}[c x])}{6 d^3 (1 - c^2 x^2)^{3/2}} - \frac{4 b c x (a + b \operatorname{ArcSin}[c x])}{3 d^3 \sqrt{1 - c^2 x^2}} + \frac{(a + b \operatorname{ArcSin}[c x])^2}{4 d^3 (1 - c^2 x^2)^2} + \frac{(a + b \operatorname{ArcSin}[c x])^2}{2 d^3 (1 - c^2 x^2)} - \\ & \frac{2 (a + b \operatorname{ArcSin}[c x])^2 \operatorname{ArcTanh}[e^{2 i \operatorname{ArcSin}[c x]}]}{d^3} - \frac{2 b^2 \operatorname{Log}[1 - c^2 x^2]}{3 d^3} + \frac{i b (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, -e^{2 i \operatorname{ArcSin}[c x]}]}{d^3} - \\ & \frac{i b (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}[c x]}]}{d^3} - \frac{b^2 \operatorname{PolyLog}[3, -e^{2 i \operatorname{ArcSin}[c x]}]}{2 d^3} + \frac{b^2 \operatorname{PolyLog}[3, e^{2 i \operatorname{ArcSin}[c x]}]}{2 d^3} \end{aligned}$$

Result (type 4, 800 leaves):

$$\begin{aligned} & \frac{a^2}{4 d^3 (-1 + c^2 x^2)^2} - \frac{a^2}{2 d^3 (-1 + c^2 x^2)} + \frac{a^2 \operatorname{Log}[c x]}{d^3} - \frac{a^2 \operatorname{Log}[1 - c^2 x^2]}{2 d^3} - \\ & \frac{1}{d^3} \frac{2 a b}{2} \left( -\frac{5 (\sqrt{1 - c^2 x^2} - \operatorname{ArcSin}[c x])}{16 (-1 + c x)} - \frac{5 (\sqrt{1 - c^2 x^2} + \operatorname{ArcSin}[c x])}{16 (1 + c x)} - \frac{(-2 + c x) \sqrt{1 - c^2 x^2} + 3 \operatorname{ArcSin}[c x]}{48 (-1 + c x)^2} - \right. \\ & \left. \frac{(2 + c x) \sqrt{1 - c^2 x^2} + 3 \operatorname{ArcSin}[c x]}{48 (1 + c x)^2} - \operatorname{ArcSin}[c x] \operatorname{Log}[1 - e^{2 i \operatorname{ArcSin}[c x]}] + \right. \\ & \left. \frac{1}{2} \left( \frac{3}{2} i \pi \operatorname{ArcSin}[c x] - \frac{1}{2} i \operatorname{ArcSin}[c x]^2 + 2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] - \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + 2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - \right. \right. \\ & \left. \left. 2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])] - 2 i \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] \right) + \right. \\ & \left. \frac{1}{2} \left( \frac{1}{2} i \pi \operatorname{ArcSin}[c x] - \frac{1}{2} i \operatorname{ArcSin}[c x]^2 + 2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] + \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + 2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - \right. \right. \\ & \left. \left. 2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])] - 2 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] \right) + \right. \\ & \left. \frac{1}{2} i (\operatorname{ArcSin}[c x]^2 + \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}[c x]}]) \right) - \frac{1}{24 d^3} b^2 \left( \frac{i \pi^3}{1 - c^2 x^2} - \frac{2}{(1 - c^2 x^2)^{3/2}} + \frac{4 c x \operatorname{ArcSin}[c x]}{(1 - c^2 x^2)^{3/2}} + \frac{32 c x \operatorname{ArcSin}[c x]}{\sqrt{1 - c^2 x^2}} - \right. \\ & \left. \frac{6 \operatorname{ArcSin}[c x]^2}{(1 - c^2 x^2)^2} - \frac{12 \operatorname{ArcSin}[c x]^2}{1 - c^2 x^2} - 16 i \operatorname{ArcSin}[c x]^3 - 24 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 - e^{-2 i \operatorname{ArcSin}[c x]}] + \right. \\ & \left. 24 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 + e^{2 i \operatorname{ArcSin}[c x]}] + 32 \operatorname{Log}[\sqrt{1 - c^2 x^2}] - 24 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, e^{-2 i \operatorname{ArcSin}[c x]}] - \right. \\ & \left. 24 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, -e^{2 i \operatorname{ArcSin}[c x]}] - 12 \operatorname{PolyLog}[3, e^{-2 i \operatorname{ArcSin}[c x]}] + 12 \operatorname{PolyLog}[3, -e^{2 i \operatorname{ArcSin}[c x]}] \right) \end{aligned}$$

### Problem 207: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^2}{x^2 (d - c^2 d x^2)^3} dx$$

Optimal (type 4, 429 leaves, 27 steps):

$$\begin{aligned} & \frac{b^2 c^2 x}{12 d^3 (1 - c^2 x^2)} - \frac{b c (a + b \operatorname{ArcSin}[c x])}{6 d^3 (1 - c^2 x^2)^{3/2}} - \frac{7 b c (a + b \operatorname{ArcSin}[c x])}{4 d^3 \sqrt{1 - c^2 x^2}} - \frac{(a + b \operatorname{ArcSin}[c x])^2}{d^3 x (1 - c^2 x^2)^2} + \\ & \frac{5 c^2 x (a + b \operatorname{ArcSin}[c x])^2}{4 d^3 (1 - c^2 x^2)^2} + \frac{15 c^2 x (a + b \operatorname{ArcSin}[c x])^2}{8 d^3 (1 - c^2 x^2)} - \frac{15 i c (a + b \operatorname{ArcSin}[c x])^2 \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[c x]}]}{4 d^3} - \\ & \frac{4 b c (a + b \operatorname{ArcSin}[c x]) \operatorname{ArcTanh}[e^{i \operatorname{ArcSin}[c x]}]}{d^3} + \frac{11 b^2 c \operatorname{ArcTanh}[c x]}{6 d^3} + \frac{2 i b^2 c \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c x]}]}{d^3} + \\ & \frac{15 i b c (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{4 d^3} - \frac{15 i b c (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{4 d^3} - \\ & \frac{2 i b^2 c \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c x]}]}{d^3} - \frac{15 b^2 c \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[c x]}]}{4 d^3} + \frac{15 b^2 c \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[c x]}]}{4 d^3} \end{aligned}$$

Result (type 4, 1416 leaves):

$$\begin{aligned} & -\frac{a^2}{d^3 x} + \frac{a^2 c^2 x}{4 d^3 (-1 + c^2 x^2)^2} - \frac{7 a^2 c^2 x}{8 d^3 (-1 + c^2 x^2)} - \frac{15 a^2 c \operatorname{Log}[1 - c x]}{16 d^3} + \frac{15 a^2 c \operatorname{Log}[1 + c x]}{16 d^3} - \\ & \frac{1}{d^3} \frac{2 a b c}{2} \left( -\frac{7 (\sqrt{1 - c^2 x^2} - \operatorname{ArcSin}[c x])}{16 (-1 + c x)} + \frac{\operatorname{ArcSin}[c x]}{c x} + \frac{7 (\sqrt{1 - c^2 x^2} + \operatorname{ArcSin}[c x])}{16 (1 + c x)} - \right. \\ & \left. \frac{(-2 + c x) \sqrt{1 - c^2 x^2} + 3 \operatorname{ArcSin}[c x]}{48 (-1 + c x)^2} + \frac{(2 + c x) \sqrt{1 - c^2 x^2} + 3 \operatorname{ArcSin}[c x]}{48 (1 + c x)^2} - \operatorname{Log}[c x] + \operatorname{Log}[1 + \sqrt{1 - c^2 x^2}] + \right. \\ & \left. \frac{15}{16} \left( \frac{3}{2} i \pi \operatorname{ArcSin}[c x] - \frac{1}{2} i \operatorname{ArcSin}[c x]^2 + 2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] - \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + 2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - \right. \right. \\ & \left. \left. 2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])] - 2 i \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] \right) - \right. \\ & \left. \frac{15}{16} \left( \frac{1}{2} i \pi \operatorname{ArcSin}[c x] - \frac{1}{2} i \operatorname{ArcSin}[c x]^2 + 2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] + \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + 2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - \right. \right. \\ & \left. \left. 2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])] - 2 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] \right) \right) - \right. \end{aligned}$$

$$\begin{aligned}
& \frac{1}{d^3} b^2 c \left( -2 i \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c x]}] + \frac{1}{24} \left( 44 \operatorname{ArcSin}[c x] + 15 \operatorname{ArcSin}[c x]^3 - 45 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + \right. \right. \\
& 45 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - 45 \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[-\frac{1}{2} - \frac{i}{2}\right] e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} (-i + e^{i \operatorname{ArcSin}[c x]}) \left. \right) + \\
& 45 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[\frac{1}{2} + \frac{i}{2}\right] e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} (-i + e^{i \operatorname{ArcSin}[c x]}) - 45 \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} ((1+i) + (1-i) e^{i \operatorname{ArcSin}[c x]})\right] - \\
& 45 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} ((1+i) + (1-i) e^{i \operatorname{ArcSin}[c x]})\right] + 44 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] - \\
& 45 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] + 45 \pi \operatorname{ArcSin}[c x] \operatorname{Log}[-\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \\
& 44 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] + 45 \pi \operatorname{ArcSin}[c x] \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \\
& 45 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] - 90 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] + \\
& 90 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] + 90 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[c x]}] - 90 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[c x]}] \Big) - \\
& \frac{1}{384 c x (1 - c^2 x^2)^2} \left( 4 + 88 c x \operatorname{ArcSin}[c x] - 54 \operatorname{ArcSin}[c x]^2 + 30 c x \operatorname{ArcSin}[c x]^3 - 240 \operatorname{ArcSin}[c x]^2 \cos[2 \operatorname{ArcSin}[c x]] - \right. \\
& 4 \cos[4 \operatorname{ArcSin}[c x]] - 90 \operatorname{ArcSin}[c x]^2 \cos[4 \operatorname{ArcSin}[c x]] + 96 c x \operatorname{ArcSin}[c x] \operatorname{Log}[1 - e^{i \operatorname{ArcSin}[c x]}] - \\
& 96 c x \operatorname{ArcSin}[c x] \operatorname{Log}[1 + e^{i \operatorname{ArcSin}[c x]}] - 768 i c x (1 - c^2 x^2)^2 \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c x]}] - \\
& 200 \operatorname{ArcSin}[c x] \sin[2 \operatorname{ArcSin}[c x]] + 132 \operatorname{ArcSin}[c x] \sin[3 \operatorname{ArcSin}[c x]] + 45 \operatorname{ArcSin}[c x]^3 \sin[3 \operatorname{ArcSin}[c x]] + \\
& 144 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - e^{i \operatorname{ArcSin}[c x]}] \sin[3 \operatorname{ArcSin}[c x]] - 144 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + e^{i \operatorname{ArcSin}[c x]}] \sin[3 \operatorname{ArcSin}[c x]] - \\
& 84 \operatorname{ArcSin}[c x] \sin[4 \operatorname{ArcSin}[c x]] + 44 \operatorname{ArcSin}[c x] \sin[5 \operatorname{ArcSin}[c x]] + 15 \operatorname{ArcSin}[c x]^3 \sin[5 \operatorname{ArcSin}[c x]] + \\
& \left. 48 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - e^{i \operatorname{ArcSin}[c x]}] \sin[5 \operatorname{ArcSin}[c x]] - 48 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + e^{i \operatorname{ArcSin}[c x]}] \sin[5 \operatorname{ArcSin}[c x]] \right)
\end{aligned}$$

Problem 208: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^2}{x^3 (d - c^2 d x^2)^3} dx$$

Optimal (type 4, 403 leaves, 23 steps):

$$\begin{aligned}
& \frac{b^2 c^2}{12 d^3 (1 - c^2 x^2)} - \frac{b c (a + b \operatorname{ArcSin}[c x])}{d^3 x (1 - c^2 x^2)^{3/2}} + \frac{5 b c^3 x (a + b \operatorname{ArcSin}[c x])}{6 d^3 (1 - c^2 x^2)^{3/2}} - \frac{4 b c^3 x (a + b \operatorname{ArcSin}[c x])}{3 d^3 \sqrt{1 - c^2 x^2}} + \\
& \frac{3 c^2 (a + b \operatorname{ArcSin}[c x])^2}{4 d^3 (1 - c^2 x^2)^2} - \frac{(a + b \operatorname{ArcSin}[c x])^2}{2 d^3 x^2 (1 - c^2 x^2)^2} + \frac{3 c^2 (a + b \operatorname{ArcSin}[c x])^2}{2 d^3 (1 - c^2 x^2)} - \frac{6 c^2 (a + b \operatorname{ArcSin}[c x])^2 \operatorname{ArcTanh}[e^{2 i \operatorname{ArcSin}[c x]}]}{d^3} + \\
& \frac{b^2 c^2 \operatorname{Log}[x]}{d^3} - \frac{7 b^2 c^2 \operatorname{Log}[1 - c^2 x^2]}{6 d^3} + \frac{3 i b c^2 (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, -e^{2 i \operatorname{ArcSin}[c x]}]}{d^3} - \\
& \frac{3 i b c^2 (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}[c x]}]}{d^3} - \frac{3 b^2 c^2 \operatorname{PolyLog}[3, -e^{2 i \operatorname{ArcSin}[c x]}]}{2 d^3} + \frac{3 b^2 c^2 \operatorname{PolyLog}[3, e^{2 i \operatorname{ArcSin}[c x]}]}{2 d^3}
\end{aligned}$$

Result (type 4, 989 leaves) :

$$\begin{aligned}
& -\frac{a^2}{2 d^3 x^2} + \frac{a^2 c^2}{4 d^3 (-1 + c^2 x^2)^2} - \frac{a^2 c^2}{d^3 (-1 + c^2 x^2)} + \frac{3 a^2 c^2 \operatorname{Log}[x]}{d^3} - \frac{3 a^2 c^2 \operatorname{Log}[1 - c^2 x^2]}{2 d^3} - \\
& \frac{1}{d^3} \frac{2 a b}{2} \left( \frac{c^2 ((2 - c x) \sqrt{1 - c^2 x^2} - 3 \operatorname{ArcSin}[c x])}{48 (-1 + c x)^2} - \frac{9 c^2 (\sqrt{1 - c^2 x^2} - \operatorname{ArcSin}[c x])}{16 (-1 + c x)} - \right. \\
& \left. \frac{9 c^3 (\sqrt{1 - c^2 x^2} + \operatorname{ArcSin}[c x])}{16 (c + c^2 x)} + \frac{c x \sqrt{1 - c^2 x^2} + \operatorname{ArcSin}[c x]}{2 x^2} - \frac{c^2 ((2 + c x) \sqrt{1 - c^2 x^2} + 3 \operatorname{ArcSin}[c x])}{48 (1 + c x)^2} + \right. \\
& \left. \frac{3}{2} c^3 \left( \frac{3 i \pi \operatorname{ArcSin}[c x]}{2 c} - \frac{i \operatorname{ArcSin}[c x]^2}{2 c} + \frac{2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}]}{c} - \frac{\pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}]}{c} + \frac{2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}]}{c} - \right. \right. \\
& \left. \left. \frac{2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]]}{c} + \frac{\pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]}{c} - \frac{2 i \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{c} \right) + \right. \\
& \left. \frac{3}{2} c^3 \left( \frac{i \pi \operatorname{ArcSin}[c x]}{2 c} - \frac{i \operatorname{ArcSin}[c x]^2}{2 c} + \frac{2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}]}{c} + \frac{\pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}]}{c} + \frac{2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}]}{c} - \right. \right. \\
& \left. \left. \frac{2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]]}{c} - \frac{\pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]}{c} - \frac{2 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{c} \right) - \right. \\
& \left. 3 c^2 \left( \operatorname{ArcSin}[c x] \operatorname{Log}[1 - e^{2 i \operatorname{ArcSin}[c x]}] - \frac{1}{2} i (\operatorname{ArcSin}[c x]^2 + \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}[c x]}]) \right) \right) - \\
& \frac{1}{d^3} b^2 c^2 \left( \frac{i \pi^3}{8} - \frac{1}{12 (1 - c^2 x^2)} + \frac{c x \operatorname{ArcSin}[c x]}{6 (1 - c^2 x^2)^{3/2}} + \frac{7 c x \operatorname{ArcSin}[c x]}{3 \sqrt{1 - c^2 x^2}} + \frac{\sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x]}{c x} + \frac{\operatorname{ArcSin}[c x]^2}{2 c^2 x^2} - \right. \\
& \left. \frac{\operatorname{ArcSin}[c x]^2}{4 (1 - c^2 x^2)^2} - \frac{\operatorname{ArcSin}[c x]^2}{1 - c^2 x^2} - 2 i \operatorname{ArcSin}[c x]^3 - 3 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 - e^{-2 i \operatorname{ArcSin}[c x]}] + \right. \\
& \left. 3 \operatorname{ArcSin}[c x]^2 \operatorname{Log}[1 + e^{2 i \operatorname{ArcSin}[c x]}] - \operatorname{Log}[c x] + \frac{7}{3} \operatorname{Log}[\sqrt{1 - c^2 x^2}] - 3 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, e^{-2 i \operatorname{ArcSin}[c x]}] - \right. \\
& \left. 3 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, -e^{2 i \operatorname{ArcSin}[c x]}] - \frac{3}{2} \operatorname{PolyLog}[3, e^{-2 i \operatorname{ArcSin}[c x]}] + \frac{3}{2} \operatorname{PolyLog}[3, -e^{2 i \operatorname{ArcSin}[c x]}] \right)
\end{aligned}$$

**Problem 209: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^2}{x^4 (d - c^2 d x^2)^3} dx$$

Optimal (type 4, 572 leaves, 43 steps):

$$\begin{aligned}
 & -\frac{b^2 c^2}{2 d^3 x} + \frac{b^2 c^2}{6 d^3 (1 - c^2 x^2)} - \frac{b^2 c^4 x}{12 d^3 (1 - c^2 x^2)} + \frac{b c^3 (a + b \operatorname{ArcSin}[c x])}{6 d^3 (1 - c^2 x^2)^{3/2}} - \\
 & \frac{b c (a + b \operatorname{ArcSin}[c x])}{3 d^3 x^2 (1 - c^2 x^2)^{3/2}} - \frac{29 b c^3 (a + b \operatorname{ArcSin}[c x])}{12 d^3 \sqrt{1 - c^2 x^2}} - \frac{(a + b \operatorname{ArcSin}[c x])^2}{3 d^3 x^3 (1 - c^2 x^2)^2} - \frac{7 c^2 (a + b \operatorname{ArcSin}[c x])^2}{3 d^3 x (1 - c^2 x^2)^2} + \\
 & \frac{35 c^4 x (a + b \operatorname{ArcSin}[c x])^2}{12 d^3 (1 - c^2 x^2)^2} + \frac{35 c^4 x (a + b \operatorname{ArcSin}[c x])^2}{8 d^3 (1 - c^2 x^2)} - \frac{35 i c^3 (a + b \operatorname{ArcSin}[c x])^2 \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[c x]}]}{4 d^3} - \\
 & \frac{38 b c^3 (a + b \operatorname{ArcSin}[c x]) \operatorname{ArcTanh}[e^{i \operatorname{ArcSin}[c x]}]}{3 d^3} + \frac{17 b^2 c^3 \operatorname{ArcTanh}[c x]}{6 d^3} + \frac{19 i b^2 c^3 \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c x]}]}{3 d^3} + \\
 & \frac{35 i b c^3 (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{4 d^3} - \frac{35 i b c^3 (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{4 d^3} - \\
 & \frac{19 i b^2 c^3 \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c x]}]}{3 d^3} - \frac{35 b^2 c^3 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[c x]}]}{4 d^3} + \frac{35 b^2 c^3 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[c x]}]}{4 d^3}
 \end{aligned}$$

Result (type 4, 1817 leaves):

$$\begin{aligned}
 & -\frac{a^2}{3 d^3 x^3} - \frac{3 a^2 c^2}{d^3 x} + \frac{a^2 c^4 x}{4 d^3 (-1 + c^2 x^2)^2} - \frac{11 a^2 c^4 x}{8 d^3 (-1 + c^2 x^2)} - \frac{35 a^2 c^3 \operatorname{Log}[1 - c x]}{16 d^3} + \frac{35 a^2 c^3 \operatorname{Log}[1 + c x]}{16 d^3} - \frac{1}{d^3} 2 a b \\
 & \left( \frac{c \sqrt{1 - c^2 x^2}}{6 x^2} + \frac{c^3 ((2 - c x) \sqrt{1 - c^2 x^2} - 3 \operatorname{ArcSin}[c x])}{48 (-1 + c x)^2} - \frac{11 c^3 (\sqrt{1 - c^2 x^2} - \operatorname{ArcSin}[c x])}{16 (-1 + c x)} + \frac{\operatorname{ArcSin}[c x]}{3 x^3} + \frac{11 c^4 (\sqrt{1 - c^2 x^2} + \operatorname{ArcSin}[c x])}{16 (c + c^2 x)} + \right. \\
 & \frac{c^3 ((2 + c x) \sqrt{1 - c^2 x^2} + 3 \operatorname{ArcSin}[c x])}{48 (1 + c x)^2} - \frac{1}{6} c^3 \operatorname{Log}[x] + \frac{1}{6} c^3 \operatorname{Log}[1 + \sqrt{1 - c^2 x^2}] - 3 c^2 \left( -\frac{\operatorname{ArcSin}[c x]}{x} + c \operatorname{Log}[x] - c \operatorname{Log}[1 + \sqrt{1 - c^2 x^2}] \right) + \\
 & \frac{35}{16} c^4 \left( \frac{3 i \pi \operatorname{ArcSin}[c x]}{2 c} - \frac{i \operatorname{ArcSin}[c x]^2}{2 c} + \frac{2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}]}{c} - \frac{\pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}]}{c} + \frac{2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}]}{c} - \right. \\
 & \frac{2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]]}{c} + \frac{\pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]}{c} - \frac{2 i \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{c} \Bigg) - \\
 & \frac{35}{16} c^4 \left( \frac{i \pi \operatorname{ArcSin}[c x]}{2 c} - \frac{i \operatorname{ArcSin}[c x]^2}{2 c} + \frac{2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}]}{c} + \frac{\pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}]}{c} + \frac{2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}]}{c} - \right. \\
 & \frac{2 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]]}{c} - \frac{\pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]]}{c} - \frac{2 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{c} \Bigg)
 \end{aligned}$$

$$\begin{aligned}
& \frac{1}{d^3} b^2 c^3 \left( -\frac{35}{24} \operatorname{ArcSin}[c x]^3 - \frac{1}{12} \left( -2 \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] - 19 \operatorname{ArcSin}[c x]^2 \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right) \csc \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \right. \\
& \frac{1}{12} \operatorname{ArcSin}[c x] \csc \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]^2 + \frac{1}{24} \operatorname{ArcSin}[c x]^2 \cot \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \csc \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]^2 - \\
& \frac{38}{3} \left( \frac{1}{8} i \operatorname{ArcSin}[c x]^2 - \frac{1}{2} \operatorname{ArcSin}[c x] \log \left[ 1 + e^{i \operatorname{ArcSin}[c x]} \right] + \frac{1}{2} i \operatorname{PolyLog} \left[ 2, -e^{i \operatorname{ArcSin}[c x]} \right] \right) - \\
& \frac{38}{3} \left( \frac{1}{2} \operatorname{ArcSin}[c x] \log \left[ 1 - e^{i \operatorname{ArcSin}[c x]} \right] - \frac{1}{2} i \left( \frac{1}{4} \operatorname{ArcSin}[c x]^2 + \operatorname{PolyLog} \left[ 2, e^{i \operatorname{ArcSin}[c x]} \right] \right) \right) + \\
& \frac{1}{24} \left( 68 \operatorname{ArcSin}[c x] + 35 \operatorname{ArcSin}[c x]^3 - 105 \operatorname{ArcSin}[c x]^2 \log \left[ 1 - i e^{i \operatorname{ArcSin}[c x]} \right] + \right. \\
& 105 \operatorname{ArcSin}[c x]^2 \log \left[ 1 + i e^{i \operatorname{ArcSin}[c x]} \right] - 105 \pi \operatorname{ArcSin}[c x] \log \left[ \left( -\frac{1}{2} - \frac{i}{2} \right) e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} (-i + e^{i \operatorname{ArcSin}[c x]}) \right] + \\
& 105 \operatorname{ArcSin}[c x]^2 \log \left[ \left( \frac{1}{2} + \frac{i}{2} \right) e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} (-i + e^{i \operatorname{ArcSin}[c x]}) \right] - 105 \pi \operatorname{ArcSin}[c x] \log \left[ \frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSin}[c x]} ((1+i) + (1-i) e^{i \operatorname{ArcSin}[c x]}) \right] - \\
& 105 \operatorname{ArcSin}[c x]^2 \log \left[ \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] - \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right] - \\
& 105 \operatorname{ArcSin}[c x]^2 \log \left[ \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] - \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right] + 105 \pi \operatorname{ArcSin}[c x] \log \left[ -\cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right] - \\
& 68 \log \left[ \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right] + 105 \pi \operatorname{ArcSin}[c x] \log \left[ \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right] + \\
& 105 \operatorname{ArcSin}[c x]^2 \log \left[ \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right] - 210 i \operatorname{ArcSin}[c x] \operatorname{PolyLog} \left[ 2, -i e^{i \operatorname{ArcSin}[c x]} \right] + \\
& 210 i \operatorname{ArcSin}[c x] \operatorname{PolyLog} \left[ 2, i e^{i \operatorname{ArcSin}[c x]} \right] + 210 \operatorname{PolyLog} \left[ 3, -i e^{i \operatorname{ArcSin}[c x]} \right] - 210 \operatorname{PolyLog} \left[ 3, i e^{i \operatorname{ArcSin}[c x]} \right] \Big) - \\
& \frac{1}{12} \operatorname{ArcSin}[c x] \sec \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]^2 - \frac{\operatorname{ArcSin}[c x]^2}{16 \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] - \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right)^4} - \frac{2 - 2 \operatorname{ArcSin}[c x] + 33 \operatorname{ArcSin}[c x]^2}{48 \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] - \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right)^2} + \\
& \frac{\operatorname{ArcSin}[c x] \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]}{12 \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] - \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right)^3} + \frac{17 \operatorname{ArcSin}[c x] \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]}{6 \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] - \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right)} + \\
& \frac{\operatorname{ArcSin}[c x]^2}{16 \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right)^4} - \frac{\operatorname{ArcSin}[c x] \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]}{12 \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right)^3} - \\
& \frac{-2 - 2 \operatorname{ArcSin}[c x] - 33 \operatorname{ArcSin}[c x]^2}{48 \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right)^2} - \frac{17 \operatorname{ArcSin}[c x] \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]}{6 \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right)} - \\
& \frac{1}{12} \sec \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \left( -2 \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] - 19 \operatorname{ArcSin}[c x]^2 \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right) +
\end{aligned}$$

$$\frac{1}{24} \operatorname{ArcSin}[c x]^2 \sec \left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]^2 \tan \left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \Bigg)$$

Problem 276: Unable to integrate problem.

$$\int x^m (d - c^2 d x^2)^3 (a + b \operatorname{ArcSin}[c x])^2 dx$$

Optimal (type 5, 1312 leaves, 23 steps):

$$\begin{aligned}
& \frac{2 b^2 c^2 d^3 x^{3+m}}{(3+m)(7+m)^2} + \frac{30 b^2 c^2 d^3 x^{3+m}}{(3+m)^2 (5+m)(7+m)^2} + \frac{36 b^2 c^2 d^3 x^{3+m}}{(3+m)^2 (5+m)^2 (7+m)} + \frac{12 b^2 c^2 d^3 x^{3+m}}{(3+m)(5+m)^2 (7+m)} + \\
& \frac{48 b^2 c^2 d^3 x^{3+m}}{(3+m)^3 (5+m)(7+m)} + \frac{10 b^2 c^2 d^3 x^{3+m}}{(7+m)^2 (15+8m+m^2)} - \frac{10 b^2 c^4 d^3 x^{5+m}}{(5+m)^2 (7+m)^2} - \frac{4 b^2 c^4 d^3 x^{5+m}}{(5+m)(7+m)^2} - \frac{12 b^2 c^4 d^3 x^{5+m}}{(5+m)^3 (7+m)} + \frac{2 b^2 c^6 d^3 x^{7+m}}{(7+m)^3} - \\
& \frac{36 b c d^3 x^{2+m} \sqrt{1-c^2 x^2} (a+b \operatorname{ArcSin}[c x])}{(3+m)(5+m)^2 (7+m)} - \frac{48 b c d^3 x^{2+m} \sqrt{1-c^2 x^2} (a+b \operatorname{ArcSin}[c x])}{(3+m)^2 (5+m)(7+m)} - \frac{30 b c d^3 x^{2+m} \sqrt{1-c^2 x^2} (a+b \operatorname{ArcSin}[c x])}{(7+m)^2 (15+8m+m^2)} - \\
& \frac{10 b c d^3 x^{2+m} (1-c^2 x^2)^{3/2} (a+b \operatorname{ArcSin}[c x])}{(5+m)(7+m)^2} - \frac{12 b c d^3 x^{2+m} (1-c^2 x^2)^{3/2} (a+b \operatorname{ArcSin}[c x])}{(5+m)^2 (7+m)} - \frac{2 b c d^3 x^{2+m} (1-c^2 x^2)^{5/2} (a+b \operatorname{ArcSin}[c x])}{(7+m)^2} + \\
& \frac{48 d^3 x^{1+m} (a+b \operatorname{ArcSin}[c x])^2}{(5+m)(7+m)(3+4m+m^2)} + \frac{24 d^3 x^{1+m} (1-c^2 x^2) (a+b \operatorname{ArcSin}[c x])^2}{(7+m)(15+8m+m^2)} + \frac{6 d^3 x^{1+m} (1-c^2 x^2)^2 (a+b \operatorname{ArcSin}[c x])^2}{(5+m)(7+m)} + \\
& \frac{d^3 x^{1+m} (1-c^2 x^2)^3 (a+b \operatorname{ArcSin}[c x])^2}{7+m} - \frac{48 b c d^3 x^{2+m} (a+b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2+m}{2}, \frac{4+m}{2}, c^2 x^2\right]}{(2+m)(3+m)^2 (5+m)(7+m)} - \\
& \frac{30 b c d^3 x^{2+m} (a+b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2+m}{2}, \frac{4+m}{2}, c^2 x^2\right]}{(5+m)(7+m)^2 (6+5m+m^2)} - \\
& \frac{36 b c d^3 x^{2+m} (a+b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2+m}{2}, \frac{4+m}{2}, c^2 x^2\right]}{(5+m)^2 (7+m)(6+5m+m^2)} - \\
& \frac{96 b c d^3 x^{2+m} (a+b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2+m}{2}, \frac{4+m}{2}, c^2 x^2\right]}{(5+m)(7+m)(6+11m+6m^2+m^3)} + \\
& \frac{30 b^2 c^2 d^3 x^{3+m} \operatorname{HypergeometricPFQ}\left[\left\{1, \frac{3}{2}+\frac{m}{2}, \frac{3}{2}+\frac{m}{2}\right\}, \left\{2+\frac{m}{2}, \frac{5}{2}+\frac{m}{2}\right\}, c^2 x^2\right]}{(2+m)(3+m)^2 (5+m)(7+m)} + \\
& \frac{36 b^2 c^2 d^3 x^{3+m} \operatorname{HypergeometricPFQ}\left[\left\{1, \frac{3}{2}+\frac{m}{2}, \frac{3}{2}+\frac{m}{2}\right\}, \left\{2+\frac{m}{2}, \frac{5}{2}+\frac{m}{2}\right\}, c^2 x^2\right]}{(2+m)(3+m)^2 (5+m)^2 (7+m)} + \\
& \frac{48 b^2 c^2 d^3 x^{3+m} \operatorname{HypergeometricPFQ}\left[\left\{1, \frac{3}{2}+\frac{m}{2}, \frac{3}{2}+\frac{m}{2}\right\}, \left\{2+\frac{m}{2}, \frac{5}{2}+\frac{m}{2}\right\}, c^2 x^2\right]}{(2+m)(3+m)^3 (5+m)(7+m)} + \\
& \frac{96 b^2 c^2 d^3 x^{3+m} \operatorname{HypergeometricPFQ}\left[\left\{1, \frac{3}{2}+\frac{m}{2}, \frac{3}{2}+\frac{m}{2}\right\}, \left\{2+\frac{m}{2}, \frac{5}{2}+\frac{m}{2}\right\}, c^2 x^2\right]}{(3+m)^2 (5+m)(7+m)(2+3m+m^2)}
\end{aligned}$$

Result (type 8, 29 leaves) :

$$\int x^m (d - c^2 d x^2)^3 (a + b \operatorname{ArcSin}[c x])^2 dx$$

### Problem 277: Unable to integrate problem.

$$\int x^m (d - c^2 dx^2)^2 (a + b \operatorname{ArcSin}[c x])^2 dx$$

Optimal (type 5, 756 leaves, 13 steps):

$$\begin{aligned}
& \frac{6 b^2 c^2 d^2 x^{3+m}}{(3+m)^2 (5+m)^2} + \frac{2 b^2 c^2 d^2 x^{3+m}}{(3+m) (5+m)^2} + \frac{8 b^2 c^2 d^2 x^{3+m}}{(3+m)^3 (5+m)} - \frac{2 b^2 c^4 d^2 x^{5+m}}{(5+m)^3} - \\
& \frac{6 b c d^2 x^{2+m} \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])}{(3+m) (5+m)^2} - \frac{8 b c d^2 x^{2+m} \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])}{(3+m)^2 (5+m)} - \\
& \frac{2 b c d^2 x^{2+m} (1 - c^2 x^2)^{3/2} (a + b \operatorname{ArcSin}[c x])}{(5+m)^2} + \frac{8 d^2 x^{1+m} (a + b \operatorname{ArcSin}[c x])^2}{(5+m) (3+4m+m^2)} + \frac{4 d^2 x^{1+m} (1 - c^2 x^2) (a + b \operatorname{ArcSin}[c x])^2}{15+8m+m^2} + \\
& \frac{d^2 x^{1+m} (1 - c^2 x^2)^2 (a + b \operatorname{ArcSin}[c x])^2}{5+m} - \frac{8 b c d^2 x^{2+m} (a + b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2+m}{2}, \frac{4+m}{2}, c^2 x^2\right]}{(2+m) (3+m)^2 (5+m)} - \\
& \frac{6 b c d^2 x^{2+m} (a + b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2+m}{2}, \frac{4+m}{2}, c^2 x^2\right]}{(5+m)^2 (6+5m+m^2)} - \frac{16 b c d^2 x^{2+m} (a + b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2+m}{2}, \frac{4+m}{2}, c^2 x^2\right]}{(5+m) (6+11m+6m^2+m^3)} + \\
& \frac{6 b^2 c^2 d^2 x^{3+m} \operatorname{HypergeometricPFQ}\left[\left\{1, \frac{3}{2} + \frac{m}{2}, \frac{3}{2} + \frac{m}{2}\right\}, \left\{2 + \frac{m}{2}, \frac{5}{2} + \frac{m}{2}\right\}, c^2 x^2\right]}{(2+m) (3+m)^2 (5+m)} + \\
& \frac{8 b^2 c^2 d^2 x^{3+m} \operatorname{HypergeometricPFQ}\left[\left\{1, \frac{3}{2} + \frac{m}{2}, \frac{3}{2} + \frac{m}{2}\right\}, \left\{2 + \frac{m}{2}, \frac{5}{2} + \frac{m}{2}\right\}, c^2 x^2\right]}{(2+m) (3+m)^3 (5+m)} + \\
& \frac{16 b^2 c^2 d^2 x^{3+m} \operatorname{HypergeometricPFQ}\left[\left\{1, \frac{3}{2} + \frac{m}{2}, \frac{3}{2} + \frac{m}{2}\right\}, \left\{2 + \frac{m}{2}, \frac{5}{2} + \frac{m}{2}\right\}, c^2 x^2\right]}{(3+m)^2 (5+m) (2+3m+m^2)}
\end{aligned}$$

Result (type 8, 29 leaves):

$$\int x^m (d - c^2 dx^2)^2 (a + b \operatorname{ArcSin}[c x])^2 dx$$

### Problem 278: Unable to integrate problem.

$$\int x^m (d - c^2 dx^2) (a + b \operatorname{ArcSin}[c x])^2 dx$$

Optimal (type 5, 371 leaves, 6 steps):

$$\begin{aligned}
& \frac{2 b^2 c^2 d x^{3+m}}{(3+m)^3} - \frac{2 b c d x^{2+m} \sqrt{1-c^2 x^2} (a+b \operatorname{ArcSin}[c x])}{(3+m)^2} + \frac{2 d x^{1+m} (a+b \operatorname{ArcSin}[c x])^2}{3+4m+m^2} + \frac{d x^{1+m} (1-c^2 x^2) (a+b \operatorname{ArcSin}[c x])^2}{3+m} - \\
& \frac{2 b c d x^{2+m} (a+b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2+m}{2}, \frac{4+m}{2}, c^2 x^2\right]}{(2+m)(3+m)^2} - \frac{4 b c d x^{2+m} (a+b \operatorname{ArcSin}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2+m}{2}, \frac{4+m}{2}, c^2 x^2\right]}{6+11m+6m^2+m^3} + \\
& \frac{2 b^2 c^2 d x^{3+m} \operatorname{HypergeometricPFQ}\left[\left\{1, \frac{3}{2}+\frac{m}{2}, \frac{3}{2}+\frac{m}{2}\right\}, \left\{2+\frac{m}{2}, \frac{5}{2}+\frac{m}{2}\right\}, c^2 x^2\right]}{(2+m)(3+m)^3} + \\
& \frac{4 b^2 c^2 d x^{3+m} \operatorname{HypergeometricPFQ}\left[\left\{1, \frac{3}{2}+\frac{m}{2}, \frac{3}{2}+\frac{m}{2}\right\}, \left\{2+\frac{m}{2}, \frac{5}{2}+\frac{m}{2}\right\}, c^2 x^2\right]}{(3+m)^2 (2+3m+m^2)}
\end{aligned}$$

Result (type 8, 27 leaves):

$$\int x^m (d - c^2 d x^2) (a + b \operatorname{ArcSin}[c x])^2 dx$$

Problem 292: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{ArcSin}[ax]^3}{c - a^2 c x^2} dx$$

Optimal (type 4, 200 leaves, 10 steps):

$$\begin{aligned}
& -\frac{2 i \operatorname{ArcSin}[ax]^3 \operatorname{ArcTan}\left[e^{i \operatorname{ArcSin}[ax]}\right]}{a c} + \frac{3 i \operatorname{ArcSin}[ax]^2 \operatorname{PolyLog}\left[2, -i e^{i \operatorname{ArcSin}[ax]}\right]}{a c} - \\
& \frac{3 i \operatorname{ArcSin}[ax]^2 \operatorname{PolyLog}\left[2, i e^{i \operatorname{ArcSin}[ax]}\right]}{a c} - \frac{6 \operatorname{ArcSin}[ax] \operatorname{PolyLog}\left[3, -i e^{i \operatorname{ArcSin}[ax]}\right]}{a c} + \\
& \frac{6 \operatorname{ArcSin}[ax] \operatorname{PolyLog}\left[3, i e^{i \operatorname{ArcSin}[ax]}\right]}{a c} - \frac{6 i \operatorname{PolyLog}\left[4, -i e^{i \operatorname{ArcSin}[ax]}\right]}{a c} + \frac{6 i \operatorname{PolyLog}\left[4, i e^{i \operatorname{ArcSin}[ax]}\right]}{a c}
\end{aligned}$$

Result (type 4, 556 leaves):

$$\begin{aligned}
& -\frac{1}{a c} \left( \frac{7 i \pi^4}{64} + \frac{1}{8} i \pi^3 \operatorname{ArcSin}[a x] - \frac{3}{8} i \pi^2 \operatorname{ArcSin}[a x]^2 + \frac{1}{2} i \pi \operatorname{ArcSin}[a x]^3 - \frac{1}{4} i \operatorname{ArcSin}[a x]^4 - \frac{3}{4} \pi^2 \operatorname{ArcSin}[a x] \operatorname{Log}[1 - i e^{-i \operatorname{ArcSin}[a x]}] + \right. \\
& \quad \frac{3}{2} \pi \operatorname{ArcSin}[a x]^2 \operatorname{Log}[1 - i e^{-i \operatorname{ArcSin}[a x]}] + \frac{1}{8} \pi^3 \operatorname{Log}[1 + i e^{-i \operatorname{ArcSin}[a x]}] - \operatorname{ArcSin}[a x]^3 \operatorname{Log}[1 + i e^{-i \operatorname{ArcSin}[a x]}] - \\
& \quad \frac{1}{8} \pi^3 \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[a x]}] + \frac{3}{4} \pi^2 \operatorname{ArcSin}[a x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[a x]}] - \frac{3}{2} \pi \operatorname{ArcSin}[a x]^2 \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[a x]}] + \\
& \quad \operatorname{ArcSin}[a x]^3 \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[a x]}] - \frac{1}{8} \pi^3 \operatorname{Log}[\operatorname{Tan}\left(\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a x])\right)] - 3 i \operatorname{ArcSin}[a x]^2 \operatorname{PolyLog}[2, -i e^{-i \operatorname{ArcSin}[a x]}] - \\
& \quad \frac{3}{4} i \pi (\pi - 4 \operatorname{ArcSin}[a x]) \operatorname{PolyLog}[2, i e^{-i \operatorname{ArcSin}[a x]}] - \frac{3}{4} i \pi^2 \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[a x]}] + 3 i \pi \operatorname{ArcSin}[a x] \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[a x]}] - \\
& \quad 3 i \operatorname{ArcSin}[a x]^2 \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[a x]}] - 6 \operatorname{ArcSin}[a x] \operatorname{PolyLog}[3, -i e^{-i \operatorname{ArcSin}[a x]}] + 3 \pi \operatorname{PolyLog}[3, i e^{-i \operatorname{ArcSin}[a x]}] - \\
& \quad \left. 3 \pi \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[a x]}] + 6 \operatorname{ArcSin}[a x] \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[a x]}] + 6 i \operatorname{PolyLog}[4, -i e^{-i \operatorname{ArcSin}[a x]}] + 6 i \operatorname{PolyLog}[4, -i e^{i \operatorname{ArcSin}[a x]}] \right)
\end{aligned}$$

Problem 293: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{ArcSin}[a x]^3}{(c - a^2 c x^2)^2} dx$$

Optimal (type 4, 337 leaves, 18 steps):

$$\begin{aligned}
& -\frac{3 \operatorname{ArcSin}[a x]^2}{2 a c^2 \sqrt{1 - a^2 x^2}} + \frac{x \operatorname{ArcSin}[a x]^3}{2 c^2 (1 - a^2 x^2)} - \frac{6 i \operatorname{ArcSin}[a x] \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[a x]}]}{a c^2} - \\
& \frac{i \operatorname{ArcSin}[a x]^3 \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[a x]}]}{a c^2} + \frac{3 i \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[a x]}]}{a c^2} + \frac{3 i \operatorname{ArcSin}[a x]^2 \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[a x]}]}{2 a c^2} - \\
& \frac{3 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[a x]}]}{a c^2} - \frac{3 i \operatorname{ArcSin}[a x]^2 \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[a x]}]}{2 a c^2} - \frac{3 \operatorname{ArcSin}[a x] \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[a x]}]}{a c^2} + \\
& \frac{3 \operatorname{ArcSin}[a x] \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[a x]}]}{a c^2} - \frac{3 i \operatorname{PolyLog}[4, -i e^{i \operatorname{ArcSin}[a x]}]}{a c^2} + \frac{3 i \operatorname{PolyLog}[4, i e^{i \operatorname{ArcSin}[a x]}]}{a c^2}
\end{aligned}$$

Result (type 4, 747 leaves):

$$\frac{1}{128 a c^2} \left( -7 i \pi^4 - 8 i \pi^3 \operatorname{ArcSin}[a x] - 192 \operatorname{ArcSin}[a x]^2 + 24 i \pi^2 \operatorname{ArcSin}[a x]^2 - 32 i \pi \operatorname{ArcSin}[a x]^3 - \frac{32 \operatorname{ArcSin}[a x]^3}{-1 + a x} + 16 i \operatorname{ArcSin}[a x]^4 + \right.$$

$$48 \pi^2 \operatorname{ArcSin}[a x] \operatorname{Log}[1 - i e^{-i \operatorname{ArcSin}[a x]}] - 96 \pi \operatorname{ArcSin}[a x]^2 \operatorname{Log}[1 - i e^{-i \operatorname{ArcSin}[a x]}] - 8 \pi^3 \operatorname{Log}[1 + i e^{-i \operatorname{ArcSin}[a x]}] +$$

$$64 \operatorname{ArcSin}[a x]^3 \operatorname{Log}[1 + i e^{-i \operatorname{ArcSin}[a x]}] + 384 \operatorname{ArcSin}[a x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[a x]}] + 8 \pi^3 \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[a x]}] -$$

$$384 \operatorname{ArcSin}[a x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[a x]}] - 48 \pi^2 \operatorname{ArcSin}[a x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[a x]}] + 96 \pi \operatorname{ArcSin}[a x]^2 \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[a x]}] -$$

$$64 \operatorname{ArcSin}[a x]^3 \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[a x]}] + 8 \pi^3 \operatorname{Log}\left[\tan\left(\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a x])\right)\right] + 192 i \operatorname{ArcSin}[a x]^2 \operatorname{PolyLog}[2, -i e^{-i \operatorname{ArcSin}[a x]}] +$$

$$48 i \pi (\pi - 4 \operatorname{ArcSin}[a x]) \operatorname{PolyLog}[2, i e^{-i \operatorname{ArcSin}[a x]}] + 384 i \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[a x]}] + 48 i \pi^2 \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[a x]}] -$$

$$192 i \pi \operatorname{ArcSin}[a x] \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[a x]}] + 192 i \operatorname{ArcSin}[a x]^2 \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[a x]}] - 384 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[a x]}] +$$

$$384 \operatorname{ArcSin}[a x] \operatorname{PolyLog}[3, -i e^{-i \operatorname{ArcSin}[a x]}] - 192 \pi \operatorname{PolyLog}[3, i e^{-i \operatorname{ArcSin}[a x]}] + 192 \pi \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[a x]}] -$$

$$384 \operatorname{ArcSin}[a x] \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[a x]}] - 384 i \operatorname{PolyLog}[4, -i e^{-i \operatorname{ArcSin}[a x]}] - 384 i \operatorname{PolyLog}[4, -i e^{i \operatorname{ArcSin}[a x]}] -$$

$$\left. \frac{192 \operatorname{ArcSin}[a x]^2 \sin[\frac{1}{2} \operatorname{ArcSin}[a x]]}{\cos[\frac{1}{2} \operatorname{ArcSin}[a x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[a x]]} - \frac{32 \operatorname{ArcSin}[a x]^3}{(\cos[\frac{1}{2} \operatorname{ArcSin}[a x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[a x]])^2} + \frac{192 \operatorname{ArcSin}[a x]^2 \sin[\frac{1}{2} \operatorname{ArcSin}[a x]]}{\cos[\frac{1}{2} \operatorname{ArcSin}[a x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[a x]]} \right)$$

Problem 294: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{ArcSin}[a x]^3}{(c - a^2 c x^2)^3} dx$$

Optimal (type 4, 455 leaves, 28 steps):

$$\begin{aligned} & -\frac{1}{4 a c^3 \sqrt{1 - a^2 x^2}} + \frac{x \operatorname{ArcSin}[a x]}{4 c^3 (1 - a^2 x^2)} - \frac{\operatorname{ArcSin}[a x]^2}{4 a c^3 (1 - a^2 x^2)^{3/2}} - \frac{9 \operatorname{ArcSin}[a x]^2}{8 a c^3 \sqrt{1 - a^2 x^2}} + \frac{x \operatorname{ArcSin}[a x]^3}{4 c^3 (1 - a^2 x^2)^2} + \\ & \frac{3 x \operatorname{ArcSin}[a x]^3}{8 c^3 (1 - a^2 x^2)} - \frac{5 i \operatorname{ArcSin}[a x] \operatorname{Arctan}[e^{i \operatorname{ArcSin}[a x]}]}{a c^3} - \frac{3 i \operatorname{ArcSin}[a x]^3 \operatorname{Arctan}[e^{i \operatorname{ArcSin}[a x]}]}{4 a c^3} + \\ & \frac{5 i \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[a x]}]}{2 a c^3} + \frac{9 i \operatorname{ArcSin}[a x]^2 \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[a x]}]}{8 a c^3} - \frac{5 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[a x]}]}{2 a c^3} - \\ & \frac{9 i \operatorname{ArcSin}[a x]^2 \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[a x]}]}{8 a c^3} - \frac{9 \operatorname{ArcSin}[a x] \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSin}[a x]}]}{4 a c^3} + \\ & \frac{9 \operatorname{ArcSin}[a x] \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSin}[a x]}]}{4 a c^3} - \frac{9 i \operatorname{PolyLog}[4, -i e^{i \operatorname{ArcSin}[a x]}]}{4 a c^3} + \frac{9 i \operatorname{PolyLog}[4, i e^{i \operatorname{ArcSin}[a x]}]}{4 a c^3} \end{aligned}$$

Result (type 4, 1544 leaves):

$$-\frac{1}{a c^3} \left( \frac{1}{4} (1 + 5 \operatorname{ArcSin}[a x]^2) - \right.$$

$$\begin{aligned}
& \frac{5}{2} (\operatorname{ArcSin}[ax] (\operatorname{Log}[1 - e^{i \operatorname{ArcSin}[ax]}] - \operatorname{Log}[1 + e^{i \operatorname{ArcSin}[ax]}]) + i (\operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[ax]}] - \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[ax]}])) - \\
& \frac{3}{8} \left( \frac{1}{8} \pi^3 \operatorname{Log}[\operatorname{Cot}\left(\frac{1}{2} \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)\right)] + \frac{3}{4} \pi^2 \left( \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right) \left(\operatorname{Log}[1 - e^{i \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)}] - \operatorname{Log}[1 + e^{i \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)}]\right) + \right. \right. \\
& \quad \left. \left. i \left(\operatorname{PolyLog}[2, -e^{i \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)}] - \operatorname{PolyLog}[2, e^{i \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)}]\right)\right) - \\
& \frac{3}{2} \pi \left(\left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)^2 \left(\operatorname{Log}[1 - e^{i \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)}] - \operatorname{Log}[1 + e^{i \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)}]\right) + 2 i \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right) \right. \\
& \quad \left. \left(\operatorname{PolyLog}[2, -e^{i \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)}] - \operatorname{PolyLog}[2, e^{i \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)}]\right) + 2 \left(-\operatorname{PolyLog}[3, -e^{i \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)}] + \operatorname{PolyLog}[3, e^{i \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)}]\right)\right) + \\
& 8 \left( \frac{1}{64} i \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)^4 + \frac{1}{4} i \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right)^4 - \frac{1}{8} \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)^3 \operatorname{Log}[1 + e^{i \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)}] - \right. \\
& \quad \left. \frac{1}{8} \pi^3 \left(i \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right) - \operatorname{Log}[1 + e^{2 i \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right)}]\right) - \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right)^3 \operatorname{Log}[1 + e^{2 i \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right)}] + \right. \\
& \quad \left. \frac{3}{8} i \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)^2 \operatorname{PolyLog}[2, -e^{i \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)}] + \frac{3}{4} \pi^2 \left(\frac{1}{2} i \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right)^2 - \right. \right. \\
& \quad \left. \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right) \operatorname{Log}[1 + e^{2 i \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right)}] + \frac{1}{2} i \operatorname{PolyLog}[2, -e^{2 i \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right)}]\right) + \\
& \quad \left. \frac{3}{2} i \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right)^2 \operatorname{PolyLog}[2, -e^{2 i \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right)}] - \frac{3}{4} \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right) \operatorname{PolyLog}[3, -e^{i \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)}] - \right. \\
& \quad \left. \frac{3}{2} \pi \left(\frac{1}{3} i \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right)^3 - \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right)^2 \operatorname{Log}[1 + e^{2 i \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right)}] + i \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right) \right. \right. \\
& \quad \left. \left. \operatorname{PolyLog}[2, -e^{2 i \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right)}] - \frac{1}{2} \operatorname{PolyLog}[3, -e^{2 i \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right)}]\right) - \frac{3}{2} \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right) \right. \\
& \quad \left. \operatorname{PolyLog}[3, -e^{2 i \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right)}] - \frac{3}{4} i \operatorname{PolyLog}[4, -e^{i \left(\frac{\pi}{2} - \operatorname{ArcSin}[ax]\right)}] - \frac{3}{4} i \operatorname{PolyLog}[4, -e^{2 i \left(\frac{\pi}{2} + \frac{1}{2} \left(-\frac{\pi}{2} + \operatorname{ArcSin}[ax]\right)\right)}]\right) - \right. \\
& \quad \left. \frac{\operatorname{ArcSin}[ax]^3}{16 \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[ax]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[ax]\right]\right)^4} - \frac{2 \operatorname{ArcSin}[ax] - \operatorname{ArcSin}[ax]^2 + 3 \operatorname{ArcSin}[ax]^3}{16 \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[ax]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[ax]\right]\right)^2} + \right. \\
& \quad \left. \frac{\operatorname{ArcSin}[ax]^2 \sin\left[\frac{1}{2} \operatorname{ArcSin}[ax]\right]}{8 \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[ax]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[ax]\right]\right)^3} + \right. \\
& \quad \left. \frac{\operatorname{ArcSin}[ax]^3}{16 \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[ax]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[ax]\right]\right)^4} - \right. \\
& \quad \left. \frac{\operatorname{ArcSin}[ax]^2 \sin\left[\frac{1}{2} \operatorname{ArcSin}[ax]\right]}{8 \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[ax]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[ax]\right]\right)^3} \right)
\end{aligned}$$

$$\left. \begin{aligned} & -\frac{2 \operatorname{ArcSin}[ax] - \operatorname{ArcSin}[ax]^2 - 3 \operatorname{ArcSin}[ax]^3}{16 (\cos[\frac{1}{2} \operatorname{ArcSin}[ax]] + \sin[\frac{1}{2} \operatorname{ArcSin}[ax]])^2} - \\ & -\frac{\sin[\frac{1}{2} \operatorname{ArcSin}[ax]] - 5 \operatorname{ArcSin}[ax]^2 \sin[\frac{1}{2} \operatorname{ArcSin}[ax]]}{4 (\cos[\frac{1}{2} \operatorname{ArcSin}[ax]] - \sin[\frac{1}{2} \operatorname{ArcSin}[ax]])} - \\ & \frac{\sin[\frac{1}{2} \operatorname{ArcSin}[ax]] + 5 \operatorname{ArcSin}[ax]^2 \sin[\frac{1}{2} \operatorname{ArcSin}[ax]]}{4 (\cos[\frac{1}{2} \operatorname{ArcSin}[ax]] + \sin[\frac{1}{2} \operatorname{ArcSin}[ax]])} \end{aligned} \right\}$$

**Problem 419:** Attempted integration timed out after 120 seconds.

$$\int \frac{x}{(1 - c^2 x^2)^{3/2} (a + b \operatorname{ArcSin}[c x])^2} dx$$

Optimal (type 9, 28 leaves, 0 steps):

$$\text{Unintegrable}\left[ \frac{x}{(1 - c^2 x^2)^{3/2} (a + b \operatorname{ArcSin}[c x])^2}, x \right]$$

Result (type 1, 1 leaves):

???

**Problem 424:** Attempted integration timed out after 120 seconds.

$$\int \frac{x^3}{(1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])^2} dx$$

Optimal (type 9, 30 leaves, 0 steps):

$$\text{Unintegrable}\left[ \frac{x^3}{(1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])^2}, x \right]$$

Result (type 1, 1 leaves):

???

**Problem 426:** Attempted integration timed out after 120 seconds.

$$\int \frac{x}{(1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])^2} dx$$

Optimal (type 9, 28 leaves, 0 steps):

$$\text{Unintegrable} \left[ \frac{x}{(1 - c^2 x^2)^{5/2} (a + b \text{ArcSin}[c x])^2}, x \right]$$

Result (type 1, 1 leaves):

???

**Problem 428:** Attempted integration timed out after 120 seconds.

$$\int \frac{1}{x (1 - c^2 x^2)^{5/2} (a + b \text{ArcSin}[c x])^2} dx$$

Optimal (type 9, 30 leaves, 0 steps):

$$\text{Unintegrable} \left[ \frac{1}{x (1 - c^2 x^2)^{5/2} (a + b \text{ArcSin}[c x])^2}, x \right]$$

Result (type 1, 1 leaves):

???

**Problem 441:** Unable to integrate problem.

$$\int \left( -\frac{3 x}{8 (1 - x^2) \sqrt{\text{ArcSin}[x]}} + \frac{x \text{ArcSin}[x]^{3/2}}{(1 - x^2)^2} \right) dx$$

Optimal (type 3, 42 leaves, 3 steps):

$$-\frac{3 x \sqrt{\text{ArcSin}[x]}}{4 \sqrt{1 - x^2}} + \frac{\text{ArcSin}[x]^{3/2}}{2 (1 - x^2)}$$

Result (type 8, 40 leaves):

$$\int \left( -\frac{3 x}{8 (1 - x^2) \sqrt{\text{ArcSin}[x]}} + \frac{x \text{ArcSin}[x]^{3/2}}{(1 - x^2)^2} \right) dx$$

**Problem 515:** Result more than twice size of optimal antiderivative.

$$\int \frac{(f - c f x)^{3/2} (a + b \text{ArcSin}[c x])}{(d + c d x)^{5/2}} dx$$

Optimal (type 3, 324 leaves, 9 steps):

$$\begin{aligned} & -\frac{4 b f^4 (1 - c^2 x^2)^{5/2}}{3 c (1 + c x) (d + c d x)^{5/2} (f - c f x)^{5/2}} - \frac{b f^4 (1 - c^2 x^2)^{5/2} \operatorname{ArcSin}[c x]^2}{2 c (d + c d x)^{5/2} (f - c f x)^{5/2}} - \frac{2 f^4 (1 - c x)^3 (1 - c^2 x^2) (a + b \operatorname{ArcSin}[c x])}{3 c (d + c d x)^{5/2} (f - c f x)^{5/2}} + \\ & \frac{2 f^4 (1 - c x) (1 - c^2 x^2)^2 (a + b \operatorname{ArcSin}[c x])}{c (d + c d x)^{5/2} (f - c f x)^{5/2}} + \frac{f^4 (1 - c^2 x^2)^{5/2} \operatorname{ArcSin}[c x] (a + b \operatorname{ArcSin}[c x])}{c (d + c d x)^{5/2} (f - c f x)^{5/2}} - \frac{8 b f^4 (1 - c^2 x^2)^{5/2} \operatorname{Log}[1 + c x]}{3 c (d + c d x)^{5/2} (f - c f x)^{5/2}} \end{aligned}$$

Result (type 3, 736 leaves):

$$\begin{aligned} & \frac{\sqrt{-f (-1 + c x)} \sqrt{d (1 + c x)} \left( -\frac{4 a f}{3 d^3 (1+c x)^2} + \frac{8 a f}{3 d^3 (1+c x)} \right)}{c} - \frac{a f^{3/2} \operatorname{ArcTan}\left[ \frac{c x \sqrt{-f (-1+c x)} \sqrt{d (1+c x)}}{\sqrt{d} \sqrt{f} (-1+c x) (1+c x)} \right]}{c d^{5/2}} - \\ & \left( b f \sqrt{d + c d x} \sqrt{f - c f x} \sqrt{-d f (1 - c^2 x^2)} \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) \right. \\ & \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \left( -8 + 6 \operatorname{ArcSin}[c x] + 9 \operatorname{ArcSin}[c x]^2 - 84 \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right] \right) + \right. \\ & \left. \cos\left[\frac{3}{2} \operatorname{ArcSin}[c x]\right] \left( (14 - 3 \operatorname{ArcSin}[c x]) \operatorname{ArcSin}[c x] + 28 \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right] \right) + \right. \\ & 2 \left( -4 + 4 \operatorname{ArcSin}[c x] + 6 \operatorname{ArcSin}[c x]^2 + \sqrt{1 - c^2 x^2} \left( \operatorname{ArcSin}[c x] (14 + 3 \operatorname{ArcSin}[c x]) - 28 \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right] \right) - \right. \\ & \left. 56 \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right] \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) / \\ & \left( 12 c d^3 (-1 + c x) \sqrt{-(d + c d x) (f - c f x)} \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right)^4 \right) - \\ & \left( b f \sqrt{d + c d x} \sqrt{f - c f x} \sqrt{-d f (1 - c^2 x^2)} \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) \right. \\ & \left( \cos\left[\frac{3}{2} \operatorname{ArcSin}[c x]\right] \left( \operatorname{ArcSin}[c x] + 2 \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right] \right) - \right. \\ & \left. \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \left( 4 + 3 \operatorname{ArcSin}[c x] + 6 \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right] \right) + \right. \\ & 2 \left( -2 + 2 \operatorname{ArcSin}[c x] + \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] - 4 \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right] - \right. \\ & \left. 2 \sqrt{1 - c^2 x^2} \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right] \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) / \\ & \left( 6 c d^3 (-1 + c x) \sqrt{-(d + c d x) (f - c f x)} \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right)^4 \right) \end{aligned}$$

### Problem 521: Result more than twice size of optimal antiderivative.

$$\int \frac{(f - c f x)^{5/2} (a + b \operatorname{ArcSin}[c x])}{(d + c d x)^{5/2}} dx$$

Optimal (type 3, 420 leaves, 10 steps):

$$\begin{aligned} & -\frac{b f^5 x (1 - c^2 x^2)^{5/2}}{(d + c d x)^{5/2} (f - c f x)^{5/2}} - \frac{8 b f^5 (1 - c^2 x^2)^{5/2}}{3 c (1 + c x) (d + c d x)^{5/2} (f - c f x)^{5/2}} - \frac{5 b f^5 (1 - c^2 x^2)^{5/2} \operatorname{ArcSin}[c x]^2}{2 c (d + c d x)^{5/2} (f - c f x)^{5/2}} - \\ & \frac{2 f^5 (1 - c x)^4 (1 - c^2 x^2) (a + b \operatorname{ArcSin}[c x])}{3 c (d + c d x)^{5/2} (f - c f x)^{5/2}} + \frac{10 f^5 (1 - c x)^2 (1 - c^2 x^2)^2 (a + b \operatorname{ArcSin}[c x])}{3 c (d + c d x)^{5/2} (f - c f x)^{5/2}} + \\ & \frac{5 f^5 (1 - c^2 x^2)^3 (a + b \operatorname{ArcSin}[c x])}{c (d + c d x)^{5/2} (f - c f x)^{5/2}} + \frac{5 f^5 (1 - c^2 x^2)^{5/2} \operatorname{ArcSin}[c x] (a + b \operatorname{ArcSin}[c x])}{c (d + c d x)^{5/2} (f - c f x)^{5/2}} - \frac{28 b f^5 (1 - c^2 x^2)^{5/2} \operatorname{Log}[1 + c x]}{3 c (d + c d x)^{5/2} (f - c f x)^{5/2}} \end{aligned}$$

Result (type 3, 1170 leaves):

$$\begin{aligned} & \frac{\sqrt{-f (-1 + c x)} \sqrt{d (1 + c x)} \left( \frac{a f^2}{d^3} - \frac{8 a f^2}{3 d^3 (1 + c x)^2} + \frac{28 a f^2}{3 d^3 (1 + c x)} \right)}{c} - \frac{5 a f^{5/2} \operatorname{ArcTan}\left[ \frac{c x \sqrt{-f (-1 + c x)} \sqrt{d (1 + c x)}}{\sqrt{d} \sqrt{f} (-1 + c x) (1 + c x)} \right]}{c d^{5/2}} - \\ & \left( b f^2 \sqrt{d + c d x} \sqrt{f - c f x} \sqrt{-d f (1 - c^2 x^2)} \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) \right. \\ & \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \left( -8 + 6 \operatorname{ArcSin}[c x] + 9 \operatorname{ArcSin}[c x]^2 - 84 \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) \right. + \\ & \left. \cos\left[\frac{3}{2} \operatorname{ArcSin}[c x]\right] \left( (14 - 3 \operatorname{ArcSin}[c x]) \operatorname{ArcSin}[c x] + 28 \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) \right. + \\ & 2 \left( -4 + 4 \operatorname{ArcSin}[c x] + 6 \operatorname{ArcSin}[c x]^2 + \sqrt{1 - c^2 x^2} \left( \operatorname{ArcSin}[c x] (14 + 3 \operatorname{ArcSin}[c x]) - 28 \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) \right. - \\ & \left. 56 \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right] \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) \Big/ \\ & \left( 6 c d^3 (-1 + c x) \sqrt{-(d + c d x) (f - c f x)} \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right)^4 \right) - \\ & \left( b f^2 \sqrt{d + c d x} \sqrt{f - c f x} \sqrt{-d f (1 - c^2 x^2)} \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) \right. \\ & \left( \cos\left[\frac{3}{2} \operatorname{ArcSin}[c x]\right] \left( \operatorname{ArcSin}[c x] + 2 \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) \right. - \\ & \left. \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \left( 4 + 3 \operatorname{ArcSin}[c x] + 6 \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) \right) + \\ & 2 \left( -2 + 2 \operatorname{ArcSin}[c x] + \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] - 4 \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) \right. - \end{aligned}$$

$$\begin{aligned}
& 2 \sqrt{1 - c^2 x^2} \operatorname{Log} \left[ \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right] \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \Big) \Big) \Big) / \\
& \left( 6 c d^3 (-1 + c x) \sqrt{- (d + c d x) (f - c f x)} \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right)^4 \right) - \\
& \left( b f^2 \sqrt{d + c d x} \sqrt{f - c f x} \sqrt{-d f (1 - c^2 x^2)} \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] - \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right) \right. \\
& \left( 3 \cos \left[ \frac{5}{2} \operatorname{ArcSin}[c x] \right] - 3 \operatorname{ArcSin}[c x] \cos \left[ \frac{5}{2} \operatorname{ArcSin}[c x] \right] + \right. \\
& \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \left( -20 + 24 \operatorname{ArcSin}[c x] + 27 \operatorname{ArcSin}[c x]^2 - 156 \operatorname{Log} [\cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]] \right) + \\
& \cos \left[ \frac{3}{2} \operatorname{ArcSin}[c x] \right] \left( 9 + 35 \operatorname{ArcSin}[c x] - 9 \operatorname{ArcSin}[c x]^2 + 52 \operatorname{Log} [\cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]] \right) - 20 \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] - \\
& 24 \operatorname{ArcSin}[c x] \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + 27 \operatorname{ArcSin}[c x]^2 \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] - 156 \operatorname{Log} [\cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]] \\
& \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] - 9 \sin \left[ \frac{3}{2} \operatorname{ArcSin}[c x] \right] + 35 \operatorname{ArcSin}[c x] \sin \left[ \frac{3}{2} \operatorname{ArcSin}[c x] \right] + 9 \operatorname{ArcSin}[c x]^2 \sin \left[ \frac{3}{2} \operatorname{ArcSin}[c x] \right] - \\
& 52 \operatorname{Log} [\cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]] \sin \left[ \frac{3}{2} \operatorname{ArcSin}[c x] \right] + 3 \sin \left[ \frac{5}{2} \operatorname{ArcSin}[c x] \right] + 3 \operatorname{ArcSin}[c x] \sin \left[ \frac{5}{2} \operatorname{ArcSin}[c x] \right] \Big) \Big) \Big) / \\
& \left( 12 c d^3 (-1 + c x) \sqrt{- (d + c d x) (f - c f x)} \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right)^4 \right)
\end{aligned}$$

**Problem 529: Result more than twice size of optimal antiderivative.**

$$\int \frac{(d + c d x)^{3/2} (a + b \operatorname{ArcSin}[c x])}{(f - c f x)^{3/2}} dx$$

Optimal (type 3, 252 leaves, 10 steps):

$$\begin{aligned}
& - \frac{b d^3 x (1 - c^2 x^2)^{3/2}}{(d + c d x)^{3/2} (f - c f x)^{3/2}} + \frac{4 d^3 (1 + c x) (1 - c^2 x^2) (a + b \operatorname{ArcSin}[c x])}{c (d + c d x)^{3/2} (f - c f x)^{3/2}} + \\
& \frac{d^3 (1 - c^2 x^2)^2 (a + b \operatorname{ArcSin}[c x])}{c (d + c d x)^{3/2} (f - c f x)^{3/2}} - \frac{3 d^3 (1 - c^2 x^2)^{3/2} (a + b \operatorname{ArcSin}[c x])^2}{2 b c (d + c d x)^{3/2} (f - c f x)^{3/2}} + \frac{4 b d^3 (1 - c^2 x^2)^{3/2} \operatorname{Log}[1 - c x]}{c (d + c d x)^{3/2} (f - c f x)^{3/2}}
\end{aligned}$$

Result (type 3, 514 leaves):

$$\begin{aligned}
& \frac{1}{2 c f^2} d \left( \frac{2 a (-5 + c x) \sqrt{d + c d x} \sqrt{f - c f x}}{-1 + c x} + 6 a \sqrt{d} \sqrt{f} \operatorname{ArcTan} \left[ \frac{c x \sqrt{d + c d x} \sqrt{f - c f x}}{\sqrt{d} \sqrt{f} (-1 + c^2 x^2)} \right] - \right. \\
& \left( b (1 + c x) \sqrt{d + c d x} \sqrt{f - c f x} \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \left( (-4 + \operatorname{ArcSin}[c x]) \operatorname{ArcSin}[c x] - 8 \log[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) \right. \right. \\
& \left. \left( \operatorname{ArcSin}[c x] (4 + \operatorname{ArcSin}[c x]) - 8 \log[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) \Big/ \\
& \left( \sqrt{1 - c^2 x^2} \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right)^2 \right) - \\
& \left( 2 b (1 + c x) \sqrt{d + c d x} \sqrt{f - c f x} \left( \operatorname{ArcSin}[c x]^2 \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) \right. \right. \\
& \left. \left( c x - 4 \log[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) - \right. \\
& \left. \left. \operatorname{ArcSin}[c x] \left( \left( 2 + \sqrt{1 - c^2 x^2} \right) \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \left( -2 + \sqrt{1 - c^2 x^2} \right) \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) \right) \right) \Big/ \\
& \left. \left( \sqrt{1 - c^2 x^2} \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right)^2 \right) \right)
\end{aligned}$$

**Problem 534: Result more than twice size of optimal antiderivative.**

$$\int \frac{(d + c d x)^{5/2} (a + b \operatorname{ArcSin}[c x])}{(f - c f x)^{5/2}} d x$$

Optimal (type 3, 419 leaves, 10 steps):

$$\begin{aligned}
& \frac{b d^5 x (1 - c^2 x^2)^{5/2}}{(d + c d x)^{5/2} (f - c f x)^{5/2}} - \frac{8 b d^5 (1 - c^2 x^2)^{5/2}}{3 c (1 - c x) (d + c d x)^{5/2} (f - c f x)^{5/2}} - \frac{5 b d^5 (1 - c^2 x^2)^{5/2} \operatorname{ArcSin}[c x]^2}{2 c (d + c d x)^{5/2} (f - c f x)^{5/2}} + \\
& \frac{2 d^5 (1 + c x)^4 (1 - c^2 x^2) (a + b \operatorname{ArcSin}[c x])}{3 c (d + c d x)^{5/2} (f - c f x)^{5/2}} - \frac{10 d^5 (1 + c x)^2 (1 - c^2 x^2)^2 (a + b \operatorname{ArcSin}[c x])}{3 c (d + c d x)^{5/2} (f - c f x)^{5/2}} - \\
& \frac{5 d^5 (1 - c^2 x^2)^3 (a + b \operatorname{ArcSin}[c x])}{c (d + c d x)^{5/2} (f - c f x)^{5/2}} + \frac{5 d^5 (1 - c^2 x^2)^{5/2} \operatorname{ArcSin}[c x] (a + b \operatorname{ArcSin}[c x])}{c (d + c d x)^{5/2} (f - c f x)^{5/2}} - \frac{28 b d^5 (1 - c^2 x^2)^{5/2} \log[1 - c x]}{3 c (d + c d x)^{5/2} (f - c f x)^{5/2}}
\end{aligned}$$

Result (type 3, 1181 leaves):

$$\begin{aligned}
& \frac{\sqrt{-f(-1+cx)} \sqrt{d(1+cx)} \left( -\frac{ad^2}{f^3} + \frac{8ad^2}{3f^3(-1+cx)^2} + \frac{28ad^2}{3f^3(-1+cx)} \right) - \frac{5ad^{5/2} \operatorname{ArcTan}\left[ \frac{cx\sqrt{-f(-1+cx)} \sqrt{d(1+cx)}}{\sqrt{d}\sqrt{f}(-1+cx)(1+cx)} \right]}{c f^{5/2}} + }{c} \\
& \left( b d^2 \sqrt{d+c dx} \sqrt{f-c fx} \sqrt{-df(1-c^2x^2)} \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \left( -4 + 3 \operatorname{ArcSin}[cx] - 6 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) \right. \right. \\
& \left. \left. - \cos\left[\frac{3}{2} \operatorname{ArcSin}[cx]\right] \left( \operatorname{ArcSin}[cx] - 2 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) \right) + \right. \\
& \left. 2 \left( 2 + 2 \operatorname{ArcSin}[cx] + \sqrt{1-c^2x^2} \operatorname{ArcSin}[cx] + 4 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) + \right. \\
& \left. \left. 2 \sqrt{1-c^2x^2} \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) \right) / \\
& \left( 6cf^3 \sqrt{-(d+cdx)(f-cfx)} \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right)^4 \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) \right) + \\
& \left( b d^2 \sqrt{d+c dx} \sqrt{f-c fx} \sqrt{-df(1-c^2x^2)} \right. \\
& \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \left( -8 - 6 \operatorname{ArcSin}[cx] + 9 \operatorname{ArcSin}[cx]^2 - 84 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) + \right. \\
& \left. \left. \cos\left[\frac{3}{2} \operatorname{ArcSin}[cx]\right] \left( -\operatorname{ArcSin}[cx] (14 + 3 \operatorname{ArcSin}[cx]) + 28 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) + \right. \right. \\
& \left. \left. 2 \left( 4 + 4 \operatorname{ArcSin}[cx] - 6 \operatorname{ArcSin}[cx]^2 + 56 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) + \right. \right. \\
& \left. \left. \sqrt{1-c^2x^2} \left( (14 - 3 \operatorname{ArcSin}[cx]) \operatorname{ArcSin}[cx] + 28 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) \right) \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) / \right. \\
& \left( 6cf^3 \sqrt{-(d+cdx)(f-cfx)} \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right)^4 \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) \right) + \\
& \left( b d^2 \sqrt{d+c dx} \sqrt{f-c fx} \sqrt{-df(1-c^2x^2)} \left( 3 \cos\left[\frac{5}{2} \operatorname{ArcSin}[cx]\right] + 3 \operatorname{ArcSin}[cx] \cos\left[\frac{5}{2} \operatorname{ArcSin}[cx]\right] + \right. \right. \\
& \left. \left. \cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \left( -20 - 24 \operatorname{ArcSin}[cx] + 27 \operatorname{ArcSin}[cx]^2 - 156 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) + \right. \right. \\
& \left. \left. \cos\left[\frac{3}{2} \operatorname{ArcSin}[cx]\right] \left( 9 - 35 \operatorname{ArcSin}[cx] - 9 \operatorname{ArcSin}[cx]^2 + 52 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) + 20 \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] - \right. \right. \\
& \left. \left. 24 \operatorname{ArcSin}[cx] \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] - 27 \operatorname{ArcSin}[cx]^2 \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] + 156 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) \right. \\
& \left. \left. \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] + 9 \sin\left[\frac{3}{2} \operatorname{ArcSin}[cx]\right] + 35 \operatorname{ArcSin}[cx] \sin\left[\frac{3}{2} \operatorname{ArcSin}[cx]\right] - 9 \operatorname{ArcSin}[cx]^2 \sin\left[\frac{3}{2} \operatorname{ArcSin}[cx]\right] + \right. \right. \\
& \left. \left. 52 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) \sin\left[\frac{3}{2} \operatorname{ArcSin}[cx]\right] - 3 \sin\left[\frac{5}{2} \operatorname{ArcSin}[cx]\right] + 3 \operatorname{ArcSin}[cx] \sin\left[\frac{5}{2} \operatorname{ArcSin}[cx]\right] \right) / \right. \\
& \left( 12cf^3 \sqrt{-(d+cdx)(f-cfx)} \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right)^4 \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) \right)
\end{aligned}$$

### Problem 551: Result more than twice size of optimal antiderivative.

$$\int \frac{(e - c e x)^{3/2} (a + b \operatorname{ArcSin}[c x])^2}{(d + c d x)^{5/2}} dx$$

Optimal (type 4, 544 leaves, 21 steps):

$$\begin{aligned} & \frac{8 i e^4 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])^2}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} + \frac{e^4 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])^3}{3 b c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \frac{8 b^2 e^4 (1 - c^2 x^2)^{5/2} \operatorname{Cot}\left[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]\right]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} + \\ & \frac{8 e^4 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])^2 \operatorname{Cot}\left[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]\right]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \frac{4 b e^4 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Csc}\left[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]\right]^2}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \\ & \frac{2 e^4 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])^2 \operatorname{Cot}\left[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]\right] \operatorname{Csc}\left[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]\right]^2}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \\ & \frac{32 b e^4 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[c x]}\right]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} + \frac{32 i b^2 e^4 (1 - c^2 x^2)^{5/2} \operatorname{PolyLog}\left[2, i e^{i \operatorname{ArcSin}[c x]}\right]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} \end{aligned}$$

Result (type 4, 1430 leaves):

$$\begin{aligned} & \frac{\sqrt{-e (-1 + c x)} \sqrt{d (1 + c x)} \left(-\frac{4 a^2 e}{3 d^3 (1+c x)^2} + \frac{8 a^2 e}{3 d^3 (1+c x)}\right) - \frac{a^2 e^{3/2} \operatorname{ArcTan}\left[\frac{c x \sqrt{-e (-1+c x)} \sqrt{d (1+c x)}}{\sqrt{d} \sqrt{e} (-1+c x) (1+c x)}\right]}{c d^{5/2}}}{c} - \\ & \left(a b e \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)} \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)\right. \\ & \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \left(-8 + 6 \operatorname{ArcSin}[c x] + 9 \operatorname{ArcSin}[c x]^2 - 84 \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right]\right) + \right. \\ & \left.\cos\left[\frac{3}{2} \operatorname{ArcSin}[c x]\right] \left((14 - 3 \operatorname{ArcSin}[c x]) \operatorname{ArcSin}[c x] + 28 \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right]\right) + \right. \\ & \left.2 \left(-4 + 4 \operatorname{ArcSin}[c x] + 6 \operatorname{ArcSin}[c x]^2 + \sqrt{1 - c^2 x^2} \left(\operatorname{ArcSin}[c x] (14 + 3 \operatorname{ArcSin}[c x]) - 28 \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right]\right) - \right. \\ & \left.56 \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right] \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right) \Big/ \right. \\ & \left(6 c d^3 (-1 + c x) \sqrt{- (d + c d x) (e - c e x)} \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)^4\right) - \\ & \left(a b e \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)} \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)\right. \\ & \left(\cos\left[\frac{3}{2} \operatorname{ArcSin}[c x]\right] \left(\operatorname{ArcSin}[c x] + 2 \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right]\right) - \right. \end{aligned}$$

$$\begin{aligned}
& \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \left(4 + 3 \operatorname{ArcSin}[c x] + 6 \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right]\right) + \\
& 2 \left(-2 + 2 \operatorname{ArcSin}[c x] + \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] - 4 \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right]\right) - \\
& 2 \sqrt{1 - c^2 x^2} \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right] \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\Big) \Big) / \\
& \left(3 c d^3 (-1 + c x) \sqrt{- (d + c d x) (e - c e x)} \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)^4\right) - \\
& \left(b^2 e (-1 + c x) \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)} \left(-i \pi \operatorname{ArcSin}[c x] + (1 + i) \operatorname{ArcSin}[c x]^2 - \right.\right. \\
& 4 \pi \operatorname{Log}\left[1 + e^{-i \operatorname{ArcSin}[c x]}\right] - 2 (\pi + 2 \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[c x]}\right] + 4 \pi \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right] + \\
& 2 \pi \operatorname{Log}\left[\sin\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]\right] + 4 i \operatorname{PolyLog}\left[2, i e^{i \operatorname{ArcSin}[c x]}\right] + \frac{4 \operatorname{ArcSin}[c x]^2 \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]}{\left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)^3} - \\
& \left.\left.\frac{2 \operatorname{ArcSin}[c x] (2 + \operatorname{ArcSin}[c x])}{\left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)^2} - \frac{2 (-4 + \operatorname{ArcSin}[c x]^2) \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]}{\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]}\right)\right) / \\
& \left(3 c d^3 \sqrt{- (d + c d x) (e - c e x)} \sqrt{1 - c^2 x^2} \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)^2\right) + \\
& \left(b^2 e (-1 + c x) \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)} \left(7 i \pi \operatorname{ArcSin}[c x] - (7 + 7 i) \operatorname{ArcSin}[c x]^2 - \operatorname{ArcSin}[c x]^3 + \right.\right. \\
& 28 \pi \operatorname{Log}\left[1 + e^{-i \operatorname{ArcSin}[c x]}\right] + 14 (\pi + 2 \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[c x]}\right] - 28 \pi \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right] - \\
& 14 \pi \operatorname{Log}\left[\sin\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]\right] - 28 i \operatorname{PolyLog}\left[2, i e^{i \operatorname{ArcSin}[c x]}\right] - \frac{4 \operatorname{ArcSin}[c x]^2 \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]}{\left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)^3} + \\
& \left.\left.\frac{2 \operatorname{ArcSin}[c x] (2 + \operatorname{ArcSin}[c x])}{\left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)^2} + \frac{2 (-4 + 7 \operatorname{ArcSin}[c x]^2) \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]}{\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]}\right)\right) / \\
& \left(3 c d^3 \sqrt{- (d + c d x) (e - c e x)} \sqrt{1 - c^2 x^2} \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)^2\right)
\end{aligned}$$

Problem 556: Result more than twice size of optimal antiderivative.

$$\int \frac{(e - c e x)^{5/2} (a + b \operatorname{ArcSin}[c x])^2}{(d + c d x)^{3/2}} dx$$

Optimal (type 4, 918 leaves, 28 steps):

$$\begin{aligned} & \frac{8 a b e^4 x (1 - c^2 x^2)^{3/2}}{(d + c d x)^{3/2} (e - c e x)^{3/2}} + \frac{8 b^2 e^4 (1 - c^2 x^2)^2}{c (d + c d x)^{3/2} (e - c e x)^{3/2}} - \frac{b^2 e^4 x (1 - c^2 x^2)^2}{4 (d + c d x)^{3/2} (e - c e x)^{3/2}} + \frac{b^2 e^4 (1 - c^2 x^2)^{3/2} \operatorname{ArcSin}[c x]}{4 c (d + c d x)^{3/2} (e - c e x)^{3/2}} + \\ & \frac{8 b^2 e^4 x (1 - c^2 x^2)^{3/2} \operatorname{ArcSin}[c x]}{(d + c d x)^{3/2} (e - c e x)^{3/2}} - \frac{b c e^4 x^2 (1 - c^2 x^2)^{3/2} (a + b \operatorname{ArcSin}[c x])}{2 (d + c d x)^{3/2} (e - c e x)^{3/2}} - \frac{8 e^4 (1 - c^2 x^2) (a + b \operatorname{ArcSin}[c x])^2}{c (d + c d x)^{3/2} (e - c e x)^{3/2}} + \\ & \frac{8 e^4 x (1 - c^2 x^2) (a + b \operatorname{ArcSin}[c x])^2}{(d + c d x)^{3/2} (e - c e x)^{3/2}} - \frac{8 i e^4 (1 - c^2 x^2)^{3/2} (a + b \operatorname{ArcSin}[c x])^2}{c (d + c d x)^{3/2} (e - c e x)^{3/2}} - \frac{4 e^4 (1 - c^2 x^2)^2 (a + b \operatorname{ArcSin}[c x])^2}{c (d + c d x)^{3/2} (e - c e x)^{3/2}} + \\ & \frac{e^4 x (1 - c^2 x^2)^2 (a + b \operatorname{ArcSin}[c x])^2}{(d + c d x)^{3/2} (e - c e x)^{3/2}} - \frac{5 e^4 (1 - c^2 x^2)^{3/2} (a + b \operatorname{ArcSin}[c x])^3}{2 b c (d + c d x)^{3/2} (e - c e x)^{3/2}} - \frac{32 i b e^4 (1 - c^2 x^2)^{3/2} (a + b \operatorname{ArcSin}[c x]) \operatorname{ArcTan}[e^{i \operatorname{ArcSin}[c x]}]}{c (d + c d x)^{3/2} (e - c e x)^{3/2}} + \\ & \frac{16 b e^4 (1 - c^2 x^2)^{3/2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}[1 + e^{2i \operatorname{ArcSin}[c x]}]}{c (d + c d x)^{3/2} (e - c e x)^{3/2}} + \frac{16 i b^2 e^4 (1 - c^2 x^2)^{3/2} \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}]}{c (d + c d x)^{3/2} (e - c e x)^{3/2}} - \\ & \frac{16 i b^2 e^4 (1 - c^2 x^2)^{3/2} \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{c (d + c d x)^{3/2} (e - c e x)^{3/2}} - \frac{8 i b^2 e^4 (1 - c^2 x^2)^{3/2} \operatorname{PolyLog}[2, -e^{2i \operatorname{ArcSin}[c x]}]}{c (d + c d x)^{3/2} (e - c e x)^{3/2}} \end{aligned}$$

Result (type 4, 2279 leaves):

$$\begin{aligned} & \sqrt{-e (-1 + c x)} \sqrt{d (1 + c x)} \left( -\frac{4 a^2 e^2}{d^2} + \frac{a^2 c e^2 x}{2 d^2} - \frac{8 a^2 e^2}{d^2 (1+c x)} \right) + \\ & c \\ & \frac{15 a^2 e^{5/2} \operatorname{ArcTan}\left[\frac{c x \sqrt{-e (-1+c x)} \sqrt{d (1+c x)}}{\sqrt{d} \sqrt{e} (-1+c x) (1+c x)}\right]}{2 c d^{3/2}} - \left( a b e^2 \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)} \right. \\ & \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \left( \operatorname{ArcSin}[c x] (4 + \operatorname{ArcSin}[c x]) - 8 \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right] \right) + \right. \\ & \left. \left( (-4 + \operatorname{ArcSin}[c x]) \operatorname{ArcSin}[c x] - 8 \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right] \right) \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) / \\ & \left( c d^2 \sqrt{-(d + c d x) (e - c e x)} \sqrt{1 - c^2 x^2} \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) \right) - \left( 4 a b e^2 \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)} \right. \\ & \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \left( -c x + 2 \operatorname{ArcSin}[c x] + \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] + \operatorname{ArcSin}[c x]^2 - 4 \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right] \right) + \right. \\ & \left. \left( -c x - 2 \operatorname{ArcSin}[c x] + \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] + \operatorname{ArcSin}[c x]^2 - 4 \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right] \right) \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) / \\ & \left( c d^2 \sqrt{-(d + c d x) (e - c e x)} \sqrt{1 - c^2 x^2} \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) \right) - \end{aligned}$$

$$\begin{aligned}
& \left( b^2 e^2 \sqrt{d + c dx} \sqrt{e - c ex} \sqrt{-de(1 - c^2 x^2)} \right. \\
& \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \left( -6 i \pi \operatorname{ArcSin}[cx] + (6 + 6 i) \operatorname{ArcSin}[cx]^2 + \operatorname{ArcSin}[cx]^3 - 24 \pi \operatorname{Log}\left[1 + e^{-i \operatorname{ArcSin}[cx]}\right] - \right. \right. \\
& \quad \left. \left. 12 (\pi + 2 \operatorname{ArcSin}[cx]) \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[cx]}\right] + 24 \pi \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]\right] + 12 \pi \operatorname{Log}\left[\sin\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right]\right] \right) + \right. \\
& \left. \left( -6 i \pi \operatorname{ArcSin}[cx] - (6 - 6 i) \operatorname{ArcSin}[cx]^2 + \operatorname{ArcSin}[cx]^3 - 24 \pi \operatorname{Log}\left[1 + e^{-i \operatorname{ArcSin}[cx]}\right] - 12 (\pi + 2 \operatorname{ArcSin}[cx]) \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[cx]}\right] + \right. \right. \\
& \quad \left. \left. 24 \pi \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]\right] + 12 \pi \operatorname{Log}\left[\sin\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right]\right] \right) \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] + \right. \\
& \left. \left. 24 i \operatorname{PolyLog}\left[2, i e^{i \operatorname{ArcSin}[cx]}\right] \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) \right) \right) / \\
& \left( 3 c d^2 \sqrt{-(d + c dx)(e - c ex)} \sqrt{1 - c^2 x^2} \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) \right) - \\
& \left( 2 b^2 e^2 \sqrt{d + c dx} \sqrt{e - c ex} \sqrt{-de(1 - c^2 x^2)} \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \left( 3 \sqrt{1 - c^2 x^2} (-2 + \operatorname{ArcSin}[cx]^2) + 2 \left( -3 i \pi \operatorname{ArcSin}[cx] - 3 c x \operatorname{ArcSin}[cx] + \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. (3 + 3 i) \operatorname{ArcSin}[cx]^2 + \operatorname{ArcSin}[cx]^3 - 12 \pi \operatorname{Log}\left[1 + e^{-i \operatorname{ArcSin}[cx]}\right] - 6 \pi \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[cx]}\right] - 12 \operatorname{ArcSin}[cx] \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[cx]}\right] + \right. \right. \right. \\
& \quad \left. \left. \left. 12 \pi \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]\right] + 6 \pi \operatorname{Log}\left[\sin\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right]\right] \right) + \left( 3 \sqrt{1 - c^2 x^2} (-2 + \operatorname{ArcSin}[cx]^2) + \right. \right. \\
& \quad \left. \left. 2 \left( -3 i \pi \operatorname{ArcSin}[cx] - 3 c x \operatorname{ArcSin}[cx] - (3 - 3 i) \operatorname{ArcSin}[cx]^2 + \operatorname{ArcSin}[cx]^3 - 12 \pi \operatorname{Log}\left[1 + e^{-i \operatorname{ArcSin}[cx]}\right] - 6 \pi \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[cx]}\right] - \right. \right. \\
& \quad \left. \left. 12 \operatorname{ArcSin}[cx] \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[cx]}\right] + 12 \pi \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]\right] + 6 \pi \operatorname{Log}\left[\sin\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right]\right] \right) \right) \right) \\
& \left. \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] + 24 i \operatorname{PolyLog}\left[2, i e^{i \operatorname{ArcSin}[cx]}\right] \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) \right) / \\
& \left( 3 c d^2 \sqrt{-(d + c dx)(e - c ex)} \sqrt{1 - c^2 x^2} \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) \right) - \\
& \left( b^2 e^2 \sqrt{d + c dx} \sqrt{e - c ex} \sqrt{-de(1 - c^2 x^2)} \right. \\
& \left( 96 i \operatorname{PolyLog}\left[2, i e^{i \operatorname{ArcSin}[cx]}\right] \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right) + \sin\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \right. \\
& \quad \left( -24 i \pi \operatorname{ArcSin}[cx] - 48 c x \operatorname{ArcSin}[cx] - (24 - 24 i) \operatorname{ArcSin}[cx]^2 + 10 \operatorname{ArcSin}[cx]^3 + 3 \sqrt{1 - c^2 x^2} (-16 + c x + 8 \operatorname{ArcSin}[cx]^2) - \right. \\
& \quad \left. 3 \operatorname{ArcSin}[cx] \operatorname{Cos}[2 \operatorname{ArcSin}[cx]] - 96 \pi \operatorname{Log}\left[1 + e^{-i \operatorname{ArcSin}[cx]}\right] - 48 \pi \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[cx]}\right] - 96 \operatorname{ArcSin}[cx] \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[cx]}\right] + \right. \\
& \quad \left. 96 \pi \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]\right] + 48 \pi \operatorname{Log}\left[\sin\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right]\right] - 3 \operatorname{ArcSin}[cx]^2 \operatorname{Sin}[2 \operatorname{ArcSin}[cx]] \right) + \cos\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right] \\
& \quad \left( -24 i \pi \operatorname{ArcSin}[cx] - 48 c x \operatorname{ArcSin}[cx] + (24 + 24 i) \operatorname{ArcSin}[cx]^2 + 10 \operatorname{ArcSin}[cx]^3 + 3 \sqrt{1 - c^2 x^2} (-16 + c x + 8 \operatorname{ArcSin}[cx]^2) - \right. \\
& \quad \left. 3 \operatorname{ArcSin}[cx] \operatorname{Cos}[2 \operatorname{ArcSin}[cx]] - 96 \pi \operatorname{Log}\left[1 + e^{-i \operatorname{ArcSin}[cx]}\right] - 48 \pi \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[cx]}\right] - 96 \operatorname{ArcSin}[cx] \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[cx]}\right] + \right)
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{96 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + 48 \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] - 3 \operatorname{ArcSin}[c x]^2 \sin[2 \operatorname{ArcSin}[c x]]}{12 c d^2 \sqrt{-(d + c d x)} (e - c e x) \sqrt{1 - c^2 x^2}} \right) \\
& \left( \frac{(15 + 14 \operatorname{ArcSin}[c x]) \cos[\frac{3}{2} \operatorname{ArcSin}[c x]] - \cos[\frac{5}{2} \operatorname{ArcSin}[c x]] + 2 \operatorname{ArcSin}[c x] \cos[\frac{5}{2} \operatorname{ArcSin}[c x]] + 4 \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] \left( -4 + 12 \operatorname{ArcSin}[c x] + 5 \operatorname{ArcSin}[c x]^2 - 16 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] \right) - 16 \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] - 48 \operatorname{ArcSin}[c x] \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] + 20 \operatorname{ArcSin}[c x]^2 \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] - 64 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] - 15 \sin[\frac{3}{2} \operatorname{ArcSin}[c x]] + 14 \operatorname{ArcSin}[c x] \sin[\frac{3}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{5}{2} \operatorname{ArcSin}[c x]] - 2 \operatorname{ArcSin}[c x] \sin[\frac{5}{2} \operatorname{ArcSin}[c x]]}{8 c d^2 \sqrt{-(d + c d x)} (e - c e x) \sqrt{1 - c^2 x^2}} \right) \\
& \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right)
\end{aligned}$$

**Problem 557:** Result more than twice size of optimal antiderivative.

$$\int \frac{(e - c e x)^{5/2} (a + b \operatorname{ArcSin}[c x])^2}{(d + c d x)^{5/2}} dx$$

Optimal (type 4, 729 leaves, 25 steps):

$$\begin{aligned}
& -\frac{2 a b e^5 x (1 - c^2 x^2)^{5/2}}{(d + c d x)^{5/2} (e - c e x)^{5/2}} - \frac{2 b^2 e^5 (1 - c^2 x^2)^3}{c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \frac{2 b^2 e^5 x (1 - c^2 x^2)^{5/2} \operatorname{ArcSin}[c x]}{(d + c d x)^{5/2} (e - c e x)^{5/2}} + \frac{28 i e^5 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])^2}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} + \\
& \frac{e^5 (1 - c^2 x^2)^3 (a + b \operatorname{ArcSin}[c x])^2}{c (d + c d x)^{5/2} (e - c e x)^{5/2}} + \frac{5 e^5 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])^3}{3 b c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \frac{16 b^2 e^5 (1 - c^2 x^2)^{5/2} \operatorname{Cot}[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} + \\
& \frac{28 e^5 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])^2 \operatorname{Cot}[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \frac{8 b e^5 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Csc}[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]]^2}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \\
& \frac{4 e^5 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])^2 \operatorname{Cot}[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]] \operatorname{Csc}[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]]^2}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \\
& \frac{112 b e^5 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} + \frac{112 i b^2 e^5 (1 - c^2 x^2)^{5/2} \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}}
\end{aligned}$$

Result (type 4, 2326 leaves):

$$\begin{aligned}
& \frac{\sqrt{-e(-1+cx)} \sqrt{d(1+cx)} \left( \frac{a^2 e^2}{d^3} - \frac{8 a^2 e^2}{3 d^3 (1+cx)^2} + \frac{28 a^2 e^2}{3 d^3 (1+cx)} \right)}{c} - \frac{5 a^2 e^{5/2} \operatorname{ArcTan} \left[ \frac{c x \sqrt{-e(-1+cx)} \sqrt{d(1+cx)}}{\sqrt{d} \sqrt{e} (-1+cx) (1+cx)} \right]}{c d^{5/2}} - \\
& \left( a b e^2 \sqrt{d+c dx} \sqrt{e-c ex} \sqrt{-d e(1-c^2 x^2)} \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] - \sin \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \right) \right. \\
& \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \left( -8 + 6 \operatorname{ArcSin}[cx] + 9 \operatorname{ArcSin}[cx]^2 - 84 \log \left[ \cos \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \right] \right) + \\
& \cos \left[ \frac{3}{2} \operatorname{ArcSin}[cx] \right] \left( (14 - 3 \operatorname{ArcSin}[cx]) \operatorname{ArcSin}[cx] + 28 \log \left[ \cos \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \right] \right) + \\
& 2 \left( -4 + 4 \operatorname{ArcSin}[cx] + 6 \operatorname{ArcSin}[cx]^2 + \sqrt{1-c^2 x^2} \left( \operatorname{ArcSin}[cx] (14 + 3 \operatorname{ArcSin}[cx]) - 28 \log \left[ \cos \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \right] \right) - \right. \\
& \left. 56 \log \left[ \cos \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \right] \sin \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \right) / \\
& \left( 3 c d^3 (-1+cx) \sqrt{-(d+c dx)(e-c ex)} \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \right)^4 \right) - \\
& \left( a b e^2 \sqrt{d+c dx} \sqrt{e-c ex} \sqrt{-d e(1-c^2 x^2)} \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] - \sin \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \right) \right. \\
& \left( \cos \left[ \frac{3}{2} \operatorname{ArcSin}[cx] \right] \left( \operatorname{ArcSin}[cx] + 2 \log \left[ \cos \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \right] \right) - \right. \\
& \left. \cos \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \left( 4 + 3 \operatorname{ArcSin}[cx] + 6 \log \left[ \cos \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \right] \right) + \right. \\
& 2 \left( -2 + 2 \operatorname{ArcSin}[cx] + \sqrt{1-c^2 x^2} \operatorname{ArcSin}[cx] - 4 \log \left[ \cos \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \right] \right. \\
& \left. \left. - 2 \sqrt{1-c^2 x^2} \log \left[ \cos \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \right] \right) \sin \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \right) / \\
& \left( 3 c d^3 (-1+cx) \sqrt{-(d+c dx)(e-c ex)} \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \right)^4 \right) - \\
& \left( b^2 e^2 (-1+cx) \sqrt{d+c dx} \sqrt{e-c ex} \sqrt{-d e(1-c^2 x^2)} \left( - \frac{6 c x \operatorname{ArcSin}[cx]}{\sqrt{1-c^2 x^2}} + \frac{(13+13 i) \operatorname{ArcSin}[cx]^2}{\sqrt{1-c^2 x^2}} + \frac{3 \operatorname{ArcSin}[cx]^3}{\sqrt{1-c^2 x^2}} + 3 (-2+\operatorname{ArcSin}[cx]^2) + \right. \right. \\
& \left. \left. \frac{1}{\sqrt{1-c^2 x^2}} 13 \left( -i \pi \operatorname{ArcSin}[cx] - 4 \pi \log \left[ 1 + e^{-i \operatorname{ArcSin}[cx]} \right] - 2 (\pi + 2 \operatorname{ArcSin}[cx]) \log \left[ 1 - i e^{i \operatorname{ArcSin}[cx]} \right] + 4 \pi \log \left[ \cos \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \right] + \right. \right. \\
& \left. \left. 2 \pi \log \left[ \sin \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx]) \right] \right] + 4 i \operatorname{PolyLog} \left[ 2, i e^{i \operatorname{ArcSin}[cx]} \right] \right) + \frac{4 \operatorname{ArcSin}[cx]^2 \sin \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right]}{\sqrt{1-c^2 x^2} \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[cx] \right] \right)^3} - \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{2 \operatorname{ArcSin}[c x] (2 + \operatorname{ArcSin}[c x])}{\sqrt{1 - c^2 x^2} (\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])^2} + \frac{2 (4 - 13 \operatorname{ArcSin}[c x]^2) \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]}{\sqrt{1 - c^2 x^2} (\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])} \Bigg) \Bigg) \\
& \left( 3 c d^3 \sqrt{-(d + c dx)} (e - c ex) \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right)^2 \right) - \\
& \left( b^2 e^2 (-1 + c x) \sqrt{d + c dx} \sqrt{e - c ex} \sqrt{-d e (1 - c^2 x^2)} \left( -i \pi \operatorname{ArcSin}[c x] + (1 + i) \operatorname{ArcSin}[c x]^2 - \right. \right. \\
& \left. \left. 4 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] - 2 (\pi + 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + 4 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \right. \right. \\
& \left. \left. 2 \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])] \right] + 4 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] + \frac{4 \operatorname{ArcSin}[c x]^2 \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]}{(\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])^3} - \right. \right. \\
& \left. \left. \frac{2 \operatorname{ArcSin}[c x] (2 + \operatorname{ArcSin}[c x])}{(\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])^2} - \frac{2 (-4 + \operatorname{ArcSin}[c x]^2) \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]}{\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]} \right) \right) \Bigg) \\
& \left( 3 c d^3 \sqrt{-(d + c dx)} (e - c ex) \sqrt{1 - c^2 x^2} \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right)^2 \right) + \\
& \left( 2 b^2 e^2 (-1 + c x) \sqrt{d + c dx} \sqrt{e - c ex} \sqrt{-d e (1 - c^2 x^2)} \left( 7 i \pi \operatorname{ArcSin}[c x] - (7 + 7 i) \operatorname{ArcSin}[c x]^2 - \operatorname{ArcSin}[c x]^3 + \right. \right. \\
& \left. \left. 28 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] + 14 (\pi + 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - 28 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \right. \right. \\
& \left. \left. 14 \pi \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])] \right] - 28 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] - \frac{4 \operatorname{ArcSin}[c x]^2 \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]}{(\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])^3} + \right. \right. \\
& \left. \left. \frac{2 \operatorname{ArcSin}[c x] (2 + \operatorname{ArcSin}[c x])}{(\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])^2} + \frac{2 (-4 + 7 \operatorname{ArcSin}[c x]^2) \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]}{\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]} \right) \right) \Bigg) \\
& \left( 3 c d^3 \sqrt{-(d + c dx)} (e - c ex) \sqrt{1 - c^2 x^2} \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right)^2 \right) - \\
& \left( a b e^2 \sqrt{d + c dx} \sqrt{e - c ex} \sqrt{-d e (1 - c^2 x^2)} \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) \right. \\
& \left. \left( 3 \cos[\frac{5}{2} \operatorname{ArcSin}[c x]] - 3 \operatorname{ArcSin}[c x] \cos[\frac{5}{2} \operatorname{ArcSin}[c x]] + \right. \right. \\
& \left. \left. \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] \left( -20 + 24 \operatorname{ArcSin}[c x] + 27 \operatorname{ArcSin}[c x]^2 - 156 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] \right) + \right. \right)
\end{aligned}$$

$$\begin{aligned} & \cos\left[\frac{3}{2}\arcsin(cx)\right]\left(9 + 35\arcsin(cx) - 9\arcsin(cx)^2 + 52\log\left[\cos\left[\frac{1}{2}\arcsin(cx)\right] + \sin\left[\frac{1}{2}\arcsin(cx)\right]\right]\right) - 20\sin\left[\frac{1}{2}\arcsin(cx)\right] - \\ & 24\arcsin(cx)\sin\left[\frac{1}{2}\arcsin(cx)\right] + 27\arcsin(cx)^2\sin\left[\frac{1}{2}\arcsin(cx)\right] - 156\log\left[\cos\left[\frac{1}{2}\arcsin(cx)\right] + \sin\left[\frac{1}{2}\arcsin(cx)\right]\right] \\ & \sin\left[\frac{1}{2}\arcsin(cx)\right] - 9\sin\left[\frac{3}{2}\arcsin(cx)\right] + 35\arcsin(cx)\sin\left[\frac{3}{2}\arcsin(cx)\right] + 9\arcsin(cx)^2\sin\left[\frac{3}{2}\arcsin(cx)\right] - \\ & 52\log\left[\cos\left[\frac{1}{2}\arcsin(cx)\right] + \sin\left[\frac{1}{2}\arcsin(cx)\right]\right]\sin\left[\frac{3}{2}\arcsin(cx)\right] + 3\sin\left[\frac{5}{2}\arcsin(cx)\right] + 3\arcsin(cx)\sin\left[\frac{5}{2}\arcsin(cx)\right]\Big) \Bigg) / \\ & \left(6cd^3(-1+cx)\sqrt{-(d+cdx)(e-cex)}\left(\cos\left[\frac{1}{2}\arcsin(cx)\right] + \sin\left[\frac{1}{2}\arcsin(cx)\right]\right)^4\right) \end{aligned}$$

**Problem 561:** Result more than twice size of optimal antiderivative.

$$\int \frac{(a+b\arcsin(cx))^2}{\sqrt{d+cdx}\sqrt{e-cex}} dx$$

Optimal (type 3, 55 leaves, 2 steps):

$$\frac{\sqrt{1-c^2x^2}(a+b\arcsin(cx))^3}{3bc\sqrt{d+cdx}\sqrt{e-cex}}$$

Result (type 3, 159 leaves):

$$\frac{\frac{3ab\sqrt{1-c^2x^2}\arcsin(cx)^2}{\sqrt{d+cdx}\sqrt{e-cex}} + \frac{b^2\sqrt{1-c^2x^2}\arcsin(cx)^3}{\sqrt{d+cdx}\sqrt{e-cex}} - \frac{3a^2\arctan\left[\frac{cx\sqrt{d+cdx}\sqrt{e-cex}}{\sqrt{d}\sqrt{e}(-1+c^2x^2)}\right]}{\sqrt{d}\sqrt{e}}}{3c}$$

**Problem 564:** Result more than twice size of optimal antiderivative.

$$\int \frac{(d+cdx)^{5/2}(a+b\arcsin(cx))^2}{(e-cex)^{3/2}} dx$$

Optimal (type 4, 918 leaves, 28 steps):

$$\begin{aligned}
& - \frac{8 a b d^4 x (1 - c^2 x^2)^{3/2}}{(d + c d x)^{3/2} (e - c e x)^{3/2}} - \frac{8 b^2 d^4 (1 - c^2 x^2)^2}{c (d + c d x)^{3/2} (e - c e x)^{3/2}} - \frac{b^2 d^4 x (1 - c^2 x^2)^2}{4 (d + c d x)^{3/2} (e - c e x)^{3/2}} + \frac{b^2 d^4 (1 - c^2 x^2)^{3/2} \text{ArcSin}[c x]}{4 c (d + c d x)^{3/2} (e - c e x)^{3/2}} - \\
& \frac{8 b^2 d^4 x (1 - c^2 x^2)^{3/2} \text{ArcSin}[c x]}{(d + c d x)^{3/2} (e - c e x)^{3/2}} - \frac{b c d^4 x^2 (1 - c^2 x^2)^{3/2} (a + b \text{ArcSin}[c x])}{2 (d + c d x)^{3/2} (e - c e x)^{3/2}} + \frac{8 d^4 (1 - c^2 x^2) (a + b \text{ArcSin}[c x])^2}{c (d + c d x)^{3/2} (e - c e x)^{3/2}} + \\
& \frac{8 d^4 x (1 - c^2 x^2) (a + b \text{ArcSin}[c x])^2}{(d + c d x)^{3/2} (e - c e x)^{3/2}} - \frac{8 i d^4 (1 - c^2 x^2)^{3/2} (a + b \text{ArcSin}[c x])^2}{c (d + c d x)^{3/2} (e - c e x)^{3/2}} + \frac{4 d^4 (1 - c^2 x^2)^2 (a + b \text{ArcSin}[c x])^2}{c (d + c d x)^{3/2} (e - c e x)^{3/2}} + \\
& \frac{d^4 x (1 - c^2 x^2)^2 (a + b \text{ArcSin}[c x])^2}{2 (d + c d x)^{3/2} (e - c e x)^{3/2}} - \frac{5 d^4 (1 - c^2 x^2)^{3/2} (a + b \text{ArcSin}[c x])^3}{2 b c (d + c d x)^{3/2} (e - c e x)^{3/2}} + \frac{32 i b d^4 (1 - c^2 x^2)^{3/2} (a + b \text{ArcSin}[c x]) \text{ArcTan}[e^{i \text{ArcSin}[c x]}]}{c (d + c d x)^{3/2} (e - c e x)^{3/2}} + \\
& \frac{16 b d^4 (1 - c^2 x^2)^{3/2} (a + b \text{ArcSin}[c x]) \text{Log}[1 + e^{2 i \text{ArcSin}[c x]}]}{c (d + c d x)^{3/2} (e - c e x)^{3/2}} - \frac{16 i b^2 d^4 (1 - c^2 x^2)^{3/2} \text{PolyLog}[2, -i e^{i \text{ArcSin}[c x]}]}{c (d + c d x)^{3/2} (e - c e x)^{3/2}} + \\
& \frac{16 i b^2 d^4 (1 - c^2 x^2)^{3/2} \text{PolyLog}[2, i e^{i \text{ArcSin}[c x]}]}{c (d + c d x)^{3/2} (e - c e x)^{3/2}} - \frac{8 i b^2 d^4 (1 - c^2 x^2)^{3/2} \text{PolyLog}[2, -e^{2 i \text{ArcSin}[c x]}]}{c (d + c d x)^{3/2} (e - c e x)^{3/2}}
\end{aligned}$$

Result (type 4, 2029 leaves):

$$\begin{aligned}
& \frac{\sqrt{-e (-1 + c x)} \sqrt{d (1 + c x)} \left( \frac{4 a^2 d^2}{e^2} + \frac{a^2 c d^2 x}{2 e^2} - \frac{8 a^2 d^2}{e^2 (-1 + c x)} \right)}{c} + \\
& \frac{15 a^2 d^{5/2} \text{ArcTan}\left[\frac{c x \sqrt{-e (-1 + c x)} \sqrt{d (1 + c x)}}{\sqrt{d} \sqrt{e} (-1 + c x) (1 + c x)}\right]}{2 c e^{3/2}} - \left( a b d^2 (1 + c x) \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)} \right. \\
& \left( \cos\left[\frac{1}{2} \text{ArcSin}[c x]\right] \left( (-4 + \text{ArcSin}[c x]) \text{ArcSin}[c x] - 8 \log[\cos[\frac{1}{2} \text{ArcSin}[c x]] - \sin[\frac{1}{2} \text{ArcSin}[c x]]] \right) - \right. \\
& \left. \left( \text{ArcSin}[c x] (4 + \text{ArcSin}[c x]) - 8 \log[\cos[\frac{1}{2} \text{ArcSin}[c x]] - \sin[\frac{1}{2} \text{ArcSin}[c x]]] \right) \sin[\frac{1}{2} \text{ArcSin}[c x]] \right) / \\
& \left( c e^2 \sqrt{-(d + c d x) (e - c e x)} \sqrt{1 - c^2 x^2} \left( \cos\left[\frac{1}{2} \text{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \text{ArcSin}[c x]\right] \right) \left( \cos\left[\frac{1}{2} \text{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \text{ArcSin}[c x]\right] \right)^2 \right) + \\
& \left( 4 a b d^2 (1 + c x) \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)} \right. \\
& \left( \cos\left[\frac{1}{2} \text{ArcSin}[c x]\right] \left( -c x + 2 \text{ArcSin}[c x] + \sqrt{1 - c^2 x^2} \text{ArcSin}[c x] - \text{ArcSin}[c x]^2 + 4 \log[\cos[\frac{1}{2} \text{ArcSin}[c x]] - \sin[\frac{1}{2} \text{ArcSin}[c x]]] \right) + \right. \\
& \left. \left( c x + 2 \text{ArcSin}[c x] - \sqrt{1 - c^2 x^2} \text{ArcSin}[c x] + \text{ArcSin}[c x]^2 - 4 \log[\cos[\frac{1}{2} \text{ArcSin}[c x]] - \sin[\frac{1}{2} \text{ArcSin}[c x]]] \right) \sin[\frac{1}{2} \text{ArcSin}[c x]] \right) / \\
& \left( c e^2 \sqrt{-(d + c d x) (e - c e x)} \sqrt{1 - c^2 x^2} \left( \cos\left[\frac{1}{2} \text{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \text{ArcSin}[c x]\right] \right) \left( \cos\left[\frac{1}{2} \text{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \text{ArcSin}[c x]\right] \right)^2 \right) -
\end{aligned}$$

$$\begin{aligned}
& \left( b^2 d^2 (1+c x) \sqrt{d+c dx} \sqrt{e-c ex} \sqrt{-d e (1-c^2 x^2)} \left( -18 i \pi \operatorname{ArcSin}[c x] - (6-6 i) \operatorname{ArcSin}[c x]^2 + \operatorname{ArcSin}[c x]^3 - \right. \right. \\
& 24 \pi \operatorname{Log}[1+e^{-i} \operatorname{ArcSin}[c x]] + 12 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[1+i e^i \operatorname{ArcSin}[c x]] + 24 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \\
& \left. \left. 12 \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])] + 24 i \operatorname{PolyLog}[2, -i e^i \operatorname{ArcSin}[c x]] - \frac{12 \operatorname{ArcSin}[c x]^2 \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]}{\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]}] \right) \right) / \\
& \left( 3 c e^2 \sqrt{-(d+c dx) (e-c ex)} \sqrt{1-c^2 x^2} \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right)^2 \right) - \\
& \left( b^2 d^2 (1+c x) \sqrt{d+c dx} \sqrt{e-c ex} \sqrt{-d e (1-c^2 x^2)} \left( \frac{96 c x \operatorname{ArcSin}[c x]}{\sqrt{1-c^2 x^2}} - \frac{(48-48 i) \operatorname{ArcSin}[c x]^2}{\sqrt{1-c^2 x^2}} + \frac{20 \operatorname{ArcSin}[c x]^3}{\sqrt{1-c^2 x^2}} - \right. \right. \\
& 48 (-2 + \operatorname{ArcSin}[c x]^2) - 6 c x (-1 + 2 \operatorname{ArcSin}[c x]^2) - \frac{6 \operatorname{ArcSin}[c x] \cos[2 \operatorname{ArcSin}[c x]]}{\sqrt{1-c^2 x^2}} + \frac{1}{\sqrt{1-c^2 x^2}} \\
& 48 \left( -3 i \pi \operatorname{ArcSin}[c x] - 4 \pi \operatorname{Log}[1+e^{-i} \operatorname{ArcSin}[c x]] + 2 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[1+i e^i \operatorname{ArcSin}[c x]] + 4 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \right. \\
& \left. \left. 2 \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])] + 4 i \operatorname{PolyLog}[2, -i e^i \operatorname{ArcSin}[c x]] - \frac{96 \operatorname{ArcSin}[c x]^2 \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]}{\sqrt{1-c^2 x^2} (\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])} \right) \right) / \\
& \left( 24 c e^2 \sqrt{-(d+c dx) (e-c ex)} \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right)^2 \right) - \\
& \left( 2 b^2 d^2 (1+c x) \sqrt{d+c dx} \sqrt{e-c ex} \sqrt{-d e (1-c^2 x^2)} \left( 6 + \frac{6 c x \operatorname{ArcSin}[c x]}{\sqrt{1-c^2 x^2}} - 3 \operatorname{ArcSin}[c x]^2 - \frac{(6-6 i) \operatorname{ArcSin}[c x]^2}{\sqrt{1-c^2 x^2}} + \frac{2 \operatorname{ArcSin}[c x]^3}{\sqrt{1-c^2 x^2}} + \right. \right. \\
& \frac{1}{\sqrt{1-c^2 x^2}} 6 \left( -3 i \pi \operatorname{ArcSin}[c x] - 4 \pi \operatorname{Log}[1+e^{-i} \operatorname{ArcSin}[c x]] + 2 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[1+i e^i \operatorname{ArcSin}[c x]] + 4 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \right. \\
& \left. \left. 2 \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])] + 4 i \operatorname{PolyLog}[2, -i e^i \operatorname{ArcSin}[c x]] - \frac{12 \operatorname{ArcSin}[c x]^2 \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]}{\sqrt{1-c^2 x^2} (\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])} \right) \right) / \\
& \left( 3 c e^2 \sqrt{-(d+c dx) (e-c ex)} \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right)^2 \right) + \left( a b d^2 (1+c x) \sqrt{d+c dx} \sqrt{e-c ex} \right. \\
& \sqrt{-d e (1-c^2 x^2)} \left( (-15 + 14 \operatorname{ArcSin}[c x]) \cos[\frac{3}{2} \operatorname{ArcSin}[c x]] + \cos[\frac{5}{2} \operatorname{ArcSin}[c x]] + 2 \operatorname{ArcSin}[c x] \cos[\frac{5}{2} \operatorname{ArcSin}[c x]] + \right. \\
& \left. \left. \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] \left( 16 + 48 \operatorname{ArcSin}[c x] - 20 \operatorname{ArcSin}[c x]^2 + 64 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] \right) - \right. \right. \\
& 16 \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] + 48 \operatorname{ArcSin}[c x] \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] + 20 \operatorname{ArcSin}[c x]^2 \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] - 
\end{aligned}$$

$$\begin{aligned} & - \frac{64 \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] - 15 \sin[\frac{3}{2} \operatorname{ArcSin}[c x]] - \\ & 14 \operatorname{ArcSin}[c x] \sin[\frac{3}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{5}{2} \operatorname{ArcSin}[c x]] + 2 \operatorname{ArcSin}[c x] \sin[\frac{5}{2} \operatorname{ArcSin}[c x]]}{\left(8 c e^2 \sqrt{-(d+c d x)} (e-c e x) \sqrt{1-c^2 x^2}\right) \left(\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]\right) \left(\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]\right)^2} \end{aligned}$$

**Problem 568:** Result more than twice size of optimal antiderivative.

$$\int \frac{(a+b \operatorname{ArcSin}[c x])^2}{(d+c d x)^{3/2} (e-c e x)^{3/2}} dx$$

Optimal (type 4, 217 leaves, 7 steps):

$$\begin{aligned} & \frac{x (1-c^2 x^2) (a+b \operatorname{ArcSin}[c x])^2}{(d+c d x)^{3/2} (e-c e x)^{3/2}} - \frac{\frac{i}{2} (1-c^2 x^2)^{3/2} (a+b \operatorname{ArcSin}[c x])^2}{c (d+c d x)^{3/2} (e-c e x)^{3/2}} + \\ & \frac{2 b (1-c^2 x^2)^{3/2} (a+b \operatorname{ArcSin}[c x]) \operatorname{Log}[1+e^{2 i \operatorname{ArcSin}[c x]}]}{c (d+c d x)^{3/2} (e-c e x)^{3/2}} - \frac{\frac{i}{2} b^2 (1-c^2 x^2)^{3/2} \operatorname{PolyLog}[2, -e^{2 i \operatorname{ArcSin}[c x]}]}{c (d+c d x)^{3/2} (e-c e x)^{3/2}} \end{aligned}$$

Result (type 4, 550 leaves):

$$\begin{aligned} & \frac{1}{c d e \sqrt{d+c d x} \sqrt{e-c e x}} \left( a^2 c x + 2 a b c x \operatorname{ArcSin}[c x] + 2 \frac{i}{2} b^2 \pi \sqrt{1-c^2 x^2} \operatorname{ArcSin}[c x] + b^2 c x \operatorname{ArcSin}[c x]^2 - \frac{i}{2} b^2 \sqrt{1-c^2 x^2} \operatorname{ArcSin}[c x]^2 + \right. \\ & 4 b^2 \pi \sqrt{1-c^2 x^2} \operatorname{Log}[1+e^{-i \operatorname{ArcSin}[c x]}] + b^2 \pi \sqrt{1-c^2 x^2} \operatorname{Log}[1-\frac{i}{2} e^{i \operatorname{ArcSin}[c x]}] + 2 b^2 \sqrt{1-c^2 x^2} \operatorname{ArcSin}[c x] \operatorname{Log}[1-\frac{i}{2} e^{i \operatorname{ArcSin}[c x]}] - \\ & b^2 \pi \sqrt{1-c^2 x^2} \operatorname{Log}[1+\frac{i}{2} e^{i \operatorname{ArcSin}[c x]}] + 2 b^2 \sqrt{1-c^2 x^2} \operatorname{ArcSin}[c x] \operatorname{Log}[1+\frac{i}{2} e^{i \operatorname{ArcSin}[c x]}] - 4 b^2 \pi \sqrt{1-c^2 x^2} \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \\ & b^2 \pi \sqrt{1-c^2 x^2} \operatorname{Log}[-\cos[\frac{1}{4} (\pi+2 \operatorname{ArcSin}[c x])] ] + 2 a b \sqrt{1-c^2 x^2} \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \\ & 2 a b \sqrt{1-c^2 x^2} \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] - b^2 \pi \sqrt{1-c^2 x^2} \operatorname{Log}[\sin[\frac{1}{4} (\pi+2 \operatorname{ArcSin}[c x])] ] - \\ & \left. 2 \frac{i}{2} b^2 \sqrt{1-c^2 x^2} \operatorname{PolyLog}[2, -\frac{i}{2} e^{i \operatorname{ArcSin}[c x]}] - 2 \frac{i}{2} b^2 \sqrt{1-c^2 x^2} \operatorname{PolyLog}[2, \frac{i}{2} e^{i \operatorname{ArcSin}[c x]}] \right) \end{aligned}$$

**Problem 570:** Result more than twice size of optimal antiderivative.

$$\int \frac{(d+c d x)^{5/2} (a+b \operatorname{ArcSin}[c x])^2}{(e-c e x)^{5/2}} dx$$

Optimal (type 4, 730 leaves, 25 steps):

$$\begin{aligned}
& \frac{2 a b d^5 x (1 - c^2 x^2)^{5/2}}{(d + c d x)^{5/2} (e - c e x)^{5/2}} + \frac{2 b^2 d^5 (1 - c^2 x^2)^3}{c (d + c d x)^{5/2} (e - c e x)^{5/2}} + \frac{2 b^2 d^5 x (1 - c^2 x^2)^{5/2} \text{ArcSin}[c x]}{(d + c d x)^{5/2} (e - c e x)^{5/2}} - \frac{28 i d^5 (1 - c^2 x^2)^{5/2} (a + b \text{ArcSin}[c x])^2}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \\
& \frac{d^5 (1 - c^2 x^2)^3 (a + b \text{ArcSin}[c x])^2}{c (d + c d x)^{5/2} (e - c e x)^{5/2}} + \frac{5 d^5 (1 - c^2 x^2)^{5/2} (a + b \text{ArcSin}[c x])^3}{3 b c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \frac{112 b d^5 (1 - c^2 x^2)^{5/2} (a + b \text{ArcSin}[c x]) \text{Log}[1 - i e^{-i \text{ArcSin}[c x]}]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \\
& \frac{112 i b^2 d^5 (1 - c^2 x^2)^{5/2} \text{PolyLog}[2, i e^{-i \text{ArcSin}[c x]}]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \frac{8 b d^5 (1 - c^2 x^2)^{5/2} (a + b \text{ArcSin}[c x]) \text{Sec}[\frac{\pi}{4} + \frac{1}{2} \text{ArcSin}[c x]]^2}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} + \\
& \frac{16 b^2 d^5 (1 - c^2 x^2)^{5/2} \text{Tan}[\frac{\pi}{4} + \frac{1}{2} \text{ArcSin}[c x]]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \frac{28 d^5 (1 - c^2 x^2)^{5/2} (a + b \text{ArcSin}[c x])^2 \text{Tan}[\frac{\pi}{4} + \frac{1}{2} \text{ArcSin}[c x]]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} + \\
& \frac{4 d^5 (1 - c^2 x^2)^{5/2} (a + b \text{ArcSin}[c x])^2 \text{Sec}[\frac{\pi}{4} + \frac{1}{2} \text{ArcSin}[c x]]^2 \text{Tan}[\frac{\pi}{4} + \frac{1}{2} \text{ArcSin}[c x]]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}}
\end{aligned}$$

Result (type 4, 2300 leaves):

$$\begin{aligned}
& \frac{\sqrt{-e (-1 + c x)} \sqrt{d (1 + c x)} \left(-\frac{a^2 d^2}{e^3} + \frac{8 a^2 d^2}{3 e^3 (-1 + c x)^2} + \frac{28 a^2 d^2}{3 e^3 (-1 + c x)}\right)}{c} - \frac{5 a^2 d^{5/2} \text{ArcTan}\left[\frac{c x \sqrt{-e (-1 + c x)} \sqrt{d (1 + c x)}}{\sqrt{d} \sqrt{e} (-1 + c x) (1 + c x)}\right]}{c e^{5/2}} + \\
& \left(a b d^2 \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)} \left(\cos\left[\frac{1}{2} \text{ArcSin}[c x]\right] \left(-4 + 3 \text{ArcSin}[c x] - 6 \text{Log}[\cos[\frac{1}{2} \text{ArcSin}[c x]] - \sin[\frac{1}{2} \text{ArcSin}[c x]]]\right)\right.\right. - \\
& \left.\cos\left[\frac{3}{2} \text{ArcSin}[c x]\right] \left(\text{ArcSin}[c x] - 2 \text{Log}[\cos[\frac{1}{2} \text{ArcSin}[c x]] - \sin[\frac{1}{2} \text{ArcSin}[c x]]]\right)\right) + \\
& 2 \left(2 + 2 \text{ArcSin}[c x] + \sqrt{1 - c^2 x^2} \text{ArcSin}[c x] + 4 \text{Log}[\cos[\frac{1}{2} \text{ArcSin}[c x]] - \sin[\frac{1}{2} \text{ArcSin}[c x]]] + \right. \\
& \left.2 \sqrt{1 - c^2 x^2} \text{Log}[\cos[\frac{1}{2} \text{ArcSin}[c x]] - \sin[\frac{1}{2} \text{ArcSin}[c x]]]\right) \sin[\frac{1}{2} \text{ArcSin}[c x]]\Bigg)/ \\
& \left(3 c e^3 \sqrt{-(d + c d x) (e - c e x)} \left(\cos[\frac{1}{2} \text{ArcSin}[c x]] - \sin[\frac{1}{2} \text{ArcSin}[c x]]\right)^4 \left(\cos[\frac{1}{2} \text{ArcSin}[c x]] + \sin[\frac{1}{2} \text{ArcSin}[c x]]\right)\right) + \\
& \left(a b d^2 \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)} \right. \\
& \left(\cos[\frac{1}{2} \text{ArcSin}[c x]] \left(-8 - 6 \text{ArcSin}[c x] + 9 \text{ArcSin}[c x]^2 - 84 \text{Log}[\cos[\frac{1}{2} \text{ArcSin}[c x]] - \sin[\frac{1}{2} \text{ArcSin}[c x]]]\right) + \right. \\
& \left.\cos[\frac{3}{2} \text{ArcSin}[c x]] \left(-\text{ArcSin}[c x] (14 + 3 \text{ArcSin}[c x]) + 28 \text{Log}[\cos[\frac{1}{2} \text{ArcSin}[c x]] - \sin[\frac{1}{2} \text{ArcSin}[c x]]]\right) + \right. \\
& \left.2 \left(4 + 4 \text{ArcSin}[c x] - 6 \text{ArcSin}[c x]^2 + 56 \text{Log}[\cos[\frac{1}{2} \text{ArcSin}[c x]] - \sin[\frac{1}{2} \text{ArcSin}[c x]]] + \right. \right. \\
& \left.\left.\sqrt{1 - c^2 x^2} \left((14 - 3 \text{ArcSin}[c x]) \text{ArcSin}[c x] + 28 \text{Log}[\cos[\frac{1}{2} \text{ArcSin}[c x]] - \sin[\frac{1}{2} \text{ArcSin}[c x]]]\right)\right) \sin[\frac{1}{2} \text{ArcSin}[c x]]\right)
\end{aligned}$$

$$\begin{aligned}
& \left( 3 c e^3 \sqrt{-(d + c d x) (e - c e x)} \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] - \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right)^4 \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right) \right) + \\
& \left( b^2 d^2 (1 + c x) \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)} \right. \\
& \left. \left( -3 i \pi \operatorname{ArcSin}[c x] + \frac{4 \operatorname{ArcSin}[c x]}{-1 + c x} - (1 - i) \operatorname{ArcSin}[c x]^2 - \frac{2 \operatorname{ArcSin}[c x]^2}{-1 + c x} - 4 \pi \operatorname{Log}[1 + e^{-i} \operatorname{ArcSin}[c x]] + 2 \pi \operatorname{Log}[1 + i e^i \operatorname{ArcSin}[c x]] - \right. \right. \\
& \left. \left. 4 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^i \operatorname{ArcSin}[c x]] + 4 \pi \operatorname{Log}[\cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]] - 2 \pi \operatorname{Log}[-\cos \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]] + \right. \right. \\
& \left. \left. 4 i \operatorname{PolyLog}[2, -i e^i \operatorname{ArcSin}[c x]] + \frac{2 (4 + \operatorname{ArcSin}[c x]^2 + c x (-4 + \operatorname{ArcSin}[c x]^2)) \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]}{\left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] - \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right)^3} \right) \right) / \\
& \left( 3 c e^3 \sqrt{-(d + c d x) (e - c e x)} \sqrt{1 - c^2 x^2} \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right)^2 \right) + \\
& \left( b^2 d^2 (1 + c x) \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)} \right. \\
& \left. \left( 6 + \frac{6 c x \operatorname{ArcSin}[c x]}{\sqrt{1 - c^2 x^2}} - \frac{2 (-2 + \operatorname{ArcSin}[c x]) \operatorname{ArcSin}[c x]}{(-1 + c x) \sqrt{1 - c^2 x^2}} - 3 \operatorname{ArcSin}[c x]^2 - \frac{(13 - 13 i) \operatorname{ArcSin}[c x]^2}{\sqrt{1 - c^2 x^2}} + \frac{3 \operatorname{ArcSin}[c x]^3}{\sqrt{1 - c^2 x^2}} + \right. \right. \\
& \left. \left. \frac{1}{\sqrt{1 - c^2 x^2}} 13 \left( -3 i \pi \operatorname{ArcSin}[c x] - 4 \pi \operatorname{Log}[1 + e^{-i} \operatorname{ArcSin}[c x]] + 2 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[1 + i e^i \operatorname{ArcSin}[c x]] + \right. \right. \\
& \left. \left. 4 \pi \operatorname{Log}[\cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]] - 2 \pi \operatorname{Log}[-\cos \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]] + 4 i \operatorname{PolyLog}[2, -i e^i \operatorname{ArcSin}[c x]] + \right. \right. \\
& \left. \left. \frac{4 \operatorname{ArcSin}[c x]^2 \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]}{\sqrt{1 - c^2 x^2} \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] - \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right)^3} + \frac{2 (4 - 13 \operatorname{ArcSin}[c x]^2) \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]}{\sqrt{1 - c^2 x^2} \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] - \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right)} \right) \right) \right) / \\
& \left( 3 c e^3 \sqrt{-(d + c d x) (e - c e x)} \left( \cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right] \right)^2 \right) + \\
& \left( 2 b^2 d^2 (1 + c x) \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)} \right. \\
& \left. \left( -21 i \pi \operatorname{ArcSin}[c x] - \frac{2 (-2 + \operatorname{ArcSin}[c x]) \operatorname{ArcSin}[c x]}{-1 + c x} - (7 - 7 i) \operatorname{ArcSin}[c x]^2 + \operatorname{ArcSin}[c x]^3 - 28 \pi \operatorname{Log}[1 + e^{-i} \operatorname{ArcSin}[c x]] + \right. \right. \\
& \left. \left. \right. \right)
\end{aligned}$$

$$\begin{aligned}
& 14 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 + i e^{i \operatorname{ArcSin}[c x]}\right] + 28 \pi \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right] - 14 \pi \operatorname{Log}\left[-\cos\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]\right] + \\
& 28 i \operatorname{PolyLog}\left[2, -i e^{i \operatorname{ArcSin}[c x]}\right] + \frac{4 \operatorname{ArcSin}[c x]^2 \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]}{\left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)^3} + \frac{2 (4 - 7 \operatorname{ArcSin}[c x]^2) \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]}{\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]} \Bigg) / \\
& \left(3 c e^3 \sqrt{-(d + c d x)} (e - c e x) \sqrt{1 - c^2 x^2} \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)^2\right) + \\
& \left(a b d^2 \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)}\right) \left(3 \cos\left[\frac{5}{2} \operatorname{ArcSin}[c x]\right] + 3 \operatorname{ArcSin}[c x] \cos\left[\frac{5}{2} \operatorname{ArcSin}[c x]\right] + \right. \\
& \left.\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \left(-20 - 24 \operatorname{ArcSin}[c x] + 27 \operatorname{ArcSin}[c x]^2 - 156 \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)\right. + \right. \\
& \left.\cos\left[\frac{3}{2} \operatorname{ArcSin}[c x]\right] \left(9 - 35 \operatorname{ArcSin}[c x] - 9 \operatorname{ArcSin}[c x]^2 + 52 \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)\right. + 20 \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \right. \\
& \left.24 \operatorname{ArcSin}[c x] \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - 27 \operatorname{ArcSin}[c x]^2 \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + 156 \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right]\right. + \right. \\
& \left.\sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + 9 \sin\left[\frac{3}{2} \operatorname{ArcSin}[c x]\right] + 35 \operatorname{ArcSin}[c x] \sin\left[\frac{3}{2} \operatorname{ArcSin}[c x]\right] - 9 \operatorname{ArcSin}[c x]^2 \sin\left[\frac{3}{2} \operatorname{ArcSin}[c x]\right] + \right. \\
& \left.52 \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right] \sin\left[\frac{3}{2} \operatorname{ArcSin}[c x]\right] - 3 \sin\left[\frac{5}{2} \operatorname{ArcSin}[c x]\right] + 3 \operatorname{ArcSin}[c x] \sin\left[\frac{5}{2} \operatorname{ArcSin}[c x]\right]\right) / \\
& \left(6 c e^3 \sqrt{-(d + c d x)} (e - c e x) \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)^4 \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)\right)
\end{aligned}$$

**Problem 571:** Result more than twice size of optimal antiderivative.

$$\int \frac{(d + c d x)^{3/2} (a + b \operatorname{ArcSin}[c x])^2}{(e - c e x)^{5/2}} dx$$

Optimal (type 4, 544 leaves, 21 steps):

$$\begin{aligned}
& - \frac{8 i d^4 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])^2}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} + \frac{d^4 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])^3}{3 b c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \frac{32 b d^4 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}[1 - i e^{-i \operatorname{ArcSin}[c x]}]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} \\
& + \frac{32 i b^2 d^4 (1 - c^2 x^2)^{5/2} \operatorname{PolyLog}[2, i e^{-i \operatorname{ArcSin}[c x]}]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \frac{4 b d^4 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Sec}\left[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]\right]^2}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} + \\
& \frac{8 b^2 d^4 (1 - c^2 x^2)^{5/2} \operatorname{Tan}\left[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]\right]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \frac{8 d^4 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])^2 \operatorname{Tan}\left[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]\right]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} + \\
& \frac{2 d^4 (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])^2 \operatorname{Sec}\left[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]\right]^2 \operatorname{Tan}\left[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]\right]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}}
\end{aligned}$$

Result (type 4, 1411 leaves):

$$\begin{aligned}
& \frac{\sqrt{-e (-1 + c x)} \sqrt{d (1 + c x)} \left(\frac{4 a^2 d}{3 e^3 (-1+c x)^2} + \frac{8 a^2 d}{3 e^3 (-1+c x)}\right)}{c} - \frac{a^2 d^{3/2} \operatorname{ArcTan}\left[\frac{c x \sqrt{-e (-1+c x)} \sqrt{d (1+c x)}}{\sqrt{d} \sqrt{e} (-1+c x) (1+c x)}\right]}{c e^{5/2}} + \\
& \left(a b d \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)} \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \left(-4 + 3 \operatorname{ArcSin}[c x] - 6 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]]\right) - \right.\right. \\
& \cos\left[\frac{3}{2} \operatorname{ArcSin}[c x]\right] \left(\operatorname{ArcSin}[c x] - 2 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]]\right) + \\
& 2 \left(2 + 2 \operatorname{ArcSin}[c x] + \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] + 4 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]] + \right. \\
& \left.2 \sqrt{1 - c^2 x^2} \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]]\right) \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\Bigg)/ \\
& \left(3 c e^3 \sqrt{-(d + c d x) (e - c e x)} \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)^4 \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)\right) + \\
& \left(a b d \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)} \right. \\
& \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \left(-8 - 6 \operatorname{ArcSin}[c x] + 9 \operatorname{ArcSin}[c x]^2 - 84 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]]\right) + \right. \\
& \cos\left[\frac{3}{2} \operatorname{ArcSin}[c x]\right] \left(-\operatorname{ArcSin}[c x] (14 + 3 \operatorname{ArcSin}[c x]) + 28 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]]\right) + \\
& 2 \left(4 + 4 \operatorname{ArcSin}[c x] - 6 \operatorname{ArcSin}[c x]^2 + 56 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]] + \right. \\
& \left.\sqrt{1 - c^2 x^2} \left((14 - 3 \operatorname{ArcSin}[c x]) \operatorname{ArcSin}[c x] + 28 \operatorname{Log}[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]]\right)\right) \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\Bigg)/ \\
& \left(6 c e^3 \sqrt{-(d + c d x) (e - c e x)} \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)^4 \left(\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right)\right) +
\end{aligned}$$

$$\begin{aligned}
& \left( b^2 d (1 + c x) \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)} \right. \\
& \left. \left( -3 \pm \pi \operatorname{ArcSin}[c x] + \frac{4 \operatorname{ArcSin}[c x]}{-1 + c x} - (1 - \pm i) \operatorname{ArcSin}[c x]^2 - \frac{2 \operatorname{ArcSin}[c x]^2}{-1 + c x} - 4 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] + 2 \pi \operatorname{Log}[1 + \pm i e^{i \operatorname{ArcSin}[c x]}] - \right. \right. \\
& \left. \left. 4 \operatorname{ArcSin}[c x] \operatorname{Log}[1 + \pm i e^{i \operatorname{ArcSin}[c x]}] + 4 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - 2 \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] + \right. \right. \\
& \left. \left. 4 \pm i \operatorname{PolyLog}[2, -\pm i e^{i \operatorname{ArcSin}[c x]}] + \frac{2 (4 + \operatorname{ArcSin}[c x]^2 + c x (-4 + \operatorname{ArcSin}[c x]^2)) \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]}{(\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])^3} \right) \right) / \\
& \left( 3 c e^3 \sqrt{-(d + c d x) (e - c e x)} \sqrt{1 - c^2 x^2} \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right)^2 \right) + \\
& \left( b^2 d (1 + c x) \sqrt{d + c d x} \sqrt{e - c e x} \sqrt{-d e (1 - c^2 x^2)} \right. \\
& \left. \left( -21 \pm \pi \operatorname{ArcSin}[c x] - \frac{2 (-2 + \operatorname{ArcSin}[c x]) \operatorname{ArcSin}[c x]}{-1 + c x} - (7 - 7 \pm i) \operatorname{ArcSin}[c x]^2 + \operatorname{ArcSin}[c x]^3 - 28 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] + \right. \right. \\
& \left. \left. 14 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[1 + \pm i e^{i \operatorname{ArcSin}[c x]}] + 28 \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - 14 \pi \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] + \right. \right. \\
& \left. \left. 28 \pm i \operatorname{PolyLog}[2, -\pm i e^{i \operatorname{ArcSin}[c x]}] + \frac{4 \operatorname{ArcSin}[c x]^2 \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]}{(\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])^3} + \frac{2 (4 - 7 \operatorname{ArcSin}[c x]^2) \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]}{\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]} \right) \right) / \\
& \left( 3 c e^3 \sqrt{-(d + c d x) (e - c e x)} \sqrt{1 - c^2 x^2} \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right)^2 \right)
\end{aligned}$$

**Problem 575: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^2}{(d + c d x)^{5/2} (e - c e x)^{5/2}} dx$$

Optimal (type 4, 366 leaves, 10 steps):

$$\frac{b^2 x (1 - c^2 x^2)^2}{3 (d + c d x)^{5/2} (e - c e x)^{5/2}} - \frac{b (1 - c^2 x^2)^{3/2} (a + b \operatorname{ArcSin}[c x])}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} + \frac{x (1 - c^2 x^2) (a + b \operatorname{ArcSin}[c x])^2}{3 (d + c d x)^{5/2} (e - c e x)^{5/2}} + \frac{2 x (1 - c^2 x^2)^2 (a + b \operatorname{ArcSin}[c x])^2}{3 (d + c d x)^{5/2} (e - c e x)^{5/2}} -$$

$$\frac{2 i (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])^2}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} + \frac{4 b (1 - c^2 x^2)^{5/2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}[1 + e^{2i \operatorname{ArcSin}[c x]}]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}} - \frac{2 i b^2 (1 - c^2 x^2)^{5/2} \operatorname{PolyLog}[2, -e^{2i \operatorname{ArcSin}[c x]}]}{3 c (d + c d x)^{5/2} (e - c e x)^{5/2}}$$

Result (type 4, 1243 leaves):

$$\begin{aligned} & \sqrt{-e (-1 + c x)} \sqrt{d (1 + c x)} \left( \frac{a^2}{12 d^3 e^3 (-1 + c x)^2} - \frac{a^2}{3 d^3 e^3 (-1 + c x)} - \frac{a^2}{12 d^3 e^3 (1 + c x)^2} - \frac{a^2}{3 d^3 e^3 (1 + c x)} \right) + \\ & \frac{1}{c d^2 e^2} b^2 \left( \frac{\operatorname{ArcSin}[c x]^2 (\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]) \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]}{6 \sqrt{d (1 + c x)} \sqrt{e - c e x} (\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])^2} - \right. \\ & \frac{\operatorname{ArcSin}[c x] (2 + \operatorname{ArcSin}[c x]) (\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])}{12 \sqrt{d (1 + c x)} \sqrt{e - c e x} (\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])} + \\ & \frac{(-2 + \operatorname{ArcSin}[c x]) \operatorname{ArcSin}[c x] (\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])}{12 \sqrt{d (1 + c x)} \sqrt{e - c e x} (\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])} + \\ & \left. \left( 4 \sqrt{2} \left( \frac{1}{4} e^{-\frac{i \pi}{4}} \operatorname{ArcSin}[c x]^2 - \frac{1}{\sqrt{2}} \left( -\frac{3}{4} i \pi \operatorname{ArcSin}[c x] - 2 \left( -\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x] \right) \operatorname{Log}[1 - e^{2i (-\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x])}] - \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] + \right. \right. \right. \right. \\ & \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \frac{1}{2} \pi \operatorname{Log}[-\sin[\frac{\pi}{4} - \frac{1}{2} \operatorname{ArcSin}[c x]]] + i \operatorname{PolyLog}[2, e^{2i (-\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x])}] \left. \right) \\ & \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) \Big/ \left( 3 \sqrt{d (1 + c x)} \sqrt{e - c e x} \right) - \\ & \left( 4 \sqrt{2} \left( \frac{1}{4} e^{\frac{i \pi}{4}} \operatorname{ArcSin}[c x]^2 + \frac{1}{\sqrt{2}} \left( -\frac{1}{4} i \pi \operatorname{ArcSin}[c x] - 2 \left( \frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x] \right) \operatorname{Log}[1 - e^{2i (\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x])}] - \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] + \right. \right. \right. \right. \\ & \pi \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \frac{1}{2} \pi \operatorname{Log}[\sin[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]]] + i \operatorname{PolyLog}[2, e^{2i (\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x])}] \left. \right) \\ & \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) \Big/ \left( 3 \sqrt{d (1 + c x)} \sqrt{e - c e x} \right) + \\ & \frac{\operatorname{ArcSin}[c x]^2 \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] (\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])}{6 \sqrt{d (1 + c x)} \sqrt{e - c e x} (\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])^2} + \\ & \left( \left( \cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) \left( \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] + 2 \operatorname{ArcSin}[c x]^2 \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) \right) \Big/ \left( 3 \sqrt{d (1 + c x)} \sqrt{e - c e x} \right) + \end{aligned}$$

$$\left( \left( \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) \left( \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + 2 \operatorname{ArcSin}[c x]^2 \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right) \right) / \left( 3 \sqrt{d (1+c x)} \sqrt{e - c e x} \right) + \\ \left( a b \left( -1 + \frac{3 c x \operatorname{ArcSin}[c x]}{\sqrt{1 - c^2 x^2}} + 2 \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right] + 2 \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right] + \right. \right. \\ 2 \cos[2 \operatorname{ArcSin}[c x]] \left( \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right] + \operatorname{Log}\left[ \cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] \right] + \right. \\ \left. \left. \frac{\operatorname{ArcSin}[c x] \sin[3 \operatorname{ArcSin}[c x]]}{\sqrt{1 - c^2 x^2}} \right) \right) / \left( 3 c d^2 e^2 \sqrt{d (1+c x)} \sqrt{e - c e x} \sqrt{1 - c^2 x^2} \right)$$

**Problem 588:** Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^2}{\sqrt{d + c d x} \sqrt{e - c e x}} dx$$

Optimal (type 3, 55 leaves, 2 steps):

$$\frac{\sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])^3}{3 b c \sqrt{d + c d x} \sqrt{e - c e x}}$$

Result (type 3, 159 leaves):

$$\frac{\frac{3 a b \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x]^2}{\sqrt{d + c d x} \sqrt{e - c e x}} + \frac{b^2 \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x]^3}{\sqrt{d + c d x} \sqrt{e - c e x}} - \frac{3 a^2 \operatorname{ArcTan}\left[\frac{c x \sqrt{d + c d x} \sqrt{e - c e x}}{\sqrt{d} \sqrt{e} (-1 + c^2 x^2)}\right]}{\sqrt{d} \sqrt{e}}}{3 c}$$

**Problem 591:** Result more than twice size of optimal antiderivative.

$$\int \frac{x^2 (a + b \operatorname{ArcSin}[c x])^2}{(d + c d x)^{3/2} (e - c e x)^{3/2}} dx$$

Optimal (type 4, 295 leaves, 8 steps):

$$\frac{x (a + b \operatorname{ArcSin}[c x])^2}{c^2 d e \sqrt{d + c d x} \sqrt{e - c e x}} - \frac{i \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])^2}{c^3 d e \sqrt{d + c d x} \sqrt{e - c e x}} - \frac{\sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])^3}{3 b c^3 d e \sqrt{d + c d x} \sqrt{e - c e x}} + \\ \frac{2 b \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}[1 + e^{2 i \operatorname{ArcSin}[c x]}]}{c^3 d e \sqrt{d + c d x} \sqrt{e - c e x}} - \frac{i b^2 \sqrt{1 - c^2 x^2} \operatorname{PolyLog}[2, -e^{2 i \operatorname{ArcSin}[c x]}]}{c^3 d e \sqrt{d + c d x} \sqrt{e - c e x}}$$

Result (type 4, 636 leaves):

$$\begin{aligned}
& \frac{1}{3 c^3 d^{3/2} e^2 \sqrt{d + c d x} \sqrt{e - c e x}} \\
& \left( 3 a^2 c \sqrt{d} e x + 3 a^2 \sqrt{e} \sqrt{d + c d x} \sqrt{e - c e x} \operatorname{ArcTan} \left[ \frac{c x \sqrt{d + c d x} \sqrt{e - c e x}}{\sqrt{d} \sqrt{e} (-1 + c^2 x^2)} \right] + 3 a b \sqrt{d} e \left( 2 c x \operatorname{ArcSin}[c x] + \sqrt{1 - c^2 x^2} \right. \right. \\
& \left. \left( -\operatorname{ArcSin}[c x]^2 + 2 \left( \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]] \right) + \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] \right) \right) + \\
& b^2 \sqrt{d} e \left( 6 i \pi \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] + 3 c x \operatorname{ArcSin}[c x]^2 - 3 i \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x]^2 - \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x]^3 + \right. \\
& 12 \pi \sqrt{1 - c^2 x^2} \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] + 3 \pi \sqrt{1 - c^2 x^2} \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + 6 \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - \\
& 3 \pi \sqrt{1 - c^2 x^2} \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + 6 \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - 12 \pi \sqrt{1 - c^2 x^2} \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + \\
& 3 \pi \sqrt{1 - c^2 x^2} \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] - 3 \pi \sqrt{1 - c^2 x^2} \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] - \\
& \left. 6 i \sqrt{1 - c^2 x^2} \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] - 6 i \sqrt{1 - c^2 x^2} \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] \right)
\end{aligned}$$

Problem 593: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^2}{(d + c d x)^{3/2} (e - c e x)^{3/2}} dx$$

Optimal (type 4, 217 leaves, 7 steps):

$$\begin{aligned}
& \frac{x (1 - c^2 x^2) (a + b \operatorname{ArcSin}[c x])^2 - i (1 - c^2 x^2)^{3/2} (a + b \operatorname{ArcSin}[c x])^2}{(d + c d x)^{3/2} (e - c e x)^{3/2}} + \\
& \frac{2 b (1 - c^2 x^2)^{3/2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}[1 + e^{2 i \operatorname{ArcSin}[c x]}] - i b^2 (1 - c^2 x^2)^{3/2} \operatorname{PolyLog}[2, -e^{2 i \operatorname{ArcSin}[c x]}]}{c (d + c d x)^{3/2} (e - c e x)^{3/2}}
\end{aligned}$$

Result (type 4, 550 leaves):

$$\frac{1}{c d e \sqrt{d + c x} \sqrt{e - c x}} \left( a^2 c x + 2 a b c x \operatorname{ArcSin}[c x] + 2 i b^2 \pi \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] + b^2 c x \operatorname{ArcSin}[c x]^2 - i b^2 \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x]^2 + 4 b^2 \pi \sqrt{1 - c^2 x^2} \operatorname{Log}[1 + e^{-i} \operatorname{ArcSin}[c x]] + b^2 \pi \sqrt{1 - c^2 x^2} \operatorname{Log}[1 - i e^{i} \operatorname{ArcSin}[c x]] + 2 b^2 \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] \operatorname{Log}[1 + i e^{i} \operatorname{ArcSin}[c x]] - 4 b^2 \pi \sqrt{1 - c^2 x^2} \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]]] + b^2 \pi \sqrt{1 - c^2 x^2} \operatorname{Log}[-\cos[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] + 2 a b \sqrt{1 - c^2 x^2} \operatorname{Log}[\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]]] - b^2 \pi \sqrt{1 - c^2 x^2} \operatorname{Log}[\sin[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]] - 2 i b^2 \sqrt{1 - c^2 x^2} \operatorname{PolyLog}[2, -i e^{i} \operatorname{ArcSin}[c x]] - 2 i b^2 \sqrt{1 - c^2 x^2} \operatorname{PolyLog}[2, i e^{i} \operatorname{ArcSin}[c x]] \right)$$

**Problem 641: Result more than twice size of optimal antiderivative.**

$$\int \frac{x^5 (a + b \operatorname{ArcSin}[c x])}{(d + e x^2)^3} dx$$

Optimal (type 4, 705 leaves, 27 steps):

$$\begin{aligned} & \frac{b c d x \sqrt{1 - c^2 x^2}}{8 e^2 (c^2 d + e) (d + e x^2)} - \frac{d^2 (a + b \operatorname{ArcSin}[c x])}{4 e^3 (d + e x^2)^2} + \frac{d (a + b \operatorname{ArcSin}[c x])}{e^3 (d + e x^2)} - \frac{i (a + b \operatorname{ArcSin}[c x])^2}{2 b e^3} - \\ & \frac{b c \sqrt{d} \operatorname{ArcTan}[\frac{\sqrt{c^2 d + e} x}{\sqrt{d} \sqrt{1 - c^2 x^2}}]}{e^3 \sqrt{c^2 d + e}} + \frac{b c \sqrt{d} (2 c^2 d + e) \operatorname{ArcTan}[\frac{\sqrt{c^2 d + e} x}{\sqrt{d} \sqrt{1 - c^2 x^2}}]}{8 e^3 (c^2 d + e)^{3/2}} + \frac{(a + b \operatorname{ArcSin}[c x]) \operatorname{Log}[1 - \frac{\sqrt{e} e^{i} \operatorname{ArcSin}[c x]}{i c \sqrt{-d} - \sqrt{c^2 d + e}}]}{2 e^3} + \\ & \frac{(a + b \operatorname{ArcSin}[c x]) \operatorname{Log}[1 + \frac{\sqrt{e} e^{i} \operatorname{ArcSin}[c x]}{i c \sqrt{-d} - \sqrt{c^2 d + e}}]}{2 e^3} + \frac{(a + b \operatorname{ArcSin}[c x]) \operatorname{Log}[1 - \frac{\sqrt{e} e^{i} \operatorname{ArcSin}[c x]}{i c \sqrt{-d} + \sqrt{c^2 d + e}}]}{2 e^3} + \frac{(a + b \operatorname{ArcSin}[c x]) \operatorname{Log}[1 + \frac{\sqrt{e} e^{i} \operatorname{ArcSin}[c x]}{i c \sqrt{-d} + \sqrt{c^2 d + e}}]}{2 e^3} - \\ & \frac{i b \operatorname{PolyLog}[2, -\frac{\sqrt{e} e^{i} \operatorname{ArcSin}[c x]}{i c \sqrt{-d} - \sqrt{c^2 d + e}}]}{2 e^3} - \frac{i b \operatorname{PolyLog}[2, \frac{\sqrt{e} e^{i} \operatorname{ArcSin}[c x]}{i c \sqrt{-d} - \sqrt{c^2 d + e}}]}{2 e^3} - \frac{i b \operatorname{PolyLog}[2, -\frac{\sqrt{e} e^{i} \operatorname{ArcSin}[c x]}{i c \sqrt{-d} + \sqrt{c^2 d + e}}]}{2 e^3} - \frac{i b \operatorname{PolyLog}[2, \frac{\sqrt{e} e^{i} \operatorname{ArcSin}[c x]}{i c \sqrt{-d} + \sqrt{c^2 d + e}}]}{2 e^3} \end{aligned}$$

Result (type 4, 1547 leaves):

$$\begin{aligned}
& - \frac{ad^2}{4e^3(d+ex^2)^2} + \frac{ad}{e^3(d+ex^2)} + \frac{a \operatorname{Log}[d+ex^2]}{2e^3} + b \\
& - \frac{7 \pm \sqrt{d}}{16e^3} \left( \frac{c \operatorname{Log} \left[ -\frac{2e(\sqrt{e} - i c^2 \sqrt{d} x + \sqrt{c^2 d + e} \sqrt{1-c^2 x^2})}{c \sqrt{c^2 d + e} (-i \sqrt{d} + \sqrt{e} x)} \right]}{\sqrt{c^2 d + e}} \right) - \\
& \frac{d \left( -\frac{c \sqrt{1-c^2 x^2}}{(c^2 d + e)(-i \sqrt{d} + \sqrt{e} x)} - \frac{\operatorname{ArcSin}[cx]}{\sqrt{e} (-i \sqrt{d} + \sqrt{e} x)^2} - \frac{i c^3 \sqrt{d} \left( \operatorname{Log}[4] + \operatorname{Log} \left[ \frac{e \sqrt{c^2 d + e} (\sqrt{e} - i c^2 \sqrt{d} x + \sqrt{c^2 d + e} \sqrt{1-c^2 x^2})}{c^3 (d+i \sqrt{d} \sqrt{e} x)} \right] \right)}{\sqrt{e} (c^2 d + e)^{3/2}} \right)}{16e^{5/2}} - \\
& \frac{7 \pm \sqrt{d}}{16e^3} \left( -\frac{\operatorname{ArcSin}[cx]}{\pm \sqrt{d} + \sqrt{e} x} - \frac{c \operatorname{Log} \left[ \frac{2e(\sqrt{e} + i c^2 \sqrt{d} x + \sqrt{c^2 d + e} \sqrt{1-c^2 x^2})}{c \sqrt{c^2 d + e} (i \sqrt{d} + \sqrt{e} x)} \right]}{\sqrt{c^2 d + e}} \right) - \\
& \frac{d \left( -\frac{c \sqrt{1-c^2 x^2}}{(c^2 d + e)(i \sqrt{d} + \sqrt{e} x)} - \frac{\operatorname{ArcSin}[cx]}{\sqrt{e} (i \sqrt{d} + \sqrt{e} x)^2} + \frac{i c^3 \sqrt{d} \left( \operatorname{Log}[4] + \operatorname{Log} \left[ \frac{e \sqrt{c^2 d + e} (\sqrt{e} + i c^2 \sqrt{d} x + \sqrt{c^2 d + e} \sqrt{1-c^2 x^2})}{c^3 (d-i \sqrt{d} \sqrt{e} x)} \right] \right)}{\sqrt{e} (c^2 d + e)^{3/2}} \right)}{16e^{5/2}} + \\
& \frac{1}{16e^3} \left( \frac{1}{i(\pi - 2 \operatorname{ArcSin}[cx])^2 - 32 \pm \operatorname{ArcSin} \left[ \frac{\sqrt{1 - \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right] \operatorname{ArcTan} \left[ \frac{(c \sqrt{d} - i \sqrt{e}) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx]) \right]}{\sqrt{c^2 d + e}} \right]} - \right. \\
& \left. 4 \left( \pi + 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 - \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[cx] \right) \operatorname{Log} \left[ \frac{e^{-i \operatorname{ArcSin}[cx]} (c \sqrt{d} - \sqrt{c^2 d + e} + \sqrt{e} e^{i \operatorname{ArcSin}[cx]})}{\sqrt{e}} \right] \right)
\end{aligned}$$

$$\begin{aligned}
& 4 \left( \pi - 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 - \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log} \left[ \frac{e^{-i \operatorname{ArcSin}[c x]} (c \sqrt{d} + \sqrt{c^2 d + e} + \sqrt{e} e^{i \operatorname{ArcSin}[c x]})}{\sqrt{e}} \right] + \\
& 4 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c \sqrt{d} + i c \sqrt{e} x] + 8 \operatorname{ArcSin}[c x] \operatorname{Log}[c \sqrt{d} + i c \sqrt{e} x] + \\
& 8 i \left( \operatorname{PolyLog}[2, \frac{(-c \sqrt{d} + \sqrt{c^2 d + e}) e^{-i \operatorname{ArcSin}[c x]}}{\sqrt{e}}] + \operatorname{PolyLog}[2, -\frac{(c \sqrt{d} + \sqrt{c^2 d + e}) e^{-i \operatorname{ArcSin}[c x]}}{\sqrt{e}}] \right) + \\
& \frac{1}{16 e^3} \left( i (\pi - 2 \operatorname{ArcSin}[c x])^2 - 32 i \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right] \operatorname{ArcTan} \left[ \frac{(c \sqrt{d} + i \sqrt{e}) \operatorname{Cot}[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])] }{\sqrt{c^2 d + e}} \right] - \right. \\
& 4 \left( \pi - 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log} \left[ 1 - \frac{(c \sqrt{d} + \sqrt{c^2 d + e}) e^{-i \operatorname{ArcSin}[c x]}}{\sqrt{e}} \right] - 4 \left( \pi + 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \\
& \left. \operatorname{Log} \left[ \frac{e^{-i \operatorname{ArcSin}[c x]} (-c \sqrt{d} + \sqrt{c^2 d + e} + \sqrt{e} e^{i \operatorname{ArcSin}[c x]})}{\sqrt{e}} \right] + 4 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c \sqrt{d} - i c \sqrt{e} x] + \right. \\
& \left. 8 \operatorname{ArcSin}[c x] \operatorname{Log}[c \sqrt{d} - i c \sqrt{e} x] + 8 i \left( \operatorname{PolyLog}[2, \frac{(c \sqrt{d} - \sqrt{c^2 d + e}) e^{-i \operatorname{ArcSin}[c x]}}{\sqrt{e}}] + \operatorname{PolyLog}[2, \frac{(c \sqrt{d} + \sqrt{c^2 d + e}) e^{-i \operatorname{ArcSin}[c x]}}{\sqrt{e}}] \right) \right)
\end{aligned}$$

Problem 644: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{x (d + e x^2)^3} dx$$

Optimal (type 4, 727 leaves, 32 steps):

$$\begin{aligned} & -\frac{b c e x \sqrt{1 - c^2 x^2}}{8 d^2 (c^2 d + e) (d + e x^2)} + \frac{a + b \operatorname{ArcSin}[c x]}{4 d (d + e x^2)^2} + \frac{a + b \operatorname{ArcSin}[c x]}{2 d^2 (d + e x^2)} - \frac{b c \operatorname{ArcTan}\left[\frac{\sqrt{c^2 d + e} x}{\sqrt{d} \sqrt{1 - c^2 x^2}}\right]}{2 d^{5/2} \sqrt{c^2 d + e}} - \frac{b c (2 c^2 d + e) \operatorname{ArcTan}\left[\frac{\sqrt{c^2 d + e} x}{\sqrt{d} \sqrt{1 - c^2 x^2}}\right]}{8 d^{5/2} (c^2 d + e)^{3/2}} - \\ & \frac{(a + b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 - \frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{i c \sqrt{-d} - \sqrt{c^2 d + e}}\right]}{2 d^3} - \frac{(a + b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 + \frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{i c \sqrt{-d} - \sqrt{c^2 d + e}}\right]}{2 d^3} - \frac{(a + b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 - \frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{i c \sqrt{-d} + \sqrt{c^2 d + e}}\right]}{2 d^3} - \\ & \frac{(a + b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 + \frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{i c \sqrt{-d} + \sqrt{c^2 d + e}}\right]}{2 d^3} + \frac{(a + b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 - e^{2 i \operatorname{ArcSin}[c x]}\right]}{d^3} + \frac{i b \operatorname{PolyLog}\left[2, -\frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{i c \sqrt{-d} - \sqrt{c^2 d + e}}\right]}{2 d^3} + \\ & \frac{i b \operatorname{PolyLog}\left[2, \frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{i c \sqrt{-d} - \sqrt{c^2 d + e}}\right]}{2 d^3} + \frac{i b \operatorname{PolyLog}\left[2, -\frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{i c \sqrt{-d} + \sqrt{c^2 d + e}}\right]}{2 d^3} + \frac{i b \operatorname{PolyLog}\left[2, \frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{i c \sqrt{-d} + \sqrt{c^2 d + e}}\right]}{2 d^3} - \frac{i b \operatorname{PolyLog}\left[2, e^{2 i \operatorname{ArcSin}[c x]}\right]}{2 d^3} \end{aligned}$$

Result (type 4, 1601 leaves):

$$\begin{aligned} & \frac{a}{4 d (d + e x^2)^2} + \frac{a}{2 d^2 (d + e x^2)} + \frac{a \operatorname{Log}[x]}{d^3} - \frac{a \operatorname{Log}[d + e x^2]}{2 d^3} + b \left( -\frac{5 \frac{i}{2} \left( \frac{\operatorname{ArcSin}[c x]}{-i \sqrt{d} + \sqrt{e} x} + \frac{c \operatorname{Log}\left[-\frac{2 e \left(\sqrt{e} - i c^2 \sqrt{d} x + \sqrt{c^2 d + e} \sqrt{1 - c^2 x^2}\right)}{c \sqrt{c^2 d + e} (-i \sqrt{d} + \sqrt{e} x)}\right]}{\sqrt{c^2 d + e}} \right)}{16 d^{5/2}} + \frac{1}{16 d^2} \right. \\ & \left. - \sqrt{e} \left( -\frac{c \sqrt{1 - c^2 x^2}}{(c^2 d + e) (-i \sqrt{d} + \sqrt{e} x)} - \frac{\operatorname{ArcSin}[c x]}{\sqrt{e} (-i \sqrt{d} + \sqrt{e} x)^2} - \frac{i c^3 \sqrt{d} \left( \operatorname{Log}[4] + \operatorname{Log}\left[\frac{e \sqrt{c^2 d + e} \left(\sqrt{e} - i c^2 \sqrt{d} x + \sqrt{c^2 d + e} \sqrt{1 - c^2 x^2}\right)}{c^3 (d + i \sqrt{d} \sqrt{e} x)}\right]\right)}{\sqrt{e} (c^2 d + e)^{3/2}} \right) \right) \end{aligned}$$

$$\frac{5 \text{i} \left( -\frac{\text{ArcSin}[c x]}{i \sqrt{d} + \sqrt{e} x} - \frac{c \log \left[ \frac{2 e \left(\sqrt{e} + i c^2 \sqrt{d} x + \sqrt{c^2 d + e} \sqrt{1 - c^2 x^2}\right)}{c \sqrt{c^2 d + e} \left(i \sqrt{d} + \sqrt{e} x\right)}\right]}{\sqrt{c^2 d + e}} \right) \sqrt{e} \left( -\frac{c \sqrt{1 - c^2 x^2}}{(c^2 d + e) \left(i \sqrt{d} + \sqrt{e} x\right)} - \frac{\text{ArcSin}[c x]}{\sqrt{e} \left(i \sqrt{d} + \sqrt{e} x\right)^2} + \frac{i c^3 \sqrt{d} \left(\log [4] + \log \left[ \frac{e \sqrt{c^2 d + e} \left(\sqrt{e} + i c^2 \sqrt{d} x + \sqrt{c^2 d + e} \sqrt{1 - c^2 x^2}\right)}{c^3 \left(d - i \sqrt{d} \sqrt{e} x\right)}\right]\right)}{\sqrt{e} (c^2 d + e)^{3/2}} \right)}{16 d^{5/2}} -$$

$$\frac{1}{16 d^3} \left( \text{i} \left(\pi - 2 \text{ArcSin}[c x]\right)^2 - 32 \text{i} \text{ArcSin}\left[\frac{\sqrt{1 - \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}}\right] \text{ArcTan}\left[\frac{\left(c \sqrt{d} - i \sqrt{e}\right) \text{Cot}\left[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])\right]}{\sqrt{c^2 d + e}}\right] - \right.$$

$$4 \left( \pi + 4 \text{ArcSin}\left[\frac{\sqrt{1 - \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}}\right] - 2 \text{ArcSin}[c x] \right) \text{Log}\left[\frac{e^{-i \text{ArcSin}[c x]} \left(c \sqrt{d} - \sqrt{c^2 d + e} + \sqrt{e} e^{i \text{ArcSin}[c x]}\right)}{\sqrt{e}}\right] -$$

$$4 \left( \pi - 4 \text{ArcSin}\left[\frac{\sqrt{1 - \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}}\right] - 2 \text{ArcSin}[c x] \right) \text{Log}\left[\frac{e^{-i \text{ArcSin}[c x]} \left(c \sqrt{d} + \sqrt{c^2 d + e} + \sqrt{e} e^{i \text{ArcSin}[c x]}\right)}{\sqrt{e}}\right] +$$

$$4 (\pi - 2 \text{ArcSin}[c x]) \text{Log}[c \sqrt{d} + i c \sqrt{e} x] + 8 \text{ArcSin}[c x] \text{Log}[c \sqrt{d} + i c \sqrt{e} x] +$$

$$8 \text{i} \left( \text{PolyLog}\left[2, \frac{\left(-c \sqrt{d} + \sqrt{c^2 d + e}\right) e^{-i \text{ArcSin}[c x]}}{\sqrt{e}}\right] + \text{PolyLog}\left[2, -\frac{\left(c \sqrt{d} + \sqrt{c^2 d + e}\right) e^{-i \text{ArcSin}[c x]}}{\sqrt{e}}\right] \right) -$$

$$\frac{1}{16 d^3} \left( \text{i} \left(\pi - 2 \text{ArcSin}[c x]\right)^2 - 32 \text{i} \text{ArcSin}\left[\frac{\sqrt{1 - \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}}\right] \text{ArcTan}\left[\frac{\left(c \sqrt{d} + i \sqrt{e}\right) \text{Cot}\left[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])\right]}{\sqrt{c^2 d + e}}\right] - \right)$$

$$4 \left( \pi - 4 \text{ArcSin}\left[\frac{\sqrt{1 + \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}}\right] - 2 \text{ArcSin}[c x] \right) \text{Log}\left[1 - \frac{\left(c \sqrt{d} + \sqrt{c^2 d + e}\right) e^{-i \text{ArcSin}[c x]}}{\sqrt{e}}\right] -$$

$$\begin{aligned}
& 4 \left( \pi + 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log} \left[ \frac{e^{-i \operatorname{ArcSin}[c x]} (-c \sqrt{d} + \sqrt{c^2 d + e} + \sqrt{e} e^{i \operatorname{ArcSin}[c x]})}{\sqrt{e}} \right] + \\
& 4 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c \sqrt{d} - i c \sqrt{e} x] + 8 \operatorname{ArcSin}[c x] \operatorname{Log}[c \sqrt{d} - i c \sqrt{e} x] + \\
& 8 i \left( \operatorname{PolyLog}[2, \frac{(c \sqrt{d} - \sqrt{c^2 d + e}) e^{-i \operatorname{ArcSin}[c x]}}{\sqrt{e}}] + \operatorname{PolyLog}[2, \frac{(c \sqrt{d} + \sqrt{c^2 d + e}) e^{-i \operatorname{ArcSin}[c x]}}{\sqrt{e}}] \right) + \\
& \frac{\operatorname{ArcSin}[c x] \operatorname{Log}[1 - e^{2 i \operatorname{ArcSin}[c x]}] - \frac{1}{2} i (\operatorname{ArcSin}[c x]^2 + \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}[c x]}])}{d^3} \Bigg)
\end{aligned}$$

**Problem 645: Result more than twice size of optimal antiderivative.**

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{x^3 (d + e x^2)^3} dx$$

Optimal (type 4, 783 leaves, 34 steps):

$$\begin{aligned}
& -\frac{b c \sqrt{1-c^2 x^2}}{2 d^3 x} + \frac{b c e^2 x \sqrt{1-c^2 x^2}}{8 d^3 (c^2 d+e) (d+e x^2)} - \frac{a+b \operatorname{ArcSin}[c x]}{2 d^3 x^2} - \frac{e (a+b \operatorname{ArcSin}[c x])}{4 d^2 (d+e x^2)^2} - \frac{e (a+b \operatorname{ArcSin}[c x])}{d^3 (d+e x^2)} + \\
& \frac{b c e \operatorname{ArcTan}\left[\frac{\sqrt{c^2 d+e} x}{\sqrt{d} \sqrt{1-c^2 x^2}}\right]}{d^{7/2} \sqrt{c^2 d+e}} + \frac{b c e (2 c^2 d+e) \operatorname{ArcTan}\left[\frac{\sqrt{c^2 d+e} x}{\sqrt{d} \sqrt{1-c^2 x^2}}\right]}{8 d^{7/2} (c^2 d+e)^{3/2}} + \frac{3 e (a+b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1-\frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{i c \sqrt{-d}-\sqrt{c^2 d+e}}\right]}{2 d^4} + \\
& \frac{3 e (a+b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1+\frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{i c \sqrt{-d}-\sqrt{c^2 d+e}}\right]}{2 d^4} + \frac{3 e (a+b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1-\frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{i c \sqrt{-d}+\sqrt{c^2 d+e}}\right]}{2 d^4} + \frac{3 e (a+b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1+\frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{i c \sqrt{-d}+\sqrt{c^2 d+e}}\right]}{2 d^4} - \\
& \frac{3 e (a+b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1-e^{2 i \operatorname{ArcSin}[c x]}\right]}{d^4} - \frac{3 i b e \operatorname{PolyLog}\left[2,-\frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{i c \sqrt{-d}-\sqrt{c^2 d+e}}\right]}{2 d^4} - \frac{3 i b e \operatorname{PolyLog}\left[2,-\frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{i c \sqrt{-d}-\sqrt{c^2 d+e}}\right]}{2 d^4} - \\
& \frac{3 i b e \operatorname{PolyLog}\left[2,-\frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{i c \sqrt{-d}+\sqrt{c^2 d+e}}\right]}{2 d^4} - \frac{3 i b e \operatorname{PolyLog}\left[2,\frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{i c \sqrt{-d}+\sqrt{c^2 d+e}}\right]}{2 d^4} + \frac{3 i b e \operatorname{PolyLog}\left[2,e^{2 i \operatorname{ArcSin}[c x]}\right]}{2 d^4}
\end{aligned}$$

Result (type 4, 1653 leaves):

$$\begin{aligned}
& -\frac{a}{2 d^3 x^2} - \frac{a e}{4 d^2 (d+e x^2)^2} - \frac{a e}{d^3 (d+e x^2)} - \frac{3 a e \operatorname{Log}[x]}{d^4} + \frac{3 a e \operatorname{Log}[d+e x^2]}{2 d^4} + \\
& b \left( -\frac{c x \sqrt{1-c^2 x^2} + \operatorname{ArcSin}[c x]}{2 d^3 x^2} + \frac{9 i e \left( \frac{c \operatorname{Log}\left[-\frac{2 e \left(\sqrt{e}-i c^2 \sqrt{d} x+\sqrt{c^2 d+e} \sqrt{1-c^2 x^2}\right)}{c \sqrt{c^2 d+e} \left(-i \sqrt{d}+\sqrt{e} x\right)}\right]}{\frac{\operatorname{ArcSin}[c x]}{-i \sqrt{d}+\sqrt{e} x} + \frac{\sqrt{c^2 d+e}}{\sqrt{c^2 d+e}}}\right)}{16 d^{7/2}} - \frac{1}{16 d^3} \right)
\end{aligned}$$

$$e^{3/2} \left( -\frac{c \sqrt{1-c^2 x^2}}{(c^2 d+e) \left(-i \sqrt{d}+\sqrt{e} x\right)} - \frac{\operatorname{ArcSin}[c x]}{\sqrt{e} \left(-i \sqrt{d}+\sqrt{e} x\right)^2} - \frac{i c^3 \sqrt{d} \left(\operatorname{Log}[4]+\operatorname{Log}\left[\frac{e \sqrt{c^2 d+e} \left(\sqrt{e}-i c^2 \sqrt{d} x+\sqrt{c^2 d+e} \sqrt{1-c^2 x^2}\right)}{c^3 (d+i \sqrt{d} \sqrt{e} x)}\right]\right)}{\sqrt{e} (c^2 d+e)^{3/2}} \right) +$$

$$\begin{aligned}
& \frac{9 \ln e \left( -\frac{\text{ArcSin}[cx]}{i \sqrt{d} + \sqrt{e} x} - \frac{c \log \left[ \frac{2 e \left( \sqrt{e} + i c^2 \sqrt{d} x + \sqrt{c^2 d + e} \sqrt{1 - c^2 x^2} \right)}{c \sqrt{c^2 d + e} \left( i \sqrt{d} + \sqrt{e} x \right)} \right]}{\sqrt{c^2 d + e}} \right) - }{16 d^{7/2}} \\
& + \frac{e^{3/2} \left( -\frac{c \sqrt{1 - c^2 x^2}}{(c^2 d + e) \left( i \sqrt{d} + \sqrt{e} x \right)} - \frac{\text{ArcSin}[cx]}{\sqrt{e} \left( i \sqrt{d} + \sqrt{e} x \right)^2} + \frac{i c^3 \sqrt{d} \left( \log[4] + \log \left[ \frac{e \sqrt{c^2 d + e} \left( \sqrt{e} + i c^2 \sqrt{d} x + \sqrt{c^2 d + e} \sqrt{1 - c^2 x^2} \right)}{c^3 \left( d - i \sqrt{d} \sqrt{e} x \right)} \right] \right)}{\sqrt{e} (c^2 d + e)^{3/2}} \right)}{16 d^3} \\
& + \frac{1}{16 d^4} 3 e \left( \frac{i}{\pi - 2 \text{ArcSin}[cx]} - 32 \frac{i}{\text{ArcSin} \left[ \frac{\sqrt{1 - \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right]} \text{ArcTan} \left[ \frac{(c \sqrt{d} - i \sqrt{e}) \cot \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[cx]) \right]}{\sqrt{c^2 d + e}} \right] - \right. \\
& \left. 4 \left( \pi + 4 \text{ArcSin} \left[ \frac{\sqrt{1 - \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right] - 2 \text{ArcSin}[cx] \right) \log \left[ \frac{e^{-i \text{ArcSin}[cx]} (c \sqrt{d} - \sqrt{c^2 d + e} + \sqrt{e} e^{i \text{ArcSin}[cx]})}{\sqrt{e}} \right] - \right. \\
& \left. 4 \left( \pi - 4 \text{ArcSin} \left[ \frac{\sqrt{1 - \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right] - 2 \text{ArcSin}[cx] \right) \log \left[ \frac{e^{-i \text{ArcSin}[cx]} (c \sqrt{d} + \sqrt{c^2 d + e} + \sqrt{e} e^{i \text{ArcSin}[cx]})}{\sqrt{e}} \right] + \right. \\
& \left. 4 (\pi - 2 \text{ArcSin}[cx]) \log [c \sqrt{d} + i c \sqrt{e} x] + 8 \text{ArcSin}[cx] \log [c \sqrt{d} + i c \sqrt{e} x] + \right. \\
& \left. 8 \frac{i}{\ln e} \left( \text{PolyLog}[2, \frac{(-c \sqrt{d} + \sqrt{c^2 d + e}) e^{-i \text{ArcSin}[cx]}}{\sqrt{e}}] + \text{PolyLog}[2, -\frac{(c \sqrt{d} + \sqrt{c^2 d + e}) e^{-i \text{ArcSin}[cx]}}{\sqrt{e}}] \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{16 d^4} 3 e \left( \text{ArcSin}[c x]^2 - 32 \text{ArcSin}\left[\frac{\sqrt{1 + \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}}\right] \text{ArcTan}\left[\frac{(c \sqrt{d} + i \sqrt{e}) \cot\left[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])\right]}{\sqrt{c^2 d + e}}\right] - \right. \\
& 4 \left( \pi - 4 \text{ArcSin}\left[\frac{\sqrt{1 + \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}}\right] - 2 \text{ArcSin}[c x] \right) \text{Log}\left[1 - \frac{(c \sqrt{d} + \sqrt{c^2 d + e}) e^{-i \text{ArcSin}[c x]}}{\sqrt{e}}\right] - 4 \left( \pi + 4 \text{ArcSin}\left[\frac{\sqrt{1 + \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}}\right] - 2 \text{ArcSin}[c x] \right) \\
& \text{Log}\left[\frac{e^{-i \text{ArcSin}[c x]} (-c \sqrt{d} + \sqrt{c^2 d + e} + \sqrt{e} e^{i \text{ArcSin}[c x]})}{\sqrt{e}}\right] + 4 (\pi - 2 \text{ArcSin}[c x]) \text{Log}[c \sqrt{d} - i c \sqrt{e} x] + 8 \text{ArcSin}[c x] \\
& \text{Log}[c \sqrt{d} - i c \sqrt{e} x] + 8 i \left( \text{PolyLog}[2, \frac{(c \sqrt{d} - \sqrt{c^2 d + e}) e^{-i \text{ArcSin}[c x]}}{\sqrt{e}}] + \text{PolyLog}[2, \frac{(c \sqrt{d} + \sqrt{c^2 d + e}) e^{-i \text{ArcSin}[c x]}}{\sqrt{e}}] \right) - \\
& \left. \frac{3 e (\text{ArcSin}[c x] \text{Log}[1 - e^{2 i \text{ArcSin}[c x]}] - \frac{1}{2} i (\text{ArcSin}[c x]^2 + \text{PolyLog}[2, e^{2 i \text{ArcSin}[c x]}]))}{d^4} \right)
\end{aligned}$$

**Problem 651:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{a + b \text{ArcSin}[c x]}{(d + e x^2)^{3/2}} dx$$

Optimal (type 3, 70 leaves, 6 steps):

$$\frac{x (a + b \operatorname{ArcSin}[c x])}{d \sqrt{d + e x^2}} + \frac{b \operatorname{ArcTan} \left[ \frac{\sqrt{e} \sqrt{1 - c^2 x^2}}{c \sqrt{d + e x^2}} \right]}{d \sqrt{e}}$$

Result (type 6, 164 leaves):

$$\frac{1}{\sqrt{d + e x^2}} x \left( - \left( \left( 2 b c x \operatorname{AppellF1} \left[ 1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d} \right] \right) / \left( \sqrt{1 - c^2 x^2} \left( 4 d \operatorname{AppellF1} \left[ 1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d} \right] + x^2 \left( -e \operatorname{AppellF1} \left[ 2, \frac{1}{2}, \frac{3}{2}, 3, c^2 x^2, -\frac{e x^2}{d} \right] + c^2 d \operatorname{AppellF1} \left[ 2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d} \right] \right) \right) \right) + \frac{a + b \operatorname{ArcSin}[c x]}{d} \right)$$

**Problem 652:** Result unnecessarily involves higher level functions.

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{(d + e x^2)^{5/2}} dx$$

Optimal (type 3, 146 leaves, 7 steps):

$$\frac{b c \sqrt{1 - c^2 x^2}}{3 d (c^2 d + e) \sqrt{d + e x^2}} + \frac{x (a + b \operatorname{ArcSin}[c x])}{3 d (d + e x^2)^{3/2}} + \frac{2 x (a + b \operatorname{ArcSin}[c x])}{3 d^2 \sqrt{d + e x^2}} + \frac{2 b \operatorname{ArcTan} \left[ \frac{\sqrt{e} \sqrt{1 - c^2 x^2}}{c \sqrt{d + e x^2}} \right]}{3 d^2 \sqrt{e}}$$

Result (type 6, 231 leaves):

$$\frac{1}{3 d^2 (d + e x^2)^{3/2}} \left( \frac{b c d \sqrt{1 - c^2 x^2} (d + e x^2)}{c^2 d + e} + a x (3 d + 2 e x^2) - \left( 4 b c d x^2 (d + e x^2) \operatorname{AppellF1} \left[ 1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d} \right] \right) / \left( \sqrt{1 - c^2 x^2} \left( 4 d \operatorname{AppellF1} \left[ 1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d} \right] + x^2 \left( -e \operatorname{AppellF1} \left[ 2, \frac{1}{2}, \frac{3}{2}, 3, c^2 x^2, -\frac{e x^2}{d} \right] + c^2 d \operatorname{AppellF1} \left[ 2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d} \right] \right) \right) \right) + b x (3 d + 2 e x^2) \operatorname{ArcSin}[c x]$$

**Problem 653:** Result unnecessarily involves higher level functions.

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{(d + e x^2)^{7/2}} dx$$

Optimal (type 3, 226 leaves, 8 steps):

$$\begin{aligned} & \frac{b c \sqrt{1 - c^2 x^2}}{15 d (c^2 d + e) (d + e x^2)^{3/2}} + \frac{2 b c (3 c^2 d + 2 e) \sqrt{1 - c^2 x^2}}{15 d^2 (c^2 d + e)^2 \sqrt{d + e x^2}} + \\ & \frac{x (a + b \operatorname{ArcSin}[c x])}{5 d (d + e x^2)^{5/2}} + \frac{4 x (a + b \operatorname{ArcSin}[c x])}{15 d^2 (d + e x^2)^{3/2}} + \frac{8 x (a + b \operatorname{ArcSin}[c x])}{15 d^3 \sqrt{d + e x^2}} + \frac{8 b \operatorname{ArcTan}\left[\frac{\sqrt{e} \sqrt{1 - c^2 x^2}}{c \sqrt{d + e x^2}}\right]}{15 d^3 \sqrt{e}} \end{aligned}$$

Result (type 6, 304 leaves):

$$\begin{aligned} & \frac{1}{15 d^3 (d + e x^2)^{5/2}} \left( \frac{b c d^2 \sqrt{1 - c^2 x^2} (d + e x^2)}{c^2 d + e} + \frac{2 b c d (3 c^2 d + 2 e) \sqrt{1 - c^2 x^2} (d + e x^2)^2}{(c^2 d + e)^2} + a x (15 d^2 + 20 d e x^2 + 8 e^2 x^4) - \right. \\ & \left. \left( 16 b c d x^2 (d + e x^2)^2 \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right] \right) \Big/ \left( \sqrt{1 - c^2 x^2} \left( 4 d \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right] + \right. \right. \right. \\ & \left. \left. \left. x^2 \left( -e \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] + c^2 d \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] \right) \right) \right) + b x (15 d^2 + 20 d e x^2 + 8 e^2 x^4) \operatorname{ArcSin}[c x] \right) \end{aligned}$$

Problem 663: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^2}{d + e x^2} dx$$

Optimal (type 4, 821 leaves, 22 steps):

$$\begin{aligned}
& \frac{\left(a + b \operatorname{ArcSin}[cx]\right)^2 \operatorname{Log}\left[1 - \frac{\sqrt{e} e^{i \operatorname{ArcSin}[cx]}}{i c \sqrt{-d} - \sqrt{c^2 d + e}}\right] - \left(a + b \operatorname{ArcSin}[cx]\right)^2 \operatorname{Log}\left[1 + \frac{\sqrt{e} e^{i \operatorname{ArcSin}[cx]}}{i c \sqrt{-d} - \sqrt{c^2 d + e}}\right]}{2 \sqrt{-d} \sqrt{e}} \\
& - \frac{\left(a + b \operatorname{ArcSin}[cx]\right)^2 \operatorname{Log}\left[1 - \frac{\sqrt{e} e^{i \operatorname{ArcSin}[cx]}}{i c \sqrt{-d} + \sqrt{c^2 d + e}}\right] - \left(a + b \operatorname{ArcSin}[cx]\right)^2 \operatorname{Log}\left[1 + \frac{\sqrt{e} e^{i \operatorname{ArcSin}[cx]}}{i c \sqrt{-d} + \sqrt{c^2 d + e}}\right]}{2 \sqrt{-d} \sqrt{e}} \\
& + \frac{i b \left(a + b \operatorname{ArcSin}[cx]\right) \operatorname{PolyLog}\left[2, -\frac{\sqrt{e} e^{i \operatorname{ArcSin}[cx]}}{i c \sqrt{-d} - \sqrt{c^2 d + e}}\right] - i b \left(a + b \operatorname{ArcSin}[cx]\right) \operatorname{PolyLog}\left[2, \frac{\sqrt{e} e^{i \operatorname{ArcSin}[cx]}}{i c \sqrt{-d} - \sqrt{c^2 d + e}}\right]}{\sqrt{-d} \sqrt{e}} \\
& - \frac{i b \left(a + b \operatorname{ArcSin}[cx]\right) \operatorname{PolyLog}\left[2, -\frac{\sqrt{e} e^{i \operatorname{ArcSin}[cx]}}{i c \sqrt{-d} + \sqrt{c^2 d + e}}\right] - i b \left(a + b \operatorname{ArcSin}[cx]\right) \operatorname{PolyLog}\left[2, \frac{\sqrt{e} e^{i \operatorname{ArcSin}[cx]}}{i c \sqrt{-d} + \sqrt{c^2 d + e}}\right]}{\sqrt{-d} \sqrt{e}} \\
& + \frac{b^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{e} e^{i \operatorname{ArcSin}[cx]}}{i c \sqrt{-d} - \sqrt{c^2 d + e}}\right] - b^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{e} e^{i \operatorname{ArcSin}[cx]}}{i c \sqrt{-d} - \sqrt{c^2 d + e}}\right] - b^2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{e} e^{i \operatorname{ArcSin}[cx]}}{i c \sqrt{-d} + \sqrt{c^2 d + e}}\right] + b^2 \operatorname{PolyLog}\left[3, \frac{\sqrt{e} e^{i \operatorname{ArcSin}[cx]}}{i c \sqrt{-d} + \sqrt{c^2 d + e}}\right]}{\sqrt{-d} \sqrt{e}}
\end{aligned}$$

Result (type 4, 3335 leaves):

$$\begin{aligned}
& \frac{1}{8 \sqrt{d} \sqrt{e}} \\
& \left( 8 a^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} x}{\sqrt{d}}\right] + 4 i a b \left( 8 i \operatorname{ArcSin}\left[\frac{\sqrt{1 - \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}}\right] \operatorname{ArcTan}\left[\frac{(c \sqrt{d} - i \sqrt{e}) \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right]}{\sqrt{c^2 d + e}}\right] - 8 i \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}}\right] \operatorname{ArcTan}\left[\frac{(c \sqrt{d} + i \sqrt{e}) \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right]}{\sqrt{c^2 d + e}}\right] \right) \right. \\
& - \left( \pi - 4 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}}\right] - 2 \operatorname{ArcSin}[cx] \right) \operatorname{Log}\left[1 - \frac{(c \sqrt{d} + \sqrt{c^2 d + e}) e^{-i \operatorname{ArcSin}[cx]}}{\sqrt{e}}\right] + \\
& \left. \left( \pi + 4 \operatorname{ArcSin}\left[\frac{\sqrt{1 - \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}}\right] - 2 \operatorname{ArcSin}[cx] \right) \operatorname{Log}\left[\frac{e^{-i \operatorname{ArcSin}[cx]} (c \sqrt{d} - \sqrt{c^2 d + e} + \sqrt{e} e^{i \operatorname{ArcSin}[cx]})}{\sqrt{e}}\right] \right)
\end{aligned}$$

$$\begin{aligned}
& \left( \pi + 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log} \left[ \frac{e^{-i \operatorname{ArcSin}[c x]} (-c \sqrt{d} + \sqrt{c^2 d + e} + \sqrt{e} e^{i \operatorname{ArcSin}[c x]})}{\sqrt{e}} \right] + \\
& \left( \pi - 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 - \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log} \left[ \frac{e^{-i \operatorname{ArcSin}[c x]} (c \sqrt{d} + \sqrt{c^2 d + e} + \sqrt{e} e^{i \operatorname{ArcSin}[c x]})}{\sqrt{e}} \right] + \\
& (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c (\sqrt{d} - i \sqrt{e} x)] + 2 \operatorname{ArcSin}[c x] \operatorname{Log}[c (\sqrt{d} - i \sqrt{e} x)] - \\
& (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c (\sqrt{d} + i \sqrt{e} x)] - 2 \operatorname{ArcSin}[c x] \operatorname{Log}[c (\sqrt{d} + i \sqrt{e} x)] - \\
& 2 i \left( \operatorname{PolyLog}[2, \frac{(-c \sqrt{d} + \sqrt{c^2 d + e}) e^{-i \operatorname{ArcSin}[c x]}}{\sqrt{e}}] + \operatorname{PolyLog}[2, -\frac{(c \sqrt{d} + \sqrt{c^2 d + e}) e^{-i \operatorname{ArcSin}[c x]}}{\sqrt{e}}] \right) + \\
& 2 i \left( \operatorname{PolyLog}[2, \frac{(c \sqrt{d} - \sqrt{c^2 d + e}) e^{-i \operatorname{ArcSin}[c x]}}{\sqrt{e}}] + \operatorname{PolyLog}[2, \frac{(c \sqrt{d} + \sqrt{c^2 d + e}) e^{-i \operatorname{ArcSin}[c x]}}{\sqrt{e}}] \right) - \\
& 4 i b^2 \left( \operatorname{ArcSin}[c x]^2 \operatorname{Log} \left[ \frac{-c \sqrt{d} + \sqrt{c^2 d + e} - \sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{-c \sqrt{d} + \sqrt{c^2 d + e}} \right] - \operatorname{ArcSin}[c x]^2 \operatorname{Log} \left[ \frac{c \sqrt{d} + \sqrt{c^2 d + e} - \sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{c \sqrt{d} + \sqrt{c^2 d + e}} \right] + \right. \\
& \left. \pi \operatorname{ArcSin}[c x] \operatorname{Log} \left[ -\frac{e^{-i \operatorname{ArcSin}[c x]} (c \sqrt{d} + \sqrt{c^2 d + e} - \sqrt{e} e^{i \operatorname{ArcSin}[c x]})}{\sqrt{e}} \right] - 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right] \operatorname{ArcSin}[c x] \right. \\
& \left. \operatorname{Log} \left[ -\frac{e^{-i \operatorname{ArcSin}[c x]} (c \sqrt{d} + \sqrt{c^2 d + e} - \sqrt{e} e^{i \operatorname{ArcSin}[c x]})}{\sqrt{e}} \right] - \operatorname{ArcSin}[c x]^2 \operatorname{Log} \left[ -\frac{e^{-i \operatorname{ArcSin}[c x]} (c \sqrt{d} + \sqrt{c^2 d + e} - \sqrt{e} e^{i \operatorname{ArcSin}[c x]})}{\sqrt{e}} \right] - \right. \\
& \left. \pi \operatorname{ArcSin}[c x] \operatorname{Log} \left[ \frac{e^{-i \operatorname{ArcSin}[c x]} (c \sqrt{d} - \sqrt{c^2 d + e} + \sqrt{e} e^{i \operatorname{ArcSin}[c x]})}{\sqrt{e}} \right] - 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 - \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right] \operatorname{ArcSin}[c x] \right)
\end{aligned}$$

$$\begin{aligned}
& \text{Log} \left[ \frac{e^{-i \text{ArcSin}[c x]} (c \sqrt{d} - \sqrt{c^2 d + e} + \sqrt{e} e^{i \text{ArcSin}[c x]})}{\sqrt{e}} \right] + \text{ArcSin}[c x]^2 \text{Log} \left[ \frac{e^{-i \text{ArcSin}[c x]} (c \sqrt{d} - \sqrt{c^2 d + e} + \sqrt{e} e^{i \text{ArcSin}[c x]})}{\sqrt{e}} \right] - \\
& \text{ArcSin}[c x]^2 \text{Log} \left[ \frac{-c \sqrt{d} + \sqrt{c^2 d + e} + \sqrt{e} e^{i \text{ArcSin}[c x]}}{-c \sqrt{d} + \sqrt{c^2 d + e}} \right] + \pi \text{ArcSin}[c x] \text{Log} \left[ \frac{e^{-i \text{ArcSin}[c x]} (-c \sqrt{d} + \sqrt{c^2 d + e} + \sqrt{e} e^{i \text{ArcSin}[c x]})}{\sqrt{e}} \right] + \\
& 4 \text{ArcSin} \left[ \frac{\sqrt{1 + \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right] \text{ArcSin}[c x] \text{Log} \left[ \frac{e^{-i \text{ArcSin}[c x]} (-c \sqrt{d} + \sqrt{c^2 d + e} + \sqrt{e} e^{i \text{ArcSin}[c x]})}{\sqrt{e}} \right] - \\
& \text{ArcSin}[c x]^2 \text{Log} \left[ \frac{e^{-i \text{ArcSin}[c x]} (-c \sqrt{d} + \sqrt{c^2 d + e} + \sqrt{e} e^{i \text{ArcSin}[c x]})}{\sqrt{e}} \right] + \text{ArcSin}[c x]^2 \text{Log} \left[ \frac{c \sqrt{d} + \sqrt{c^2 d + e} + \sqrt{e} e^{i \text{ArcSin}[c x]}}{c \sqrt{d} + \sqrt{c^2 d + e}} \right] - \\
& \pi \text{ArcSin}[c x] \text{Log} \left[ \frac{e^{-i \text{ArcSin}[c x]} (c \sqrt{d} + \sqrt{c^2 d + e} + \sqrt{e} e^{i \text{ArcSin}[c x]})}{\sqrt{e}} \right] + 4 \text{ArcSin} \left[ \frac{\sqrt{1 - \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right] \text{ArcSin}[c x] \\
& \text{Log} \left[ \frac{e^{-i \text{ArcSin}[c x]} (c \sqrt{d} + \sqrt{c^2 d + e} + \sqrt{e} e^{i \text{ArcSin}[c x]})}{\sqrt{e}} \right] + \text{ArcSin}[c x]^2 \text{Log} \left[ \frac{e^{-i \text{ArcSin}[c x]} (c \sqrt{d} + \sqrt{c^2 d + e} + \sqrt{e} e^{i \text{ArcSin}[c x]})}{\sqrt{e}} \right] + \\
& \pi \text{ArcSin}[c x] \text{Log} \left[ \frac{(-i c x + \sqrt{1 - c^2 x^2}) (c \sqrt{d} - \sqrt{c^2 d + e} + i c \sqrt{e} x + \sqrt{e} \sqrt{1 - c^2 x^2})}{\sqrt{e}} \right] + \\
& 4 \text{ArcSin} \left[ \frac{\sqrt{1 - \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right] \text{ArcSin}[c x] \text{Log} \left[ \frac{(-i c x + \sqrt{1 - c^2 x^2}) (c \sqrt{d} - \sqrt{c^2 d + e} + i c \sqrt{e} x + \sqrt{e} \sqrt{1 - c^2 x^2})}{\sqrt{e}} \right] - \\
& \text{ArcSin}[c x]^2 \text{Log} \left[ \frac{(-i c x + \sqrt{1 - c^2 x^2}) (c \sqrt{d} - \sqrt{c^2 d + e} + i c \sqrt{e} x + \sqrt{e} \sqrt{1 - c^2 x^2})}{\sqrt{e}} \right] - \\
& \pi \text{ArcSin}[c x] \text{Log} \left[ \frac{(-i c x + \sqrt{1 - c^2 x^2}) (-c \sqrt{d} + \sqrt{c^2 d + e} + i c \sqrt{e} x + \sqrt{e} \sqrt{1 - c^2 x^2})}{\sqrt{e}} \right] - \\
& 4 \text{ArcSin} \left[ \frac{\sqrt{1 + \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}} \right] \text{ArcSin}[c x] \text{Log} \left[ \frac{(-i c x + \sqrt{1 - c^2 x^2}) (-c \sqrt{d} + \sqrt{c^2 d + e} + i c \sqrt{e} x + \sqrt{e} \sqrt{1 - c^2 x^2})}{\sqrt{e}} \right] + \\
& \text{ArcSin}[c x]^2 \text{Log} \left[ \frac{(-i c x + \sqrt{1 - c^2 x^2}) (-c \sqrt{d} + \sqrt{c^2 d + e} + i c \sqrt{e} x + \sqrt{e} \sqrt{1 - c^2 x^2})}{\sqrt{e}} \right] +
\end{aligned}$$

$$\begin{aligned}
& \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[\frac{\left(-\frac{i}{2} c x + \sqrt{1 - c^2 x^2}\right) \left(c \sqrt{d} + \sqrt{c^2 d + e} + \frac{i}{2} c \sqrt{e} x + \sqrt{e} \sqrt{1 - c^2 x^2}\right)}{\sqrt{e}}\right] - \\
& 4 \operatorname{ArcSin}\left[\frac{\sqrt{1 - \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \operatorname{Log}\left[\frac{\left(-\frac{i}{2} c x + \sqrt{1 - c^2 x^2}\right) \left(c \sqrt{d} + \sqrt{c^2 d + e} + \frac{i}{2} c \sqrt{e} x + \sqrt{e} \sqrt{1 - c^2 x^2}\right)}{\sqrt{e}}\right] - \\
& \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[\frac{\left(-\frac{i}{2} c x + \sqrt{1 - c^2 x^2}\right) \left(c \sqrt{d} + \sqrt{c^2 d + e} + \frac{i}{2} c \sqrt{e} x + \sqrt{e} \sqrt{1 - c^2 x^2}\right)}{\sqrt{e}}\right] - \\
& \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{\left(c \sqrt{d} + \sqrt{c^2 d + e}\right) \left(-\frac{i}{2} c x + \sqrt{1 - c^2 x^2}\right)}{\sqrt{e}}\right] + 4 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{i c \sqrt{d}}{\sqrt{e}}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \\
& \operatorname{Log}\left[1 - \frac{\left(c \sqrt{d} + \sqrt{c^2 d + e}\right) \left(-\frac{i}{2} c x + \sqrt{1 - c^2 x^2}\right)}{\sqrt{e}}\right] + \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 - \frac{\left(c \sqrt{d} + \sqrt{c^2 d + e}\right) \left(-\frac{i}{2} c x + \sqrt{1 - c^2 x^2}\right)}{\sqrt{e}}\right] + \\
& 2 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{c \sqrt{d} - \sqrt{c^2 d + e}}\right] - 2 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{-c \sqrt{d} + \sqrt{c^2 d + e}}\right] - \\
& 2 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, -\frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{c \sqrt{d} + \sqrt{c^2 d + e}}\right] + 2 i \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{c \sqrt{d} + \sqrt{c^2 d + e}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{c \sqrt{d} - \sqrt{c^2 d + e}}\right] + \\
& 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{-c \sqrt{d} + \sqrt{c^2 d + e}}\right] + 2 \operatorname{PolyLog}\left[3, -\frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{c \sqrt{d} + \sqrt{c^2 d + e}}\right] - 2 \operatorname{PolyLog}\left[3, \frac{\sqrt{e} e^{i \operatorname{ArcSin}[c x]}}{c \sqrt{d} + \sqrt{c^2 d + e}}\right]
\end{aligned}$$

## Test results for the 474 problems in "5.1.5 Inverse sine functions.m"

**Problem 7: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{(d + e x)^3} dx$$

Optimal (type 3, 135 leaves, 4 steps):

$$\frac{b c \sqrt{1 - c^2 x^2}}{2 (c^2 d^2 - e^2) (d + e x)} - \frac{a + b \operatorname{ArcSin}[c x]}{2 e (d + e x)^2} + \frac{b c^3 d \operatorname{ArcTan}\left[\frac{e + c^2 d x}{\sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2}}\right]}{2 e (c^2 d^2 - e^2)^{3/2}}$$

Result (type 3, 207 leaves):

$$\frac{1}{2} \left( -\frac{a}{e (d + e x)^2} + \frac{b c \sqrt{1 - c^2 x^2}}{(c^2 d^2 - e^2) (d + e x)} - \frac{b \operatorname{ArcSin}[c x]}{e (d + e x)^2} - \frac{\frac{i}{2} b c^3 d \left( \operatorname{Log}[4] + \operatorname{Log}\left[\frac{e^2 \sqrt{c^2 d^2 - e^2} (i e + i c^2 d x + \sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2})}{b c^3 d (d + e x)}\right]\right)}{(c d - e) e (c d + e) \sqrt{c^2 d^2 - e^2}} \right)$$

Problem 13: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^2}{d + e x} dx$$

Optimal (type 4, 347 leaves, 10 steps):

$$\begin{aligned} & -\frac{\frac{i}{3} (a + b \operatorname{ArcSin}[c x])^3}{b e} + \frac{(a + b \operatorname{ArcSin}[c x])^2 \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e} + \\ & \frac{(a + b \operatorname{ArcSin}[c x])^2 \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e} - \frac{2 \frac{i}{2} b (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}]}{e} - \\ & \frac{2 \frac{i}{2} b (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}]}{e} + \frac{2 b^2 \operatorname{PolyLog}[3, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}]}{e} + \frac{2 b^2 \operatorname{PolyLog}[3, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}]}{e} \end{aligned}$$

Result (type 4, 2763 leaves):

$$\begin{aligned} & \frac{a^2 \operatorname{Log}[d + e x]}{e} + \frac{1}{4 e} \\ & a b \left( \frac{\pi - 2 \operatorname{ArcSin}[c x]}{\sqrt{2}} \right)^2 - 32 \frac{i}{2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] \operatorname{ArcTan}\left[\frac{(c d - e) \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{c^2 d^2 - e^2}}\right] - 4 \left( \pi + 4 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] - 2 \operatorname{ArcSin}[c x] \right) \end{aligned}$$

$$\begin{aligned}
& \text{Log}\left[1 - \frac{\frac{i}{e} \left(-c d + \sqrt{c^2 d^2 - e^2}\right) e^{-i \text{ArcSin}[c x]}}{e}\right] - 4 \left( \pi - 4 \text{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] - 2 \text{ArcSin}[c x] \right) \text{Log}\left[1 + \frac{\frac{i}{e} \left(c d + \sqrt{c^2 d^2 - e^2}\right) e^{-i \text{ArcSin}[c x]}}{e}\right] + \\
& 4 (\pi - 2 \text{ArcSin}[c x]) \text{Log}[c d + c e x] + 8 \text{ArcSin}[c x] \text{Log}[c d + c e x] + \\
& 8 i \left( \text{PolyLog}[2, \frac{\frac{i}{e} \left(-c d + \sqrt{c^2 d^2 - e^2}\right) e^{-i \text{ArcSin}[c x]}}{e}] + \text{PolyLog}[2, -\frac{\frac{i}{e} \left(c d + \sqrt{c^2 d^2 - e^2}\right) e^{-i \text{ArcSin}[c x]}}{e}] \right) + \frac{1}{3 e \sqrt{-(-c^2 d^2 + e^2)^2}} \\
& b^2 \left( -\frac{i}{\sqrt{-(-c^2 d^2 + e^2)^2}} \text{ArcSin}[c x]^3 - 24 \frac{i}{\sqrt{-(-c^2 d^2 + e^2)^2}} \text{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] \text{ArcSin}[c x] \text{ArcTan}\left[\frac{(c d - e) \text{Cot}\left[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])\right]}{\sqrt{c^2 d^2 - e^2}}\right] + \right. \\
& \left. 24 \frac{i}{\sqrt{-(-c^2 d^2 + e^2)^2}} \text{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] \text{ArcSin}[c x] \text{ArcTan}\left[\frac{(c d - e) (\cos[\frac{1}{2} \text{ArcSin}[c x]] - \sin[\frac{1}{2} \text{ArcSin}[c x]])}{\sqrt{c^2 d^2 - e^2} (\cos[\frac{1}{2} \text{ArcSin}[c x]] + \sin[\frac{1}{2} \text{ArcSin}[c x]])}\right] - \right. \\
& \left. 3 \sqrt{-(-c^2 d^2 + e^2)^2} \pi \text{ArcSin}[c x] \text{Log}\left[1 - \frac{\frac{i}{e} \left(-c d + \sqrt{c^2 d^2 - e^2}\right) e^{-i \text{ArcSin}[c x]}}{e}\right] - 12 \sqrt{-(-c^2 d^2 + e^2)^2} \text{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] \text{ArcSin}[c x] \right. \\
& \left. \text{Log}\left[1 - \frac{\frac{i}{e} \left(-c d + \sqrt{c^2 d^2 - e^2}\right) e^{-i \text{ArcSin}[c x]}}{e}\right] + 3 \sqrt{-(-c^2 d^2 + e^2)^2} \text{ArcSin}[c x]^2 \text{Log}\left[1 - \frac{\frac{i}{e} \left(-c d + \sqrt{c^2 d^2 - e^2}\right) e^{-i \text{ArcSin}[c x]}}{e}\right] - \right. \\
& \left. 3 \sqrt{-(-c^2 d^2 + e^2)^2} \pi \text{ArcSin}[c x] \text{Log}\left[1 + \frac{\frac{i}{e} \left(c d + \sqrt{c^2 d^2 - e^2}\right) e^{-i \text{ArcSin}[c x]}}{e}\right] + 12 \sqrt{-(-c^2 d^2 + e^2)^2} \text{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] \right. \\
& \left. \text{ArcSin}[c x] \text{Log}\left[1 + \frac{\frac{i}{e} \left(c d + \sqrt{c^2 d^2 - e^2}\right) e^{-i \text{ArcSin}[c x]}}{e}\right] + 3 \sqrt{-(-c^2 d^2 + e^2)^2} \text{ArcSin}[c x]^2 \text{Log}\left[1 + \frac{\frac{i}{e} \left(c d + \sqrt{c^2 d^2 - e^2}\right) e^{-i \text{ArcSin}[c x]}}{e}\right] + \right. \\
& \left. 3 c d \sqrt{-c^2 d^2 + e^2} \text{ArcSin}[c x]^2 \text{Log}\left[1 + \frac{\frac{i}{e} e^{i \text{ArcSin}[c x]}}{-c d + \sqrt{c^2 d^2 - e^2}}\right] - 3 c d \sqrt{-c^2 d^2 + e^2} \text{ArcSin}[c x]^2 \text{Log}\left[1 - \frac{\frac{i}{e} e^{i \text{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right] - \right. \\
& \left. 3 i c d \sqrt{c^2 d^2 - e^2} \text{ArcSin}[c x]^2 \text{Log}\left[1 + \frac{e^{i \text{ArcSin}[c x]}}{\frac{i}{e} c d - \sqrt{-c^2 d^2 + e^2}}\right] + 3 \sqrt{-(-c^2 d^2 + e^2)^2} \text{ArcSin}[c x]^2 \text{Log}\left[1 + \frac{e^{i \text{ArcSin}[c x]}}{\frac{i}{e} c d - \sqrt{-c^2 d^2 + e^2}}\right] + \right.
\end{aligned}$$

$$\begin{aligned}
& 3 \pm c d \sqrt{c^2 d^2 - e^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{e e^{i \operatorname{ArcSin}[c x]}}{\pm c d + \sqrt{-c^2 d^2 + e^2}}\right] + 3 \sqrt{-(-c^2 d^2 + e^2)^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{e e^{i \operatorname{ArcSin}[c x]}}{\pm c d + \sqrt{-c^2 d^2 + e^2}}\right] + \\
& 3 \sqrt{-(-c^2 d^2 + e^2)^2} \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{(c d - \sqrt{c^2 d^2 - e^2}) (c x + \pm \sqrt{1 - c^2 x^2})}{e}\right] + \\
& 12 \sqrt{-(-c^2 d^2 + e^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{(c d - \sqrt{c^2 d^2 - e^2}) (c x + \pm \sqrt{1 - c^2 x^2})}{e}\right] - \\
& 3 \sqrt{-(-c^2 d^2 + e^2)^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{(c d - \sqrt{c^2 d^2 - e^2}) (c x + \pm \sqrt{1 - c^2 x^2})}{e}\right] + \\
& 3 \sqrt{-(-c^2 d^2 + e^2)^2} \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{(c d + \sqrt{c^2 d^2 - e^2}) (c x + \pm \sqrt{1 - c^2 x^2})}{e}\right] - \\
& 12 \sqrt{-(-c^2 d^2 + e^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{(c d + \sqrt{c^2 d^2 - e^2}) (c x + \pm \sqrt{1 - c^2 x^2})}{e}\right] - \\
& 3 \sqrt{-(-c^2 d^2 + e^2)^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{(c d + \sqrt{c^2 d^2 - e^2}) (c x + \pm \sqrt{1 - c^2 x^2})}{e}\right] - \\
& 6 \pm c d \sqrt{-c^2 d^2 + e^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{\pm e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right] + 6 \pm c d \sqrt{-c^2 d^2 + e^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{\pm e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right] - \\
& 6 c d \sqrt{c^2 d^2 - e^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{e e^{i \operatorname{ArcSin}[c x]}}{-\pm c d + \sqrt{-c^2 d^2 + e^2}}\right] - 6 \pm \sqrt{-(-c^2 d^2 + e^2)^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{e e^{i \operatorname{ArcSin}[c x]}}{-\pm c d + \sqrt{-c^2 d^2 + e^2}}\right] + \\
& 6 c d \sqrt{c^2 d^2 - e^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, -\frac{e e^{i \operatorname{ArcSin}[c x]}}{\pm c d + \sqrt{-c^2 d^2 + e^2}}\right] - 6 \pm \sqrt{-(-c^2 d^2 + e^2)^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, -\frac{e e^{i \operatorname{ArcSin}[c x]}}{\pm c d + \sqrt{-c^2 d^2 + e^2}}\right] + \\
& 6 c d \sqrt{-c^2 d^2 + e^2} \operatorname{PolyLog}\left[3, \frac{\pm e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right] - 6 c d \sqrt{-c^2 d^2 + e^2} \operatorname{PolyLog}\left[3, \frac{\pm e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right] - \\
& 6 \pm c d \sqrt{c^2 d^2 - e^2} \operatorname{PolyLog}\left[3, \frac{e e^{i \operatorname{ArcSin}[c x]}}{-\pm c d + \sqrt{-c^2 d^2 + e^2}}\right] + 6 \sqrt{-(-c^2 d^2 + e^2)^2} \operatorname{PolyLog}\left[3, \frac{e e^{i \operatorname{ArcSin}[c x]}}{-\pm c d + \sqrt{-c^2 d^2 + e^2}}\right] + \\
& 6 \pm c d \sqrt{c^2 d^2 - e^2} \operatorname{PolyLog}\left[3, -\frac{e e^{i \operatorname{ArcSin}[c x]}}{\pm c d + \sqrt{-c^2 d^2 + e^2}}\right] + 6 \sqrt{-(-c^2 d^2 + e^2)^2} \operatorname{PolyLog}\left[3, -\frac{e e^{i \operatorname{ArcSin}[c x]}}{\pm c d + \sqrt{-c^2 d^2 + e^2}}\right]
\end{aligned}$$

**Problem 14:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[cx])^2}{(d + ex)^2} dx$$

Optimal (type 4, 309 leaves, 10 steps):

$$\begin{aligned} & -\frac{(a + b \operatorname{ArcSin}[cx])^2}{e(d + ex)} - \frac{2 i b c (a + b \operatorname{ArcSin}[cx]) \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[cx]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e \sqrt{c^2 d^2 - e^2}} + \\ & \frac{2 i b c (a + b \operatorname{ArcSin}[cx]) \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[cx]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e \sqrt{c^2 d^2 - e^2}} - \frac{2 b^2 c \operatorname{PolyLog}\left[2, \frac{i e e^{i \operatorname{ArcSin}[cx]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e \sqrt{c^2 d^2 - e^2}} + \frac{2 b^2 c \operatorname{PolyLog}\left[2, \frac{i e e^{i \operatorname{ArcSin}[cx]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e \sqrt{c^2 d^2 - e^2}} \end{aligned}$$

Result (type 6, 1152 leaves):

$$\begin{aligned} & -\frac{a^2}{e(d + ex)} + 2ab \left( -\frac{c \sqrt{1 + \frac{-d - \sqrt{\frac{1}{c^2}} e}{d + ex}} \sqrt{1 + \frac{-d + \sqrt{\frac{1}{c^2}} e}{d + ex}} \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, -\frac{-d + \sqrt{\frac{1}{c^2}} e}{d + ex}, -\frac{-d - \sqrt{\frac{1}{c^2}} e}{d + ex}\right]}{e^2 \sqrt{1 - c^2 x^2}} - \frac{\operatorname{ArcSin}[cx]}{e(d + ex)} \right) + \\ & \frac{1}{e} b^2 c \left( -\frac{\operatorname{ArcSin}[cx]^2}{c d + c e x} + \frac{2 \pi \operatorname{ArcTan}\left[\frac{e + c d \operatorname{Tan}\left[\frac{1}{2} \operatorname{ArcSin}[cx]\right]}{\sqrt{c^2 d^2 - e^2}}\right]}{\sqrt{c^2 d^2 - e^2}} + \frac{1}{\sqrt{-c^2 d^2 + e^2}} \right. \\ & 2 \left( 2 \operatorname{ArcCos}\left[-\frac{c d}{e}\right] \operatorname{ArcTanh}\left[\frac{(c d - e) \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right]}{\sqrt{-c^2 d^2 + e^2}}\right] + (\pi - 2 \operatorname{ArcSin}[cx]) \operatorname{ArcTanh}\left[\frac{(c d + e) \operatorname{Tan}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right]}{\sqrt{-c^2 d^2 + e^2}}\right] \right. \\ & \left. \left. + \left( \operatorname{ArcCos}\left[-\frac{c d}{e}\right] + 2 i \left( \operatorname{ArcTanh}\left[\frac{(c d - e) \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right]}{\sqrt{-c^2 d^2 + e^2}}\right] + \operatorname{ArcTanh}\left[\frac{(c d + e) \operatorname{Tan}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right]}{\sqrt{-c^2 d^2 + e^2}}\right] \right) \right) \right) \right. \\ & \left. \operatorname{Log}\left[\frac{\sqrt{-c^2 d^2 + e^2} e^{\frac{1}{4} i (\pi - 2 \operatorname{ArcSin}[cx])}}{\sqrt{2} \sqrt{e} \sqrt{c d + c e x}}\right] + \right. \\ & \left. \left( \operatorname{ArcCos}\left[-\frac{c d}{e}\right] - 2 i \operatorname{ArcTanh}\left[\frac{(c d - e) \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right]}{\sqrt{-c^2 d^2 + e^2}}\right] - 2 i \operatorname{ArcTanh}\left[\frac{(c d + e) \operatorname{Tan}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right]}{\sqrt{-c^2 d^2 + e^2}}\right] \right) \right) \end{aligned}$$

$$\begin{aligned}
& \text{Log} \left[ \frac{\left( \frac{1}{2} - \frac{i}{2} \right) \sqrt{-c^2 d^2 + e^2} e^{\frac{1}{2} i \text{ArcSin}[cx]}}{\sqrt{e} \sqrt{c d + c e x}} \right] - \left( \text{ArcCos} \left[ -\frac{c d}{e} \right] + 2 i \text{ArcTanh} \left[ \frac{(c d - e) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[cx]) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] \right) \\
& \text{Log} \left[ \frac{(c d + e) (-c d + e - i \sqrt{-c^2 d^2 + e^2}) (1 + i \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[cx]) \right])}{e (c d + e + \sqrt{-c^2 d^2 + e^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[cx]) \right])} \right] - \left( \text{ArcCos} \left[ -\frac{c d}{e} \right] - \right. \\
& \left. 2 i \text{ArcTanh} \left[ \frac{(c d - e) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[cx]) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] \right) \text{Log} \left[ \frac{(c d + e) (i c d - i e + \sqrt{-c^2 d^2 + e^2}) (i + \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[cx]) \right])}{e (c d + e + \sqrt{-c^2 d^2 + e^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[cx]) \right])} \right] + \\
& i \left( \text{PolyLog} [2, \frac{(c d - i \sqrt{-c^2 d^2 + e^2}) (c d + e - \sqrt{-c^2 d^2 + e^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[cx]) \right])}{e (c d + e + \sqrt{-c^2 d^2 + e^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[cx]) \right])}] - \right. \\
& \left. \text{PolyLog} [2, \frac{(c d + i \sqrt{-c^2 d^2 + e^2}) (c d + e - \sqrt{-c^2 d^2 + e^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[cx]) \right])}{e (c d + e + \sqrt{-c^2 d^2 + e^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[cx]) \right])}] \right)
\end{aligned}$$

**Problem 15: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \text{ArcSin}[cx])^2}{(d + e x)^3} dx$$

Optimal (type 4, 401 leaves, 13 steps):

$$\begin{aligned}
& \frac{b c \sqrt{1 - c^2 x^2} (a + b \text{ArcSin}[cx])}{(c^2 d^2 - e^2) (d + e x)} - \frac{(a + b \text{ArcSin}[cx])^2}{2 e (d + e x)^2} - \frac{i b c^3 d (a + b \text{ArcSin}[cx]) \text{Log} \left[ 1 - \frac{i e e^{i \text{ArcSin}[cx]}}{c d - \sqrt{c^2 d^2 - e^2}} \right]}{e (c^2 d^2 - e^2)^{3/2}} + \\
& \frac{i b c^3 d (a + b \text{ArcSin}[cx]) \text{Log} \left[ 1 - \frac{i e e^{i \text{ArcSin}[cx]}}{c d + \sqrt{c^2 d^2 - e^2}} \right]}{e (c^2 d^2 - e^2)^{3/2}} - \frac{b^2 c^2 \text{Log}[d + e x]}{e (c^2 d^2 - e^2)} - \frac{b^2 c^3 d \text{PolyLog} [2, \frac{i e e^{i \text{ArcSin}[cx]}}{c d - \sqrt{c^2 d^2 - e^2}}]}{e (c^2 d^2 - e^2)^{3/2}} + \frac{b^2 c^3 d \text{PolyLog} [2, \frac{i e e^{i \text{ArcSin}[cx]}}{c d + \sqrt{c^2 d^2 - e^2}}]}{e (c^2 d^2 - e^2)^{3/2}}
\end{aligned}$$

Result (type 6, 1363 leaves):

$$\begin{aligned}
& -\frac{a^2}{2 e (d + e x)^2} + 2 a b \left( -\frac{c \sqrt{1 + \frac{-d - \sqrt{\frac{1}{e^2}} e}{d + e x}} \sqrt{1 + \frac{-d + \sqrt{\frac{1}{e^2}} e}{d + e x}} \text{AppellF1}\left[2, \frac{1}{2}, \frac{1}{2}, 3, -\frac{-d + \sqrt{\frac{1}{e^2}} e}{d + e x}, -\frac{-d - \sqrt{\frac{1}{e^2}} e}{d + e x}\right]}{4 e^2 (d + e x) \sqrt{1 - c^2 x^2}} - \frac{\text{ArcSin}[c x]}{2 e (d + e x)^2} \right) + \\
& b^2 c^2 \left( \frac{\sqrt{1 - c^2 x^2} \text{ArcSin}[c x]}{(c d - e) (c d + e) (c d + c e x)} - \frac{\text{ArcSin}[c x]^2}{2 e (c d + c e x)^2} + \frac{\text{Log}\left[1 + \frac{e x}{d}\right]}{e (-c^2 d^2 + e^2)} - \right. \\
& \frac{1}{e (-c^2 d^2 + e^2)} c d \left( \frac{\pi \text{ArcTan}\left[\frac{e+c d \tan\left(\frac{1}{2} \text{ArcSin}[c x]\right)}{\sqrt{c^2 d^2 - e^2}}\right]}{\sqrt{c^2 d^2 - e^2}} + \frac{1}{\sqrt{-c^2 d^2 + e^2}} \left( 2 \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right) \text{ArcTanh}\left[\frac{(c d + e) \cot\left(\frac{1}{2} \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)\right)}{\sqrt{-c^2 d^2 + e^2}}\right] - \right. \right. \\
& 2 \text{ArcCos}\left[-\frac{c d}{e}\right] \text{ArcTanh}\left[\frac{(-c d + e) \tan\left(\frac{1}{2} \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)\right)}{\sqrt{-c^2 d^2 + e^2}}\right] + \left( \text{ArcCos}\left[-\frac{c d}{e}\right] - 2 \text{i} \left( \text{ArcTanh}\left[\frac{(c d + e) \cot\left(\frac{1}{2} \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)\right)}{\sqrt{-c^2 d^2 + e^2}}\right] - \right. \right. \\
& \left. \left. \text{ArcTanh}\left[\frac{(-c d + e) \tan\left(\frac{1}{2} \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)\right)}{\sqrt{-c^2 d^2 + e^2}}\right] \right) \right) \text{Log}\left[\frac{\sqrt{-c^2 d^2 + e^2} e^{-\frac{1}{2} i \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)}}{\sqrt{2} \sqrt{e} \sqrt{c d + c e x}}\right] + \right. \\
& \left( \text{ArcCos}\left[-\frac{c d}{e}\right] + 2 \text{i} \left( \text{ArcTanh}\left[\frac{(c d + e) \cot\left(\frac{1}{2} \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)\right)}{\sqrt{-c^2 d^2 + e^2}}\right] - \text{ArcTanh}\left[\frac{(-c d + e) \tan\left(\frac{1}{2} \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)\right)}{\sqrt{-c^2 d^2 + e^2}}\right] \right) \right) \\
& \text{Log}\left[\frac{\sqrt{-c^2 d^2 + e^2} e^{\frac{1}{2} i \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)}}{\sqrt{2} \sqrt{e} \sqrt{c d + c e x}}\right] - \left( \text{ArcCos}\left[-\frac{c d}{e}\right] + 2 \text{i} \text{ArcTanh}\left[\frac{(-c d + e) \tan\left(\frac{1}{2} \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)\right)}{\sqrt{-c^2 d^2 + e^2}}\right] \right) \\
& \text{Log}\left[1 - \frac{\left(c d - \text{i} \sqrt{-c^2 d^2 + e^2}\right) \left(c d + e - \sqrt{-c^2 d^2 + e^2} \tan\left(\frac{1}{2} \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)\right)\right)}{e \left(c d + e + \sqrt{-c^2 d^2 + e^2} \tan\left(\frac{1}{2} \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)\right)\right)}\right] + \left( -\text{ArcCos}\left[-\frac{c d}{e}\right] + 2 \text{i} \text{ArcTanh}\left[ \right. \right. \\
& \left. \left. \frac{(-c d + e) \tan\left(\frac{1}{2} \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)\right)}{\sqrt{-c^2 d^2 + e^2}}\right] \right) \text{Log}\left[1 - \frac{\left(c d + \text{i} \sqrt{-c^2 d^2 + e^2}\right) \left(c d + e - \sqrt{-c^2 d^2 + e^2} \tan\left(\frac{1}{2} \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)\right)\right)}{e \left(c d + e + \sqrt{-c^2 d^2 + e^2} \tan\left(\frac{1}{2} \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)\right)\right)}\right] + \\
& \text{i} \left( \text{PolyLog}\left[2, \frac{\left(c d - \text{i} \sqrt{-c^2 d^2 + e^2}\right) \left(c d + e - \sqrt{-c^2 d^2 + e^2} \tan\left(\frac{1}{2} \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)\right)\right)}{e \left(c d + e + \sqrt{-c^2 d^2 + e^2} \tan\left(\frac{1}{2} \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)\right)\right)}\right] -
\end{aligned}$$

$$\text{PolyLog}\left[2, \frac{\left(c d + i \sqrt{-c^2 d^2 + e^2}\right) \left(c d + e - \sqrt{-c^2 d^2 + e^2} \tan\left[\frac{1}{2} \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)\right]\right)}{e \left(c d + e + \sqrt{-c^2 d^2 + e^2} \tan\left[\frac{1}{2} \left(\frac{\pi}{2} - \text{ArcSin}[c x]\right)\right]\right)}\right]\right]$$

Problem 28: Unable to integrate problem.

$$\int (d + e x)^m (a + b \text{ArcSin}[c x]) dx$$

Optimal (type 6, 154 leaves, 3 steps):

$$-\frac{b c (d + e x)^{2+m} \sqrt{1 - \frac{c (d+e x)}{c d-e}} \sqrt{1 - \frac{c (d+e x)}{c d+e}} \text{AppellF1}\left[2+m, \frac{1}{2}, \frac{1}{2}, 3+m, \frac{c (d+e x)}{c d-e}, \frac{c (d+e x)}{c d+e}\right]}{e^2 (1+m) (2+m) \sqrt{1-c^2 x^2}} + \frac{(d + e x)^{1+m} (a + b \text{ArcSin}[c x])}{e (1+m)}$$

Result (type 8, 18 leaves):

$$\int (d + e x)^m (a + b \text{ArcSin}[c x]) dx$$

Problem 39: Result more than twice size of optimal antiderivative.

$$\int \frac{(d - c^2 d x^2)^{3/2} (a + b \text{ArcSin}[c x])}{f + g x} dx$$

Optimal (type 4, 1073 leaves, 29 steps):

$$\begin{aligned}
& -\frac{a d (c f - g) (c f + g) \sqrt{d - c^2 d x^2}}{g^3} - \frac{b c d x \sqrt{d - c^2 d x^2}}{3 g \sqrt{1 - c^2 x^2}} + \frac{b c d (c f - g) (c f + g) x \sqrt{d - c^2 d x^2}}{g^3 \sqrt{1 - c^2 x^2}} - \frac{b c^3 d f x^2 \sqrt{d - c^2 d x^2}}{4 g^2 \sqrt{1 - c^2 x^2}} + \frac{b c^3 d x^3 \sqrt{d - c^2 d x^2}}{9 g \sqrt{1 - c^2 x^2}} - \\
& \frac{b d (c f - g) (c f + g) \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x]}{g^3} + \frac{c^2 d f x \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])}{2 g^2} + \frac{d (1 - c^2 x^2) \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])}{3 g} + \\
& \frac{c d f \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])^2}{4 b g^2 \sqrt{1 - c^2 x^2}} - \frac{c d (c f - g) (c f + g) x \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])^2}{2 b g^3 \sqrt{1 - c^2 x^2}} - \frac{d (c^2 f^2 - g^2)^2 \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])^2}{2 b c g^4 (f + g x) \sqrt{1 - c^2 x^2}} - \\
& \frac{d (c f - g) (c f + g) \sqrt{1 - c^2 x^2} \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])^2}{2 b c g^2 (f + g x)} + \frac{a d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2} \operatorname{ArcTan}\left[\frac{g + c^2 f x}{\sqrt{c^2 f^2 - g^2} \sqrt{1 - c^2 x^2}}\right]}{g^4 \sqrt{1 - c^2 x^2}} - \\
& \frac{i b d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^4 \sqrt{1 - c^2 x^2}} + \frac{i b d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^4 \sqrt{1 - c^2 x^2}} - \\
& \frac{b d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2} \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^4 \sqrt{1 - c^2 x^2}} + \frac{b d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2} \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^4 \sqrt{1 - c^2 x^2}}
\end{aligned}$$

Result (type 4, 3456 leaves):

$$\begin{aligned}
& \sqrt{-d (-1 + c^2 x^2)} \left( \frac{a d (-3 c^2 f^2 + 4 g^2)}{3 g^3} + \frac{a c^2 d f x}{2 g^2} - \frac{a c^2 d x^2}{3 g} \right) + \frac{a c d^{3/2} f (2 c^2 f^2 - 3 g^2) \operatorname{ArcTan}\left[\frac{c x \sqrt{-d (-1 + c^2 x^2)}}{\sqrt{d} \sqrt{-1 + c^2 x^2}}\right]}{2 g^4} + \\
& \frac{a d^{3/2} (-c^2 f^2 + g^2)^{3/2} \operatorname{Log}[f + g x]}{g^4} - \frac{a d^{3/2} (-c^2 f^2 + g^2)^{3/2} \operatorname{Log}[d g + c^2 d f x + \sqrt{d} \sqrt{-c^2 f^2 + g^2} \sqrt{-d (-1 + c^2 x^2)}]}{g^4} + \\
& \frac{1}{2 g^2} b d \sqrt{d (1 - c^2 x^2)} \left( -\frac{2 c g x}{\sqrt{1 - c^2 x^2}} + 2 g \operatorname{ArcSin}[c x] + \frac{c f \operatorname{ArcSin}[c x]^2}{\sqrt{1 - c^2 x^2}} + \frac{1}{\sqrt{1 - c^2 x^2}} 2 (-c f + g) (c f + g) \right. \\
& \left. \frac{\pi \operatorname{ArcTan}\left[\frac{g + c f \tan\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]}{\sqrt{c^2 f^2 - g^2}}\right]}{\sqrt{c^2 f^2 - g^2}} + \frac{1}{\sqrt{-c^2 f^2 + g^2}} \left( 2 \operatorname{ArcCos}\left[-\frac{c f}{g}\right] \operatorname{ArcTanh}\left[\frac{(c f - g) \cot\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2 + g^2}}\right] + (\pi - 2 \operatorname{ArcSin}[c x]) \right. \right. \\
& \left. \left. \operatorname{ArcTanh}\left[\frac{(c f + g) \tan\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2 + g^2}}\right] \right) + \left( \operatorname{ArcCos}\left[-\frac{c f}{g}\right] + 2 \operatorname{ArcTanh}\left[\frac{(c f - g) \cot\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2 + g^2}}\right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \left( \text{ArcTanh} \left[ \frac{(c f + g) \ Tan \left[ \frac{1}{4} (\pi + 2 \ ArcSin[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \ Log \left[ \frac{e^{\frac{1}{4} i (\pi - 2 \ ArcSin[c x])} \sqrt{-c^2 f^2 + g^2}}{\sqrt{2} \sqrt{g} \sqrt{c f + c g x}} \right] + \right. \\
& \left. \left( \text{ArcCos} \left[ -\frac{c f}{g} \right] - 2 i \text{ArcTanh} \left[ \frac{(c f - g) \ Cot \left[ \frac{1}{4} (\pi + 2 \ ArcSin[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] - 2 i \text{ArcTanh} \left[ \frac{(c f + g) \ Tan \left[ \frac{1}{4} (\pi + 2 \ ArcSin[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \right. \\
& \left. \ Log \left[ \frac{\left(\frac{1}{2} - \frac{i}{2}\right) e^{\frac{1}{2} i \ ArcSin[c x]} \sqrt{-c^2 f^2 + g^2}}{\sqrt{g} \sqrt{c f + c g x}} \right] - \left( \text{ArcCos} \left[ -\frac{c f}{g} \right] + 2 i \text{ArcTanh} \left[ \frac{(c f - g) \ Cot \left[ \frac{1}{4} (\pi + 2 \ ArcSin[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \right. \\
& \left. \ Log \left[ \frac{(c f + g) \left(-c f + g - i \sqrt{-c^2 f^2 + g^2}\right) \left(1 + i \ Cot \left[ \frac{1}{4} (\pi + 2 \ ArcSin[c x]) \right]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \ Cot \left[ \frac{1}{4} (\pi + 2 \ ArcSin[c x]) \right]\right)} \right] - \left( \text{ArcCos} \left[ -\frac{c f}{g} \right] - 2 i \right. \right. \\
& \left. \left. \text{ArcTanh} \left[ \frac{(c f - g) \ Cot \left[ \frac{1}{4} (\pi + 2 \ ArcSin[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \ Log \left[ \frac{(c f + g) \left(i c f - i g + \sqrt{-c^2 f^2 + g^2}\right) \left(i + \ Cot \left[ \frac{1}{4} (\pi + 2 \ ArcSin[c x]) \right]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \ Cot \left[ \frac{1}{4} (\pi + 2 \ ArcSin[c x]) \right]\right)} \right] + \right. \\
& \left. \left. i \left( \text{PolyLog} \left[ 2, \frac{\left(c f - i \sqrt{-c^2 f^2 + g^2}\right) \left(c f + g - \sqrt{-c^2 f^2 + g^2} \ Cot \left[ \frac{1}{4} (\pi + 2 \ ArcSin[c x]) \right]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \ Cot \left[ \frac{1}{4} (\pi + 2 \ ArcSin[c x]) \right]\right)} \right] - \text{PolyLog} \left[ 2, \right. \right. \right. \\
& \left. \left. \left. \frac{\left(c f + i \sqrt{-c^2 f^2 + g^2}\right) \left(c f + g - \sqrt{-c^2 f^2 + g^2} \ Cot \left[ \frac{1}{4} (\pi + 2 \ ArcSin[c x]) \right]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \ Cot \left[ \frac{1}{4} (\pi + 2 \ ArcSin[c x]) \right]\right)} \right] \right) \right) \right] + \\
& b d \left( -\frac{1}{8 \sqrt{1 - c^2 x^2}} \sqrt{d (1 - c^2 x^2)} \left( \frac{\pi \text{ArcTan} \left[ \frac{g + c f \ Tan \left[ \frac{1}{2} \ ArcSin[c x] \right]}{\sqrt{c^2 f^2 - g^2}} \right]}{\sqrt{c^2 f^2 - g^2}} + \frac{1}{\sqrt{-c^2 f^2 + g^2}} \left( 2 \text{ArcCos} \left[ -\frac{c f}{g} \right] \right. \right. \right. \\
& \left. \left. \left. \text{ArcTanh} \left[ \frac{(c f - g) \ Cot \left[ \frac{1}{4} (\pi + 2 \ ArcSin[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + (\pi - 2 \ ArcSin[c x]) \text{ArcTanh} \left[ \frac{(c f + g) \ Tan \left[ \frac{1}{4} (\pi + 2 \ ArcSin[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + \right. \right. \right. \\
& \left. \left. \left. \left( \text{ArcCos} \left[ -\frac{c f}{g} \right] + 2 i \left( \text{ArcTanh} \left[ \frac{(c f - g) \ Cot \left[ \frac{1}{4} (\pi + 2 \ ArcSin[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + \text{ArcTanh} \left[ \frac{(c f + g) \ Tan \left[ \frac{1}{4} (\pi + 2 \ ArcSin[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \text{Log} \left[ \frac{\frac{1}{4} i (\pi - 2 \text{ArcSin}[c x]) \sqrt{-c^2 f^2 + g^2}}{\sqrt{2} \sqrt{g} \sqrt{c f + c g x}} \right] + \\
& \left( \text{ArcCos} \left[ -\frac{c f}{g} \right] - 2 i \text{ArcTanh} \left[ \frac{(c f - g) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] - 2 i \text{ArcTanh} \left[ \frac{(c f + g) \text{Tan} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \\
& \text{Log} \left[ \frac{\left(\frac{1}{2} - \frac{i}{2}\right) e^{\frac{1}{2} i \text{ArcSin}[c x]} \sqrt{-c^2 f^2 + g^2}}{\sqrt{g} \sqrt{c f + c g x}} \right] - \left( \text{ArcCos} \left[ -\frac{c f}{g} \right] + 2 i \text{ArcTanh} \left[ \frac{(c f - g) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \\
& \text{Log} \left[ \frac{(c f + g) \left(-c f + g - i \sqrt{-c^2 f^2 + g^2}\right) \left(1 + i \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]\right)} \right] - \left( \text{ArcCos} \left[ -\frac{c f}{g} \right] - 2 i \right. \\
& \left. \text{ArcTanh} \left[ \frac{(c f - g) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \text{Log} \left[ \frac{(c f + g) \left(i c f - i g + \sqrt{-c^2 f^2 + g^2}\right) \left(i + \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]\right)} \right] + \\
& i \left( \text{PolyLog} \left[ 2, \frac{\left(c f - i \sqrt{-c^2 f^2 + g^2}\right) \left(c f + g - \sqrt{-c^2 f^2 + g^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]\right)} \right] - \text{PolyLog} \left[ 2, \right. \\
& \left. \frac{\left(c f + i \sqrt{-c^2 f^2 + g^2}\right) \left(c f + g - \sqrt{-c^2 f^2 + g^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]\right)} \right] \right) + \\
& \frac{1}{72 g^4 \sqrt{1 - c^2 x^2}} \sqrt{d (1 - c^2 x^2)} \left( -18 c g (-4 c^2 f^2 + g^2) x + 18 g (-4 c^2 f^2 + g^2) \sqrt{1 - c^2 x^2} \text{ArcSin}[c x] - \right. \\
& 18 c f (2 c^2 f^2 - g^2) \text{ArcSin}[c x]^2 + 9 c f g^2 \cos[2 \text{ArcSin}[c x]] + \\
& 6 g^3 \text{ArcSin}[c x] \cos[3 \text{ArcSin}[c x]] + 9 (8 c^4 f^4 - 8 c^2 f^2 g^2 + g^4) \\
& \left. \frac{\pi \text{ArcTan} \left[ \frac{g + c f \tan \left[ \frac{1}{2} \text{ArcSin}[c x] \right]}{\sqrt{c^2 f^2 - g^2}} \right]}{\sqrt{c^2 f^2 - g^2}} + \frac{1}{\sqrt{-c^2 f^2 + g^2}} \left( 2 \text{ArcCos} \left[ -\frac{c f}{g} \right] \text{ArcTanh} \left[ \frac{(c f - g) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + (\pi - 2 \text{ArcSin}[c x]) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \operatorname{ArcTanh} \left[ \frac{(c f + g) \tan \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + \left( \operatorname{ArcCos} \left[ -\frac{c f}{g} \right] + 2 \operatorname{i} \operatorname{ArcTanh} \left[ \frac{(c f - g) \cot \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + \right. \\
& \quad \left. \operatorname{ArcTanh} \left[ \frac{(c f + g) \tan \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \operatorname{Log} \left[ \frac{e^{\frac{1}{4} \operatorname{i} (\pi - 2 \operatorname{ArcSin}[c x])} \sqrt{-c^2 f^2 + g^2}}{\sqrt{2} \sqrt{g} \sqrt{c f + c g x}} \right] + \\
& \left( \operatorname{ArcCos} \left[ -\frac{c f}{g} \right] - 2 \operatorname{i} \operatorname{ArcTanh} \left[ \frac{(c f - g) \cot \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] - 2 \operatorname{i} \operatorname{ArcTanh} \left[ \frac{(c f + g) \tan \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \\
& \operatorname{Log} \left[ \frac{\left(\frac{1}{2} - \frac{\operatorname{i}}{2}\right) e^{\frac{1}{2} \operatorname{i} \operatorname{ArcSin}[c x]} \sqrt{-c^2 f^2 + g^2}}{\sqrt{g} \sqrt{c f + c g x}} \right] - \left( \operatorname{ArcCos} \left[ -\frac{c f}{g} \right] + 2 \operatorname{i} \operatorname{ArcTanh} \left[ \frac{(c f - g) \cot \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \operatorname{Log} \left[ \right. \\
& \quad \left. \frac{(c f + g) \left(-c f + g - \operatorname{i} \sqrt{-c^2 f^2 + g^2}\right) \left(1 + \operatorname{i} \cot \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \cot \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]\right)} \right] - \left( \operatorname{ArcCos} \left[ -\frac{c f}{g} \right] - 2 \operatorname{i} \right. \\
& \quad \left. \operatorname{ArcTanh} \left[ \frac{(c f - g) \cot \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \operatorname{Log} \left[ \frac{(c f + g) \left(\operatorname{i} c f - \operatorname{i} g + \sqrt{-c^2 f^2 + g^2}\right) \left(\operatorname{i} + \cot \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \cot \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]\right)} \right] + \\
& \operatorname{i} \left( \operatorname{PolyLog} [2, \frac{(c f - \operatorname{i} \sqrt{-c^2 f^2 + g^2}) (c f + g - \sqrt{-c^2 f^2 + g^2} \cot \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right])}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \cot \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]\right)}] - \right. \\
& \quad \left. \operatorname{PolyLog} [2, \frac{(c f + \operatorname{i} \sqrt{-c^2 f^2 + g^2}) (c f + g - \sqrt{-c^2 f^2 + g^2} \cot \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right])}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \cot \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]\right)}] \right) \right) + \\
& \left. \left. \left. 18 c f g^2 \operatorname{ArcSin}[c x] \sin[2 \operatorname{ArcSin}[c x]] - 2 g^3 \sin[3 \operatorname{ArcSin}[c x]] \right) \right\} \right)
\end{aligned}$$

Problem 43: Result more than twice size of optimal antiderivative.

$$\int \frac{(d - c^2 dx)^{5/2} (a + b \operatorname{ArcSin}[cx])}{f + g x} dx$$

Optimal (type 4, 1648 leaves, 37 steps):

$$\begin{aligned}
& \frac{a d^2 (c^2 f^2 - g^2)^2 \sqrt{d - c^2 dx^2}}{g^5} + \frac{2 b c d^2 x \sqrt{d - c^2 dx^2}}{15 g \sqrt{1 - c^2 x^2}} + \frac{b c d^2 (c^2 f^2 - 2 g^2) x \sqrt{d - c^2 dx^2}}{3 g^3 \sqrt{1 - c^2 x^2}} - \frac{b c d^2 (c^2 f^2 - g^2)^2 x \sqrt{d - c^2 dx^2}}{g^5 \sqrt{1 - c^2 x^2}} - \\
& \frac{b c^3 d^2 f x^2 \sqrt{d - c^2 dx^2}}{16 g^2 \sqrt{1 - c^2 x^2}} + \frac{b c^3 d^2 f (c^2 f^2 - 2 g^2) x^2 \sqrt{d - c^2 dx^2}}{4 g^4 \sqrt{1 - c^2 x^2}} + \frac{b c^3 d^2 x^3 \sqrt{d - c^2 dx^2}}{45 g \sqrt{1 - c^2 x^2}} - \frac{b c^3 d^2 (c^2 f^2 - 2 g^2) x^3 \sqrt{d - c^2 dx^2}}{9 g^3 \sqrt{1 - c^2 x^2}} + \\
& \frac{b c^5 d^2 f x^4 \sqrt{d - c^2 dx^2}}{16 g^2 \sqrt{1 - c^2 x^2}} - \frac{b c^5 d^2 x^5 \sqrt{d - c^2 dx^2}}{25 g \sqrt{1 - c^2 x^2}} + \frac{b d^2 (c^2 f^2 - g^2)^2 \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx]}{g^5} + \frac{c^2 d^2 f x \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])}{8 g^2} - \\
& \frac{c^2 d^2 f (c^2 f^2 - 2 g^2) x \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])}{2 g^4} - \frac{c^4 d^2 f x^3 \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])}{4 g^2} - \\
& \frac{d^2 (1 - c^2 x^2) \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])}{3 g} - \frac{d^2 (c^2 f^2 - 2 g^2) (1 - c^2 x^2) \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])}{3 g^3} + \\
& \frac{d^2 (1 - c^2 x^2)^2 \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])}{5 g} - \frac{c d^2 f \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])^2}{16 b g^2 \sqrt{1 - c^2 x^2}} - \frac{c d^2 f (c^2 f^2 - 2 g^2) \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])^2}{4 b g^4 \sqrt{1 - c^2 x^2}} + \\
& \frac{c d^2 (c^2 f^2 - g^2)^2 x \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])^2}{2 b g^5 \sqrt{1 - c^2 x^2}} + \frac{d^2 (c^2 f^2 - g^2)^3 \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])^2}{2 b c g^6 (f + g x) \sqrt{1 - c^2 x^2}} + \\
& \frac{d^2 (c^2 f^2 - g^2)^2 \sqrt{1 - c^2 x^2} \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])^2}{2 b c g^4 (f + g x)} - \frac{a d^2 (c^2 f^2 - g^2)^{5/2} \sqrt{d - c^2 dx^2} \operatorname{ArcTan}\left[\frac{g + c^2 f x}{\sqrt{c^2 f^2 - g^2} \sqrt{1 - c^2 x^2}}\right]}{g^6 \sqrt{1 - c^2 x^2}} + \\
& \frac{\pm b d^2 (c^2 f^2 - g^2)^{5/2} \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx] \operatorname{Log}\left[1 - \frac{\pm e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^6 \sqrt{1 - c^2 x^2}} - \frac{\pm b d^2 (c^2 f^2 - g^2)^{5/2} \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx] \operatorname{Log}\left[1 - \frac{\pm e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^6 \sqrt{1 - c^2 x^2}} + \\
& \frac{b d^2 (c^2 f^2 - g^2)^{5/2} \sqrt{d - c^2 dx^2} \operatorname{PolyLog}\left[2, \frac{\pm e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^6 \sqrt{1 - c^2 x^2}} - \frac{b d^2 (c^2 f^2 - g^2)^{5/2} \sqrt{d - c^2 dx^2} \operatorname{PolyLog}\left[2, \frac{\pm e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^6 \sqrt{1 - c^2 x^2}}
\end{aligned}$$

Result (type 4, 8113 leaves):

$$\sqrt{-d (-1 + c^2 x^2)} \left( \frac{a d^2 (15 c^4 f^4 - 35 c^2 f^2 g^2 + 23 g^4)}{15 g^5} - \frac{a c^2 d^2 f (4 c^2 f^2 - 9 g^2) x}{8 g^4} - \frac{a c^2 d^2 (-5 c^2 f^2 + 11 g^2) x^2}{15 g^3} - \frac{a c^4 d^2 f x^3}{4 g^2} + \frac{a c^4 d^2 x^4}{5 g} \right)$$

$$\begin{aligned}
& \frac{a c d^{5/2} f (8 c^4 f^4 - 20 c^2 f^2 g^2 + 15 g^4) \operatorname{ArcTan}\left[\frac{c x \sqrt{-d (-1+c^2 x^2)}}{\sqrt{d} (-1+c^2 x^2)}\right]}{8 g^6} + \frac{a d^{5/2} (-c^2 f^2 + g^2)^{5/2} \log[f + g x]}{g^6} - \\
& \frac{a d^{5/2} (-c^2 f^2 + g^2)^{5/2} \log[d g + c^2 d f x + \sqrt{d} \sqrt{-c^2 f^2 + g^2} \sqrt{-d (-1+c^2 x^2)}]}{g^6} + \\
& \frac{1}{2 g^2} b d^2 \sqrt{d (1-c^2 x^2)} \left( -\frac{2 c g x}{\sqrt{1-c^2 x^2}} + 2 g \operatorname{ArcSin}[c x] + \frac{c f \operatorname{ArcSin}[c x]^2}{\sqrt{1-c^2 x^2}} + \frac{1}{\sqrt{1-c^2 x^2}} 2 (-c f + g) (c f + g) \right. \\
& \left. \frac{\pi \operatorname{ArcTan}\left[\frac{g+c f \tan\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]}{\sqrt{c^2 f^2-g^2}}\right]}{\sqrt{c^2 f^2-g^2}} + \frac{1}{\sqrt{-c^2 f^2+g^2}} \left( 2 \operatorname{ArcCos}\left[-\frac{c f}{g}\right] \operatorname{ArcTanh}\left[\frac{(c f-g) \cot\left[\frac{1}{4} (\pi+2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2+g^2}}\right] + (\pi-2 \operatorname{ArcSin}[c x]) \right. \right. \\
& \left. \left. \operatorname{ArcTanh}\left[\frac{(c f+g) \tan\left[\frac{1}{4} (\pi+2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2+g^2}}\right] + \left( \operatorname{ArcCos}\left[-\frac{c f}{g}\right] + 2 i \operatorname{ArcTanh}\left[\frac{(c f-g) \cot\left[\frac{1}{4} (\pi+2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2+g^2}}\right] + \right. \right. \right. \\
& \left. \left. \left. \operatorname{ArcTanh}\left[\frac{(c f+g) \tan\left[\frac{1}{4} (\pi+2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2+g^2}}\right] \right) \right) \operatorname{Log}\left[\frac{e^{\frac{1}{4} i (\pi-2 \operatorname{ArcSin}[c x])} \sqrt{-c^2 f^2+g^2}}{\sqrt{2} \sqrt{g} \sqrt{c f+c g x}}\right] + \right. \\
& \left. \left( \operatorname{ArcCos}\left[-\frac{c f}{g}\right] - 2 i \operatorname{ArcTanh}\left[\frac{(c f-g) \cot\left[\frac{1}{4} (\pi+2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2+g^2}}\right] - 2 i \operatorname{ArcTanh}\left[\frac{(c f+g) \tan\left[\frac{1}{4} (\pi+2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2+g^2}}\right] \right) \right. \\
& \left. \operatorname{Log}\left[\frac{\left(\frac{1}{2}-\frac{i}{2}\right) e^{\frac{1}{2} i \operatorname{ArcSin}[c x]} \sqrt{-c^2 f^2+g^2}}{\sqrt{g} \sqrt{c f+c g x}}\right] - \left( \operatorname{ArcCos}\left[-\frac{c f}{g}\right] + 2 i \operatorname{ArcTanh}\left[\frac{(c f-g) \cot\left[\frac{1}{4} (\pi+2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2+g^2}}\right] \right) \right. \\
& \left. \operatorname{Log}\left[\frac{(c f+g) \left(-c f+g-i \sqrt{-c^2 f^2+g^2}\right) \left(1+i \cot\left[\frac{1}{4} (\pi+2 \operatorname{ArcSin}[c x])\right]\right)}{g \left(c f+g+\sqrt{-c^2 f^2+g^2} \cot\left[\frac{1}{4} (\pi+2 \operatorname{ArcSin}[c x])\right]\right)}\right] - \left( \operatorname{ArcCos}\left[-\frac{c f}{g}\right] - 2 i \right. \right. \\
& \left. \left. \operatorname{ArcTanh}\left[\frac{(c f-g) \cot\left[\frac{1}{4} (\pi+2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2+g^2}}\right]\right) \operatorname{Log}\left[\frac{(c f+g) \left(i c f-i g+\sqrt{-c^2 f^2+g^2}\right) \left(i+i \cot\left[\frac{1}{4} (\pi+2 \operatorname{ArcSin}[c x])\right]\right)}{g \left(c f+g+\sqrt{-c^2 f^2+g^2} \cot\left[\frac{1}{4} (\pi+2 \operatorname{ArcSin}[c x])\right]\right)}\right] + \right)
\end{aligned}$$

$$\begin{aligned}
& \pm \left( \text{PolyLog}[2, \frac{\left( c f - i \sqrt{-c^2 f^2 + g^2} \right) \left( c f + g - \sqrt{-c^2 f^2 + g^2} \right) \cot[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])]}{g \left( c f + g + \sqrt{-c^2 f^2 + g^2} \right) \cot[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])]}] - \text{PolyLog}[2, \right. \\
& \quad \left. \frac{\left( c f + i \sqrt{-c^2 f^2 + g^2} \right) \left( c f + g - \sqrt{-c^2 f^2 + g^2} \right) \cot[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])] \left( c f + g + \sqrt{-c^2 f^2 + g^2} \right) \cot[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])] \right)] \right) \Bigg) + \\
& 2 b d^2 \left( -\frac{1}{8 \sqrt{1 - c^2 x^2}} \sqrt{d (1 - c^2 x^2)} \left( \frac{\pi \text{ArcTan}[\frac{g + c f \tan[\frac{1}{2} \text{ArcSin}[c x]]}{\sqrt{c^2 f^2 - g^2}}]}{\sqrt{c^2 f^2 - g^2}} + \frac{1}{\sqrt{-c^2 f^2 + g^2}} \left( 2 \text{ArcCos}[-\frac{c f}{g}] \right. \right. \right. \\
& \quad \left. \left. \left. \text{ArcTanh}[\frac{(c f - g) \cot[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])] \sqrt{-c^2 f^2 + g^2}}{\sqrt{-c^2 f^2 + g^2}}] + (\pi - 2 \text{ArcSin}[c x]) \text{ArcTanh}[\frac{(c f + g) \tan[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])] \sqrt{-c^2 f^2 + g^2}}{\sqrt{-c^2 f^2 + g^2}}] + \right. \right. \right. \\
& \quad \left. \left. \left. \text{ArcCos}[-\frac{c f}{g}] + 2 i \left( \text{ArcTanh}[\frac{(c f - g) \cot[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])] \sqrt{-c^2 f^2 + g^2}}{\sqrt{-c^2 f^2 + g^2}}] + \text{ArcTanh}[\frac{(c f + g) \tan[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])] \sqrt{-c^2 f^2 + g^2}}{\sqrt{-c^2 f^2 + g^2}}] \right) \right) \right) \right. \\
& \quad \left. \text{Log}[\frac{e^{\frac{1}{4} i (\pi - 2 \text{ArcSin}[c x])} \sqrt{-c^2 f^2 + g^2}}{\sqrt{2} \sqrt{g} \sqrt{c f + c g x}}] + \right. \\
& \quad \left. \left( \text{ArcCos}[-\frac{c f}{g}] - 2 i \text{ArcTanh}[\frac{(c f - g) \cot[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])] \sqrt{-c^2 f^2 + g^2}}{\sqrt{-c^2 f^2 + g^2}}] - 2 i \text{ArcTanh}[\frac{(c f + g) \tan[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])] \sqrt{-c^2 f^2 + g^2}}{\sqrt{-c^2 f^2 + g^2}}] \right) \right. \\
& \quad \left. \text{Log}[\frac{\left(\frac{1}{2} - \frac{i}{2}\right) e^{\frac{1}{2} i \text{ArcSin}[c x]} \sqrt{-c^2 f^2 + g^2}}{\sqrt{g} \sqrt{c f + c g x}}] - \left( \text{ArcCos}[-\frac{c f}{g}] + 2 i \text{ArcTanh}[\frac{(c f - g) \cot[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])] \sqrt{-c^2 f^2 + g^2}}{\sqrt{-c^2 f^2 + g^2}}] \right) \right. \\
& \quad \left. \text{Log}[\frac{(c f + g) \left(-c f + g - i \sqrt{-c^2 f^2 + g^2}\right) \left(1 + i \cot[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])] \right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \right) \cot[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])]}] - \left( \text{ArcCos}[-\frac{c f}{g}] - 2 i \right. \right. \\
& \quad \left. \left. \text{ArcTanh}[\frac{(c f - g) \cot[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])] \sqrt{-c^2 f^2 + g^2}}{\sqrt{-c^2 f^2 + g^2}}] \right) \text{Log}[\frac{(c f + g) \left(i c f - i g + \sqrt{-c^2 f^2 + g^2}\right) \left(i + \cot[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])] \right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \right) \cot[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])]}] \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{\text{PolyLog}[2, \frac{(c f - i \sqrt{-c^2 f^2 + g^2}) (c f + g - \sqrt{-c^2 f^2 + g^2} \cot[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]}{g (c f + g + \sqrt{-c^2 f^2 + g^2} \cot[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]}]} - \text{PolyLog}[2, \\
& \frac{(c f + i \sqrt{-c^2 f^2 + g^2}) (c f + g - \sqrt{-c^2 f^2 + g^2} \cot[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]}{g (c f + g + \sqrt{-c^2 f^2 + g^2} \cot[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]} \Big) \Big] \Big) \Big] + \\
& \frac{1}{72 g^4 \sqrt{1 - c^2 x^2}} \sqrt{d (1 - c^2 x^2)} \left( -18 c g (-4 c^2 f^2 + g^2) x + 18 g (-4 c^2 f^2 + g^2) \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x] - 18 c f (2 c^2 f^2 - g^2) \operatorname{ArcSin}[c x]^2 + \right. \\
& 9 c f g^2 \cos[2 \operatorname{ArcSin}[c x]] + 6 g^3 \operatorname{ArcSin}[c x] \cos[3 \operatorname{ArcSin}[c x]] + 9 (8 c^4 f^4 - 8 c^2 f^2 g^2 + g^4) \\
& \left( \frac{\pi \operatorname{ArcTan}[\frac{g + c f \tan[\frac{1}{2} \operatorname{ArcSin}[c x]]}{\sqrt{c^2 f^2 - g^2}}]}{\sqrt{c^2 f^2 - g^2}} + \frac{1}{\sqrt{-c^2 f^2 + g^2}} \left( 2 \operatorname{ArcCos}[-\frac{c f}{g}] \operatorname{ArcTanh}[\frac{(c f - g) \cot[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]}{\sqrt{-c^2 f^2 + g^2}}] + (\pi - 2 \operatorname{ArcSin}[c x]) \right. \right. \\
& \left. \left. \operatorname{ArcTanh}[\frac{(c f + g) \tan[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]}{\sqrt{-c^2 f^2 + g^2}}] \right) + \left( \operatorname{ArcCos}[-\frac{c f}{g}] + 2 i \left( \operatorname{ArcTanh}[\frac{(c f - g) \cot[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]}{\sqrt{-c^2 f^2 + g^2}}] + \right. \right. \right. \\
& \left. \left. \left. \operatorname{ArcTanh}[\frac{(c f + g) \tan[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]}{\sqrt{-c^2 f^2 + g^2}}] \right) \right) \operatorname{Log}[\frac{e^{\frac{1}{4} i (\pi - 2 \operatorname{ArcSin}[c x])} \sqrt{-c^2 f^2 + g^2}}{\sqrt{2} \sqrt{g} \sqrt{c f + c g x}}] + \right. \\
& \left( \operatorname{ArcCos}[-\frac{c f}{g}] - 2 i \operatorname{ArcTanh}[\frac{(c f - g) \cot[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]}{\sqrt{-c^2 f^2 + g^2}}] - 2 i \operatorname{ArcTanh}[\frac{(c f + g) \tan[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]}{\sqrt{-c^2 f^2 + g^2}}] \right) \\
& \operatorname{Log}[\frac{\left(\frac{1}{2} - \frac{i}{2}\right) e^{\frac{1}{2} i \operatorname{ArcSin}[c x]} \sqrt{-c^2 f^2 + g^2}}{\sqrt{g} \sqrt{c f + c g x}}] - \left( \operatorname{ArcCos}[-\frac{c f}{g}] + 2 i \operatorname{ArcTanh}[\frac{(c f - g) \cot[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]}{\sqrt{-c^2 f^2 + g^2}}] \right) \operatorname{Log}[ \\
& \frac{(c f + g) \left(-c f + g - i \sqrt{-c^2 f^2 + g^2}\right) \left(1 + i \cot[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \cot[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])]\right)}] - \left( \operatorname{ArcCos}[-\frac{c f}{g}] - 2 i \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left( \text{ArcTanh} \left[ \frac{(c f - g) \cot \left[ \frac{1}{4} (\pi + 2 \arcsin[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \log \left[ \frac{(c f + g) \left( i c f - i g + \sqrt{-c^2 f^2 + g^2} \right) \left( i + \cot \left[ \frac{1}{4} (\pi + 2 \arcsin[c x]) \right] \right)}{g \left( c f + g + \sqrt{-c^2 f^2 + g^2} \right) \cot \left[ \frac{1}{4} (\pi + 2 \arcsin[c x]) \right]} \right] + \right. \\
& \left. i \left( \text{PolyLog}[2, \frac{(c f - i \sqrt{-c^2 f^2 + g^2}) (c f + g - \sqrt{-c^2 f^2 + g^2}) \cot \left[ \frac{1}{4} (\pi + 2 \arcsin[c x]) \right]}{g (c f + g + \sqrt{-c^2 f^2 + g^2}) \cot \left[ \frac{1}{4} (\pi + 2 \arcsin[c x]) \right]}] - \right. \right. \\
& \left. \left. \text{PolyLog}[2, \frac{(c f + i \sqrt{-c^2 f^2 + g^2}) (c f + g - \sqrt{-c^2 f^2 + g^2}) \cot \left[ \frac{1}{4} (\pi + 2 \arcsin[c x]) \right]}{g (c f + g + \sqrt{-c^2 f^2 + g^2}) \cot \left[ \frac{1}{4} (\pi + 2 \arcsin[c x]) \right]}] \right) \right) + \\
& \left. \left. \left. 18 c f g^2 \arcsin[c x] \sin[2 \arcsin[c x]] - 2 g^3 \sin[3 \arcsin[c x]] \right) \right] - b d^2 \right) \\
& \left( \frac{1}{32 g^2 \sqrt{1 - c^2 x^2}} \sqrt{d (1 - c^2 x^2)} \left( -2 c g x + 2 g \sqrt{1 - c^2 x^2} \arcsin[c x] + c f \arcsin[c x]^2 + (-2 c^2 f^2 + g^2) \right. \right. \\
& \left. \left. \frac{\pi \arctan \left[ \frac{g + c f \tan \left[ \frac{1}{2} \arcsin[c x] \right]}{\sqrt{c^2 f^2 - g^2}} \right]}{\sqrt{c^2 f^2 - g^2}} + \frac{1}{\sqrt{-c^2 f^2 + g^2}} \left( 2 \arccos \left[ -\frac{c f}{g} \right] \text{ArcTanh} \left[ \frac{(c f - g) \cot \left[ \frac{1}{4} (\pi + 2 \arcsin[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + (\pi - 2 \arcsin[c x]) \right. \right. \right. \\
& \left. \left. \left. \text{ArcTanh} \left[ \frac{(c f + g) \tan \left[ \frac{1}{4} (\pi + 2 \arcsin[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + \left( \arccos \left[ -\frac{c f}{g} \right] + 2 i \left( \text{ArcTanh} \left[ \frac{(c f - g) \cot \left[ \frac{1}{4} (\pi + 2 \arcsin[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + \right. \right. \right. \right. \\
& \left. \left. \left. \left. \text{ArcTanh} \left[ \frac{(c f + g) \tan \left[ \frac{1}{4} (\pi + 2 \arcsin[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \right) \log \left[ \frac{e^{\frac{1}{4} i (\pi - 2 \arcsin[c x])} \sqrt{-c^2 f^2 + g^2}}{\sqrt{2} \sqrt{g} \sqrt{c f + c g x}} \right] + \right. \\
& \left. \left. \left. \left. \left( \arccos \left[ -\frac{c f}{g} \right] - 2 i \text{ArcTanh} \left[ \frac{(c f - g) \cot \left[ \frac{1}{4} (\pi + 2 \arcsin[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] - 2 i \text{ArcTanh} \left[ \frac{(c f + g) \tan \left[ \frac{1}{4} (\pi + 2 \arcsin[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \text{Log} \left[ \frac{\left( \frac{1}{2} - \frac{i}{2} \right) e^{\frac{1}{2} i \text{ArcSin}[c x]} \sqrt{-c^2 f^2 + g^2}}{\sqrt{g} \sqrt{c f + c g x}} \right] - \left( \text{ArcCos} \left[ -\frac{c f}{g} \right] + 2 i \text{ArcTanh} \left[ \frac{(c f - g) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \text{Log} [ \\
& \frac{(c f + g) \left( -c f + g - i \sqrt{-c^2 f^2 + g^2} \right) \left( 1 + i \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right] \right)}{g \left( c f + g + \sqrt{-c^2 f^2 + g^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right] \right)} - \left( \text{ArcCos} \left[ -\frac{c f}{g} \right] - 2 i \right. \\
& \left. \text{ArcTanh} \left[ \frac{(c f - g) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \text{Log} \left[ \frac{(c f + g) \left( i c f - i g + \sqrt{-c^2 f^2 + g^2} \right) \left( i + \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right] \right)}{g \left( c f + g + \sqrt{-c^2 f^2 + g^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right] \right)} + \right. \\
& \left. i \left( \text{PolyLog} [2, \frac{(c f - i \sqrt{-c^2 f^2 + g^2}) (c f + g - \sqrt{-c^2 f^2 + g^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{g (c f + g + \sqrt{-c^2 f^2 + g^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right])}] - \right. \right. \\
& \left. \left. \text{PolyLog} [2, \frac{(c f + i \sqrt{-c^2 f^2 + g^2}) (c f + g - \sqrt{-c^2 f^2 + g^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{g (c f + g + \sqrt{-c^2 f^2 + g^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right])}] \right) \right) \right] - \\
& \frac{1}{16 \sqrt{1 - c^2 x^2}} \sqrt{d (1 - c^2 x^2)} \left( \frac{\pi \text{ArcTan} \left[ \frac{g + c f \text{Tan} \left[ \frac{1}{2} \text{ArcSin}[c x] \right]}{\sqrt{c^2 f^2 - g^2}} \right]}{\sqrt{c^2 f^2 - g^2}} + \frac{1}{\sqrt{-c^2 f^2 + g^2}} \left( 2 \text{ArcCos} \left[ -\frac{c f}{g} \right] \text{ArcTanh} \left[ \frac{(c f - g) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + \right. \right. \\
& \left. \left. (\pi - 2 \text{ArcSin}[c x]) \text{ArcTanh} \left[ \frac{(c f + g) \text{Tan} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + \right. \right. \\
& \left. \left. \left( \text{ArcCos} \left[ -\frac{c f}{g} \right] + 2 i \left( \text{ArcTanh} \left[ \frac{(c f - g) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + \text{ArcTanh} \left[ \frac{(c f + g) \text{Tan} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \right) \right) \\
& \text{Log} \left[ \frac{e^{\frac{1}{4} i (\pi - 2 \text{ArcSin}[c x])} \sqrt{-c^2 f^2 + g^2}}{\sqrt{2} \sqrt{g} \sqrt{c f + c g x}} \right] + \\
& \left( \text{ArcCos} \left[ -\frac{c f}{g} \right] - 2 i \text{ArcTanh} \left[ \frac{(c f - g) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] - 2 i \text{ArcTanh} \left[ \frac{(c f + g) \text{Tan} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right)
\end{aligned}$$

$$\begin{aligned}
& \text{Log} \left[ \frac{\left( \frac{1}{2} - \frac{i}{2} \right) e^{\frac{1}{2} i \text{ArcSin}[c x]} \sqrt{-c^2 f^2 + g^2}}{\sqrt{g} \sqrt{c f + c g x}} \right] - \left( \text{ArcCos} \left[ -\frac{c f}{g} \right] + 2 i \text{ArcTanh} \left[ \frac{(c f - g) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \\
& \text{Log} \left[ \frac{(c f + g) \left( -c f + g - i \sqrt{-c^2 f^2 + g^2} \right) \left( 1 + i \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right] \right)}{g \left( c f + g + \sqrt{-c^2 f^2 + g^2} \right) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]} \right] - \left( \text{ArcCos} \left[ -\frac{c f}{g} \right] - \right. \\
& \left. 2 i \text{ArcTanh} \left[ \frac{(c f - g) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \text{Log} \left[ \frac{(c f + g) \left( i c f - i g + \sqrt{-c^2 f^2 + g^2} \right) \left( i + \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right] \right)}{g \left( c f + g + \sqrt{-c^2 f^2 + g^2} \right) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]} \right] + \\
& i \left( \text{PolyLog} [2, \frac{(c f - i \sqrt{-c^2 f^2 + g^2}) (c f + g - \sqrt{-c^2 f^2 + g^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right])}{g (c f + g + \sqrt{-c^2 f^2 + g^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right])}] - \right. \\
& \left. \text{PolyLog} [2, \frac{(c f + i \sqrt{-c^2 f^2 + g^2}) (c f + g - \sqrt{-c^2 f^2 + g^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right])}{g (c f + g + \sqrt{-c^2 f^2 + g^2} \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right])}] \right) \right) + \\
& \frac{1}{144 g^4 \sqrt{1 - c^2 x^2}} \sqrt{d (1 - c^2 x^2)} \left( -18 c g (-4 c^2 f^2 + g^2) x + 18 g (-4 c^2 f^2 + g^2) \sqrt{1 - c^2 x^2} \text{ArcSin}[c x] - \right. \\
& 18 c f (2 c^2 f^2 - g^2) \text{ArcSin}[c x]^2 + 9 c f g^2 \cos[2 \text{ArcSin}[c x]] + \\
& 6 g^3 \text{ArcSin}[c x] \cos[3 \text{ArcSin}[c x]] + 9 (8 c^4 f^4 - 8 c^2 f^2 g^2 + g^4) \\
& \left. \left( \frac{\pi \text{ArcTan} \left[ \frac{g + c f \tan \left[ \frac{1}{2} \text{ArcSin}[c x] \right]}{\sqrt{c^2 f^2 - g^2}} \right]}{\sqrt{c^2 f^2 - g^2}} + \frac{1}{\sqrt{-c^2 f^2 + g^2}} \left( 2 \text{ArcCos} \left[ -\frac{c f}{g} \right] \text{ArcTanh} \left[ \frac{(c f - g) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + (\pi - 2 \text{ArcSin}[c x]) \right. \right. \\
& \left. \left. \text{ArcTanh} \left[ \frac{(c f + g) \tan \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + \left( \text{ArcCos} \left[ -\frac{c f}{g} \right] + 2 i \left( \text{ArcTanh} \left[ \frac{(c f - g) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + \right. \right. \right. \right. \right)
\end{aligned}$$



$$\begin{aligned}
& \frac{16 c^5 f^5 \operatorname{ArcSin}[c x]^2}{g^6} - \frac{16 c^3 f^3 \operatorname{ArcSin}[c x]^2}{g^4} + \\
& \frac{3 c f \operatorname{ArcSin}[c x]^2}{g^2} + \frac{2 c f (-2 c^2 f^2 + g^2) \cos[2 \operatorname{ArcSin}[c x]]}{g^4} - \\
& \frac{8 c^2 f^2 \operatorname{ArcSin}[c x] \cos[3 \operatorname{ArcSin}[c x]]}{3 g^3} + \\
& \frac{2 \operatorname{ArcSin}[c x] \cos[3 \operatorname{ArcSin}[c x]]}{3 g} + \\
& \frac{c f \cos[4 \operatorname{ArcSin}[c x]]}{4 g^2} + \frac{2 \operatorname{ArcSin}[c x] \cos[5 \operatorname{ArcSin}[c x]]}{5 g} + \\
& \frac{1}{g^6} (-2 c^2 f^2 + g^2) (16 c^4 f^4 - 16 c^2 f^2 g^2 + g^4) \\
& \left( \frac{\pi \operatorname{ArcTan}\left[\frac{g+c f \tan\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]}{\sqrt{c^2 f^2 - g^2}}\right]}{\sqrt{c^2 f^2 - g^2}} + \frac{1}{\sqrt{-c^2 f^2 + g^2}} \right) \left( 2 \operatorname{ArcCos}\left[-\frac{c f}{g}\right] \operatorname{ArcTanh}\left[\frac{(c f - g) \cot\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2 + g^2}}\right] + (\pi - 2 \operatorname{ArcSin}[c x]) \right. \\
& \left. \operatorname{ArcTanh}\left[\frac{(c f + g) \tan\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2 + g^2}}\right] + \left( \operatorname{ArcCos}\left[-\frac{c f}{g}\right] + 2 \operatorname{i} \operatorname{ArcTanh}\left[\frac{(c f - g) \cot\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2 + g^2}}\right] + \right. \right. \\
& \left. \left. \operatorname{ArcTanh}\left[\frac{(c f + g) \tan\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2 + g^2}}\right] \right) \operatorname{Log}\left[\frac{e^{\frac{1}{4} i (\pi - 2 \operatorname{ArcSin}[c x])} \sqrt{-c^2 f^2 + g^2}}{\sqrt{2} \sqrt{g} \sqrt{c f + c g x}}\right] + \right. \\
& \left( \operatorname{ArcCos}\left[-\frac{c f}{g}\right] - 2 \operatorname{i} \operatorname{ArcTanh}\left[\frac{(c f - g) \cot\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2 + g^2}}\right] - 2 \operatorname{i} \operatorname{ArcTanh}\left[\frac{(c f + g) \tan\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2 + g^2}}\right] \right) \\
& \operatorname{Log}\left[\frac{\left(\frac{1}{2} - \frac{i}{2}\right) e^{\frac{1}{2} i \operatorname{ArcSin}[c x]} \sqrt{-c^2 f^2 + g^2}}{\sqrt{g} \sqrt{c f + c g x}}\right] - \left( \operatorname{ArcCos}\left[-\frac{c f}{g}\right] + 2 \operatorname{i} \operatorname{ArcTanh}\left[\frac{(c f - g) \cot\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2 + g^2}}\right] \right) \\
& \operatorname{Log}\left[\frac{(c f + g) \left(-c f + g - i \sqrt{-c^2 f^2 + g^2}\right) \left(1 + i \cot\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \cot\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]\right)}\right] - \left( \operatorname{ArcCos}\left[-\frac{c f}{g}\right] - 2 \operatorname{i} \operatorname{ArcTanh}\left[\frac{(c f - g) \cot\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{-c^2 f^2 + g^2}}\right] \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{\left( c f - g \right) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \operatorname{Log} \left[ \frac{(c f + g) \left( i c f - i g + \sqrt{-c^2 f^2 + g^2} \right) \left( i + \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right] \right)}{g \left( c f + g + \sqrt{-c^2 f^2 + g^2} \right) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]} \right] + i \\
& \left. \left( \operatorname{PolyLog} [2, \frac{(c f - i \sqrt{-c^2 f^2 + g^2}) (c f + g - \sqrt{-c^2 f^2 + g^2}) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{g (c f + g + \sqrt{-c^2 f^2 + g^2}) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}] - \right. \right. \\
& \left. \left. \operatorname{PolyLog} [2, \frac{(c f + i \sqrt{-c^2 f^2 + g^2}) (c f + g - \sqrt{-c^2 f^2 + g^2}) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{g (c f + g + \sqrt{-c^2 f^2 + g^2}) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}] \right) \right) - \\
& \frac{8 c^3 f^3 \operatorname{ArcSin}[c x] \operatorname{Sin}[2 \operatorname{ArcSin}[c x]]}{g^4} + \frac{4 c f \operatorname{ArcSin}[c x] \operatorname{Sin}[2 \operatorname{ArcSin}[c x]]}{g^2} + \frac{8 c^2 f^2 \operatorname{Sin}[3 \operatorname{ArcSin}[c x]]}{9 g^3} - \\
& \frac{2 \operatorname{Sin}[3 \operatorname{ArcSin}[c x]]}{9 g} + \frac{c f \operatorname{ArcSin}[c x] \operatorname{Sin}[4 \operatorname{ArcSin}[c x]]}{g^2} - \\
& \left. \frac{2 \operatorname{Sin}[5 \operatorname{ArcSin}[c x]]}{25 g} \right)
\end{aligned}$$

**Problem 47:** Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{(f + g x) \sqrt{d - c^2 d x^2}} dx$$

Optimal (type 4, 380 leaves, 10 steps):

$$\begin{aligned}
& \frac{i \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Log} \left[ 1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}} \right] + i \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Log} \left[ 1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}} \right]}{\sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 d x^2}} - \\
& \frac{b \sqrt{1 - c^2 x^2} \operatorname{PolyLog} [2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}] + b \sqrt{1 - c^2 x^2} \operatorname{PolyLog} [2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}]}{\sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 d x^2}}
\end{aligned}$$

Result (type 4, 1090 leaves):

$$\begin{aligned}
& \frac{a \operatorname{Log}[f + g x]}{\sqrt{d} \sqrt{-c^2 f^2 + g^2}} - \frac{a \operatorname{Log}[d (g + c^2 f x) + \sqrt{d} \sqrt{-c^2 f^2 + g^2} \sqrt{d - c^2 d x^2}]}{\sqrt{d} \sqrt{-c^2 f^2 + g^2}} + \\
& \frac{1}{\sqrt{d - c^2 d x^2}} b \sqrt{1 - c^2 x^2} \left( \frac{\pi \operatorname{ArcTan}\left[ \frac{g+c f \operatorname{Tan}\left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]}{\sqrt{c^2 f^2 - g^2}} \right]}{\sqrt{c^2 f^2 - g^2}} + \frac{1}{\sqrt{-c^2 f^2 + g^2}} \left( 2 \operatorname{ArcCos}\left[ -\frac{c f}{g} \right] \operatorname{ArcTanh}\left[ \frac{(c f - g) \operatorname{Cot}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + \right. \right. \\
& (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{ArcTanh}\left[ \frac{(c f + g) \operatorname{Tan}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + \left( \operatorname{ArcCos}\left[ -\frac{c f}{g} \right] + 2 i \operatorname{ArcTanh}\left[ \frac{(c f - g) \operatorname{Cot}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + \operatorname{ArcTanh}\left[ \frac{(c f + g) \operatorname{Tan}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \operatorname{Log}\left[ \frac{e^{\frac{1}{4} i (\pi - 2 \operatorname{ArcSin}[c x])} \sqrt{-c^2 f^2 + g^2}}{\sqrt{2} \sqrt{g} \sqrt{c (f + g x)}} \right] + \\
& \left. \left( \operatorname{ArcCos}\left[ -\frac{c f}{g} \right] - 2 i \operatorname{ArcTanh}\left[ \frac{(c f - g) \operatorname{Cot}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] - 2 i \operatorname{ArcTanh}\left[ \frac{(c f + g) \operatorname{Tan}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \right. \\
& \operatorname{Log}\left[ \frac{\left(\frac{1}{2} - \frac{i}{2}\right) e^{\frac{1}{2} i \operatorname{ArcSin}[c x]} \sqrt{-c^2 f^2 + g^2}}{\sqrt{g} \sqrt{c (f + g x)}} \right] - \left( \operatorname{ArcCos}\left[ -\frac{c f}{g} \right] + 2 i \operatorname{ArcTanh}\left[ \frac{(c f - g) \operatorname{Cot}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \\
& \operatorname{Log}\left[ \frac{(c f + g) \left(-c f + g - i \sqrt{-c^2 f^2 + g^2}\right) \left(1 + i \operatorname{Cot}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2}\right) \operatorname{Cot}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]} \right] - \left( \operatorname{ArcCos}\left[ -\frac{c f}{g} \right] - \right. \\
& \left. 2 i \operatorname{ArcTanh}\left[ \frac{(c f - g) \operatorname{Cot}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \operatorname{Log}\left[ \frac{(c f + g) \left(i c f - i g + \sqrt{-c^2 f^2 + g^2}\right) \left(i + \operatorname{Cot}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2}\right) \operatorname{Cot}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]} \right] + \\
& i \left( \operatorname{PolyLog}\left[ 2, \frac{\left(c f - i \sqrt{-c^2 f^2 + g^2}\right) \left(c f + g - \sqrt{-c^2 f^2 + g^2}\right) \operatorname{Cot}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2}\right) \operatorname{Cot}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]} \right] - \right. \\
& \left. \operatorname{PolyLog}\left[ 2, \frac{\left(c f + i \sqrt{-c^2 f^2 + g^2}\right) \left(c f + g - \sqrt{-c^2 f^2 + g^2}\right) \operatorname{Cot}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2}\right) \operatorname{Cot}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]} \right] \right)
\end{aligned}$$

### Problem 48: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{(f + g x)^2 \sqrt{d - c^2 d x^2}} dx$$

Optimal (type 4, 507 leaves, 13 steps):

$$\begin{aligned} & \frac{g (1 - c^2 x^2) (a + b \operatorname{ArcSin}[c x])}{(c^2 f^2 - g^2) (f + g x) \sqrt{d - c^2 d x^2}} - \frac{\frac{i c^2 f \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{(c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2}} + \\ & \frac{i c^2 f \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{(c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2}} - \frac{b c \sqrt{1 - c^2 x^2} \operatorname{Log}[f + g x]}{(c^2 f^2 - g^2) \sqrt{d - c^2 d x^2}} - \\ & \frac{b c^2 f \sqrt{1 - c^2 x^2} \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{(c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2}} + \frac{b c^2 f \sqrt{1 - c^2 x^2} \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{(c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2}} \end{aligned}$$

Result (type 4, 1414 leaves):

$$\begin{aligned} & -\frac{a g \sqrt{-d (-1 + c^2 x^2)}}{d (-c^2 f^2 + g^2) (f + g x)} + \frac{a c^2 f \operatorname{Log}[f + g x]}{\sqrt{d} (c f - g) (c f + g) \sqrt{-c^2 f^2 + g^2}} - \frac{a c^2 f \operatorname{Log}\left[d g + c^2 d f x + \sqrt{d} \sqrt{-c^2 f^2 + g^2} \sqrt{-d (-1 + c^2 x^2)}\right]}{\sqrt{d} (c f - g) (c f + g) \sqrt{-c^2 f^2 + g^2}} + \\ & b c \left( \frac{\frac{g (1 - c^2 x^2) \operatorname{ArcSin}[c x]}{(c f - g) (c f + g) (c f + c g x) \sqrt{d (1 - c^2 x^2)}} - \frac{\sqrt{1 - c^2 x^2} \operatorname{Log}\left[1 + \frac{g x}{f}\right]}{(c^2 f^2 - g^2) \sqrt{d (1 - c^2 x^2)}} + \frac{1}{(c^2 f^2 - g^2) \sqrt{d (1 - c^2 x^2)}} \right. \\ & \left. c f \sqrt{1 - c^2 x^2} \left( \frac{\pi \operatorname{ArcTan}\left[\frac{g + c f \operatorname{Tan}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]}{\sqrt{c^2 f^2 - g^2}}\right]}{\sqrt{c^2 f^2 - g^2}} + \frac{1}{\sqrt{-c^2 f^2 + g^2}} \right) \right. \\ & \left. 2 \operatorname{ArcCos}\left[-\frac{c f}{g}\right] \operatorname{ArcTanh}\left[\frac{(-c f + g) \operatorname{Tan}\left[\frac{1}{2} \left(\frac{\pi}{2} - \operatorname{ArcSin}[c x]\right)\right]}{\sqrt{-c^2 f^2 + g^2}}\right] + \left( \operatorname{ArcCos}\left[-\frac{c f}{g}\right] - 2 \frac{i}{2} \right) \right. \\ & \left. \left. \operatorname{ArcTanh}\left[\frac{(-c f + g) \operatorname{Tan}\left[\frac{1}{2} \left(\frac{\pi}{2} - \operatorname{ArcSin}[c x]\right)\right]}{\sqrt{-c^2 f^2 + g^2}}\right] \right) \operatorname{Log}\left[\frac{e^{-\frac{1}{2} i \left(\frac{\pi}{2} - \operatorname{ArcSin}[c x]\right)} \sqrt{-c^2 f^2 + g^2}}{\sqrt{2} \sqrt{g} \sqrt{c f + c g x}}\right] + \right. \end{aligned}$$

$$\begin{aligned}
& \left( \operatorname{ArcCos}\left[-\frac{c f}{g}\right] + 2 \operatorname{i} \left( \operatorname{ArcTanh}\left[\frac{(c f + g) \operatorname{Cot}\left[\frac{1}{2} \left(\frac{\pi}{2} - \operatorname{ArcSin}[c x]\right)\right]}{\sqrt{-c^2 f^2 + g^2}}\right] - \operatorname{ArcTanh}\left[\frac{(-c f + g) \operatorname{Tan}\left[\frac{1}{2} \left(\frac{\pi}{2} - \operatorname{ArcSin}[c x]\right)\right]}{\sqrt{-c^2 f^2 + g^2}}\right] \right) \right) \\
& \operatorname{Log}\left[\frac{e^{\frac{1}{2} \operatorname{i} \left(\frac{\pi}{2} - \operatorname{ArcSin}[c x]\right)} \sqrt{-c^2 f^2 + g^2}}{\sqrt{2} \sqrt{g} \sqrt{c f + c g x}}\right] - \left( \operatorname{ArcCos}\left[-\frac{c f}{g}\right] + 2 \operatorname{i} \operatorname{ArcTanh}\left[\frac{(-c f + g) \operatorname{Tan}\left[\frac{1}{2} \left(\frac{\pi}{2} - \operatorname{ArcSin}[c x]\right)\right]}{\sqrt{-c^2 f^2 + g^2}}\right] \right) \\
& \operatorname{Log}\left[1 - \frac{\left(c f - \operatorname{i} \sqrt{-c^2 f^2 + g^2}\right) \left(c f + g - \sqrt{-c^2 f^2 + g^2} \operatorname{Tan}\left[\frac{1}{2} \left(\frac{\pi}{2} - \operatorname{ArcSin}[c x]\right)\right]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \operatorname{Tan}\left[\frac{1}{2} \left(\frac{\pi}{2} - \operatorname{ArcSin}[c x]\right)\right]\right)}\right] + \left( -\operatorname{ArcCos}\left[-\frac{c f}{g}\right] + 2 \operatorname{i} \operatorname{ArcTanh}\left[\frac{(-c f + g) \operatorname{Tan}\left[\frac{1}{2} \left(\frac{\pi}{2} - \operatorname{ArcSin}[c x]\right)\right]}{\sqrt{-c^2 f^2 + g^2}}\right] \right) \operatorname{Log}\left[1 - \frac{\left(c f + \operatorname{i} \sqrt{-c^2 f^2 + g^2}\right) \left(c f + g - \sqrt{-c^2 f^2 + g^2} \operatorname{Tan}\left[\frac{1}{2} \left(\frac{\pi}{2} - \operatorname{ArcSin}[c x]\right)\right]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \operatorname{Tan}\left[\frac{1}{2} \left(\frac{\pi}{2} - \operatorname{ArcSin}[c x]\right)\right]\right)}\right] + \\
& \operatorname{i} \left( \operatorname{PolyLog}\left[2, \frac{\left(c f - \operatorname{i} \sqrt{-c^2 f^2 + g^2}\right) \left(c f + g - \sqrt{-c^2 f^2 + g^2} \operatorname{Tan}\left[\frac{1}{2} \left(\frac{\pi}{2} - \operatorname{ArcSin}[c x]\right)\right]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \operatorname{Tan}\left[\frac{1}{2} \left(\frac{\pi}{2} - \operatorname{ArcSin}[c x]\right)\right]\right)}\right] - \operatorname{PolyLog}\left[2, \frac{\left(c f + \operatorname{i} \sqrt{-c^2 f^2 + g^2}\right) \left(c f + g - \sqrt{-c^2 f^2 + g^2} \operatorname{Tan}\left[\frac{1}{2} \left(\frac{\pi}{2} - \operatorname{ArcSin}[c x]\right)\right]\right)}{g \left(c f + g + \sqrt{-c^2 f^2 + g^2} \operatorname{Tan}\left[\frac{1}{2} \left(\frac{\pi}{2} - \operatorname{ArcSin}[c x]\right)\right]\right)}\right] \right)
\end{aligned}$$

**Problem 51: Result unnecessarily involves higher level functions.**

$$\int \frac{(f + g x) (a + b \operatorname{ArcSin}[c x])}{(d - c^2 d x^2)^{3/2}} dx$$

Optimal (type 3, 144 leaves, 6 steps):

$$\begin{aligned}
& \frac{(g + c^2 f x) (a + b \operatorname{ArcSin}[c x])}{c^2 d \sqrt{d - c^2 d x^2}} + \frac{b (c f + g) \sqrt{1 - c^2 x^2} \operatorname{Log}[1 - c x]}{2 c^2 d \sqrt{d - c^2 d x^2}} + \frac{b (c f - g) \sqrt{1 - c^2 x^2} \operatorname{Log}[1 + c x]}{2 c^2 d \sqrt{d - c^2 d x^2}}
\end{aligned}$$

Result (type 4, 147 leaves):

$$\frac{1}{2 (-c^2)^{3/2} d^2 (-1 + c^2 x^2)} \sqrt{d - c^2 d x^2} \\ \left( 2 i b c g \sqrt{1 - c^2 x^2} \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \sqrt{-c^2} x \right], 1 \right] + \sqrt{-c^2} \left( 2 a (g + c^2 f x) + 2 b (g + c^2 f x) \operatorname{ArcSin}[c x] + b c f \sqrt{1 - c^2 x^2} \operatorname{Log}\left[ -1 + c^2 x^2 \right] \right) \right)$$

Problem 52: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcSin}[c x]}{(f + g x) (d - c^2 d x^2)^{3/2}} dx$$

Optimal (type 4, 654 leaves, 20 steps):

$$\begin{aligned} & -\frac{\sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Cot}\left[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]\right]}{2 d (c f - g) \sqrt{d - c^2 d x^2}} + \frac{\frac{i g^2 \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2}} - \\ & \frac{i g^2 \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2}} + \frac{b \sqrt{1 - c^2 x^2} \operatorname{Log}\left[\cos\left[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]\right]\right]}{d (c f + g) \sqrt{d - c^2 d x^2}} + \frac{b \sqrt{1 - c^2 x^2} \operatorname{Log}\left[\sin\left[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]\right]\right]}{d (c f - g) \sqrt{d - c^2 d x^2}} + \\ & \frac{b g^2 \sqrt{1 - c^2 x^2} \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2}} - \frac{b g^2 \sqrt{1 - c^2 x^2} \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2}} + \frac{\sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Tan}\left[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]\right]}{2 d (c f + g) \sqrt{d - c^2 d x^2}} \end{aligned}$$

Result (type 4, 1637 leaves):

$$\begin{aligned} & \frac{(-a g + a c^2 f x) \sqrt{-d (-1 + c^2 x^2)}}{d^2 (-c^2 f^2 + g^2) (-1 + c^2 x^2)} + \frac{a g^2 \operatorname{Log}[f + g x]}{d^{3/2} (-c f + g) (c f + g) \sqrt{-c^2 f^2 + g^2}} - \\ & \frac{a g^2 \operatorname{Log}\left[d g + c^2 d f x + \sqrt{d} \sqrt{-c^2 f^2 + g^2} \sqrt{-d (-1 + c^2 x^2)}\right]}{d^{3/2} (-c f + g) (c f + g) \sqrt{-c^2 f^2 + g^2}} - \frac{1}{d} b \left( -\frac{g \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x]}{(-c^2 f^2 + g^2) \sqrt{d (1 - c^2 x^2)}} - \right. \\ & \left. \frac{\sqrt{1 - c^2 x^2} \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right]}{(c f + g) \sqrt{d (1 - c^2 x^2)}} - \frac{\sqrt{1 - c^2 x^2} \operatorname{Log}\left[\cos\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \sin\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right]\right]}{(c f - g) \sqrt{d (1 - c^2 x^2)}} \right) \end{aligned}$$



$$\left. \left( \frac{\left( c f + g \pm \sqrt{-c^2 f^2 + g^2} \right) \left( c f + g - \sqrt{-c^2 f^2 + g^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)}{g \left( c f + g + \sqrt{-c^2 f^2 + g^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)} \right) - \right. \\ \left. \frac{\sqrt{1 - c^2 x^2} \text{ArcSin}[c x] \sin \left[ \frac{1}{2} \text{ArcSin}[c x] \right]}{(c f + g) \sqrt{d (1 - c^2 x^2)} \left( \cos \left[ \frac{1}{2} \text{ArcSin}[c x] \right] - \sin \left[ \frac{1}{2} \text{ArcSin}[c x] \right] \right)} - \frac{\sqrt{1 - c^2 x^2} \text{ArcSin}[c x] \sin \left[ \frac{1}{2} \text{ArcSin}[c x] \right]}{(c f - g) \sqrt{d (1 - c^2 x^2)} \left( \cos \left[ \frac{1}{2} \text{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \text{ArcSin}[c x] \right] \right)} \right)$$

**Problem 54: Result unnecessarily involves higher level functions.**

$$\int \frac{(f + g x)^3 (a + b \text{ArcSin}[c x])}{(d - c^2 d x^2)^{5/2}} dx$$

Optimal (type 3, 410 leaves, 10 steps):

$$-\frac{b (f + g x) (c^2 f^2 + g^2 + 2 c^2 f g x)}{6 c^3 d^2 \sqrt{1 - c^2 x^2} \sqrt{d - c^2 d x^2}} + \frac{2 (c f - g) (c f + g) (g + c^2 f x) (a + b \text{ArcSin}[c x])}{3 c^4 d^2 \sqrt{d - c^2 d x^2}} + \\ \frac{(g + c^2 f x) (f + g x)^2 (a + b \text{ArcSin}[c x])}{3 c^2 d^2 (1 - c^2 x^2) \sqrt{d - c^2 d x^2}} - \frac{b (c f - g) (c f + g)^2 \sqrt{1 - c^2 x^2} \log[1 - c x]}{3 c^4 d^2 \sqrt{d - c^2 d x^2}} - \\ \frac{b g (c f + g)^2 \sqrt{1 - c^2 x^2} \log[1 - c x]}{12 c^4 d^2 \sqrt{d - c^2 d x^2}} + \frac{b (c f - g)^2 g \sqrt{1 - c^2 x^2} \log[1 + c x]}{12 c^4 d^2 \sqrt{d - c^2 d x^2}} + \frac{b (c f - g)^2 (c f + g) \sqrt{1 - c^2 x^2} \log[1 + c x]}{3 c^4 d^2 \sqrt{d - c^2 d x^2}}$$

Result (type 4, 366 leaves):

$$\frac{1}{6 c^4 \sqrt{-c^2} d^3 (-1 + c^2 x^2)^2} \\ \sqrt{d - c^2 d x^2} \left( \pm b c g (3 c^2 f^2 - 5 g^2) (1 - c^2 x^2)^{3/2} \text{EllipticF}[\pm \text{ArcSinh}[\sqrt{-c^2} x], 1] - \sqrt{-c^2} \left( -6 a c^2 f^2 g + 4 a g^3 - 6 a c^4 f^3 x - 6 a c^2 g^3 x^2 + 4 a c^6 f^3 x^3 - 6 a c^4 f g^2 x^3 + b c^3 f^3 \sqrt{1 - c^2 x^2} + 3 b c f g^2 \sqrt{1 - c^2 x^2} + 3 b c^3 f^2 g x \sqrt{1 - c^2 x^2} + b c g^3 x \sqrt{1 - c^2 x^2} + 2 b (2 g^3 + 2 c^6 f^3 x^3 - 3 c^2 g (f^2 + g^2 x^2) - 3 c^4 f x (f^2 + g^2 x^2)) \text{ArcSin}[c x] - b c f (2 c^2 f^2 - 3 g^2) (1 - c^2 x^2)^{3/2} \log[-1 + c^2 x^2] \right) \right)$$

### Problem 55: Result unnecessarily involves higher level functions.

$$\int \frac{(f + g x)^2 (a + b \operatorname{ArcSin}[c x])}{(d - c^2 d x^2)^{5/2}} dx$$

Optimal (type 3, 271 leaves, 10 steps):

$$\begin{aligned} & -\frac{b x (2 f g + (c^2 f^2 + g^2) x)}{6 c d^2 \sqrt{1 - c^2 x^2} \sqrt{d - c^2 d x^2}} + \frac{2 f (g + c^2 f x) (a + b \operatorname{ArcSin}[c x])}{3 c^2 d^2 \sqrt{d - c^2 d x^2}} + \frac{x (f + g x)^2 (a + b \operatorname{ArcSin}[c x])}{3 d^2 (1 - c^2 x^2) \sqrt{d - c^2 d x^2}} + \\ & \frac{b (2 c f - g) (c f + g) \sqrt{1 - c^2 x^2} \operatorname{Log}[1 - c x]}{6 c^3 d^2 \sqrt{d - c^2 d x^2}} + \frac{b (c f - g) (2 c f + g) \sqrt{1 - c^2 x^2} \operatorname{Log}[1 + c x]}{6 c^3 d^2 \sqrt{d - c^2 d x^2}} \end{aligned}$$

Result (type 4, 285 leaves):

$$\begin{aligned} & \frac{1}{6 (-c^2)^{5/2} d^3 (-1 + c^2 x^2)^2} c \sqrt{d - c^2 d x^2} \left( 2 \pm b c^2 f g (1 - c^2 x^2)^{3/2} \operatorname{EllipticF}[\pm \operatorname{ArcSinh}[\sqrt{-c^2} x], 1] - \right. \\ & \sqrt{-c^2} \left( -4 a c f g - 6 a c^3 f^2 x + 4 a c^5 f^2 x^3 - 2 a c^3 g^2 x^3 + b c^2 f^2 \sqrt{1 - c^2 x^2} + b g^2 \sqrt{1 - c^2 x^2} + 2 b c^2 f g x \sqrt{1 - c^2 x^2} + \right. \\ & \left. \left. 2 b c (-2 f g - c^2 g^2 x^3 + c^2 f^2 x (-3 + 2 c^2 x^2)) \operatorname{ArcSin}[c x] - b (2 c^2 f^2 - g^2) (1 - c^2 x^2)^{3/2} \operatorname{Log}[-1 + c^2 x^2] \right) \right) \end{aligned}$$

### Problem 56: Result unnecessarily involves higher level functions.

$$\int \frac{(f + g x) (a + b \operatorname{ArcSin}[c x])}{(d - c^2 d x^2)^{5/2}} dx$$

Optimal (type 3, 228 leaves, 6 steps):

$$\begin{aligned} & -\frac{b (f + g x)}{6 c d^2 \sqrt{1 - c^2 x^2} \sqrt{d - c^2 d x^2}} + \frac{2 f x (a + b \operatorname{ArcSin}[c x])}{3 d^2 \sqrt{d - c^2 d x^2}} + \\ & \frac{(g + c^2 f x) (a + b \operatorname{ArcSin}[c x])}{3 c^2 d^2 (1 - c^2 x^2) \sqrt{d - c^2 d x^2}} - \frac{b g \sqrt{1 - c^2 x^2} \operatorname{ArcTanh}[c x]}{6 c^2 d^2 \sqrt{d - c^2 d x^2}} + \frac{b f \sqrt{1 - c^2 x^2} \operatorname{Log}[1 - c^2 x^2]}{3 c d^2 \sqrt{d - c^2 d x^2}} \end{aligned}$$

Result (type 4, 208 leaves):

$$\begin{aligned} & - \left( \left( \sqrt{d - c^2 d x^2} \left( \pm b c g (1 - c^2 x^2)^{3/2} \operatorname{EllipticF}[\pm \operatorname{ArcSinh}[\sqrt{-c^2} x], 1] + \sqrt{-c^2} \left( 2 a g + 6 a c^2 f x - 4 a c^4 f x^3 - b c f \sqrt{1 - c^2 x^2} - b c g x \sqrt{1 - c^2 x^2} + \right. \right. \right. \right. \right. \\ & \left. \left. \left. \left. \left. \left. 2 b (g + c^2 f x (3 - 2 c^2 x^2)) \operatorname{ArcSin}[c x] + 2 b c f (1 - c^2 x^2)^{3/2} \operatorname{Log}[-1 + c^2 x^2] \right) \right) \right) \right) / \left( 6 (-c^2)^{3/2} d^3 (-1 + c^2 x^2)^2 \right) \right) \end{aligned}$$

## Problem 61: Unable to integrate problem.

$$\int \frac{\sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])^2}{f + gx} dx$$

Optimal (type 4, 1442 leaves, 38 steps):

$$\begin{aligned} & \frac{a^2 \sqrt{d - c^2 dx^2}}{g} - \frac{2 b^2 \sqrt{d - c^2 dx^2}}{g} - \frac{2 a b c x \sqrt{d - c^2 dx^2}}{g \sqrt{1 - c^2 x^2}} + \frac{2 a b \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx]}{g} - \frac{2 b^2 c x \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx]}{g \sqrt{1 - c^2 x^2}} + \\ & \frac{b^2 \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx]^2}{g} + \frac{c x \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])^3}{3 b g \sqrt{1 - c^2 x^2}} - \frac{\left(1 - \frac{c^2 f^2}{g^2}\right) \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])^3}{3 b c (f + g x) \sqrt{1 - c^2 x^2}} + \\ & \frac{\sqrt{1 - c^2 x^2} \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])^3}{3 b c (f + g x)} - \frac{a^2 \sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 dx^2} \operatorname{ArcTan}\left[\frac{g + c^2 f x}{\sqrt{c^2 f^2 - g^2} \sqrt{1 - c^2 x^2}}\right]}{g^2 \sqrt{1 - c^2 x^2}} + \\ & \frac{2 i a b \sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx] \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^2 \sqrt{1 - c^2 x^2}} + \frac{i b^2 \sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx]^2 \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^2 \sqrt{1 - c^2 x^2}} - \\ & \frac{2 i a b \sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx] \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^2 \sqrt{1 - c^2 x^2}} - \frac{i b^2 \sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx]^2 \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^2 \sqrt{1 - c^2 x^2}} + \\ & \frac{2 a b \sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 dx^2} \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^2 \sqrt{1 - c^2 x^2}} + \frac{2 b^2 \sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx] \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^2 \sqrt{1 - c^2 x^2}} - \\ & \frac{2 a b \sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 dx^2} \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^2 \sqrt{1 - c^2 x^2}} - \frac{2 b^2 \sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx] \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^2 \sqrt{1 - c^2 x^2}} + \\ & \frac{2 i b^2 \sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 dx^2} \operatorname{PolyLog}\left[3, \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^2 \sqrt{1 - c^2 x^2}} - \frac{2 i b^2 \sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 dx^2} \operatorname{PolyLog}\left[3, \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^2 \sqrt{1 - c^2 x^2}} \end{aligned}$$

Result (type 8, 35 leaves):

$$\int \frac{\sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])^2}{f + gx} dx$$

**Problem 65: Unable to integrate problem.**

$$\int \frac{(d - c^2 dx^2)^{3/2} (a + b \operatorname{ArcSin}[c x])^2}{f + g x} dx$$

Optimal (type 4, 1992 leaves, 50 steps):

$$\begin{aligned}
& - \frac{4 b^2 d \sqrt{d - c^2 d x^2}}{9 g} - \frac{a^2 d (c f - g) (c f + g) \sqrt{d - c^2 d x^2}}{g^3} + \frac{2 b^2 d (c f - g) (c f + g) \sqrt{d - c^2 d x^2}}{g^3} - \frac{b^2 c^2 d f x \sqrt{d - c^2 d x^2}}{4 g^2} + \\
& \frac{2 a b c d (c f - g) (c f + g) x \sqrt{d - c^2 d x^2}}{g^3 \sqrt{1 - c^2 x^2}} - \frac{2 b^2 d (1 - c^2 x^2) \sqrt{d - c^2 d x^2}}{27 g} - \frac{2 a b d (c f - g) (c f + g) \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x]}{g^3} + \\
& \frac{b^2 c d f \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x]}{4 g^2 \sqrt{1 - c^2 x^2}} + \frac{2 b^2 c d (c f - g) (c f + g) x \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x]}{g^3 \sqrt{1 - c^2 x^2}} - \frac{b^2 d (c f - g) (c f + g) \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x]^2}{g^3} - \\
& \frac{2 b c d x \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])}{3 g \sqrt{1 - c^2 x^2}} - \frac{b c^3 d f x^2 \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])}{2 g^2 \sqrt{1 - c^2 x^2}} + \frac{2 b c^3 d x^3 \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])}{9 g \sqrt{1 - c^2 x^2}} + \\
& \frac{c^2 d f x \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])^2}{2 g^2} + \frac{d (1 - c^2 x^2) \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])^2}{3 g} + \frac{c d f \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])^3}{6 b g^2 \sqrt{1 - c^2 x^2}} - \\
& \frac{c d (c f - g) (c f + g) x \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])^3}{3 b g^3 \sqrt{1 - c^2 x^2}} - \frac{d (c^2 f^2 - g^2)^2 \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])^3}{3 b c g^4 (f + g x) \sqrt{1 - c^2 x^2}} - \\
& \frac{d (c f - g) (c f + g) \sqrt{1 - c^2 x^2} \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])^3}{3 b c g^2 (f + g x)} + \frac{a^2 d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2} \operatorname{ArcTan}\left[\frac{g + c^2 f x}{\sqrt{c^2 f^2 - g^2} \sqrt{1 - c^2 x^2}}\right]}{g^4 \sqrt{1 - c^2 x^2}} - \\
& \frac{2 i a b d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^4 \sqrt{1 - c^2 x^2}} - \frac{i b^2 d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^4 \sqrt{1 - c^2 x^2}} + \\
& \frac{2 i a b d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^4 \sqrt{1 - c^2 x^2}} - \frac{i b^2 d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^4 \sqrt{1 - c^2 x^2}} - \\
& \frac{2 a b d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2} \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^4 \sqrt{1 - c^2 x^2}} - \frac{2 b^2 d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^4 \sqrt{1 - c^2 x^2}} + \\
& \frac{2 a b d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2} \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^4 \sqrt{1 - c^2 x^2}} - \frac{2 b^2 d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^4 \sqrt{1 - c^2 x^2}} - \\
& \frac{2 i b^2 d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2} \operatorname{PolyLog}\left[3, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^4 \sqrt{1 - c^2 x^2}} + \frac{2 i b^2 d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2} \operatorname{PolyLog}\left[3, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^4 \sqrt{1 - c^2 x^2}}
\end{aligned}$$

Result (type 8, 35 leaves):

$$\int \frac{(d - c^2 dx^2)^{3/2} (a + b \operatorname{ArcSin}[cx])^2}{f + g x} dx$$

**Problem 69: Unable to integrate problem.**

$$\int \frac{(d - c^2 dx^2)^{5/2} (a + b \operatorname{ArcSin}[cx])^2}{f + g x} dx$$

Optimal (type 4, 2989 leaves, 74 steps):

$$\begin{aligned}
& \frac{52 b^2 d^2 \sqrt{d - c^2 dx^2}}{225 g} + \frac{4 b^2 d^2 (c^2 f^2 - 2 g^2) \sqrt{d - c^2 dx^2}}{9 g^3} + \frac{a^2 d^2 (c^2 f^2 - g^2)^2 \sqrt{d - c^2 dx^2}}{g^5} - \frac{2 b^2 d^2 (c^2 f^2 - g^2)^2 \sqrt{d - c^2 dx^2}}{g^5} - \\
& \frac{b^2 c^2 d^2 f x \sqrt{d - c^2 dx^2}}{64 g^2} + \frac{b^2 c^2 d^2 f (c^2 f^2 - 2 g^2) x \sqrt{d - c^2 dx^2}}{4 g^4} + \frac{b^2 c^4 d^2 f x^3 \sqrt{d - c^2 dx^2}}{32 g^2} + \frac{4 a b c d^2 x \sqrt{d - c^2 dx^2}}{15 g \sqrt{1 - c^2 x^2}} - \\
& \frac{2 a b c d^2 (c^2 f^2 - g^2)^2 x \sqrt{d - c^2 dx^2}}{g^5 \sqrt{1 - c^2 x^2}} + \frac{26 b^2 d^2 (1 - c^2 x^2) \sqrt{d - c^2 dx^2}}{675 g} + \frac{2 b^2 d^2 (c^2 f^2 - 2 g^2) (1 - c^2 x^2) \sqrt{d - c^2 dx^2}}{27 g^3} - \\
& \frac{2 b^2 d^2 (1 - c^2 x^2)^2 \sqrt{d - c^2 dx^2}}{125 g} + \frac{2 a b d^2 (c^2 f^2 - g^2)^2 \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx]}{g^5} + \frac{b^2 c d^2 f \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx]}{64 g^2 \sqrt{1 - c^2 x^2}} - \\
& \frac{b^2 c d^2 f (c^2 f^2 - 2 g^2) \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx]}{4 g^4 \sqrt{1 - c^2 x^2}} + \frac{4 b^2 c d^2 x \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx]}{15 g \sqrt{1 - c^2 x^2}} - \frac{2 b^2 c d^2 (c^2 f^2 - g^2)^2 x \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx]}{g^5 \sqrt{1 - c^2 x^2}} + \\
& \frac{b^2 d^2 (c^2 f^2 - g^2)^2 \sqrt{d - c^2 dx^2} \operatorname{ArcSin}[cx]^2}{g^5} + \frac{2 b c d^2 (c^2 f^2 - 2 g^2) x \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])}{3 g^3 \sqrt{1 - c^2 x^2}} - \frac{b c^3 d^2 f x^2 \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])}{8 g^2 \sqrt{1 - c^2 x^2}} + \\
& \frac{b c^3 d^2 f (c^2 f^2 - 2 g^2) x^2 \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])}{2 g^4 \sqrt{1 - c^2 x^2}} + \frac{2 b c^3 d^2 x^3 \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])}{45 g \sqrt{1 - c^2 x^2}} - \\
& \frac{2 b c^3 d^2 (c^2 f^2 - 2 g^2) x^3 \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])}{9 g^3 \sqrt{1 - c^2 x^2}} + \frac{b c^5 d^2 f x^4 \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])}{8 g^2 \sqrt{1 - c^2 x^2}} - \\
& \frac{2 b c^5 d^2 x^5 \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])}{25 g \sqrt{1 - c^2 x^2}} - \frac{2 d^2 \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])^2}{15 g} + \frac{c^2 d^2 f x \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])^2}{8 g^2} - \\
& \frac{c^2 d^2 f (c^2 f^2 - 2 g^2) x \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])^2}{2 g^4} - \frac{c^2 d^2 x^2 \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])^2}{15 g} - \frac{c^4 d^2 f x^3 \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])^2}{4 g^2} + \\
& \frac{c^4 d^2 x^4 \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])^2}{5 g} - \frac{d^2 (c^2 f^2 - 2 g^2) (1 - c^2 x^2) \sqrt{d - c^2 dx^2} (a + b \operatorname{ArcSin}[cx])^2}{3 g^3} -
\end{aligned}$$

$$\begin{aligned}
& \frac{c d^2 f \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])^3}{24 b g^2 \sqrt{1 - c^2 x^2}} - \frac{c d^2 f (c^2 f^2 - 2 g^2) \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])^3}{6 b g^4 \sqrt{1 - c^2 x^2}} + \\
& \frac{c d^2 (c^2 f^2 - g^2)^2 x \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])^3}{3 b g^5 \sqrt{1 - c^2 x^2}} + \frac{d^2 (c^2 f^2 - g^2)^3 \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])^3}{3 b c g^6 (f + g x) \sqrt{1 - c^2 x^2}} + \\
& \frac{d^2 (c^2 f^2 - g^2)^2 \sqrt{1 - c^2 x^2} \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcSin}[c x])^3}{3 b c g^4 (f + g x)} - \frac{a^2 d^2 (c^2 f^2 - g^2)^{5/2} \sqrt{d - c^2 d x^2} \operatorname{ArcTan}\left[\frac{g + c^2 f x}{\sqrt{c^2 f^2 - g^2} \sqrt{1 - c^2 x^2}}\right]}{g^6 \sqrt{1 - c^2 x^2}} + \\
& \frac{2 \pm a b d^2 (c^2 f^2 - g^2)^{5/2} \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{\pm e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^6 \sqrt{1 - c^2 x^2}} - \frac{\pm b^2 d^2 (c^2 f^2 - g^2)^{5/2} \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 - \frac{\pm e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^6 \sqrt{1 - c^2 x^2}} - \\
& \frac{2 \pm a b d^2 (c^2 f^2 - g^2)^{5/2} \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{\pm e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^6 \sqrt{1 - c^2 x^2}} - \frac{\pm b^2 d^2 (c^2 f^2 - g^2)^{5/2} \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 - \frac{\pm e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^6 \sqrt{1 - c^2 x^2}} + \\
& \frac{2 a b d^2 (c^2 f^2 - g^2)^{5/2} \sqrt{d - c^2 d x^2} \operatorname{PolyLog}\left[2, \frac{\pm e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^6 \sqrt{1 - c^2 x^2}} + \frac{2 b^2 d^2 (c^2 f^2 - g^2)^{5/2} \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{\pm e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^6 \sqrt{1 - c^2 x^2}} - \\
& \frac{2 a b d^2 (c^2 f^2 - g^2)^{5/2} \sqrt{d - c^2 d x^2} \operatorname{PolyLog}\left[2, \frac{\pm e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^6 \sqrt{1 - c^2 x^2}} - \frac{2 b^2 d^2 (c^2 f^2 - g^2)^{5/2} \sqrt{d - c^2 d x^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{\pm e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^6 \sqrt{1 - c^2 x^2}} + \\
& \frac{2 \pm b^2 d^2 (c^2 f^2 - g^2)^{5/2} \sqrt{d - c^2 d x^2} \operatorname{PolyLog}\left[3, \frac{\pm e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{g^6 \sqrt{1 - c^2 x^2}} - \frac{2 \pm b^2 d^2 (c^2 f^2 - g^2)^{5/2} \sqrt{d - c^2 d x^2} \operatorname{PolyLog}\left[3, \frac{\pm e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{g^6 \sqrt{1 - c^2 x^2}}
\end{aligned}$$

Result (type 8, 35 leaves) :

$$\int \frac{(d - c^2 d x^2)^{5/2} (a + b \operatorname{ArcSin}[c x])^2}{f + g x} dx$$

**Problem 73: Unable to integrate problem.**

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^2}{(f + g x) \sqrt{d - c^2 d x^2}} dx$$

Optimal (type 4, 589 leaves, 12 steps) :

$$\begin{aligned}
& - \frac{\frac{i \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])^2 \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{\sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 d x^2}} + \frac{\frac{i \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])^2 \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{\sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 d x^2}}}{\sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 d x^2}} - \\
& \frac{2 b \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{\sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 d x^2}} + \frac{2 b \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{\sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 d x^2}} - \\
& \frac{2 i b^2 \sqrt{1 - c^2 x^2} \operatorname{PolyLog}\left[3, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{\sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 d x^2}} + \frac{2 i b^2 \sqrt{1 - c^2 x^2} \operatorname{PolyLog}\left[3, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{\sqrt{c^2 f^2 - g^2} \sqrt{d - c^2 d x^2}}
\end{aligned}$$

Result (type 8, 35 leaves):

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^2}{(f + g x) \sqrt{d - c^2 d x^2}} dx$$

Problem 74: Attempted integration timed out after 120 seconds.

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^2}{(f + g x)^2 \sqrt{d - c^2 d x^2}} dx$$

Optimal (type 4, 1113 leaves, 20 steps):

$$\begin{aligned}
& \frac{\frac{i c \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])^2}{(c^2 f^2 - g^2) \sqrt{d - c^2 d x^2}} + \frac{g (1 - c^2 x^2) (a + b \operatorname{ArcSin}[c x])^2}{(c^2 f^2 - g^2) (f + g x) \sqrt{d - c^2 d x^2}} - \\
& \frac{2 b c \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right] - \frac{i c^2 f \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])^2 \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{(c^2 f^2 - g^2) \sqrt{d - c^2 d x^2}} - \\
& \frac{2 b c \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right] + \frac{i c^2 f \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])^2 \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{(c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2}} + \\
& \frac{2 i b^2 c \sqrt{1 - c^2 x^2} \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right] - 2 b c^2 f \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{(c^2 f^2 - g^2) \sqrt{d - c^2 d x^2}} + \\
& \frac{2 i b^2 c \sqrt{1 - c^2 x^2} \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right] + 2 b c^2 f \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{(c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2}} - \\
& \frac{2 i b^2 c^2 f \sqrt{1 - c^2 x^2} \operatorname{PolyLog}\left[3, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right] + 2 i b^2 c^2 f \sqrt{1 - c^2 x^2} \operatorname{PolyLog}\left[3, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{(c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2}}
\end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 78: Unable to integrate problem.**

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^2}{(f + g x) (d - c^2 d x^2)^{3/2}} dx$$

Optimal (type 4, 1137 leaves, 28 steps):

$$\begin{aligned}
& - \frac{\frac{i}{2} \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])^2}{2 d (c f - g) \sqrt{d - c^2 d x^2}} + \frac{\frac{i}{2} \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])^2}{2 d (c f + g) \sqrt{d - c^2 d x^2}} - \\
& \frac{\sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])^2 \operatorname{Cot}\left[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]\right]}{2 d (c f - g) \sqrt{d - c^2 d x^2}} + \frac{2 b \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 - i e^{-i \operatorname{ArcSin}[c x]}\right]}{d (c f + g) \sqrt{d - c^2 d x^2}} + \\
& \frac{2 b \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[c x]}\right]}{d (c f - g) \sqrt{d - c^2 d x^2}} + \frac{\frac{i}{2} g^2 \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])^2 \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2}} - \\
& \frac{\frac{i}{2} g^2 \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])^2 \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2}} + \frac{2 \frac{i}{2} b^2 \sqrt{1 - c^2 x^2} \operatorname{PolyLog}[2, i e^{-i \operatorname{ArcSin}[c x]}]}{d (c f + g) \sqrt{d - c^2 d x^2}} - \\
& \frac{2 \frac{i}{2} b^2 \sqrt{1 - c^2 x^2} \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}]}{d (c f - g) \sqrt{d - c^2 d x^2}} + \frac{2 b g^2 \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}]}{d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2}} - \\
& \frac{2 b g^2 \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x]) \operatorname{PolyLog}[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}]}{d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2}} + \frac{2 \frac{i}{2} b^2 g^2 \sqrt{1 - c^2 x^2} \operatorname{PolyLog}[3, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}]}{d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2}} - \\
& \frac{2 \frac{i}{2} b^2 g^2 \sqrt{1 - c^2 x^2} \operatorname{PolyLog}[3, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}]}{d (c^2 f^2 - g^2)^{3/2} \sqrt{d - c^2 d x^2}} + \frac{\sqrt{1 - c^2 x^2} (a + b \operatorname{ArcSin}[c x])^2 \operatorname{Tan}\left[\frac{\pi}{4} + \frac{1}{2} \operatorname{ArcSin}[c x]\right]}{2 d (c f + g) \sqrt{d - c^2 d x^2}}
\end{aligned}$$

Result (type 8, 35 leaves) :

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^2}{(f + g x) (d - c^2 d x^2)^{3/2}} dx$$

Problem 83: Unable to integrate problem.

$$\int \frac{(a + b \operatorname{ArcSin}[c x])^3 \operatorname{Log}\left[h (f + g x)^m\right]}{\sqrt{1 - c^2 x^2}} dx$$

Optimal (type 4, 634 leaves, 15 steps) :

$$\begin{aligned}
& \frac{\frac{\imath m (a + b \operatorname{ArcSin}[cx])^5}{20 b^2 c} - \frac{m (a + b \operatorname{ArcSin}[cx])^4 \operatorname{Log}\left[1 - \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{4 b c} - \frac{m (a + b \operatorname{ArcSin}[cx])^4 \operatorname{Log}\left[1 - \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{4 b c} + } \\
& \frac{(a + b \operatorname{ArcSin}[cx])^4 \operatorname{Log}[h (f + g x)^m]}{4 b c} + \frac{\frac{\imath m (a + b \operatorname{ArcSin}[cx])^3 \operatorname{PolyLog}[2, \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}]}{c} + } \\
& \frac{\frac{\imath m (a + b \operatorname{ArcSin}[cx])^3 \operatorname{PolyLog}[2, \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}]}{c} - \frac{3 b m (a + b \operatorname{ArcSin}[cx])^2 \operatorname{PolyLog}[3, \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}]}{c} - } \\
& \frac{3 b m (a + b \operatorname{ArcSin}[cx])^2 \operatorname{PolyLog}[3, \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}]}{c} - \frac{6 \frac{\imath b^2 m (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[4, \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}]}{c} - } \\
& \frac{6 i b^2 m (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[4, \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}]}{c} + \frac{6 b^3 m \operatorname{PolyLog}[5, \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}]}{c} + \frac{6 b^3 m \operatorname{PolyLog}[5, \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}]}{c}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{(a + b \operatorname{ArcSin}[cx])^3 \operatorname{Log}[h (f + g x)^m]}{\sqrt{1 - c^2 x^2}} dx$$

### Problem 84: Unable to integrate problem.

$$\int \frac{(a + b \operatorname{ArcSin}[cx])^2 \operatorname{Log}[h (f + g x)^m]}{\sqrt{1 - c^2 x^2}} dx$$

Optimal (type 4, 514 leaves, 13 steps):

$$\begin{aligned}
& \frac{\frac{\imath m (a + b \operatorname{ArcSin}[cx])^4}{12 b^2 c} - \frac{m (a + b \operatorname{ArcSin}[cx])^3 \operatorname{Log}\left[1 - \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{3 b c} - \frac{m (a + b \operatorname{ArcSin}[cx])^3 \operatorname{Log}\left[1 - \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{3 b c} + } \\
& \frac{(a + b \operatorname{ArcSin}[cx])^3 \operatorname{Log}[h (f + g x)^m]}{3 b c} + \frac{\frac{\imath m (a + b \operatorname{ArcSin}[cx])^2 \operatorname{PolyLog}[2, \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}]}{c} + } \\
& \frac{\frac{\imath m (a + b \operatorname{ArcSin}[cx])^2 \operatorname{PolyLog}[2, \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}]}{c} - \frac{2 b m (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[3, \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}]}{c} - } \\
& \frac{2 b m (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}[3, \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}]}{c} - \frac{2 \frac{\imath b^2 m \operatorname{PolyLog}[4, \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}]}{c} - \frac{2 \frac{\imath b^2 m \operatorname{PolyLog}[4, \frac{\imath e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}]}{c}}{c}}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{(a + b \operatorname{ArcSin}[cx])^2 \operatorname{Log}[h(f + gx)^m]}{\sqrt{1 - c^2 x^2}} dx$$

Problem 85: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[cx]) \operatorname{Log}[h(f + gx)^m]}{\sqrt{1 - c^2 x^2}} dx$$

Optimal (type 4, 390 leaves, 11 steps):

$$\begin{aligned} & \frac{\frac{i m (a + b \operatorname{ArcSin}[cx])^3}{6 b^2 c} - \frac{m (a + b \operatorname{ArcSin}[cx])^2 \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{2 b c} - \frac{m (a + b \operatorname{ArcSin}[cx])^2 \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{2 b c} + \\ & \frac{(a + b \operatorname{ArcSin}[cx])^2 \operatorname{Log}[h(f + gx)^m]}{2 b c} + \frac{\frac{i m (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{c} + \\ & \frac{i m (a + b \operatorname{ArcSin}[cx]) \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{c} - \frac{b m \operatorname{PolyLog}\left[3, \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{c} - \frac{b m \operatorname{PolyLog}\left[3, \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{c}} \end{aligned}$$

Result (type 4, 5941 leaves):

$$\begin{aligned} & \frac{m \operatorname{ArcSin}[cx] (2 a + b \operatorname{ArcSin}[cx]) \operatorname{Log}[f + gx]}{2 c} + \frac{a \operatorname{ArcSin}[cx] (-m \operatorname{Log}[f + gx] + \operatorname{Log}[h(f + gx)^m])}{c} - \\ & a c g m \left( -\frac{1}{2 c^3 \left(-\frac{1}{c} - \frac{f}{g}\right) g} \left( \frac{3}{2} i \pi \operatorname{ArcSin}[cx] - \frac{1}{2} i \operatorname{ArcSin}[cx]^2 + 2 \pi \operatorname{Log}\left[1 + e^{-i \operatorname{ArcSin}[cx]}\right] - \pi \operatorname{Log}\left[1 + i e^{i \operatorname{ArcSin}[cx]}\right] + 2 \operatorname{ArcSin}[cx] \right. \right. \\ & \left. \left. \operatorname{Log}\left[1 + i e^{i \operatorname{ArcSin}[cx]}\right] - 2 \pi \operatorname{Log}\left[\cos\left(\frac{1}{2} \operatorname{ArcSin}[cx]\right)\right] + \pi \operatorname{Log}\left[-\cos\left(\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right)\right] - 2 i \operatorname{PolyLog}\left[2, -i e^{i \operatorname{ArcSin}[cx]}\right] \right) + \right. \\ & \left. \frac{1}{2 c^3 \left(\frac{1}{c} - \frac{f}{g}\right) g} \left( \frac{1}{2} i \pi \operatorname{ArcSin}[cx] - \frac{1}{2} i \operatorname{ArcSin}[cx]^2 + 2 \pi \operatorname{Log}\left[1 + e^{-i \operatorname{ArcSin}[cx]}\right] + \pi \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[cx]}\right] + \right. \right. \\ & \left. \left. 2 \operatorname{ArcSin}[cx] \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSin}[cx]}\right] - 2 \pi \operatorname{Log}\left[\cos\left(\frac{1}{2} \operatorname{ArcSin}[cx]\right)\right] - \pi \operatorname{Log}\left[\sin\left(\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[cx])\right)\right] - 2 i \operatorname{PolyLog}\left[2, i e^{i \operatorname{ArcSin}[cx]}\right] \right) + \right) \end{aligned}$$

$$\begin{aligned}
& \frac{1}{8 c^2 \left(-\frac{1}{c} - \frac{f}{g}\right) \left(\frac{1}{c} - \frac{f}{g}\right) g^3} f^2 \left( \frac{\sqrt{1 + \frac{c f}{g}}}{\sqrt{2}} \right) \operatorname{ArcTan} \left[ \frac{(c f - g) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{c^2 f^2 - g^2}} \right] - \\
& 4 \left( \frac{\pi + 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{c f}{g}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x]}{\pi - 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{c f}{g}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x]} \right) \operatorname{Log} \left[ 1 - \frac{i e^{-i \operatorname{ArcSin}[c x]} (-c f + \sqrt{c^2 f^2 - g^2})}{g} \right] - 4 \left( \frac{\sqrt{1 + \frac{c f}{g}}}{\sqrt{2}} \right) \\
& \operatorname{Log} \left[ 1 + \frac{i e^{-i \operatorname{ArcSin}[c x]} (c f + \sqrt{c^2 f^2 - g^2})}{g} \right] + 4 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c f + c g x] + 8 \operatorname{ArcSin}[c x] \operatorname{Log}[c f + c g x] + \\
& 8 i \left( \operatorname{PolyLog} \left[ 2, \frac{i e^{-i \operatorname{ArcSin}[c x]} (-c f + \sqrt{c^2 f^2 - g^2})}{g} \right] + \operatorname{PolyLog} \left[ 2, -\frac{i e^{-i \operatorname{ArcSin}[c x]} (c f + \sqrt{c^2 f^2 - g^2})}{g} \right] \right) + \\
& \frac{1}{c} a g m \left( -\frac{1}{2 c \left(-\frac{1}{c} - \frac{f}{g}\right) g} \left( \frac{3}{2} i \pi \operatorname{ArcSin}[c x] - \frac{1}{2} i \operatorname{ArcSin}[c x]^2 + 2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] - \pi \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] + 2 \operatorname{ArcSin}[c x] \right. \right. \\
& \left. \left. \operatorname{Log}[1 + i e^{i \operatorname{ArcSin}[c x]}] - 2 \pi \operatorname{Log}[\cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]] + \pi \operatorname{Log}[-\cos \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]] - 2 i \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSin}[c x]}] \right) + \right. \\
& \left. \frac{1}{2 c \left(\frac{1}{c} - \frac{f}{g}\right) g} \left( \frac{1}{2} i \pi \operatorname{ArcSin}[c x] - \frac{1}{2} i \operatorname{ArcSin}[c x]^2 + 2 \pi \operatorname{Log}[1 + e^{-i \operatorname{ArcSin}[c x]}] + \pi \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] + \right. \right. \\
& \left. \left. 2 \operatorname{ArcSin}[c x] \operatorname{Log}[1 - i e^{i \operatorname{ArcSin}[c x]}] - 2 \pi \operatorname{Log}[\cos \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]] - \pi \operatorname{Log}[\sin \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]] - 2 i \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSin}[c x]}] \right) + \right. \\
& \left. \frac{1}{8 c^2 \left(-\frac{1}{c} - \frac{f}{g}\right) \left(\frac{1}{c} - \frac{f}{g}\right) g} \left( \frac{\sqrt{1 + \frac{c f}{g}}}{\sqrt{2}} \right) \operatorname{ArcTan} \left[ \frac{(c f - g) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{c^2 f^2 - g^2}} \right] - \right)
\end{aligned}$$

$$\begin{aligned}
& 4 \left( \pi + 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{c f}{g}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log} \left[ 1 - \frac{i e^{-i \operatorname{ArcSin}[c x]} \left( -c f + \sqrt{c^2 f^2 - g^2} \right)}{g} \right] - 4 \left( \pi - 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{c f}{g}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \\
& \operatorname{Log} \left[ 1 + \frac{i e^{-i \operatorname{ArcSin}[c x]} \left( c f + \sqrt{c^2 f^2 - g^2} \right)}{g} \right] + 4 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c f + c g x] + 8 \operatorname{ArcSin}[c x] \operatorname{Log}[c f + c g x] + \\
& 8 i \left( \operatorname{PolyLog} \left[ 2, \frac{i e^{-i \operatorname{ArcSin}[c x]} \left( -c f + \sqrt{c^2 f^2 - g^2} \right)}{g} \right] + \operatorname{PolyLog} \left[ 2, -\frac{i e^{-i \operatorname{ArcSin}[c x]} \left( c f + \sqrt{c^2 f^2 - g^2} \right)}{g} \right] \right) + \\
& b f (-m \operatorname{Log}[f + g x] + \operatorname{Log}[h (f + g x)^m]) \left( \frac{\pi \operatorname{ArcTan} \left[ \frac{g + c f \operatorname{Tan} \left[ \frac{1}{2} \operatorname{ArcSin}[c x] \right]}{\sqrt{c^2 f^2 - g^2}} \right]}{\sqrt{c^2 f^2 - g^2}} + \frac{1}{\sqrt{-c^2 f^2 + g^2}} \right. \\
& \left( 2 \operatorname{ArcCos} \left[ -\frac{c f}{g} \right] \operatorname{ArcTanh} \left[ \frac{(c f - g) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{ArcTanh} \left[ \frac{(c f + g) \operatorname{Tan} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + \right. \\
& \left. \left( \operatorname{ArcCos} \left[ -\frac{c f}{g} \right] + 2 i \left( \operatorname{ArcTanh} \left[ \frac{(c f - g) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + \operatorname{ArcTanh} \left[ \frac{(c f + g) \operatorname{Tan} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \right) \right. \\
& \left. \operatorname{Log} \left[ \frac{e^{\frac{1}{4} i (\pi - 2 \operatorname{ArcSin}[c x])} \sqrt{-c^2 f^2 + g^2}}{\sqrt{2} \sqrt{g} \sqrt{c f + c g x}} \right] + \right. \\
& \left. \left( \operatorname{ArcCos} \left[ -\frac{c f}{g} \right] - 2 i \operatorname{ArcTanh} \left[ \frac{(c f - g) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] - 2 i \operatorname{ArcTanh} \left[ \frac{(c f + g) \operatorname{Tan} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \right. \\
& \left. \operatorname{Log} \left[ \frac{\left( \frac{1}{2} - \frac{i}{2} \right) e^{\frac{1}{2} i \operatorname{ArcSin}[c x]} \sqrt{-c^2 f^2 + g^2}}{\sqrt{g} \sqrt{c f + c g x}} \right] - \left( \operatorname{ArcCos} \left[ -\frac{c f}{g} \right] + 2 i \operatorname{ArcTanh} \left[ \frac{(c f - g) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \text{Log} \left[ \frac{(c f + g) \left( -c f + g - i \sqrt{-c^2 f^2 + g^2} \right) \left( 1 + i \cot \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right] \right)}{g \left( c f + g + \sqrt{-c^2 f^2 + g^2} \right) \cot \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]} \right] - \left( \text{ArcCos} \left[ -\frac{c f}{g} \right] - \right. \\
& \left. 2 i \text{ArcTanh} \left[ \frac{(c f - g) \cot \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \text{Log} \left[ \frac{(c f + g) \left( i c f - i g + \sqrt{-c^2 f^2 + g^2} \right) \left( i + \cot \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right] \right)}{g \left( c f + g + \sqrt{-c^2 f^2 + g^2} \right) \cot \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]} \right] + \\
& i \left( \text{PolyLog} [2, \frac{(c f - i \sqrt{-c^2 f^2 + g^2}) (c f + g - \sqrt{-c^2 f^2 + g^2} \cot \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{g (c f + g + \sqrt{-c^2 f^2 + g^2} \cot \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right])}] - \right. \\
& \left. \text{PolyLog} [2, \frac{(c f + i \sqrt{-c^2 f^2 + g^2}) (c f + g - \sqrt{-c^2 f^2 + g^2} \cot \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{g (c f + g + \sqrt{-c^2 f^2 + g^2} \cot \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right])}] \right) + \\
& \frac{1}{c} b g (-m \text{Log}[f + g x] + \text{Log}[h (f + g x)^m]) \left( \frac{\text{ArcSin}[c x]^2}{2 g} - \frac{1}{g} c f \left( \frac{\pi \text{ArcTan} \left[ \frac{g + c f \tan \left[ \frac{1}{2} \text{ArcSin}[c x] \right]}{\sqrt{c^2 f^2 - g^2}} \right]}{\sqrt{c^2 f^2 - g^2}} + \frac{1}{\sqrt{-c^2 f^2 + g^2}} \right. \right. \\
& \left. \left. 2 \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \text{ArcTanh} \left[ \frac{(c f + g) \cot \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] - 2 \text{ArcCos} \left[ -\frac{c f}{g} \right] \text{ArcTanh} \left[ \frac{(-c f + g) \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] + \right. \\
& \left. \left. \text{ArcCos} \left[ -\frac{c f}{g} \right] - 2 i \left( \text{ArcTanh} \left[ \frac{(c f + g) \cot \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] - \text{ArcTanh} \left[ \frac{(-c f + g) \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \right) \right. \\
& \left. \text{Log} \left[ \frac{e^{-\frac{1}{2} i \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right)} \sqrt{-c^2 f^2 + g^2}}{\sqrt{2} \sqrt{g} \sqrt{c f + c g x}} \right] + \right. \\
& \left. \left. \text{ArcCos} \left[ -\frac{c f}{g} \right] + 2 i \left( \text{ArcTanh} \left[ \frac{(c f + g) \cot \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] - \text{ArcTanh} \left[ \frac{(-c f + g) \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \text{Log} \left[ \frac{\frac{1}{2} i \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \sqrt{-c^2 f^2 + g^2}}{\sqrt{2} \sqrt{g} \sqrt{c f + c g x}} \right] - \left( \text{ArcCos} \left[ -\frac{c f}{g} \right] + 2 i \text{ArcTanh} \left[ \frac{(-c f + g) \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \\
& \text{Log} \left[ 1 - \frac{\left( c f - i \sqrt{-c^2 f^2 + g^2} \right) \left( c f + g - \sqrt{-c^2 f^2 + g^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)}{g \left( c f + g + \sqrt{-c^2 f^2 + g^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)} \right] + \left( -\text{ArcCos} \left[ -\frac{c f}{g} \right] + 2 i \text{ArcTanh} \left[ \right. \right. \\
& \left. \left. \frac{(-c f + g) \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 f^2 + g^2}} \right] \right) \text{Log} \left[ 1 - \frac{\left( c f + i \sqrt{-c^2 f^2 + g^2} \right) \left( c f + g - \sqrt{-c^2 f^2 + g^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)}{g \left( c f + g + \sqrt{-c^2 f^2 + g^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)} \right] + \\
& i \left( \text{PolyLog} [2, \frac{\left( c f - i \sqrt{-c^2 f^2 + g^2} \right) \left( c f + g - \sqrt{-c^2 f^2 + g^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] }{g \left( c f + g + \sqrt{-c^2 f^2 + g^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] }] - \text{PolyLog} [2, \right. \\
& \left. \left. \left. \frac{\left( c f + i \sqrt{-c^2 f^2 + g^2} \right) \left( c f + g - \sqrt{-c^2 f^2 + g^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] }{g \left( c f + g + \sqrt{-c^2 f^2 + g^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] } \right) \right] \right) - \\
& \frac{1}{6 c \sqrt{-(-c^2 f^2 + g^2)^2}} b m \left( -i \sqrt{-(-c^2 f^2 + g^2)^2} \text{ArcSin}[c x]^3 - 24 i \sqrt{-(-c^2 f^2 + g^2)^2} \text{ArcSin} \left[ \frac{\sqrt{1 + \frac{c f}{g}}}{\sqrt{2}} \right] \text{ArcSin}[c x] \right. \\
& \left. \text{ArcTan} \left[ \frac{(c f - g) \cot \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{c^2 f^2 - g^2}} \right] + \right. \\
& \left. 24 i \sqrt{-(-c^2 f^2 + g^2)^2} \text{ArcSin} \left[ \frac{\sqrt{1 + \frac{c f}{g}}}{\sqrt{2}} \right] \text{ArcSin}[c x] \text{ArcTan} \left[ \frac{(c f - g) (\cos \left[ \frac{1}{2} \text{ArcSin}[c x] \right] - \sin \left[ \frac{1}{2} \text{ArcSin}[c x] \right])}{\sqrt{c^2 f^2 - g^2} (\cos \left[ \frac{1}{2} \text{ArcSin}[c x] \right] + \sin \left[ \frac{1}{2} \text{ArcSin}[c x] \right])} \right] + \right. \\
& \left. 3 c f \sqrt{-c^2 f^2 + g^2} \text{ArcSin}[c x]^2 \text{Log} \left[ 1 + \frac{i e^{i \text{ArcSin}[c x]} g}{-c f + \sqrt{c^2 f^2 - g^2}} \right] - \right.
\end{aligned}$$

$$\begin{aligned}
& 3 \sqrt{-(-c^2 f^2 + g^2)^2} \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{\frac{i}{2} e^{-i \operatorname{ArcSin}[c x]} \left(-c f + \sqrt{c^2 f^2 - g^2}\right)}{g}\right] - \\
& 12 \sqrt{-(-c^2 f^2 + g^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c f}{g}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{\frac{i}{2} e^{-i \operatorname{ArcSin}[c x]} \left(-c f + \sqrt{c^2 f^2 - g^2}\right)}{g}\right] + \\
& 3 \sqrt{-(-c^2 f^2 + g^2)^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 - \frac{\frac{i}{2} e^{-i \operatorname{ArcSin}[c x]} \left(-c f + \sqrt{c^2 f^2 - g^2}\right)}{g}\right] - \\
& 3 c f \sqrt{-c^2 f^2 + g^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 - \frac{\frac{i}{2} e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right] - \\
& 3 \sqrt{-(-c^2 f^2 + g^2)^2} \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{\frac{i}{2} e^{-i \operatorname{ArcSin}[c x]} \left(c f + \sqrt{c^2 f^2 - g^2}\right)}{g}\right] + \\
& 12 \sqrt{-(-c^2 f^2 + g^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c f}{g}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{\frac{i}{2} e^{-i \operatorname{ArcSin}[c x]} \left(c f + \sqrt{c^2 f^2 - g^2}\right)}{g}\right] + \\
& 3 \sqrt{-(-c^2 f^2 + g^2)^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{\frac{i}{2} e^{-i \operatorname{ArcSin}[c x]} \left(c f + \sqrt{c^2 f^2 - g^2}\right)}{g}\right] - \\
& 3 i c f \sqrt{c^2 f^2 - g^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{\frac{e^{i \operatorname{ArcSin}[c x]} g}{i c f - \sqrt{-c^2 f^2 + g^2}}\right] + \\
& 3 \sqrt{-(-c^2 f^2 + g^2)^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{\frac{e^{i \operatorname{ArcSin}[c x]} g}{i c f - \sqrt{-c^2 f^2 + g^2}}\right] + \\
& 3 i c f \sqrt{c^2 f^2 - g^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{\frac{e^{i \operatorname{ArcSin}[c x]} g}{i c f + \sqrt{-c^2 f^2 + g^2}}\right] + \\
& 3 \sqrt{-(-c^2 f^2 + g^2)^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{\frac{e^{i \operatorname{ArcSin}[c x]} g}{i c f + \sqrt{-c^2 f^2 + g^2}}\right] + \\
& 3 \sqrt{-(-c^2 f^2 + g^2)^2} \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{\left(c f - \sqrt{c^2 f^2 - g^2}\right) \left(c x + \frac{i}{2} \sqrt{1 - c^2 x^2}\right)}{g}\right] +
\end{aligned}$$

$$\begin{aligned}
& 12 \sqrt{-(-c^2 f^2 + g^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c f}{g}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{(c f - \sqrt{c^2 f^2 - g^2}) (c x + i \sqrt{1 - c^2 x^2})}{g}\right] - \\
& 3 \sqrt{-(-c^2 f^2 + g^2)^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{(c f - \sqrt{c^2 f^2 - g^2}) (c x + i \sqrt{1 - c^2 x^2})}{g}\right] + \\
& 3 \sqrt{-(-c^2 f^2 + g^2)^2} \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{(c f + \sqrt{c^2 f^2 - g^2}) (c x + i \sqrt{1 - c^2 x^2})}{g}\right] - \\
& 12 \sqrt{-(-c^2 f^2 + g^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c f}{g}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{(c f + \sqrt{c^2 f^2 - g^2}) (c x + i \sqrt{1 - c^2 x^2})}{g}\right] - \\
& 3 \sqrt{-(-c^2 f^2 + g^2)^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{(c f + \sqrt{c^2 f^2 - g^2}) (c x + i \sqrt{1 - c^2 x^2})}{g}\right] - \\
& 6 i c f \sqrt{-c^2 f^2 + g^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right] + \\
& 6 i c f \sqrt{-c^2 f^2 + g^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right] - \\
& 6 c f \sqrt{c^2 f^2 - g^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{e^{i \operatorname{ArcSin}[c x]} g}{-i c f + \sqrt{-c^2 f^2 + g^2}}\right] - \\
& 6 i \sqrt{-(-c^2 f^2 + g^2)^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{e^{i \operatorname{ArcSin}[c x]} g}{-i c f + \sqrt{-c^2 f^2 + g^2}}\right] + \\
& 6 c f \sqrt{c^2 f^2 - g^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, -\frac{e^{i \operatorname{ArcSin}[c x]} g}{i c f + \sqrt{-c^2 f^2 + g^2}}\right] - \\
& 6 i \sqrt{-(-c^2 f^2 + g^2)^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, -\frac{e^{i \operatorname{ArcSin}[c x]} g}{i c f + \sqrt{-c^2 f^2 + g^2}}\right] + \\
& 6 c f \sqrt{-c^2 f^2 + g^2} \operatorname{PolyLog}\left[3, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right] - 6 c f \sqrt{-c^2 f^2 + g^2} \operatorname{PolyLog}\left[3, \frac{i e^{i \operatorname{ArcSin}[c x]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right] -
\end{aligned}$$

$$\begin{aligned}
& 6 \pm c f \sqrt{c^2 f^2 - g^2} \operatorname{PolyLog}[3, \frac{e^{i \operatorname{ArcSin}[cx]} g}{- \pm c f + \sqrt{-c^2 f^2 + g^2}}] + 6 \sqrt{-(-c^2 f^2 + g^2)^2} \operatorname{PolyLog}[3, \frac{e^{i \operatorname{ArcSin}[cx]} g}{- \pm c f + \sqrt{-c^2 f^2 + g^2}}] + \\
& 6 \pm c f \sqrt{c^2 f^2 - g^2} \operatorname{PolyLog}[3, -\frac{e^{i \operatorname{ArcSin}[cx]} g}{\pm c f + \sqrt{-c^2 f^2 + g^2}}] + 6 \sqrt{-(-c^2 f^2 + g^2)^2} \operatorname{PolyLog}[3, -\frac{e^{i \operatorname{ArcSin}[cx]} g}{\pm c f + \sqrt{-c^2 f^2 + g^2}}] \Bigg)
\end{aligned}$$

**Problem 86:** Attempted integration timed out after 120 seconds.

$$\int \frac{\operatorname{Log}[h(f + g x)^m]}{\sqrt{1 - c^2 x^2}} dx$$

Optimal (type 4, 237 leaves, 9 steps):

$$\begin{aligned}
& \frac{i m \operatorname{ArcSin}[cx]^2}{2 c} - \frac{m \operatorname{ArcSin}[cx] \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{c} - \frac{m \operatorname{ArcSin}[cx] \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{c} + \\
& \frac{\operatorname{ArcSin}[cx] \operatorname{Log}[h(f + g x)^m]}{c} + \frac{i m \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f - \sqrt{c^2 f^2 - g^2}}\right]}{c} + \frac{i m \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[cx]} g}{c f + \sqrt{c^2 f^2 - g^2}}\right]}{c}
\end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 91:** Result more than twice size of optimal antiderivative.

$$\int \frac{(f + g x) (a + b \operatorname{ArcSin}[cx])}{d + e x} dx$$

Optimal (type 4, 344 leaves, 14 steps):

$$\begin{aligned}
& \frac{b g \sqrt{1 - c^2 x^2}}{c e} - \frac{i b (e f - d g) \operatorname{ArcSin}[c x]^2}{2 e^2} + \frac{g x (a + b \operatorname{ArcSin}[c x])}{e} + \frac{b (e f - d g) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^2} + \\
& \frac{b (e f - d g) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^2} - \frac{b (e f - d g) \operatorname{ArcSin}[c x] \operatorname{Log}[d + e x]}{e^2} + \\
& \frac{(e f - d g) (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}[d + e x]}{e^2} - \frac{i b (e f - d g) \operatorname{PolyLog}\left[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^2} - \frac{i b (e f - d g) \operatorname{PolyLog}\left[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^2}
\end{aligned}$$

Result (type 4, 750 leaves):

$$\begin{aligned}
& \frac{1}{8 e^2} \left( 8 a e g x + 8 a (e f - d g) \operatorname{Log}[d + e x] + b e f \left( \frac{\pi - 2 \operatorname{ArcSin}[c x]}{\sqrt{2}} \right)^2 - 32 i \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] \operatorname{ArcTan}\left[\frac{(c d - e) \operatorname{Cot}\left[\frac{1}{4}(\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{c^2 d^2 - e^2}}\right] - \right. \\
& \quad \left. 4 \left( \pi + 4 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log}\left[1 - \frac{i(-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] - \right. \\
& \quad \left. 4 \left( \pi - 4 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log}\left[1 + \frac{i(c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] + 4 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c (d + e x)] + \right. \\
& \quad \left. 8 \operatorname{ArcSin}[c x] \operatorname{Log}[c (d + e x)] + 8 i \left( \operatorname{PolyLog}[2, \frac{i(-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}] + \operatorname{PolyLog}[2, -\frac{i(c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}] \right) \right) + \right. \\
& \quad \left. b g \left( \frac{8 e \sqrt{1 - c^2 x^2}}{c} + 8 e x \operatorname{ArcSin}[c x] - d \left( \frac{\pi - 2 \operatorname{ArcSin}[c x]}{\sqrt{2}} \right)^2 - 32 i \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] \operatorname{ArcTan}\left[\frac{(c d - e) \operatorname{Cot}\left[\frac{1}{4}(\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{c^2 d^2 - e^2}}\right] - \right. \right. \\
& \quad \left. \left. 4 \left( \pi + 4 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log}\left[1 - \frac{i(-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] - 4 \left( \pi - 4 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] - 2 \operatorname{ArcSin}[c x] \right) \right. \right. \\
& \quad \left. \left. \operatorname{Log}\left[1 + \frac{i(c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] + 4 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c (d + e x)] + 8 \operatorname{ArcSin}[c x] \operatorname{Log}[c (d + e x)] + \right. \right. \\
& \quad \left. \left. 8 i \left( \operatorname{PolyLog}[2, \frac{i(-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}] + \operatorname{PolyLog}[2, -\frac{i(c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}] \right) \right) \right)
\end{aligned}$$

Problem 92: Result unnecessarily involves higher level functions.

$$\int \frac{(f + g x) (a + b \operatorname{ArcSin}[c x])}{(d + e x)^2} dx$$

Optimal (type 4, 358 leaves, 15 steps):

$$\begin{aligned} & -\frac{\frac{i b g \operatorname{ArcSin}[c x]^2}{2 e^2} - \frac{(e f - d g) (a + b \operatorname{ArcSin}[c x])}{e^2 (d + e x)}}{e^2} + \frac{\frac{b c (e f - d g) \operatorname{ArcTan}\left[\frac{e + c^2 d x}{\sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2}}\right]}{e^2 \sqrt{c^2 d^2 - e^2}}}{e^2} + \\ & \frac{\frac{b g \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^2} + \frac{b g \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^2} - \frac{b g \operatorname{ArcSin}[c x] \operatorname{Log}[d + e x]}{e^2}}{e^2} + \\ & \frac{\frac{g (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}[d + e x]}{e^2} - \frac{i b g \operatorname{PolyLog}\left[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^2} - \frac{i b g \operatorname{PolyLog}\left[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^2}}{e^2} \end{aligned}$$

Result (type 6, 590 leaves):

$$\begin{aligned}
& \frac{1}{8 e^2} \left( \frac{8 a (-e f + d g)}{d + e x} - 8 b f \left( \frac{c \sqrt{\frac{e \left( -\sqrt{\frac{1}{c^2}} + x \right)}{d+e x}} \sqrt{\frac{e \left( \sqrt{\frac{1}{c^2}} + x \right)}{d+e x}} \text{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{d_- \sqrt{\frac{1}{c^2}} e}{d+e x}, \frac{d_+ \sqrt{\frac{1}{c^2}} e}{d+e x}\right]} + \frac{e \text{ArcSin}[c x]}{d + e x} \right) \right) + 8 a g \text{Log}[d + e x] + \right. \\
& b g \left( \frac{\frac{8 d \text{ArcSin}[c x]}{d + e x} - 32 i \text{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] \text{ArcTan}\left[\frac{(c d - e) \cot\left[\frac{1}{4}(\pi + 2 \text{ArcSin}[c x])\right]}{\sqrt{c^2 d^2 - e^2}}\right]}{\pi + 4 \text{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] - 2 \text{ArcSin}[c x]} \right. \text{Log}\left[1 - \frac{i(-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \text{ArcSin}[c x]}}{e}\right] - \\
& 4 \left( \frac{\pi - 4 \text{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] - 2 \text{ArcSin}[c x]}{\pi + 4 \text{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] - 2 \text{ArcSin}[c x]} \right) \text{Log}\left[1 + \frac{i(c d + \sqrt{c^2 d^2 - e^2}) e^{-i \text{ArcSin}[c x]}}{e}\right] + 4 (\pi - 2 \text{ArcSin}[c x]) \text{Log}[c (d + e x)] + \\
& 8 \text{ArcSin}[c x] \text{Log}[c (d + e x)] - \frac{8 c d \left( \text{Log}[d + e x] - \text{Log}[e + c^2 d x + \sqrt{-c^2 d^2 + e^2} \sqrt{1 - c^2 x^2}] \right)}{\sqrt{-c^2 d^2 + e^2}} + \\
& \left. 8 i \left( \text{PolyLog}\left[2, \frac{i(-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \text{ArcSin}[c x]}}{e}\right] + \text{PolyLog}\left[2, -\frac{i(c d + \sqrt{c^2 d^2 - e^2}) e^{-i \text{ArcSin}[c x]}}{e}\right] \right) \right)
\end{aligned}$$

Problem 100: Result more than twice size of optimal antiderivative.

$$\int \frac{(f + g x + h x^2) (a + b \text{ArcSin}[c x])}{d + e x} dx$$

Optimal (type 4, 459 leaves, 15 steps):

$$\begin{aligned}
& \frac{b (4 (e g - d h) + e h x) \sqrt{1 - c^2 x^2}}{4 c e^2} - \frac{b h \operatorname{ArcSin}[c x]}{4 c^2 e} - \frac{\frac{i}{2} b (e^2 f - d e g + d^2 h) \operatorname{ArcSin}[c x]^2}{2 e^3} + \frac{(e g - d h) x (a + b \operatorname{ArcSin}[c x])}{e^2} + \\
& \frac{h x^2 (a + b \operatorname{ArcSin}[c x])}{2 e} + \frac{b (e^2 f - d e g + d^2 h) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^3} + \frac{b (e^2 f - d e g + d^2 h) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^3} - \\
& \frac{b (e^2 f - d e g + d^2 h) \operatorname{ArcSin}[c x] \operatorname{Log}[d + e x]}{e^3} + \frac{(e^2 f - d e g + d^2 h) (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}[d + e x]}{e^3} - \\
& \frac{\frac{i}{2} b (e^2 f - d e g + d^2 h) \operatorname{PolyLog}\left[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^3} - \frac{\frac{i}{2} b (e^2 f - d e g + d^2 h) \operatorname{PolyLog}\left[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^3}
\end{aligned}$$

Result (type 4, 1436 leaves):

$$\begin{aligned}
& \frac{a (e g - d h) x}{e^2} + \frac{a h x^2}{2 e} + \frac{(a e^2 f - a d e g + a d^2 h) \operatorname{Log}[d + e x]}{e^3} + \\
& \frac{1}{8 e} b f \left( \frac{i (\pi - 2 \operatorname{ArcSin}[c x])^2 - 32 i \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] \operatorname{ArcTan}\left[\frac{(c d - e) \operatorname{Cot}\left[\frac{1}{4}(\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{c^2 d^2 - e^2}}\right]}{\sqrt{c^2 d^2 - e^2}} \right. - \\
& 4 \left( \pi + 4 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log}\left[1 - \frac{i (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] - \\
& 4 \left( \pi - 4 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log}\left[1 + \frac{i (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] + 4 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c d + c e x] + \\
& 8 \operatorname{ArcSin}[c x] \operatorname{Log}[c d + c e x] + 8 i \left( \operatorname{PolyLog}\left[2, \frac{i (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] + \operatorname{PolyLog}\left[2, -\frac{i (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{c e} b g \left( \sqrt{1 - c^2 x^2} + c x \operatorname{ArcSin}[c x] - \frac{1}{8 e} c d \left( \frac{\pi - 2 \operatorname{ArcSin}[c x]}{8} \right)^2 - 32 \frac{i}{\sqrt{2}} \operatorname{ArcSin}\left[ \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right] \operatorname{ArcTan}\left[ \frac{(c d - e) \operatorname{Cot}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{c^2 d^2 - e^2}} \right] - \right. \\
& \quad \left. 4 \left( \pi + 4 \operatorname{ArcSin}\left[ \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log}\left[ 1 - \frac{i (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] - 4 \left( \pi - 4 \operatorname{ArcSin}\left[ \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \right. \\
& \quad \left. \operatorname{Log}\left[ 1 + \frac{i (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] + 4 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c d + c e x] + 8 \operatorname{ArcSin}[c x] \operatorname{Log}[c d + c e x] + \right. \\
& \quad \left. 8 i \left( \operatorname{PolyLog}\left[ 2, \frac{i (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] + \operatorname{PolyLog}\left[ 2, -\frac{i (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] \right) \right) + \\
& \frac{1}{8 c^2 e^3} b h \left( \frac{i c^2 d^2 \pi^2 - 8 c d e \sqrt{1 - c^2 x^2} - 4 i c^2 d^2 \pi \operatorname{ArcSin}[c x] - 8 c^2 d e x \operatorname{ArcSin}[c x] + 4 i c^2 d^2 \operatorname{ArcSin}[c x]^2 -}{\sqrt{1 + \frac{c d}{e}}} \right. \\
& \quad \left. 32 i c^2 d^2 \operatorname{ArcSin}\left[ \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right] \operatorname{ArcTan}\left[ \frac{(c d - e) \operatorname{Cot}\left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{c^2 d^2 - e^2}} \right] - 2 e^2 \operatorname{ArcSin}[c x] \operatorname{Cos}[2 \operatorname{ArcSin}[c x]] - \right. \\
& \quad \left. 4 c^2 d^2 \pi \operatorname{Log}\left[ 1 - \frac{i (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] - 16 c^2 d^2 \operatorname{ArcSin}\left[ \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right] \operatorname{Log}\left[ 1 - \frac{i (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] + \right. \\
& \quad \left. 8 c^2 d^2 \operatorname{ArcSin}[c x] \operatorname{Log}\left[ 1 - \frac{i (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] - 4 c^2 d^2 \pi \operatorname{Log}\left[ 1 + \frac{i (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] + \right. \\
& \quad \left. 16 c^2 d^2 \operatorname{ArcSin}\left[ \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right] \operatorname{Log}\left[ 1 + \frac{i (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] + 8 c^2 d^2 \operatorname{ArcSin}[c x] \operatorname{Log}\left[ 1 + \frac{i (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] + \right)
\end{aligned}$$

$$4 c^2 d^2 \pi \operatorname{Log}[c d + c e x] + 8 i c^2 d^2 \operatorname{PolyLog}[2, \frac{i (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}] + \\ 8 i c^2 d^2 \operatorname{PolyLog}[2, -\frac{i (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}] + e^2 \sin[2 \operatorname{ArcSin}[c x]] \Bigg)$$

**Problem 101:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(f + g x + h x^2) (a + b \operatorname{ArcSin}[c x])}{(d + e x)^2} dx$$

Optimal (type 4, 460 leaves, 16 steps):

$$\begin{aligned} & \frac{b h \sqrt{1 - c^2 x^2}}{c e^2} - \frac{i b (e g - 2 d h) \operatorname{ArcSin}[c x]^2}{2 e^3} + \frac{h x (a + b \operatorname{ArcSin}[c x])}{e^2} - \frac{(e^2 f - d e g + d^2 h) (a + b \operatorname{ArcSin}[c x])}{e^3 (d + e x)} + \\ & \frac{b c (e^2 f - d e g + d^2 h) \operatorname{ArcTan}\left[\frac{e + c^2 d x}{\sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2}}\right]}{e^3 \sqrt{c^2 d^2 - e^2}} + \frac{b (e g - 2 d h) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^3} + \\ & \frac{b (e g - 2 d h) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^3} - \frac{b (e g - 2 d h) \operatorname{ArcSin}[c x] \operatorname{Log}[d + e x]}{e^3} + \\ & \frac{(e g - 2 d h) (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}[d + e x]}{e^3} - \frac{i b (e g - 2 d h) \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}]}{e^3} - \frac{i b (e g - 2 d h) \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}]}{e^3} \end{aligned}$$

Result (type 6, 1119 leaves):

$$\begin{aligned} & \frac{a h x}{e^2} + \frac{-a e^2 f + a d e g - a d^2 h}{e^3 (d + e x)} + b f \left( -\frac{c \sqrt{1 + \frac{-d - \sqrt{\frac{1}{c^2}} e}{d + e x}} \sqrt{1 + \frac{-d + \sqrt{\frac{1}{c^2}} e}{d + e x}} \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, -\frac{-d + \sqrt{\frac{1}{c^2}} e}{d + e x}, -\frac{-d - \sqrt{\frac{1}{c^2}} e}{d + e x}\right]}{e^2 \sqrt{1 - c^2 x^2}} - \frac{\operatorname{ArcSin}[c x]}{e (d + e x)} \right) + \end{aligned}$$

$$\begin{aligned}
& \frac{(a e g - 2 a d h) \operatorname{Log}[d + e x]}{e^3} + b h \left( \frac{\sqrt{1 - c^2 x^2} + c x \operatorname{ArcSin}[c x]}{c e^2} + \frac{d^2 \left( -\frac{\operatorname{ArcSin}[c x]}{d + e x} + \frac{c (\operatorname{Log}[d + e x] - \operatorname{Log}[e + c^2 d x + \sqrt{-c^2 d^2 + e^2} \sqrt{1 - c^2 x^2}])}{\sqrt{-c^2 d^2 + e^2}} \right)}{e^3} \right) - \\
& \frac{1}{4 e^3} d \left( \frac{i (\pi - 2 \operatorname{ArcSin}[c x])^2 - 32 i \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] \operatorname{ArcTan}\left[\frac{(c d - e) \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{c^2 d^2 - e^2}}\right]}{\pi + 4 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] - 2 \operatorname{ArcSin}[c x]} \right) \operatorname{Log}\left[1 - \frac{i (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] - 4 \left( \frac{\sqrt{1 + \frac{c d}{e}}}{\pi - 4 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] - 2 \operatorname{ArcSin}[c x]} \right) \\
& \operatorname{Log}\left[1 + \frac{i (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] + 4 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c d + c e x] + 8 \operatorname{ArcSin}[c x] \operatorname{Log}[c d + c e x] + \\
& 8 i \left( \operatorname{PolyLog}\left[2, \frac{i (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] + \operatorname{PolyLog}\left[2, -\frac{i (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] \right) + \\
& b g \left( -\frac{d \left( -\frac{\operatorname{ArcSin}[c x]}{d + e x} + \frac{c (\operatorname{Log}[d + e x] - \operatorname{Log}[e + c^2 d x + \sqrt{-c^2 d^2 + e^2} \sqrt{1 - c^2 x^2}])}{\sqrt{-c^2 d^2 + e^2}} \right)}{e^2} + \frac{1}{8 e^2} \left( \frac{i (\pi - 2 \operatorname{ArcSin}[c x])^2 - 32 i \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right]}{\pi + 4 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] - 2 \operatorname{ArcSin}[c x]} \right) \operatorname{Log}\left[1 - \frac{i (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] - \right. \\
& \left. \operatorname{ArcTan}\left[\frac{(c d - e) \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{c^2 d^2 - e^2}}\right] - 4 \left( \frac{\sqrt{1 + \frac{c d}{e}}}{\pi + 4 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] - 2 \operatorname{ArcSin}[c x]} \right) \operatorname{Log}\left[1 - \frac{i (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] \right)
\end{aligned}$$

$$\begin{aligned}
& 4 \left( \pi - 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{cd}{e}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[cx] \right) \operatorname{Log} \left[ 1 + \frac{\frac{i}{e} \left( cd + \sqrt{c^2 d^2 - e^2} \right) e^{-i \operatorname{ArcSin}[cx]}}{e} \right] + 4 (\pi - 2 \operatorname{ArcSin}[cx]) \operatorname{Log}[cd + ce x] + \\
& 8 \operatorname{ArcSin}[cx] \operatorname{Log}[cd + ce x] + 8 \frac{i}{e} \left( \operatorname{PolyLog}[2, \frac{\frac{i}{e} \left( -cd + \sqrt{c^2 d^2 - e^2} \right) e^{-i \operatorname{ArcSin}[cx]}}{e}] + \operatorname{PolyLog}[2, -\frac{\frac{i}{e} \left( cd + \sqrt{c^2 d^2 - e^2} \right) e^{-i \operatorname{ArcSin}[cx]}}{e}] \right)
\end{aligned}$$

**Problem 102:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(f + g x + h x^2) (a + b \operatorname{ArcSin}[cx])}{(d + e x)^3} dx$$

Optimal (type 4, 488 leaves, 16 steps):

$$\begin{aligned}
& \frac{b c (e^2 f - d e g + d^2 h) \sqrt{1 - c^2 x^2}}{2 e^2 (c^2 d^2 - e^2) (d + e x)} - \frac{\frac{i}{e} b h \operatorname{ArcSin}[cx]^2}{2 e^3} - \frac{(e^2 f - d e g + d^2 h) (a + b \operatorname{ArcSin}[cx])}{2 e^3 (d + e x)^2} - \\
& \frac{(e g - 2 d h) (a + b \operatorname{ArcSin}[cx])}{e^3 (d + e x)} - \frac{b c (2 e^2 (e g - 2 d h) - c^2 d (e^2 f + d e g - 3 d^2 h)) \operatorname{ArcTan}[\frac{e + c^2 d x}{\sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2}}]}{2 e^3 (c^2 d^2 - e^2)^{3/2}} + \\
& \frac{b h \operatorname{ArcSin}[cx] \operatorname{Log}[1 - \frac{\frac{i}{e} e^{i \operatorname{ArcSin}[cx]}}{c d - \sqrt{c^2 d^2 - e^2}}]}{e^3} + \frac{b h \operatorname{ArcSin}[cx] \operatorname{Log}[1 - \frac{\frac{i}{e} e^{i \operatorname{ArcSin}[cx]}}{c d + \sqrt{c^2 d^2 - e^2}}]}{e^3} - \frac{b h \operatorname{ArcSin}[cx] \operatorname{Log}[d + e x]}{e^3} + \\
& \frac{h (a + b \operatorname{ArcSin}[cx]) \operatorname{Log}[d + e x]}{e^3} - \frac{\frac{i}{e} b h \operatorname{PolyLog}[2, \frac{\frac{i}{e} e^{i \operatorname{ArcSin}[cx]}}{c d - \sqrt{c^2 d^2 - e^2}}]}{e^3} - \frac{\frac{i}{e} b h \operatorname{PolyLog}[2, \frac{\frac{i}{e} e^{i \operatorname{ArcSin}[cx]}}{c d + \sqrt{c^2 d^2 - e^2}}]}{e^3}
\end{aligned}$$

Result (type 6, 1144 leaves):

$$\frac{-a e^2 f + a d e g - a d^2 h}{2 e^3 (d + e x)^2} + \frac{-a e g + 2 a d h}{e^3 (d + e x)}$$

$$b f \left( -\frac{c \sqrt{1 + \frac{-d - \sqrt{\frac{1}{c^2}} e}{d + e x}} \sqrt{1 + \frac{-d + \sqrt{\frac{1}{c^2}} e}{d + e x}} \text{AppellF1}\left[2, \frac{1}{2}, \frac{1}{2}, 3, -\frac{-d + \sqrt{\frac{1}{c^2}} e}{d + e x}, -\frac{-d - \sqrt{\frac{1}{c^2}} e}{d + e x}\right]}{4 e^2 (d + e x) \sqrt{1 - c^2 x^2}} - \frac{\text{ArcSin}[c x]}{2 e (d + e x)^2} \right) + \frac{a h \log[d + e x]}{e^3} +$$

$$b g \left( -\frac{d \left( \frac{c \sqrt{1 - c^2 x^2}}{(c^2 d^2 - e^2) (d + e x)} - \frac{\text{ArcSin}[c x]}{e (d + e x)^2} - \frac{i c^3 d \left( \text{Log}[4] + \text{Log}\left[ \frac{e^2 \sqrt{c^2 d^2 - e^2} (i e + i c^2 d x + \sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2})}{c^3 d (d + e x)} \right] \right)}{(c d - e) e (c d + e) \sqrt{c^2 d^2 - e^2}} \right)}{2 e} + \frac{-\frac{\text{ArcSin}[c x]}{d + e x} + \frac{c \left( \text{Log}[d + e x] - \text{Log}\left[ e + c^2 d x + \sqrt{-c^2 d^2 + e^2} \sqrt{1 - c^2 x^2} \right] \right)}{\sqrt{-c^2 d^2 + e^2}}}{e^2} \right) +$$

$$b h \left( \frac{d^2 \left( \frac{c \sqrt{1 - c^2 x^2}}{(c^2 d^2 - e^2) (d + e x)} - \frac{\text{ArcSin}[c x]}{e (d + e x)^2} - \frac{i c^3 d \left( \text{Log}[4] + \text{Log}\left[ \frac{e^2 \sqrt{c^2 d^2 - e^2} (i e + i c^2 d x + \sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2})}{c^3 d (d + e x)} \right] \right)}{(c d - e) e (c d + e) \sqrt{c^2 d^2 - e^2}} \right)}{2 e^2} - \frac{2 d \left( -\frac{\text{ArcSin}[c x]}{d + e x} + \frac{c \left( \text{Log}[d + e x] - \text{Log}\left[ e + c^2 d x + \sqrt{-c^2 d^2 + e^2} \sqrt{1 - c^2 x^2} \right] \right)}{\sqrt{-c^2 d^2 + e^2}} \right)}{e^3} \right) +$$

$$\frac{1}{8 e^3} \left( \frac{1}{\pi - 2 \text{ArcSin}[c x]} - 32 \frac{i}{\sqrt{2}} \text{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] \text{ArcTan}\left[\frac{(c d - e) \cot\left(\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])\right)}{\sqrt{c^2 d^2 - e^2}}\right] - \right.$$

$$\left. 4 \left( \frac{\pi + 4 \text{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] - 2 \text{ArcSin}[c x]}{\sqrt{2}} \right) \text{Log}\left[1 - \frac{e^{-i \text{ArcSin}[c x]}}{e}\right] - \right)$$

$$\begin{aligned}
& 4 \left( \pi - 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{cd}{e}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[cx] \right) \operatorname{Log} \left[ 1 + \frac{i \left( cd + \sqrt{c^2 d^2 - e^2} \right) e^{-i \operatorname{ArcSin}[cx]}}{e} \right] + 4 (\pi - 2 \operatorname{ArcSin}[cx]) \operatorname{Log}[cd + ce x] + \\
& 8 \operatorname{ArcSin}[cx] \operatorname{Log}[cd + ce x] + 8 i \left( \operatorname{PolyLog}[2, \frac{i \left( -cd + \sqrt{c^2 d^2 - e^2} \right) e^{-i \operatorname{ArcSin}[cx]}}{e}] + \operatorname{PolyLog}[2, -\frac{i \left( cd + \sqrt{c^2 d^2 - e^2} \right) e^{-i \operatorname{ArcSin}[cx]}}{e}] \right) \Bigg)
\end{aligned}$$

**Problem 109: Result more than twice size of optimal antiderivative.**

$$\int \frac{(f + g x + h x^2 + i x^3) (a + b \operatorname{ArcSin}[cx])}{d + e x} dx$$

Optimal (type 4, 623 leaves, 16 steps):

$$\begin{aligned}
& \frac{b i x^2 \sqrt{1 - c^2 x^2}}{d + e x} + \frac{b (4 (2 e^2 i + 9 c^2 (e^2 g - d e h + d^2 i)) + 9 c^2 e (e h - d i) x) \sqrt{1 - c^2 x^2}}{36 c^3 e^3} - \\
& \frac{9 c e}{4 c^2 e^2} \frac{b (e h - d i) \operatorname{ArcSin}[cx]}{2 e^4} - \frac{i b (e^3 f - d e^2 g + d^2 e h - d^3 i) \operatorname{ArcSin}[cx]^2}{2 e^4} + \\
& \frac{(e^2 g - d e h + d^2 i) x (a + b \operatorname{ArcSin}[cx])}{e^3} + \frac{(e h - d i) x^2 (a + b \operatorname{ArcSin}[cx])}{2 e^2} + \frac{i x^3 (a + b \operatorname{ArcSin}[cx])}{3 e} + \\
& \frac{b (e^3 f - d e^2 g + d^2 e h - d^3 i) \operatorname{ArcSin}[cx] \operatorname{Log} \left[ 1 - \frac{i e e^{i \operatorname{ArcSin}[cx]}}{c d - \sqrt{c^2 d^2 - e^2}} \right]}{e^4} + \frac{b (e^3 f - d e^2 g + d^2 e h - d^3 i) \operatorname{ArcSin}[cx] \operatorname{Log} \left[ 1 - \frac{i e e^{i \operatorname{ArcSin}[cx]}}{c d + \sqrt{c^2 d^2 - e^2}} \right]}{e^4} - \\
& \frac{b (e^3 f - d e^2 g + d^2 e h - d^3 i) \operatorname{ArcSin}[cx] \operatorname{Log}[d + e x]}{e^4} + \frac{(e^3 f - d e^2 g + d^2 e h - d^3 i) (a + b \operatorname{ArcSin}[cx]) \operatorname{Log}[d + e x]}{e^4} - \\
& \frac{i b (e^3 f - d e^2 g + d^2 e h - d^3 i) \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[cx]}}{c d - \sqrt{c^2 d^2 - e^2}}]}{e^4} - \frac{i b (e^3 f - d e^2 g + d^2 e h - d^3 i) \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[cx]}}{c d + \sqrt{c^2 d^2 - e^2}}]}{e^4}
\end{aligned}$$

Result (type 4, 2189 leaves):

$$\begin{aligned}
& \frac{a(e^2 g - d e h + d^2 i) x}{e^3} + \frac{a(e h - d i) x^2}{2 e^2} + \frac{a i x^3}{3 e} + \frac{(a e^3 f - a d e^2 g + a d^2 e h - a d^3 i) \operatorname{Log}[d + e x]}{e^4} + \\
& \frac{1}{8 e} b f \left( \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right) \operatorname{ArcTan} \left[ \frac{(c d - e) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{c^2 d^2 - e^2}} \right] - \\
& 4 \left( \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right) \operatorname{Log} \left[ 1 - \frac{\frac{i}{e} (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] - \\
& 4 \left( \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right) \operatorname{Log} \left[ 1 + \frac{\frac{i}{e} (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] + 4 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c d + c e x] + \\
& 8 \operatorname{ArcSin}[c x] \operatorname{Log}[c d + c e x] + 8 \frac{i}{e} \left( \operatorname{PolyLog}[2, \frac{\frac{i}{e} (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}] + \operatorname{PolyLog}[2, -\frac{\frac{i}{e} (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}] \right) + \\
& \frac{1}{c e} b g \left( \sqrt{1 - c^2 x^2} + c x \operatorname{ArcSin}[c x] - \frac{1}{8 e} c d \left( \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right) \operatorname{ArcTan} \left[ \frac{(c d - e) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{c^2 d^2 - e^2}} \right] - \right. \\
& \left. 4 \left( \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right) \operatorname{Log} \left[ 1 - \frac{\frac{i}{e} (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] - 4 \left( \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right) \operatorname{Log} \left[ 1 + \frac{\frac{i}{e} (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] \right. \\
& \left. \operatorname{Log} \left[ 1 + \frac{\frac{i}{e} (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] + 4 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c d + c e x] + 8 \operatorname{ArcSin}[c x] \operatorname{Log}[c d + c e x] + \right)
\end{aligned}$$

$$\begin{aligned}
& 8 \operatorname{Im} \left( \operatorname{PolyLog}[2, \frac{\frac{i}{e} (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}] + \operatorname{PolyLog}[2, -\frac{\frac{i}{e} (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}] \right) + \\
& \frac{1}{8 c^2 e^3} b h \left( \frac{i c^2 d^2 \pi^2 - 8 c d e \sqrt{1 - c^2 x^2} - 4 i c^2 d^2 \pi \operatorname{ArcSin}[c x] - 8 c^2 d e x \operatorname{ArcSin}[c x] + 4 i c^2 d^2 \operatorname{ArcSin}[c x]^2 -}{\sqrt{1 + \frac{c d}{e}}} \right. \\
& 32 i c^2 d^2 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] \operatorname{ArcTan}\left[\frac{(c d - e) \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{c^2 d^2 - e^2}}\right] - 2 e^2 \operatorname{ArcSin}[c x] \operatorname{Cos}[2 \operatorname{ArcSin}[c x]] - \\
& 4 c^2 d^2 \pi \operatorname{Log}\left[1 - \frac{\frac{i}{e} (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] - 16 c^2 d^2 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] \operatorname{Log}\left[1 - \frac{\frac{i}{e} (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] + \\
& 8 c^2 d^2 \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{\frac{i}{e} (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] - 4 c^2 d^2 \pi \operatorname{Log}\left[1 + \frac{\frac{i}{e} (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] + \\
& 16 c^2 d^2 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}}\right] \operatorname{Log}\left[1 + \frac{\frac{i}{e} (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] + 8 c^2 d^2 \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{\frac{i}{e} (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] + \\
& 4 c^2 d^2 \pi \operatorname{Log}[c d + c e x] + 8 i c^2 d^2 \operatorname{PolyLog}[2, \frac{\frac{i}{e} (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}] + \\
& \left. 8 i c^2 d^2 \operatorname{PolyLog}[2, -\frac{\frac{i}{e} (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}] + e^2 \operatorname{Sin}[2 \operatorname{ArcSin}[c x]] \right\} - \\
& \frac{1}{72 c^3 e^4} b i \left( 9 i c^3 d^3 \pi^2 - 72 c^2 d^2 e \sqrt{1 - c^2 x^2} - 18 e^3 \sqrt{1 - c^2 x^2} - 36 i c^3 d^3 \pi \operatorname{ArcSin}[c x] - 72 c^3 d^2 e x \operatorname{ArcSin}[c x] - \right.
\end{aligned}$$

$$\begin{aligned}
& 18 c e^3 x \operatorname{ArcSin}[c x] + 36 i c^3 d^3 \operatorname{ArcSin}[c x]^2 - 288 i c^3 d^3 \operatorname{ArcSin}\left[\frac{\sqrt{1+\frac{c d}{e}}}{\sqrt{2}}\right] \operatorname{Arctan}\left[\frac{(c d-e) \operatorname{Cot}\left[\frac{1}{4}(\pi+2 \operatorname{ArcSin}[c x])\right]}{\sqrt{c^2 d^2-e^2}}\right] - \\
& 18 c d e^2 \operatorname{ArcSin}[c x] \cos[2 \operatorname{ArcSin}[c x]] + 2 e^3 \cos[3 \operatorname{ArcSin}[c x]] - 36 c^3 d^3 \pi \log\left[1-\frac{i(-c d+\sqrt{c^2 d^2-e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] - \\
& 144 c^3 d^3 \operatorname{ArcSin}\left[\frac{\sqrt{1+\frac{c d}{e}}}{\sqrt{2}}\right] \log\left[1-\frac{i(-c d+\sqrt{c^2 d^2-e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] + \\
& 72 c^3 d^3 \operatorname{ArcSin}[c x] \log\left[1-\frac{i(-c d+\sqrt{c^2 d^2-e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] - 36 c^3 d^3 \pi \log\left[1+\frac{i(c d+\sqrt{c^2 d^2-e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] + \\
& 144 c^3 d^3 \operatorname{ArcSin}\left[\frac{\sqrt{1+\frac{c d}{e}}}{\sqrt{2}}\right] \log\left[1+\frac{i(c d+\sqrt{c^2 d^2-e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] + 72 c^3 d^3 \operatorname{ArcSin}[c x] \log\left[1+\frac{i(c d+\sqrt{c^2 d^2-e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] + \\
& 36 c^3 d^3 \pi \log[c d+c e x] + 72 i c^3 d^3 \operatorname{PolyLog}[2, \frac{i(-c d+\sqrt{c^2 d^2-e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}] + \\
& 72 i c^3 d^3 \operatorname{PolyLog}\left[2, -\frac{i(c d+\sqrt{c^2 d^2-e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] + 9 c d e^2 \sin[2 \operatorname{ArcSin}[c x]] + 6 e^3 \operatorname{ArcSin}[c x] \sin[3 \operatorname{ArcSin}[c x]] \Bigg)
\end{aligned}$$

**Problem 110:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(f+g x+h x^2+i x^3)(a+b \operatorname{ArcSin}[c x])}{(d+e x)^2} dx$$

Optimal (type 4, 617 leaves, 18 steps):

$$\begin{aligned}
& \frac{b(eh - 2di)\sqrt{1 - c^2x^2}}{ce^3} + \frac{bix\sqrt{1 - c^2x^2}}{4ce^2} - \frac{bi \operatorname{ArcSin}[cx]}{4c^2e^2} - \frac{\frac{i}{2}b(e^2g - 2deh + 3d^2i) \operatorname{ArcSin}[cx]^2}{2e^4} + \frac{(eh - 2di)(a + b \operatorname{ArcSin}[cx])}{e^3} + \\
& \frac{ix^2(a + b \operatorname{ArcSin}[cx])}{2e^2} - \frac{(e^3f - de^2g + d^2eh - d^3i)(a + b \operatorname{ArcSin}[cx])}{e^4(d + ex)} + \frac{bc(e^3f - de^2g + d^2eh - d^3i) \operatorname{ArcTan}\left[\frac{e + c^2dx}{\sqrt{c^2d^2 - e^2}\sqrt{1 - c^2x^2}}\right]}{e^4\sqrt{c^2d^2 - e^2}} + \\
& \frac{b(e^2g - 2deh + 3d^2i) \operatorname{ArcSin}[cx] \operatorname{Log}\left[1 - \frac{\frac{i}{2}e \operatorname{e}^{i \operatorname{ArcSin}[cx]}}{cd - \sqrt{c^2d^2 - e^2}}\right]}{e^4} + \frac{b(e^2g - 2deh + 3d^2i) \operatorname{ArcSin}[cx] \operatorname{Log}\left[1 - \frac{\frac{i}{2}e \operatorname{e}^{i \operatorname{ArcSin}[cx]}}{cd + \sqrt{c^2d^2 - e^2}}\right]}{e^4} - \\
& \frac{b(e^2g - 2deh + 3d^2i) \operatorname{ArcSin}[cx] \operatorname{Log}(d + ex)}{e^4} + \frac{(e^2g - 2deh + 3d^2i)(a + b \operatorname{ArcSin}[cx]) \operatorname{Log}(d + ex)}{e^4} - \\
& \frac{\frac{i}{2}b(e^2g - 2deh + 3d^2i) \operatorname{PolyLog}\left[2, \frac{\frac{i}{2}e \operatorname{e}^{i \operatorname{ArcSin}[cx]}}{cd - \sqrt{c^2d^2 - e^2}}\right]}{e^4} - \frac{\frac{i}{2}b(e^2g - 2deh + 3d^2i) \operatorname{PolyLog}\left[2, \frac{\frac{i}{2}e \operatorname{e}^{i \operatorname{ArcSin}[cx]}}{cd + \sqrt{c^2d^2 - e^2}}\right]}{e^4}
\end{aligned}$$

Result (type 6, 1688 leaves):

$$\begin{aligned}
& \frac{a(eh - 2di)x}{e^3} + \frac{aix^2}{2e^2} + \frac{-ae^3f + ad^2e^2g - ad^2eh + ad^3i}{e^4(d + ex)} + \\
& b f \left( -\frac{c \sqrt{1 + \frac{-d - \sqrt{\frac{1}{c^2}}e}{d + ex}} \sqrt{1 + \frac{-d + \sqrt{\frac{1}{c^2}}e}{d + ex}} \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, -\frac{-d + \sqrt{\frac{1}{c^2}}e}{d + ex}, -\frac{-d - \sqrt{\frac{1}{c^2}}e}{d + ex}\right] - \frac{\operatorname{ArcSin}[cx]}{e(d + ex)} \right) + \\
& \frac{(ae^2g - 2ad^2eh + 3ad^2i) \operatorname{Log}(d + ex)}{e^4} + b i \left( -\frac{2d(\sqrt{1 - c^2x^2} + cx \operatorname{ArcSin}[cx])}{ce^3} + \right. \\
& \left. \frac{\frac{1}{2} \left( \frac{1}{2}cx\sqrt{1 - c^2x^2} - \frac{1}{2}\operatorname{ArcSin}[cx] \right) + \frac{1}{2}c^2x^2\operatorname{ArcSin}[cx]}{c^2e^2} - \frac{d^3 \left( -\frac{\operatorname{ArcSin}[cx]}{d + ex} + \frac{c(\operatorname{Log}[d + ex] - \operatorname{Log}[e + c^2dx + \sqrt{-c^2d^2 + e^2}\sqrt{1 - c^2x^2}])}{\sqrt{-c^2d^2 + e^2}} \right)}{e^4} \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{8 e^4} 3 d^2 \left( \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right) \operatorname{ArcTan} \left[ \frac{(c d - e) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{c^2 d^2 - e^2}} \right] - \\
& 4 \left( \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log} \left[ 1 - \frac{\frac{i}{e} (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] - 4 \left( \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \\
& \operatorname{Log} \left[ 1 + \frac{\frac{i}{e} (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] + 4 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c d + c e x] + 8 \operatorname{ArcSin}[c x] \operatorname{Log}[c d + c e x] + \\
& 8 i \left( \operatorname{PolyLog} \left[ 2, \frac{\frac{i}{e} (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] + \operatorname{PolyLog} \left[ 2, -\frac{\frac{i}{e} (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] \right) + \\
& b h \left( \frac{\sqrt{1 - c^2 x^2} + c x \operatorname{ArcSin}[c x]}{c e^2} + \frac{d^2 \left( -\frac{\operatorname{ArcSin}[c x]}{d + e x} + \frac{c (\operatorname{Log}[d + e x] - \operatorname{Log}[e + c^2 d x + \sqrt{-c^2 d^2 + e^2}] \sqrt{1 - c^2 x^2})}{\sqrt{-c^2 d^2 + e^2}} \right)}{e^3} - \right. \\
& \left. \frac{1}{4 e^3} d \left( \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right] - 32 i \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right] \operatorname{ArcTan} \left[ \frac{(c d - e) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{c^2 d^2 - e^2}} \right] \right. \right. \\
& \left. \left. 4 \left( \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log} \left[ 1 - \frac{\frac{i}{e} (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e} \right] - 4 \left( \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{c d}{e}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \right]
\end{aligned}$$

$$\begin{aligned}
& \text{Log}\left[1 + \frac{\frac{i}{2} \left(c d + \sqrt{c^2 d^2 - e^2}\right) e^{-i \text{ArcSin}[c x]}}{e}\right] + 4 (\pi - 2 \text{ArcSin}[c x]) \text{Log}[c d + c e x] + 8 \text{ArcSin}[c x] \text{Log}[c d + c e x] + \\
& 8 i \left( \text{PolyLog}\left[2, \frac{\frac{i}{2} \left(-c d + \sqrt{c^2 d^2 - e^2}\right) e^{-i \text{ArcSin}[c x]}}{e}\right] + \text{PolyLog}\left[2, -\frac{\frac{i}{2} \left(c d + \sqrt{c^2 d^2 - e^2}\right) e^{-i \text{ArcSin}[c x]}}{e}\right] \right) + \\
& b g \left( -\frac{d \left( -\frac{\text{ArcSin}[c x]}{d+e x} + \frac{c \left( \text{Log}[d+e x] - \text{Log}[e+c^2 d x + \sqrt{-c^2 d^2+e^2} \sqrt{1-c^2 x^2}] \right)}{\sqrt{-c^2 d^2+e^2}} \right)}{e^2} + \frac{1}{8 e^2} \left( \frac{i}{2} (\pi - 2 \text{ArcSin}[c x])^2 - 32 i \text{ArcSin}\left[\frac{\sqrt{1+\frac{c d}{e}}}{\sqrt{2}}\right] \right. \right. \\
& \text{ArcTan}\left[ \frac{(c d - e) \text{Cot}\left[\frac{1}{4} (\pi + 2 \text{ArcSin}[c x])\right]}{\sqrt{c^2 d^2 - e^2}} \right] - 4 \left( \pi + 4 \text{ArcSin}\left[\frac{\sqrt{1+\frac{c d}{e}}}{\sqrt{2}}\right] - 2 \text{ArcSin}[c x] \right) \text{Log}\left[1 - \frac{\frac{i}{2} \left(-c d + \sqrt{c^2 d^2 - e^2}\right) e^{-i \text{ArcSin}[c x]}}{e}\right] - \\
& \left. \left. 4 \left( \pi - 4 \text{ArcSin}\left[\frac{\sqrt{1+\frac{c d}{e}}}{\sqrt{2}}\right] - 2 \text{ArcSin}[c x] \right) \text{Log}\left[1 + \frac{\frac{i}{2} \left(c d + \sqrt{c^2 d^2 - e^2}\right) e^{-i \text{ArcSin}[c x]}}{e}\right] + 4 (\pi - 2 \text{ArcSin}[c x]) \text{Log}[c d + c e x] + \right. \right. \\
& \left. \left. 8 \text{ArcSin}[c x] \text{Log}[c d + c e x] + 8 i \left( \text{PolyLog}\left[2, \frac{\frac{i}{2} \left(-c d + \sqrt{c^2 d^2 - e^2}\right) e^{-i \text{ArcSin}[c x]}}{e}\right] + \text{PolyLog}\left[2, -\frac{\frac{i}{2} \left(c d + \sqrt{c^2 d^2 - e^2}\right) e^{-i \text{ArcSin}[c x]}}{e}\right] \right) \right)
\end{aligned}$$

**Problem 111: Result unnecessarily involves higher level functions.**

$$\int \frac{(f + g x + h x^2 + i x^3) (a + b \text{ArcSin}[c x])}{(d + e x)^3} dx$$

Optimal (type 4, 1016 leaves, 30 steps):

$$\begin{aligned}
 & \frac{b i \sqrt{1 - c^2 x^2}}{c e^3} + \frac{5 b c d^3 i \sqrt{1 - c^2 x^2}}{2 e^3 (c^2 d^2 - e^2) (d + e x)} - \frac{b c d^2 (3 e h + 4 d i) \sqrt{1 - c^2 x^2}}{2 e^3 (c^2 d^2 - e^2) (d + e x)} + \frac{b c d (e^2 g + 4 d e h - 4 d^2 i) \sqrt{1 - c^2 x^2}}{2 e^3 (c^2 d^2 - e^2) (d + e x)} + \\
 & \frac{b c (e^3 f - 2 d e^2 g + 2 d^3 i) \sqrt{1 - c^2 x^2}}{2 e^3 (c^2 d^2 - e^2) (d + e x)} - \frac{i b (e h - 3 d i) \text{ArcSin}[c x]^2}{2 e^4} + \frac{i x (a + b \text{ArcSin}[c x])}{e^3} - \frac{(e^3 f - d e^2 g + d^2 e h - d^3 i) (a + b \text{ArcSin}[c x])}{2 e^4 (d + e x)^2} - \\
 & \frac{(e^2 g - 2 d e h + 3 d^2 i) (a + b \text{ArcSin}[c x])}{e^4 (d + e x)} + \frac{5 b c^3 d^4 i \text{ArcTan}\left[\frac{e + c^2 d x}{\sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2}}\right]}{2 e^4 (c^2 d^2 - e^2)^{3/2}} - \frac{b c d^2 (3 c^2 d h + 4 e i) \text{ArcTan}\left[\frac{e + c^2 d x}{\sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2}}\right]}{2 e^3 (c^2 d^2 - e^2)^{3/2}} + \\
 & \frac{b c d (4 e^2 (e h - 2 d i) + c^2 (d e^2 g + 4 d^3 i)) \text{ArcTan}\left[\frac{e + c^2 d x}{\sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2}}\right]}{2 e^4 (c^2 d^2 - e^2)^{3/2}} - \frac{b c (2 e^4 g - 6 d^2 e^2 i - c^2 (d e^3 f - 4 d^4 i)) \text{ArcTan}\left[\frac{e + c^2 d x}{\sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2}}\right]}{2 e^4 (c^2 d^2 - e^2)^{3/2}} + \\
 & \frac{b (e h - 3 d i) \text{ArcSin}[c x] \text{Log}\left[1 - \frac{i e e^{i \text{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^4} + \frac{b (e h - 3 d i) \text{ArcSin}[c x] \text{Log}\left[1 - \frac{i e e^{i \text{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^4} - \frac{b (e h - 3 d i) \text{ArcSin}[c x] \text{Log}[d + e x]}{e^4} + \\
 & \frac{(e h - 3 d i) (a + b \text{ArcSin}[c x]) \text{Log}[d + e x]}{e^4} - \frac{\frac{i b (e h - 3 d i) \text{PolyLog}[2, \frac{i e e^{i \text{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}]}{e^4} - \frac{\frac{i b (e h - 3 d i) \text{PolyLog}[2, \frac{i e e^{i \text{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}]}{e^4}}{e^4}
 \end{aligned}$$

Result (type 6, 1844 leaves):

$$\begin{aligned}
 & \frac{a i x}{e^3} + \frac{-a e^3 f + a d e^2 g - a d^2 e h + a d^3 i}{2 e^4 (d + e x)^2} + \frac{-a e^2 g + 2 a d e h - 3 a d^2 i}{e^4 (d + e x)} + \\
 & b f \left( -\frac{c \sqrt{1 + \frac{-d - \sqrt{\frac{1}{c^2}} e}{d + e x}} \sqrt{1 + \frac{-d + \sqrt{\frac{1}{c^2}} e}{d + e x}} \text{AppellF1}\left[2, \frac{1}{2}, \frac{1}{2}, 3, -\frac{-d + \sqrt{\frac{1}{c^2}} e}{d + e x}, -\frac{-d - \sqrt{\frac{1}{c^2}} e}{d + e x}\right]}{4 e^2 (d + e x) \sqrt{1 - c^2 x^2}} - \frac{\text{ArcSin}[c x]}{2 e (d + e x)^2} \right) + \frac{(a e h - 3 a d i) \text{Log}[d + e x]}{e^4} +
 \end{aligned}$$

$$\begin{aligned}
& \text{b g} \left( -\frac{d \left( \frac{c \sqrt{1-c^2 x^2}}{(c^2 d^2-e^2) (d+e x)} - \frac{\text{ArcSin}[c x]}{e (d+e x)^2} - \frac{i c^3 d \left( \text{Log}[4] + \text{Log} \left[ \frac{e^2 \sqrt{c^2 d^2-e^2} (i e + i c^2 d x + \sqrt{c^2 d^2-e^2} \sqrt{1-c^2 x^2})}{c^3 d (d+e x)} \right] \right)}{(c d-e) e (c d+e) \sqrt{c^2 d^2-e^2}} \right)}{2 e} + \frac{-\frac{\text{ArcSin}[c x]}{d+e x} + \frac{c \left( \text{Log}[d+e x] - \text{Log}[e+c^2 d x + \sqrt{-c^2 d^2+e^2} \sqrt{1-c^2 x^2}] \right)}{\sqrt{-c^2 d^2+e^2}}}{e^2} \right) + \\
& \text{b i} \left( \frac{\sqrt{1-c^2 x^2} + c x \text{ArcSin}[c x]}{c e^3} - \frac{d^3 \left( \frac{c \sqrt{1-c^2 x^2}}{(c^2 d^2-e^2) (d+e x)} - \frac{\text{ArcSin}[c x]}{e (d+e x)^2} - \frac{i c^3 d \left( \text{Log}[4] + \text{Log} \left[ \frac{e^2 \sqrt{c^2 d^2-e^2} (i e + i c^2 d x + \sqrt{c^2 d^2-e^2} \sqrt{1-c^2 x^2})}{c^3 d (d+e x)} \right] \right)}{(c d-e) e (c d+e) \sqrt{c^2 d^2-e^2}} \right)}{2 e^3} + \right. \\
& \left. \frac{3 d^2 \left( -\frac{\text{ArcSin}[c x]}{d+e x} + \frac{c \left( \text{Log}[d+e x] - \text{Log}[e+c^2 d x + \sqrt{-c^2 d^2+e^2} \sqrt{1-c^2 x^2}] \right)}{\sqrt{-c^2 d^2+e^2}} \right)}{e^4} - \right. \\
& \left. \frac{1}{8 e^4} 3 d \left( \frac{1}{\pm (\pi - 2 \text{ArcSin}[c x])^2 - 32 \pm \text{ArcSin} \left[ \frac{\sqrt{1+\frac{c d}{e}}}{\sqrt{2}} \right] \text{ArcTan} \left[ \frac{(c d-e) \text{Cot} \left[ \frac{1}{4} (\pi + 2 \text{ArcSin}[c x]) \right]}{\sqrt{c^2 d^2-e^2}} \right]} - \right. \right. \\
& \left. \left. 4 \left( \frac{\sqrt{1+\frac{c d}{e}}}{\sqrt{2}} - 2 \text{ArcSin}[c x] \right) \text{Log} \left[ 1 - \frac{\pm (-c d + \sqrt{c^2 d^2-e^2}) e^{-i \text{ArcSin}[c x]}}{e} \right] - 4 \left( \frac{\sqrt{1+\frac{c d}{e}}}{\sqrt{2}} - 2 \text{ArcSin}[c x] \right) \right. \right. \\
& \left. \left. \text{Log} \left[ 1 + \frac{\pm (c d + \sqrt{c^2 d^2-e^2}) e^{-i \text{ArcSin}[c x]}}{e} \right] + 4 (\pi - 2 \text{ArcSin}[c x]) \text{Log}[c d + c e x] + 8 \text{ArcSin}[c x] \text{Log}[c d + c e x] + \right. \right. 
\end{aligned}$$



$$\left. \left( 8 \operatorname{ArcSin}[c x] \operatorname{Log}[c d + c e x] + 8 i \left[ \operatorname{PolyLog}[2, \frac{i (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}] + \operatorname{PolyLog}[2, -\frac{i (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}] \right) \right) \right\}$$

**Problem 112: Result unnecessarily involves higher level functions.**

$$\int \frac{(f + g x + h x^2 + i x^3) (a + b \operatorname{ArcSin}[c x])}{(d + e x)^4} dx$$

Optimal (type 4, 1278 leaves, 29 steps):

$$\begin{aligned}
& \frac{b c (2 e^2 f - 3 d e g + 6 d^2 h) \sqrt{1 - c^2 x^2}}{12 e^2 (c^2 d^2 - e^2) (d + e x)^2} - \frac{11 b c d^3 i \sqrt{1 - c^2 x^2}}{12 e^3 (c^2 d^2 - e^2) (d + e x)^2} + \frac{b c d^2 (2 e h + 27 d i) \sqrt{1 - c^2 x^2}}{12 e^3 (c^2 d^2 - e^2) (d + e x)^2} + \\
& \frac{b c d (e^2 g - 6 d e h - 18 d^2 i) \sqrt{1 - c^2 x^2}}{12 e^3 (c^2 d^2 - e^2) (d + e x)^2} - \frac{b c (2 e^2 (e g - 4 d h) - c^2 d (2 e^2 f - d e g - 2 d^2 h)) \sqrt{1 - c^2 x^2}}{4 e^2 (c^2 d^2 - e^2)^2 (d + e x)} - \frac{11 b c^3 d^4 i \sqrt{1 - c^2 x^2}}{4 e^3 (c^2 d^2 - e^2)^2 (d + e x)} + \\
& \frac{b c d^2 (18 e^2 i + c^2 d (2 e h + 9 d i)) \sqrt{1 - c^2 x^2}}{4 e^3 (c^2 d^2 - e^2)^2 (d + e x)} - \frac{b c d (4 e^2 (e h + 6 d i) - c^2 d (e^2 g - 2 d e h + 6 d^2 i)) \sqrt{1 - c^2 x^2}}{4 e^3 (c^2 d^2 - e^2)^2 (d + e x)} - \frac{i b i \operatorname{ArcSin}[c x]^2}{2 e^4} - \\
& \frac{(e^3 f - d e^2 g + d^2 e h - d^3 i) (a + b \operatorname{ArcSin}[c x])}{3 e^4 (d + e x)^3} - \frac{(e^2 g - 2 d e h + 3 d^2 i) (a + b \operatorname{ArcSin}[c x])}{2 e^4 (d + e x)^2} - \frac{(e h - 3 d i) (a + b \operatorname{ArcSin}[c x])}{e^4 (d + e x)} + \\
& \frac{b c (4 c^4 d^2 f + 12 e^2 h + c^2 (2 e^2 f - 9 d e g + 6 d^2 h)) \operatorname{ArcTan}\left[\frac{e + c^2 d x}{\sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2}}\right]}{12 e (c^2 d^2 - e^2)^{5/2}} - \frac{11 b c^3 d^3 (2 c^2 d^2 + e^2) i \operatorname{ArcTan}\left[\frac{e + c^2 d x}{\sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2}}\right]}{12 e^4 (c^2 d^2 - e^2)^{5/2}} + \\
& \frac{b c^3 d^2 (4 c^2 d^2 h + e (2 e h + 81 d i)) \operatorname{ArcTan}\left[\frac{e + c^2 d x}{\sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2}}\right]}{12 e^3 (c^2 d^2 - e^2)^{5/2}} + \frac{b c d (2 c^4 d^2 g - 36 e^2 i + c^2 (e^2 g - 18 d e h - 18 d^2 i)) \operatorname{ArcTan}\left[\frac{e + c^2 d x}{\sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2}}\right]}{12 e^2 (c^2 d^2 - e^2)^{5/2}} + \\
& \frac{b i \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^4} + \frac{b i \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^4} - \frac{b i \operatorname{ArcSin}[c x] \operatorname{Log}[d + e x]}{e^4} + \\
& \frac{i (a + b \operatorname{ArcSin}[c x]) \operatorname{Log}[d + e x]}{e^4} - \frac{i b i \operatorname{PolyLog}\left[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^4} - \frac{i b i \operatorname{PolyLog}\left[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^4}
\end{aligned}$$

Result (type 6, 2069 leaves):

$$\begin{aligned}
& \frac{-a e^3 f + a d e^2 g - a d^2 e h + a d^3 i}{3 e^4 (d + e x)^3} + \frac{-a e^2 g + 2 a d e h - 3 a d^2 i}{2 e^4 (d + e x)^2} + \frac{-a e h + 3 a d i}{e^4 (d + e x)} + \\
& b f \left( - \frac{c \sqrt{1 + \frac{-d - \sqrt{\frac{1}{c^2}} e}{d + e x}} \sqrt{1 + \frac{-d + \sqrt{\frac{1}{c^2}} e}{d + e x}} \operatorname{AppellF1}\left[3, \frac{1}{2}, \frac{1}{2}, 4, -\frac{-d + \sqrt{\frac{1}{c^2}} e}{d + e x}, -\frac{-d - \sqrt{\frac{1}{c^2}} e}{d + e x}\right] - \frac{\operatorname{ArcSin}[c x]}{3 e (d + e x)^3} \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{\frac{a i \operatorname{Log}[d+e x]}{e^4} + b h}{e^2} + \\
& - \frac{d \left( \frac{c \sqrt{1-c^2 x^2}}{(c^2 d^2-e^2) (d+e x)} - \frac{\operatorname{ArcSin}[c x]}{e (d+e x)^2} - \frac{i c^3 d \left( \operatorname{Log}[4] + \operatorname{Log} \left[ \frac{e^2 \sqrt{c^2 d^2-e^2} \left( i e+i c^2 d x+\sqrt{c^2 d^2-e^2} \sqrt{1-c^2 x^2} \right)}{c^3 d (d+e x)} \right] \right)}{(c d-e) e (c d+e) \sqrt{c^2 d^2-e^2}} \right)}{e^2} + \\
& - \frac{\frac{\operatorname{ArcSin}[c x]}{d+e x} + \frac{c \left( \operatorname{Log}[d+e x] - \operatorname{Log}[e+c^2 d x+\sqrt{-c^2 d^2+e^2} \sqrt{1-c^2 x^2}] \right)}{\sqrt{-c^2 d^2+e^2}}}{e^3} + \frac{1}{6 e^2} d^2 \left( \frac{\sqrt{1-c^2 x^2} (-c e^2 + c^3 d (4 d + 3 e x))}{(-c^2 d^2 + e^2)^2 (d+e x)^2} - \right. \\
& \left. \frac{2 \operatorname{ArcSin}[c x]}{e (d+e x)^3} + \frac{c^3 (2 c^2 d^2 + e^2) \operatorname{Log}[d+e x]}{e (-c d+e)^2 (c d+e)^2 \sqrt{-c^2 d^2+e^2}} - \frac{c^3 (2 c^2 d^2 + e^2) \operatorname{Log}[e+c^2 d x+\sqrt{-c^2 d^2+e^2} \sqrt{1-c^2 x^2}]}{e (-c d+e)^2 (c d+e)^2 \sqrt{-c^2 d^2+e^2}} \right) + \\
& b g \left( \frac{\frac{c \sqrt{1-c^2 x^2}}{(c^2 d^2-e^2) (d+e x)} - \frac{\operatorname{ArcSin}[c x]}{e (d+e x)^2} - \frac{i c^3 d \left( \operatorname{Log}[4] + \operatorname{Log} \left[ \frac{e^2 \sqrt{c^2 d^2-e^2} \left( i e+i c^2 d x+\sqrt{c^2 d^2-e^2} \sqrt{1-c^2 x^2} \right)}{c^3 d (d+e x)} \right] \right)}{(c d-e) e (c d+e) \sqrt{c^2 d^2-e^2}}}{2 e} - \frac{1}{6 e} d \left( \frac{\sqrt{1-c^2 x^2} (-c e^2 + c^3 d (4 d + 3 e x))}{(-c^2 d^2 + e^2)^2 (d+e x)^2} - \right. \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \left( \frac{2 \operatorname{ArcSin}[c x]}{e (d+e x)^3} + \frac{c^3 (2 c^2 d^2 + e^2) \operatorname{Log}[d+e x]}{e (-c d+e)^2 (c d+e)^2 \sqrt{-c^2 d^2 + e^2}} - \frac{c^3 (2 c^2 d^2 + e^2) \operatorname{Log}[e+c^2 d x + \sqrt{-c^2 d^2 + e^2} \sqrt{1-c^2 x^2}]}{e (-c d+e)^2 (c d+e)^2 \sqrt{-c^2 d^2 + e^2}} \right) \right) + \\
& b i \left( \frac{\frac{3 d^2}{2 e^3} \left( \frac{c \sqrt{1-c^2 x^2}}{(c^2 d^2-e^2) (d+e x)} - \frac{\operatorname{ArcSin}[c x]}{e (d+e x)^2} - \frac{i c^3 d \left( \operatorname{Log}[4] + \operatorname{Log}\left[ \frac{e^{2 \sqrt{c^2 d^2-e^2}} \left( i e + i c^2 d x + \sqrt{c^2 d^2-e^2} \sqrt{1-c^2 x^2} \right)}{c^3 d (d+e x)} \right] \right)}{(c d-e) e (c d+e) \sqrt{c^2 d^2-e^2}} \right) - \frac{3 d \left( -\frac{\operatorname{ArcSin}[c x]}{d+e x} + \frac{c \left( \operatorname{Log}[d+e x] - \operatorname{Log}[e+c^2 d x + \sqrt{-c^2 d^2+e^2} \sqrt{1-c^2 x^2}] \right)}{\sqrt{-c^2 d^2+e^2}} \right)}{e^4} - \right. \\
& \left. \frac{\frac{1}{6 e^3} d^3 \left( \frac{\sqrt{1-c^2 x^2} (-c e^2 + c^3 d (4 d + 3 e x))}{(-c^2 d^2 + e^2)^2 (d+e x)^2} - \frac{2 \operatorname{ArcSin}[c x]}{e (d+e x)^3} + \right. \right. \\
& \left. \left. \frac{c^3 (2 c^2 d^2 + e^2) \operatorname{Log}[d+e x]}{e (-c d+e)^2 (c d+e)^2 \sqrt{-c^2 d^2 + e^2}} - \frac{c^3 (2 c^2 d^2 + e^2) \operatorname{Log}[e+c^2 d x + \sqrt{-c^2 d^2 + e^2} \sqrt{1-c^2 x^2}]}{e (-c d+e)^2 (c d+e)^2 \sqrt{-c^2 d^2 + e^2}} \right) + \right. \\
& \left. \frac{1}{8 e^4} \left( \frac{1}{i (\pi - 2 \operatorname{ArcSin}[c x])^2 - 32 i \operatorname{ArcSin}\left[\frac{\sqrt{1+\frac{c d}{e}}}{\sqrt{2}}\right] \operatorname{ArcTan}\left[\frac{(c d-e) \operatorname{Cot}\left[\frac{1}{4}(\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{c^2 d^2 - e^2}}\right]} - \right. \right. \\
& \left. \left. 4 \left( \pi + 4 \operatorname{ArcSin}\left[\frac{\sqrt{1+\frac{c d}{e}}}{\sqrt{2}}\right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log}\left[1 - \frac{i (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] - \right. \right. \\
& \left. \left. 4 \left( \pi - 4 \operatorname{ArcSin}\left[\frac{\sqrt{1+\frac{c d}{e}}}{\sqrt{2}}\right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log}\left[1 + \frac{i (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}\right] + 4 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c d + c e x] + \right. \right)
\end{aligned}$$

$$\left. \left( 8 \operatorname{ArcSin}[c x] \operatorname{Log}[c d + c e x] + 8 i \left( \operatorname{PolyLog}[2, \frac{i (-c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}] + \operatorname{PolyLog}[2, -\frac{i (c d + \sqrt{c^2 d^2 - e^2}) e^{-i \operatorname{ArcSin}[c x]}}{e}] \right) \right) \right)$$

Problem 113: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(f + g x) (a + b \operatorname{ArcSin}[c x])^2}{(d + e x)^3} dx$$

Optimal (type 4, 935 leaves, 33 steps):

$$\begin{aligned} & \frac{a b c (e f - d g) \sqrt{1 - c^2 x^2}}{e (c^2 d^2 - e^2) (d + e x)} + \frac{a b g^2 \operatorname{ArcSin}[c x]}{e^2 (e f - d g)} + \frac{b^2 c (e f - d g) \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x]}{e (c^2 d^2 - e^2) (d + e x)} + \frac{b^2 g^2 \operatorname{ArcSin}[c x]^2}{2 e^2 (e f - d g)} - \\ & \frac{(f + g x)^2 (a + b \operatorname{ArcSin}[c x])^2}{2 (e f - d g) (d + e x)^2} - \frac{a b c (2 e^2 g - c^2 d (e f + d g)) \operatorname{ArcTan}\left[\frac{e + c^2 d x}{\sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2}}\right]}{e^2 (c^2 d^2 - e^2)^{3/2}} - \frac{2 i b^2 c g \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^2 \sqrt{c^2 d^2 - e^2}} - \\ & \frac{i b^2 c^3 d (e f - d g) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^2 (c^2 d^2 - e^2)^{3/2}} + \frac{2 i b^2 c g \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^2 \sqrt{c^2 d^2 - e^2}} + \\ & \frac{i b^2 c^3 d (e f - d g) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^2 (c^2 d^2 - e^2)^{3/2}} - \frac{b^2 c^2 (e f - d g) \operatorname{Log}[d + e x]}{e^2 (c^2 d^2 - e^2)} - \frac{2 b^2 c g \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}]}{e^2 \sqrt{c^2 d^2 - e^2}} - \\ & \frac{b^2 c^3 d (e f - d g) \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}]}{e^2 (c^2 d^2 - e^2)^{3/2}} + \frac{2 b^2 c g \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}]}{e^2 \sqrt{c^2 d^2 - e^2}} + \frac{b^2 c^3 d (e f - d g) \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}]}{e^2 (c^2 d^2 - e^2)^{3/2}} \end{aligned}$$

Result (type 6, 3976 leaves):

$$\begin{aligned}
& -\frac{a^2 e f + a^2 d g}{2 e^2 (d + e x)^2} - \frac{a^2 g}{e^2 (d + e x)} + 2 a b f \left( -\frac{c \sqrt{1 + \frac{-d - \sqrt{\frac{1}{c^2}} e}{d + e x}} \sqrt{1 + \frac{-d + \sqrt{\frac{1}{c^2}} e}{d + e x}} \text{AppellF1}[2, \frac{1}{2}, \frac{1}{2}, 3, -\frac{-d + \sqrt{\frac{1}{c^2}} e}{d + e x}, -\frac{-d - \sqrt{\frac{1}{c^2}} e}{d + e x}]}{4 e^2 (d + e x) \sqrt{1 - c^2 x^2}} - \frac{\text{ArcSin}[c x]}{2 e (d + e x)^2} \right) + \\
& 2 a b g \left( -\frac{d \left( \frac{c \sqrt{1 - c^2 x^2}}{(c^2 d^2 - e^2) (d + e x)} - \frac{i c^3 d \left( \text{Log}[4] + \text{Log}\left[ \frac{e^2 \sqrt{c^2 d^2 - e^2} \left( i e + i c^2 d x + \sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2} \right)}{c^3 d (d + e x)} \right]} \right)}{(c d - e) e (c d + e) \sqrt{c^2 d^2 - e^2}} + \frac{-\frac{\text{ArcSin}[c x]}{d + e x} + \frac{c \left( \text{Log}[d + e x] - \text{Log}\left[ e + c^2 d x + \sqrt{-c^2 d^2 + e^2} \sqrt{1 - c^2 x^2} \right] \right)}{\sqrt{-c^2 d^2 + e^2}}}{e^2} \right) + \\
& b^2 c g \left( \frac{c d \text{ArcSin}[c x]^2}{2 e^2 (c d + c e x)^2} + \frac{-c d e \sqrt{1 - c^2 x^2} \text{ArcSin}[c x] - c^2 d^2 \text{ArcSin}[c x]^2 + e^2 \text{ArcSin}[c x]^2}{(c d - e) e^2 (c d + e) (c d + c e x)} - \frac{c d \text{Log}\left[ 1 + \frac{e x}{d} \right]}{e^2 (-c^2 d^2 + e^2)} + \right. \\
& \left. \frac{1}{-c^2 d^2 + e^2} 2 \left( \frac{\pi \text{ArcTan}\left[ \frac{e + c d \text{Tan}\left[ \frac{1}{2} \text{ArcSin}[c x] \right]}{\sqrt{c^2 d^2 - e^2}} \right]}{\sqrt{c^2 d^2 - e^2}} + \frac{1}{\sqrt{-c^2 d^2 + e^2}} \left( 2 \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \text{ArcTanh}\left[ \frac{(c d + e) \text{Cot}\left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] - \right. \right. \\
& \left. 2 \text{ArcCos}\left[ -\frac{c d}{e} \right] \text{ArcTanh}\left[ \frac{(-c d + e) \text{Tan}\left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] + \left( \text{ArcCos}\left[ -\frac{c d}{e} \right] - 2 \frac{i}{2} \left( \text{ArcTanh}\left[ \frac{(c d + e) \text{Cot}\left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] - \right. \right. \\
& \left. \left. \text{ArcTanh}\left[ \frac{(-c d + e) \text{Tan}\left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] \right) \text{Log}\left[ \frac{\sqrt{-c^2 d^2 + e^2} e^{-\frac{1}{2} i \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right)}}{\sqrt{2} \sqrt{e} \sqrt{c d + c e x}} \right] + \right. \\
& \left. \left( \text{ArcCos}\left[ -\frac{c d}{e} \right] + 2 \frac{i}{2} \left( \text{ArcTanh}\left[ \frac{(c d + e) \text{Cot}\left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] - \text{ArcTanh}\left[ \frac{(-c d + e) \text{Tan}\left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] \right) \right) \right. \\
& \left. \text{Log}\left[ \frac{\sqrt{-c^2 d^2 + e^2} e^{\frac{1}{2} i \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right)}}{\sqrt{2} \sqrt{e} \sqrt{c d + c e x}} \right] - \left( \text{ArcCos}\left[ -\frac{c d}{e} \right] + 2 \frac{i}{2} \text{ArcTanh}\left[ \frac{(-c d + e) \text{Tan}\left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \text{Log} \left[ 1 - \frac{\left( c d - i \sqrt{-c^2 d^2 + e^2} \right) \left( c d + e - \sqrt{-c^2 d^2 + e^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)}{e \left( c d + e + \sqrt{-c^2 d^2 + e^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)} \right] + \left( -\text{ArcCos} \left[ -\frac{c d}{e} \right] + 2 i \text{ArcTanh} \left[ \frac{(-c d + e) \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] \right) \text{Log} \left[ 1 - \frac{\left( c d + i \sqrt{-c^2 d^2 + e^2} \right) \left( c d + e - \sqrt{-c^2 d^2 + e^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)}{e \left( c d + e + \sqrt{-c^2 d^2 + e^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)} \right] + \\
& i \left( \text{PolyLog} [2, \frac{\left( c d - i \sqrt{-c^2 d^2 + e^2} \right) \left( c d + e - \sqrt{-c^2 d^2 + e^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)}{e \left( c d + e + \sqrt{-c^2 d^2 + e^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)] - \text{PolyLog} [2, \frac{\left( c d + i \sqrt{-c^2 d^2 + e^2} \right) \left( c d + e - \sqrt{-c^2 d^2 + e^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)}{e \left( c d + e + \sqrt{-c^2 d^2 + e^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)] \right) \Bigg] - \\
& \frac{1}{e^2 (-c^2 d^2 + e^2)} c^2 d^2 \left( \frac{\pi \text{ArcTan} \left[ \frac{e + c d \tan \left[ \frac{1}{2} \text{ArcSin}[c x] \right]}{\sqrt{c^2 d^2 - e^2}} \right]}{\sqrt{c^2 d^2 - e^2}} + \frac{1}{\sqrt{-c^2 d^2 + e^2}} \left( 2 \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \text{ArcTanh} \left[ \frac{(c d + e) \cot \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] - \right. \right. \\
& \left. \left. 2 \text{ArcCos} \left[ -\frac{c d}{e} \right] \text{ArcTanh} \left[ \frac{(-c d + e) \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] + \left( \text{ArcCos} \left[ -\frac{c d}{e} \right] - 2 i \text{ArcTanh} \left[ \frac{(c d + e) \cot \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] - \right. \right. \\
& \left. \left. \text{ArcTanh} \left[ \frac{(-c d + e) \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] \right) \right) \text{Log} \left[ \frac{\sqrt{-c^2 d^2 + e^2} e^{-\frac{1}{2} i \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right)}}{\sqrt{2} \sqrt{e} \sqrt{c d + c e x}} \right] + \\
& \left( \text{ArcCos} \left[ -\frac{c d}{e} \right] + 2 i \text{ArcTanh} \left[ \frac{(c d + e) \cot \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] - \text{ArcTanh} \left[ \frac{(-c d + e) \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] \right) \\
& \text{Log} \left[ \frac{\sqrt{-c^2 d^2 + e^2} e^{\frac{1}{2} i \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right)}}{\sqrt{2} \sqrt{e} \sqrt{c d + c e x}} \right] - \left( \text{ArcCos} \left[ -\frac{c d}{e} \right] + 2 i \text{ArcTanh} \left[ \frac{(-c d + e) \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] \right) \\
& \text{Log} \left[ 1 - \frac{\left( c d - i \sqrt{-c^2 d^2 + e^2} \right) \left( c d + e - \sqrt{-c^2 d^2 + e^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)}{e \left( c d + e + \sqrt{-c^2 d^2 + e^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)} \right] + \left( -\text{ArcCos} \left[ -\frac{c d}{e} \right] + 2 i \text{ArcTanh} \left[ \frac{(-c d + e) \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right]}{\sqrt{-c^2 d^2 + e^2}} \right] \right) \text{Log} \left[ 1 - \frac{\left( c d + i \sqrt{-c^2 d^2 + e^2} \right) \left( c d + e - \sqrt{-c^2 d^2 + e^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)}{e \left( c d + e + \sqrt{-c^2 d^2 + e^2} \tan \left[ \frac{1}{2} \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \right] \right)} \right] +
\end{aligned}$$

$$\begin{aligned}
& \text{i} \left( \text{PolyLog}[2, \frac{(c d - \text{i} \sqrt{-c^2 d^2 + e^2}) (c d + e - \sqrt{-c^2 d^2 + e^2} \tan[\frac{1}{2} (\frac{\pi}{2} - \text{ArcSin}[c x])])}{e (c d + e + \sqrt{-c^2 d^2 + e^2} \tan[\frac{1}{2} (\frac{\pi}{2} - \text{ArcSin}[c x])])}] - \right. \\
& \left. \text{PolyLog}[2, \frac{(c d + \text{i} \sqrt{-c^2 d^2 + e^2}) (c d + e - \sqrt{-c^2 d^2 + e^2} \tan[\frac{1}{2} (\frac{\pi}{2} - \text{ArcSin}[c x])])}{e (c d + e + \sqrt{-c^2 d^2 + e^2} \tan[\frac{1}{2} (\frac{\pi}{2} - \text{ArcSin}[c x])])}] \right) \Bigg) + \\
& b^2 c^2 f \left( \frac{\sqrt{1 - c^2 x^2} \text{ArcSin}[c x]}{(c d - e) (c d + e) (c d + c e x)} - \frac{\text{ArcSin}[c x]^2}{2 e (c d + c e x)^2} + \frac{\text{Log}[1 + \frac{e x}{d}]}{e (-c^2 d^2 + e^2)} - \right. \\
& \frac{1}{e (-c^2 d^2 + e^2)} \\
& \frac{c}{d} \\
& \left( \frac{\pi \text{ArcTan}[\frac{e+c d \tan[\frac{1}{2} \text{ArcSin}[c x]]}{\sqrt{c^2 d^2 - e^2}}]}{\sqrt{c^2 d^2 - e^2}} + \frac{1}{\sqrt{-c^2 d^2 + e^2}} \right. \\
& \left. \left( 2 \left( \frac{\pi}{2} - \text{ArcSin}[c x] \right) \text{ArcTanh}[\frac{(c d + e) \cot[\frac{1}{2} (\frac{\pi}{2} - \text{ArcSin}[c x])]}{\sqrt{-c^2 d^2 + e^2}}] - 2 \text{ArcCos}[-\frac{c d}{e}] \text{ArcTanh}[\frac{(-c d + e) \tan[\frac{1}{2} (\frac{\pi}{2} - \text{ArcSin}[c x])]}{\sqrt{-c^2 d^2 + e^2}}] + \right. \right. \\
& \left. \left. \text{ArcCos}[-\frac{c d}{e}] - 2 \text{i} \left( \text{ArcTanh}[\frac{(c d + e) \cot[\frac{1}{2} (\frac{\pi}{2} - \text{ArcSin}[c x])]}{\sqrt{-c^2 d^2 + e^2}}] - \text{ArcTanh}[\frac{(-c d + e) \tan[\frac{1}{2} (\frac{\pi}{2} - \text{ArcSin}[c x])]}{\sqrt{-c^2 d^2 + e^2}}] \right) \right) \right. \\
& \left. \text{Log}[\frac{\sqrt{-c^2 d^2 + e^2} e^{-\frac{1}{2} \text{i} (\frac{\pi}{2} - \text{ArcSin}[c x])}}{\sqrt{2} \sqrt{e} \sqrt{c d + c e x}}] + \right. \\
& \left. \left( \text{ArcCos}[-\frac{c d}{e}] + 2 \text{i} \left( \text{ArcTanh}[\frac{(c d + e) \cot[\frac{1}{2} (\frac{\pi}{2} - \text{ArcSin}[c x])]}{\sqrt{-c^2 d^2 + e^2}}] - \text{ArcTanh}[\frac{(-c d + e) \tan[\frac{1}{2} (\frac{\pi}{2} - \text{ArcSin}[c x])]}{\sqrt{-c^2 d^2 + e^2}}] \right) \right) \right. \\
& \left. \text{Log}[\frac{\sqrt{-c^2 d^2 + e^2} e^{\frac{1}{2} \text{i} (\frac{\pi}{2} - \text{ArcSin}[c x])}}{\sqrt{2} \sqrt{e} \sqrt{c d + c e x}}] - \left( \text{ArcCos}[-\frac{c d}{e}] + 2 \text{i} \text{ArcTanh}[\frac{(-c d + e) \tan[\frac{1}{2} (\frac{\pi}{2} - \text{ArcSin}[c x])]}{\sqrt{-c^2 d^2 + e^2}}] \right) \right)
\end{aligned}$$

Problem 114: Attempted integration timed out after 120 seconds.

$$\int \frac{(f + g x)^2 (a + b \operatorname{ArcSin}[c x])^2}{(d + e x)^3} dx$$

Optimal (type 4, 1678 leaves, 55 steps):

$$\begin{aligned}
& -\frac{a^2 (e f - d g)^2}{2 e^3 (d + e x)^2} - \frac{2 a^2 g (e f - d g)}{e^3 (d + e x)} + \frac{a b c (e f - d g)^2 \sqrt{1 - c^2 x^2}}{e^2 (c^2 d^2 - e^2) (d + e x)} - \frac{a b (e f - d g)^2 \operatorname{ArcSin}[c x]}{e^3 (d + e x)^2} - \frac{4 a b g (e f - d g) \operatorname{ArcSin}[c x]}{e^3 (d + e x)} + \\
& \frac{b^2 c (e f - d g)^2 \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x]}{e^2 (c^2 d^2 - e^2) (d + e x)} - \frac{i a b g^2 \operatorname{ArcSin}[c x]^2}{e^3} - \frac{b^2 (e f - d g)^2 \operatorname{ArcSin}[c x]^2}{2 e^3 (d + e x)^2} - \frac{2 b^2 g (e f - d g) \operatorname{ArcSin}[c x]^2}{e^3 (d + e x)} - \\
& \frac{i b^2 g^2 \operatorname{ArcSin}[c x]^3}{3 e^3} - \frac{a b c (e f - d g) (4 e^2 g - c^2 d (e f + 3 d g)) \operatorname{ArcTan}\left[\frac{e + c^2 d x}{\sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2}}\right]}{e^3 (c^2 d^2 - e^2)^{3/2}} + \frac{2 a b g^2 \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^3} - \\
& \frac{4 i b^2 c g (e f - d g) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^3 \sqrt{c^2 d^2 - e^2}} - \frac{i b^2 c^3 d (e f - d g)^2 \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^3 (c^2 d^2 - e^2)^{3/2}} + \\
& \frac{b^2 g^2 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^3} + \frac{2 a b g^2 \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^3} + \frac{4 i b^2 c g (e f - d g) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^3 \sqrt{c^2 d^2 - e^2}} + \\
& \frac{i b^2 c^3 d (e f - d g)^2 \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^3 (c^2 d^2 - e^2)^{3/2}} + \frac{b^2 g^2 \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^3} + \frac{a^2 g^2 \operatorname{Log}[d + e x]}{e^3} - \\
& \frac{b^2 c^2 (e f - d g)^2 \operatorname{Log}[d + e x]}{e^3 (c^2 d^2 - e^2)} - \frac{2 i a b g^2 \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}]}{e^3} - \frac{4 b^2 c g (e f - d g) \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}]}{e^3 \sqrt{c^2 d^2 - e^2}} - \\
& \frac{b^2 c^3 d (e f - d g)^2 \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}]}{e^3 (c^2 d^2 - e^2)^{3/2}} - \frac{2 i b^2 g^2 \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}]}{e^3} - \\
& \frac{2 i a b g^2 \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}]}{e^3} + \frac{4 b^2 c g (e f - d g) \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}]}{e^3 \sqrt{c^2 d^2 - e^2}} + \frac{b^2 c^3 d (e f - d g)^2 \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}]}{e^3 (c^2 d^2 - e^2)^{3/2}} - \\
& \frac{2 i b^2 g^2 \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}]}{e^3} + \frac{2 b^2 g^2 \operatorname{PolyLog}[3, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}]}{e^3} + \frac{2 b^2 g^2 \operatorname{PolyLog}[3, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}]}{e^3}
\end{aligned}$$

Result (type 1, 1 leaves):

???

### Problem 118: Result more than twice size of optimal antiderivative.

$$\int \frac{(d + e x + f x^2) (a + b \operatorname{ArcSin}[c x])^2}{g + h x} dx$$

Optimal (type 4, 1067 leaves, 38 steps):

$$\begin{aligned}
& -\frac{a^2 (f g - e h) x}{h^2} + \frac{2 b^2 (f g - e h) x}{h^2} + \frac{a^2 f x^2}{2 h} - \frac{b^2 f x^2}{4 h} - \frac{a b (4 (f g - e h) - f h x) \sqrt{1 - c^2 x^2}}{2 c h^2} - \\
& \frac{a b f \operatorname{ArcSin}[c x]}{2 c^2 h} - \frac{2 a b (f g - e h) x \operatorname{ArcSin}[c x]}{h^2} + \frac{a b f x^2 \operatorname{ArcSin}[c x]}{h} - \frac{2 b^2 (f g - e h) \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x]}{c h^2} + \\
& \frac{b^2 f x \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x]}{2 c h} - \frac{b^2 f \operatorname{ArcSin}[c x]^2}{4 c^2 h} - \frac{\pm a b (f g^2 - e g h + d h^2) \operatorname{ArcSin}[c x]^2}{h^3} - \frac{b^2 (f g - e h) x \operatorname{ArcSin}[c x]^2}{h^2} + \\
& \frac{b^2 f x^2 \operatorname{ArcSin}[c x]^2}{2 h} - \frac{\pm b^2 (f g^2 - e g h + d h^2) \operatorname{ArcSin}[c x]^3}{3 h^3} + \frac{2 a b (f g^2 - e g h + d h^2) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{\pm e^{i \operatorname{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}\right]}{h^3} + \\
& \frac{b^2 (f g^2 - e g h + d h^2) \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 - \frac{\pm e^{i \operatorname{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}\right]}{h^3} + \frac{2 a b (f g^2 - e g h + d h^2) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{\pm e^{i \operatorname{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}\right]}{h^3} + \\
& \frac{b^2 (f g^2 - e g h + d h^2) \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 - \frac{\pm e^{i \operatorname{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}\right]}{h^3} + \frac{a^2 (f g^2 - e g h + d h^2) \operatorname{Log}[g + h x]}{h^3} - \\
& \frac{2 \pm a b (f g^2 - e g h + d h^2) \operatorname{PolyLog}\left[2, \frac{\pm e^{i \operatorname{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}\right]}{h^3} - \frac{2 \pm b^2 (f g^2 - e g h + d h^2) \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{\pm e^{i \operatorname{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}\right]}{h^3} - \\
& \frac{2 \pm a b (f g^2 - e g h + d h^2) \operatorname{PolyLog}\left[2, \frac{\pm e^{i \operatorname{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}\right]}{h^3} - \frac{2 \pm b^2 (f g^2 - e g h + d h^2) \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{\pm e^{i \operatorname{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}\right]}{h^3} + \\
& \frac{2 b^2 (f g^2 - e g h + d h^2) \operatorname{PolyLog}\left[3, \frac{\pm e^{i \operatorname{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}\right]}{h^3} + \frac{2 b^2 (f g^2 - e g h + d h^2) \operatorname{PolyLog}\left[3, \frac{\pm e^{i \operatorname{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}\right]}{h^3}
\end{aligned}$$

Result (type 4, 8787 leaves):

$$\begin{aligned}
& \frac{a^2 (-f g + e h) x}{h^2} + \frac{a^2 f x^2}{2 h} + \frac{(a^2 f g^2 - a^2 e g h + a^2 d h^2) \operatorname{Log}[g + h x]}{h^3} +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{4 h} a b d \left( \frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}} \right) \operatorname{ArcTan} \left[ \frac{(c g - h) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{c^2 g^2 - h^2}} \right] - \\
& 4 \left( \pi + 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log} \left[ 1 - \frac{i e^{-i \operatorname{ArcSin}[c x]} (-c g + \sqrt{c^2 g^2 - h^2})}{h} \right] - \\
& 4 \left( \pi - 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log} \left[ 1 + \frac{i e^{-i \operatorname{ArcSin}[c x]} (c g + \sqrt{c^2 g^2 - h^2})}{h} \right] + 4 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c g + c h x] + \\
& 8 \operatorname{ArcSin}[c x] \operatorname{Log}[c g + c h x] + 8 i \left( \operatorname{PolyLog} \left[ 2, \frac{i e^{-i \operatorname{ArcSin}[c x]} (-c g + \sqrt{c^2 g^2 - h^2})}{h} \right] + \operatorname{PolyLog} \left[ 2, -\frac{i e^{-i \operatorname{ArcSin}[c x]} (c g + \sqrt{c^2 g^2 - h^2})}{h} \right] \right) + \\
& \frac{1}{c h} 2 a b e \left( \sqrt{1 - c^2 x^2} + c x \operatorname{ArcSin}[c x] - \frac{1}{8 h} c g \left( \frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}} \right) \operatorname{ArcTan} \left[ \frac{(c g - h) \operatorname{Cot} \left[ \frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x]) \right]}{\sqrt{c^2 g^2 - h^2}} \right] - \right. \\
& \left. 4 \left( \pi + 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \operatorname{Log} \left[ 1 - \frac{i e^{-i \operatorname{ArcSin}[c x]} (-c g + \sqrt{c^2 g^2 - h^2})}{h} \right] - 4 \left( \pi - 4 \operatorname{ArcSin} \left[ \frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}} \right] - 2 \operatorname{ArcSin}[c x] \right) \right. \\
& \left. \operatorname{Log} \left[ 1 + \frac{i e^{-i \operatorname{ArcSin}[c x]} (c g + \sqrt{c^2 g^2 - h^2})}{h} \right] + 4 (\pi - 2 \operatorname{ArcSin}[c x]) \operatorname{Log}[c g + c h x] + 8 \operatorname{ArcSin}[c x] \operatorname{Log}[c g + c h x] + \right)
\end{aligned}$$

$$\begin{aligned}
& 8 \operatorname{Im} \left( \operatorname{PolyLog}[2, \frac{i e^{-i \operatorname{ArcSin}[cx]} (-c g + \sqrt{c^2 g^2 - h^2})}{h}] + \operatorname{PolyLog}[2, -\frac{i e^{-i \operatorname{ArcSin}[cx]} (c g + \sqrt{c^2 g^2 - h^2})}{h}] \right) + \frac{1}{3 h \sqrt{-(-c^2 g^2 + h^2)^2}} \\
& b^2 d \left( -\frac{i}{2} \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}[cx]^3 - 24 \frac{i}{2} \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{cg}{h}}}{\sqrt{2}}\right] \operatorname{ArcSin}[cx] \operatorname{ArcTan}\left[\frac{(cg - h) \operatorname{Cot}\left[\frac{1}{4}(\pi + 2 \operatorname{ArcSin}[cx])\right]}{\sqrt{c^2 g^2 - h^2}}\right] + \right. \\
& 24 \frac{i}{2} \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{cg}{h}}}{\sqrt{2}}\right] \operatorname{ArcSin}[cx] \operatorname{ArcTan}\left[\frac{(cg - h) (\cos[\frac{1}{2} \operatorname{ArcSin}[cx]] - \sin[\frac{1}{2} \operatorname{ArcSin}[cx]])}{\sqrt{c^2 g^2 - h^2} (\cos[\frac{1}{2} \operatorname{ArcSin}[cx]] + \sin[\frac{1}{2} \operatorname{ArcSin}[cx]])}\right] + \\
& 3 c g \sqrt{-c^2 g^2 + h^2} \operatorname{ArcSin}[cx]^2 \operatorname{Log}\left[1 + \frac{i e^{i \operatorname{ArcSin}[cx]} h}{-c g + \sqrt{c^2 g^2 - h^2}}\right] - 3 \sqrt{-(-c^2 g^2 + h^2)^2} \pi \operatorname{ArcSin}[cx] \operatorname{Log}\left[1 - \frac{i e^{-i \operatorname{ArcSin}[cx]} (-c g + \sqrt{c^2 g^2 - h^2})}{h}\right] - \\
& 12 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{cg}{h}}}{\sqrt{2}}\right] \operatorname{ArcSin}[cx] \operatorname{Log}\left[1 - \frac{i e^{-i \operatorname{ArcSin}[cx]} (-c g + \sqrt{c^2 g^2 - h^2})}{h}\right] + \\
& 3 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}[cx]^2 \operatorname{Log}\left[1 - \frac{i e^{-i \operatorname{ArcSin}[cx]} (-c g + \sqrt{c^2 g^2 - h^2})}{h}\right] - \\
& 3 c g \sqrt{-c^2 g^2 + h^2} \operatorname{ArcSin}[cx]^2 \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[cx]} h}{c g + \sqrt{c^2 g^2 - h^2}}\right] - 3 \sqrt{-(-c^2 g^2 + h^2)^2} \pi \operatorname{ArcSin}[cx] \operatorname{Log}\left[1 + \frac{i e^{-i \operatorname{ArcSin}[cx]} (c g + \sqrt{c^2 g^2 - h^2})}{h}\right] + \\
& 12 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{cg}{h}}}{\sqrt{2}}\right] \operatorname{ArcSin}[cx] \operatorname{Log}\left[1 + \frac{i e^{-i \operatorname{ArcSin}[cx]} (c g + \sqrt{c^2 g^2 - h^2})}{h}\right] + \\
& 3 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}[cx]^2 \operatorname{Log}\left[1 + \frac{i e^{-i \operatorname{ArcSin}[cx]} (c g + \sqrt{c^2 g^2 - h^2})}{h}\right] -
\end{aligned}$$

$$\begin{aligned}
& 3 \operatorname{sgn}(c g) \sqrt{c^2 g^2 - h^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{e^{i \operatorname{ArcSin}[c x]} h}{\operatorname{sgn}(c g) - \sqrt{-c^2 g^2 + h^2}}\right] + 3 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{e^{i \operatorname{ArcSin}[c x]} h}{\operatorname{sgn}(c g) - \sqrt{-c^2 g^2 + h^2}}\right] + \\
& 3 \operatorname{sgn}(c g) \sqrt{c^2 g^2 - h^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{e^{i \operatorname{ArcSin}[c x]} h}{\operatorname{sgn}(c g) + \sqrt{-c^2 g^2 + h^2}}\right] + 3 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{e^{i \operatorname{ArcSin}[c x]} h}{\operatorname{sgn}(c g) + \sqrt{-c^2 g^2 + h^2}}\right] + \\
& 3 \sqrt{-(-c^2 g^2 + h^2)^2} \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{(c g - \sqrt{c^2 g^2 - h^2}) (c x + i \sqrt{1 - c^2 x^2})}{h}\right] + \\
& 12 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{(c g - \sqrt{c^2 g^2 - h^2}) (c x + i \sqrt{1 - c^2 x^2})}{h}\right] - \\
& 3 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{(c g - \sqrt{c^2 g^2 - h^2}) (c x + i \sqrt{1 - c^2 x^2})}{h}\right] + \\
& 3 \sqrt{-(-c^2 g^2 + h^2)^2} \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{(c g + \sqrt{c^2 g^2 - h^2}) (c x + i \sqrt{1 - c^2 x^2})}{h}\right] - \\
& 12 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{(c g + \sqrt{c^2 g^2 - h^2}) (c x + i \sqrt{1 - c^2 x^2})}{h}\right] - \\
& 3 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{(c g + \sqrt{c^2 g^2 - h^2}) (c x + i \sqrt{1 - c^2 x^2})}{h}\right] - \\
& 6 \operatorname{sgn}(c g) \sqrt{-c^2 g^2 + h^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}\right] + 6 \operatorname{sgn}(c g) \sqrt{-c^2 g^2 + h^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}\right] - \\
& 6 c g \sqrt{c^2 g^2 - h^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{e^{i \operatorname{ArcSin}[c x]} h}{-i c g + \sqrt{-c^2 g^2 + h^2}}\right] - 6 i \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{e^{i \operatorname{ArcSin}[c x]} h}{-i c g + \sqrt{-c^2 g^2 + h^2}}\right] + \\
& 6 c g \sqrt{c^2 g^2 - h^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, -\frac{e^{i \operatorname{ArcSin}[c x]} h}{i c g + \sqrt{-c^2 g^2 + h^2}}\right] - 6 i \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, -\frac{e^{i \operatorname{ArcSin}[c x]} h}{i c g + \sqrt{-c^2 g^2 + h^2}}\right] + \\
& 6 c g \sqrt{-c^2 g^2 + h^2} \operatorname{PolyLog}\left[3, \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}\right] - 6 c g \sqrt{-c^2 g^2 + h^2} \operatorname{PolyLog}\left[3, \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}\right] -
\end{aligned}$$

$$\begin{aligned}
& 6 \pm c g \sqrt{c^2 g^2 - h^2} \operatorname{PolyLog}[3, \frac{e^{i \operatorname{ArcSin}[c x]} h}{- \pm c g + \sqrt{-c^2 g^2 + h^2}}] + 6 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{PolyLog}[3, \frac{e^{i \operatorname{ArcSin}[c x]} h}{- \pm c g + \sqrt{-c^2 g^2 + h^2}}] + \\
& 6 \pm c g \sqrt{c^2 g^2 - h^2} \operatorname{PolyLog}[3, -\frac{e^{i \operatorname{ArcSin}[c x]} h}{\pm c g + \sqrt{-c^2 g^2 + h^2}}] + 6 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{PolyLog}[3, -\frac{e^{i \operatorname{ArcSin}[c x]} h}{\pm c g + \sqrt{-c^2 g^2 + h^2}}] \Bigg) + \\
& \frac{1}{c} b^2 e \left( \frac{2 \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x]}{h} + \frac{c x (-2 + \operatorname{ArcSin}[c x]^2)}{h} - \frac{1}{3 h^2 \sqrt{-(-c^2 g^2 + h^2)^2}} c g \left( - \pm \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}[c x]^3 - \right. \right. \\
& \left. \left. 24 \pm \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \operatorname{ArcTan}\left[\frac{(c g - h) \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{c^2 g^2 - h^2}}\right] + \right. \right. \\
& \left. \left. 24 \pm \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \operatorname{ArcTan}\left[\frac{(c g - h) (\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] - \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right])}{\sqrt{c^2 g^2 - h^2} (\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right] + \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[c x]\right])}\right] + 3 c g \right. \right. \\
& \left. \left. \sqrt{-c^2 g^2 + h^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{i e^{i \operatorname{ArcSin}[c x]} h}{-c g + \sqrt{c^2 g^2 - h^2}}\right] - 3 \sqrt{-(-c^2 g^2 + h^2)^2} \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e^{-i \operatorname{ArcSin}[c x]} (-c g + \sqrt{c^2 g^2 - h^2})}{h}\right] - \right. \right. \\
& \left. \left. 12 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e^{-i \operatorname{ArcSin}[c x]} (-c g + \sqrt{c^2 g^2 - h^2})}{h}\right] + 3 \sqrt{-(-c^2 g^2 + h^2)^2} \right. \right. \\
& \left. \left. \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 - \frac{i e^{-i \operatorname{ArcSin}[c x]} (-c g + \sqrt{c^2 g^2 - h^2})}{h}\right] - 3 c g \sqrt{-c^2 g^2 + h^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}\right] - \right. \right. \\
& \left. \left. 3 \sqrt{-(-c^2 g^2 + h^2)^2} \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{i e^{-i \operatorname{ArcSin}[c x]} (c g + \sqrt{c^2 g^2 - h^2})}{h}\right] + 12 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}}\right] \right. \right)
\end{aligned}$$

$$\begin{aligned}
& \text{ArcSin}[c x] \log \left[ 1 + \frac{i e^{-i \text{ArcSin}[c x]} \left( c g + \sqrt{c^2 g^2 - h^2} \right)}{h} \right] + 3 \sqrt{-(-c^2 g^2 + h^2)^2} \text{ArcSin}[c x]^2 \log \left[ 1 + \frac{i e^{-i \text{ArcSin}[c x]} \left( c g + \sqrt{c^2 g^2 - h^2} \right)}{h} \right] - \\
& 3 i c g \sqrt{c^2 g^2 - h^2} \text{ArcSin}[c x]^2 \log \left[ 1 + \frac{e^{i \text{ArcSin}[c x]} h}{i c g - \sqrt{-c^2 g^2 + h^2}} \right] + 3 \sqrt{-(-c^2 g^2 + h^2)^2} \text{ArcSin}[c x]^2 \log \left[ 1 + \frac{e^{i \text{ArcSin}[c x]} h}{i c g - \sqrt{-c^2 g^2 + h^2}} \right] + \\
& 3 i c g \sqrt{c^2 g^2 - h^2} \text{ArcSin}[c x]^2 \log \left[ 1 + \frac{e^{i \text{ArcSin}[c x]} h}{i c g + \sqrt{-c^2 g^2 + h^2}} \right] + 3 \sqrt{-(-c^2 g^2 + h^2)^2} \text{ArcSin}[c x]^2 \log \left[ 1 + \frac{e^{i \text{ArcSin}[c x]} h}{i c g + \sqrt{-c^2 g^2 + h^2}} \right] + 3 \\
& \sqrt{-(-c^2 g^2 + h^2)^2} \pi \text{ArcSin}[c x] \log \left[ 1 + \frac{\left( c g - \sqrt{c^2 g^2 - h^2} \right) \left( c x + i \sqrt{1 - c^2 x^2} \right)}{h} \right] + 12 \sqrt{-(-c^2 g^2 + h^2)^2} \text{ArcSin} \left[ \frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}} \right] \text{ArcSin}[c x] \\
& \log \left[ 1 + \frac{\left( c g - \sqrt{c^2 g^2 - h^2} \right) \left( c x + i \sqrt{1 - c^2 x^2} \right)}{h} \right] - 3 \sqrt{-(-c^2 g^2 + h^2)^2} \text{ArcSin}[c x]^2 \log \left[ 1 + \frac{\left( c g - \sqrt{c^2 g^2 - h^2} \right) \left( c x + i \sqrt{1 - c^2 x^2} \right)}{h} \right] + 3 \\
& \sqrt{-(-c^2 g^2 + h^2)^2} \pi \text{ArcSin}[c x] \log \left[ 1 + \frac{\left( c g + \sqrt{c^2 g^2 - h^2} \right) \left( c x + i \sqrt{1 - c^2 x^2} \right)}{h} \right] - 12 \sqrt{-(-c^2 g^2 + h^2)^2} \text{ArcSin} \left[ \frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}} \right] \text{ArcSin}[c x] \\
& \log \left[ 1 + \frac{\left( c g + \sqrt{c^2 g^2 - h^2} \right) \left( c x + i \sqrt{1 - c^2 x^2} \right)}{h} \right] - 3 \sqrt{-(-c^2 g^2 + h^2)^2} \text{ArcSin}[c x]^2 \log \left[ 1 + \frac{\left( c g + \sqrt{c^2 g^2 - h^2} \right) \left( c x + i \sqrt{1 - c^2 x^2} \right)}{h} \right] - \\
& 6 i c g \sqrt{-c^2 g^2 + h^2} \text{ArcSin}[c x] \text{PolyLog}[2, \frac{i e^{i \text{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}] + 6 i c g \sqrt{-c^2 g^2 + h^2} \text{ArcSin}[c x] \text{PolyLog}[2, \frac{i e^{i \text{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}] - \\
& 6 c g \sqrt{c^2 g^2 - h^2} \text{ArcSin}[c x] \text{PolyLog}[2, \frac{e^{i \text{ArcSin}[c x]} h}{-i c g + \sqrt{-c^2 g^2 + h^2}}] - 6 i \sqrt{-(-c^2 g^2 + h^2)^2} \text{ArcSin}[c x] \text{PolyLog}[2, \frac{e^{i \text{ArcSin}[c x]} h}{-i c g + \sqrt{-c^2 g^2 + h^2}}] + \\
& 6 c g \sqrt{c^2 g^2 - h^2} \text{ArcSin}[c x] \text{PolyLog}[2, \frac{e^{i \text{ArcSin}[c x]} h}{i c g + \sqrt{-c^2 g^2 + h^2}}] - 6 i \sqrt{-(-c^2 g^2 + h^2)^2} \text{ArcSin}[c x] \text{PolyLog}[2, \frac{e^{i \text{ArcSin}[c x]} h}{i c g + \sqrt{-c^2 g^2 + h^2}}] + \\
& 6 c g \sqrt{-c^2 g^2 + h^2} \text{PolyLog}[3, \frac{i e^{i \text{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}] - 6 c g \sqrt{-c^2 g^2 + h^2} \text{PolyLog}[3, \frac{i e^{i \text{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}] - \\
& 6 i c g \sqrt{c^2 g^2 - h^2} \text{PolyLog}[3, \frac{e^{i \text{ArcSin}[c x]} h}{-i c g + \sqrt{-c^2 g^2 + h^2}}] + 6 \sqrt{-(-c^2 g^2 + h^2)^2} \text{PolyLog}[3, \frac{e^{i \text{ArcSin}[c x]} h}{-i c g + \sqrt{-c^2 g^2 + h^2}}] +
\end{aligned}$$

$$\begin{aligned}
& \left. \left( 6 i c g \sqrt{c^2 g^2 - h^2} \operatorname{PolyLog}[3, -\frac{e^{i \operatorname{ArcSin}[c x]} h}{i c g + \sqrt{-c^2 g^2 + h^2}}] + 6 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{PolyLog}[3, -\frac{e^{i \operatorname{ArcSin}[c x]} h}{i c g + \sqrt{-c^2 g^2 + h^2}}] \right) \right) + \\
& \frac{1}{4 c^2 h^3} a b f \left( i c^2 g^2 \pi^2 - 8 c g h \sqrt{1 - c^2 x^2} - 4 i c^2 g^2 \pi \operatorname{ArcSin}[c x] - 8 c^2 g h x \operatorname{ArcSin}[c x] + 4 i c^2 g^2 \operatorname{ArcSin}[c x]^2 - \right. \\
& 32 i c^2 g^2 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}}\right] \operatorname{ArcTan}\left[\frac{(c g - h) \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[c x])\right]}{\sqrt{c^2 g^2 - h^2}}\right] - \\
& 2 h^2 \operatorname{ArcSin}[c x] \operatorname{Cos}[2 \operatorname{ArcSin}[c x]] - 4 c^2 g^2 \pi \operatorname{Log}\left[1 - \frac{i e^{-i \operatorname{ArcSin}[c x]} (-c g + \sqrt{c^2 g^2 - h^2})}{h}\right] - \\
& 16 c^2 g^2 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}}\right] \operatorname{Log}\left[1 - \frac{i e^{-i \operatorname{ArcSin}[c x]} (-c g + \sqrt{c^2 g^2 - h^2})}{h}\right] + \\
& 8 c^2 g^2 \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e^{-i \operatorname{ArcSin}[c x]} (-c g + \sqrt{c^2 g^2 - h^2})}{h}\right] - 4 c^2 g^2 \pi \operatorname{Log}\left[1 + \frac{i e^{-i \operatorname{ArcSin}[c x]} (c g + \sqrt{c^2 g^2 - h^2})}{h}\right] + \\
& 16 c^2 g^2 \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}}\right] \operatorname{Log}\left[1 + \frac{i e^{-i \operatorname{ArcSin}[c x]} (c g + \sqrt{c^2 g^2 - h^2})}{h}\right] + \\
& 8 c^2 g^2 \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{i e^{-i \operatorname{ArcSin}[c x]} (c g + \sqrt{c^2 g^2 - h^2})}{h}\right] + \\
& 4 c^2 g^2 \pi \operatorname{Log}[c g + c h x] + 8 i c^2 g^2 \operatorname{PolyLog}[2, \frac{i e^{-i \operatorname{ArcSin}[c x]} (-c g + \sqrt{c^2 g^2 - h^2})}{h}] +
\end{aligned}$$

$$\begin{aligned}
& \left. \left( 8 \operatorname{Im} c^2 g^2 \operatorname{PolyLog}[2, -\frac{i e^{-i \operatorname{ArcSin}[c x]} (c g + \sqrt{c^2 g^2 - h^2})}{h}] + h^2 \sin[2 \operatorname{ArcSin}[c x]] \right) + \right. \\
& \frac{1}{c^2} b^2 f \left( -\frac{2 c g \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x]}{h^2} - \frac{c^2 g x (-2 + \operatorname{ArcSin}[c x]^2)}{h^2} - \frac{(-1 + 2 \operatorname{ArcSin}[c x]^2) \cos[2 \operatorname{ArcSin}[c x]]}{8 h} + \right. \\
& \left. \left. \frac{1}{3 h^3 \sqrt{-(-c^2 g^2 + h^2)^2}} c^2 g^2 \left( -i \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}[c x]^3 - \right. \right. \right. \\
& \left. \left. \left. 24 i \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \operatorname{ArcTan}\left[\frac{(c g - h) \cot[\frac{1}{4}(\pi + 2 \operatorname{ArcSin}[c x])]}{\sqrt{c^2 g^2 - h^2}}\right] + \right. \right. \\
& \left. \left. \left. 24 i \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \operatorname{ArcTan}\left[\frac{(c g - h) (\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] - \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])}{\sqrt{c^2 g^2 - h^2} (\cos[\frac{1}{2} \operatorname{ArcSin}[c x]] + \sin[\frac{1}{2} \operatorname{ArcSin}[c x]])}\right] + 3 c g \right. \right. \right. \\
& \left. \left. \left. \sqrt{-c^2 g^2 + h^2} \operatorname{ArcSin}[c x]^2 \log\left[1 + \frac{i e^{i \operatorname{ArcSin}[c x]} h}{-c g + \sqrt{c^2 g^2 - h^2}}\right] - 3 \sqrt{-(-c^2 g^2 + h^2)^2} \pi \operatorname{ArcSin}[c x] \log\left[1 - \frac{i e^{-i \operatorname{ArcSin}[c x]} (-c g + \sqrt{c^2 g^2 - h^2})}{h}\right] - \right. \right. \\
& \left. \left. \left. 12 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \log\left[1 - \frac{i e^{-i \operatorname{ArcSin}[c x]} (-c g + \sqrt{c^2 g^2 - h^2})}{h}\right] + 3 \sqrt{-(-c^2 g^2 + h^2)^2} \right. \right. \right. \\
& \left. \left. \left. \operatorname{ArcSin}[c x]^2 \log\left[1 - \frac{i e^{-i \operatorname{ArcSin}[c x]} (-c g + \sqrt{c^2 g^2 - h^2})}{h}\right] - 3 c g \sqrt{-c^2 g^2 + h^2} \operatorname{ArcSin}[c x]^2 \log\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}\right] - \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 3 \sqrt{-(-c^2 g^2 + h^2)^2} \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{i e^{-i \operatorname{ArcSin}[c x]} (c g + \sqrt{c^2 g^2 - h^2})}{h}\right] + 12 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}}\right] \\
& \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{i e^{-i \operatorname{ArcSin}[c x]} (c g + \sqrt{c^2 g^2 - h^2})}{h}\right] + 3 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{i e^{-i \operatorname{ArcSin}[c x]} (c g + \sqrt{c^2 g^2 - h^2})}{h}\right] - \\
& 3 i c g \sqrt{c^2 g^2 - h^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{e^{i \operatorname{ArcSin}[c x]} h}{i c g - \sqrt{-c^2 g^2 + h^2}}\right] + 3 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{e^{i \operatorname{ArcSin}[c x]} h}{i c g - \sqrt{-c^2 g^2 + h^2}}\right] + \\
& 3 i c g \sqrt{c^2 g^2 - h^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{e^{i \operatorname{ArcSin}[c x]} h}{i c g + \sqrt{-c^2 g^2 + h^2}}\right] + 3 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{e^{i \operatorname{ArcSin}[c x]} h}{i c g + \sqrt{-c^2 g^2 + h^2}}\right] + \\
& 3 \sqrt{-(-c^2 g^2 + h^2)^2} \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{(c g - \sqrt{c^2 g^2 - h^2}) (c x + i \sqrt{1 - c^2 x^2})}{h}\right] + \\
& 12 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{(c g - \sqrt{c^2 g^2 - h^2}) (c x + i \sqrt{1 - c^2 x^2})}{h}\right] - 3 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}[c x]^2 \\
& \operatorname{Log}\left[1 + \frac{(c g - \sqrt{c^2 g^2 - h^2}) (c x + i \sqrt{1 - c^2 x^2})}{h}\right] + 3 \sqrt{-(-c^2 g^2 + h^2)^2} \pi \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{(c g + \sqrt{c^2 g^2 - h^2}) (c x + i \sqrt{1 - c^2 x^2})}{h}\right] - \\
& 12 \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{c g}{h}}}{\sqrt{2}}\right] \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 + \frac{(c g + \sqrt{c^2 g^2 - h^2}) (c x + i \sqrt{1 - c^2 x^2})}{h}\right] - 3 \sqrt{-(-c^2 g^2 + h^2)^2} \\
& \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 + \frac{(c g + \sqrt{c^2 g^2 - h^2}) (c x + i \sqrt{1 - c^2 x^2})}{h}\right] - 6 i c g \sqrt{-c^2 g^2 + h^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}\right] + \\
& 6 i c g \sqrt{-c^2 g^2 + h^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}\right] - 6 c g \sqrt{c^2 g^2 - h^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{e^{i \operatorname{ArcSin}[c x]} h}{-i c g + \sqrt{-c^2 g^2 + h^2}}\right] - \\
& 6 i \sqrt{-(-c^2 g^2 + h^2)^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, \frac{e^{i \operatorname{ArcSin}[c x]} h}{-i c g + \sqrt{-c^2 g^2 + h^2}}\right] + 6 c g \sqrt{c^2 g^2 - h^2} \operatorname{ArcSin}[c x] \operatorname{PolyLog}\left[2, -\frac{e^{i \operatorname{ArcSin}[c x]} h}{i c g + \sqrt{-c^2 g^2 + h^2}}\right] -
\end{aligned}$$

$$\begin{aligned}
& 6 \frac{\sqrt{-(-c^2 g^2 + h^2)^2}}{\text{ArcSin}[c x] \text{PolyLog}[2, -\frac{e^{i \text{ArcSin}[c x]} h}{i c g + \sqrt{-c^2 g^2 + h^2}}] + 6 c g \sqrt{-c^2 g^2 + h^2} \text{PolyLog}[3, \frac{i e^{i \text{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}] - \\
& 6 c g \sqrt{-c^2 g^2 + h^2} \text{PolyLog}[3, \frac{i e^{i \text{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}] - 6 i c g \sqrt{c^2 g^2 - h^2} \text{PolyLog}[3, \frac{e^{i \text{ArcSin}[c x]} h}{-i c g + \sqrt{-c^2 g^2 + h^2}}] + \\
& 6 \frac{\sqrt{-(-c^2 g^2 + h^2)^2}}{\text{PolyLog}[3, \frac{e^{i \text{ArcSin}[c x]} h}{-i c g + \sqrt{-c^2 g^2 + h^2}}] + 6 i c g \sqrt{c^2 g^2 - h^2} \text{PolyLog}[3, -\frac{e^{i \text{ArcSin}[c x]} h}{i c g + \sqrt{-c^2 g^2 + h^2}}] + \\
& 6 \sqrt{-(-c^2 g^2 + h^2)^2} \text{PolyLog}[3, -\frac{e^{i \text{ArcSin}[c x]} h}{i c g + \sqrt{-c^2 g^2 + h^2}}] \Bigg) + \frac{\text{ArcSin}[c x] \text{Sin}[2 \text{ArcSin}[c x]]}{4 h} \Bigg)
\end{aligned}$$

**Problem 119: Unable to integrate problem.**

$$\int \frac{(d + e x + f x^2) (a + b \text{ArcSin}[c x])^2}{(g + h x)^2} dx$$

Optimal (type 4, 1323 leaves, 45 steps):

$$\begin{aligned}
& \frac{a^2 f x}{h^2} - \frac{2 b^2 f x}{h^2} - \frac{a^2 (f g^2 - e g h + d h^2)}{h^3 (g + h x)} + \frac{2 a b f \sqrt{1 - c^2 x^2}}{c h^2} + \frac{2 a b f x \operatorname{ArcSin}[c x]}{h^2} - \frac{2 a b (f g^2 - e g h + d h^2) \operatorname{ArcSin}[c x]}{h^3 (g + h x)} + \\
& \frac{2 b^2 f \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x]}{c h^2} + \frac{i a b (2 f g - e h) \operatorname{ArcSin}[c x]^2}{h^3} + \frac{b^2 f x \operatorname{ArcSin}[c x]^2}{h^2} - \frac{b^2 (f g^2 - e g h + d h^2) \operatorname{ArcSin}[c x]^2}{h^3 (g + h x)} + \\
& \frac{i b^2 (2 f g - e h) \operatorname{ArcSin}[c x]^3}{3 h^3} + \frac{2 a b c (f g^2 - e g h + d h^2) \operatorname{ArcTan}\left[\frac{h + c^2 g x}{\sqrt{c^2 g^2 - h^2} \sqrt{1 - c^2 x^2}}\right]}{h^3 \sqrt{c^2 g^2 - h^2}} - \frac{2 a b (2 f g - e h) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}\right]}{h^3} - \\
& \frac{2 i b^2 c (f g^2 - e g h + d h^2) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}\right]}{h^3 \sqrt{c^2 g^2 - h^2}} - \frac{b^2 (2 f g - e h) \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}\right]}{h^3} - \\
& \frac{2 a b (2 f g - e h) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}\right]}{h^3} + \frac{2 i b^2 c (f g^2 - e g h + d h^2) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}\right]}{h^3 \sqrt{c^2 g^2 - h^2}} - \\
& \frac{b^2 (2 f g - e h) \operatorname{ArcSin}[c x]^2 \operatorname{Log}\left[1 - \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}\right]}{h^3} - \frac{a^2 (2 f g - e h) \operatorname{Log}[g + h x]}{h^3} + \frac{2 i a b (2 f g - e h) \operatorname{PolyLog}[2, \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}]}{h^3} - \\
& \frac{2 b^2 c (f g^2 - e g h + d h^2) \operatorname{PolyLog}[2, \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}]}{h^3 \sqrt{c^2 g^2 - h^2}} + \frac{2 i b^2 (2 f g - e h) \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}]}{h^3} + \\
& \frac{2 i a b (2 f g - e h) \operatorname{PolyLog}[2, \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}]}{h^3} + \frac{2 b^2 c (f g^2 - e g h + d h^2) \operatorname{PolyLog}[2, \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}]}{h^3 \sqrt{c^2 g^2 - h^2}} + \\
& \frac{2 i b^2 (2 f g - e h) \operatorname{ArcSin}[c x] \operatorname{PolyLog}[2, \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}]}{h^3} - \frac{2 b^2 (2 f g - e h) \operatorname{PolyLog}[3, \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g - \sqrt{c^2 g^2 - h^2}}]}{h^3} - \frac{2 b^2 (2 f g - e h) \operatorname{PolyLog}[3, \frac{i e^{i \operatorname{ArcSin}[c x]} h}{c g + \sqrt{c^2 g^2 - h^2}}]}{h^3}
\end{aligned}$$

Result (type 8, 30 leaves):

$$\int \frac{(d + e x + f x^2) (a + b \operatorname{ArcSin}[c x])^2}{(g + h x)^2} dx$$

### Problem 120: Unable to integrate problem.

$$\int \frac{(e f + 2 d h x + e h x^2) (a + b \operatorname{ArcSin}[c x])^2}{(d + e x)^2} dx$$

Optimal (type 4, 520 leaves, 20 steps):

$$\begin{aligned} & -\frac{2 b^2 h x}{e} + \frac{2 a b h \sqrt{1 - c^2 x^2}}{c e} + \frac{2 b^2 h \sqrt{1 - c^2 x^2} \operatorname{ArcSin}[c x]}{c e} + \frac{h x (a + b \operatorname{ArcSin}[c x])^2}{e} - \frac{\left(f - \frac{d^2 h}{e^2}\right) (a + b \operatorname{ArcSin}[c x])^2}{d + e x} + \\ & \frac{2 a b c (e^2 f - d^2 h) \operatorname{ArcTan}\left[\frac{e + c^2 d x}{\sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2}}\right]}{e^2 \sqrt{c^2 d^2 - e^2}} - \frac{2 i b^2 c (e^2 f - d^2 h) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^2 \sqrt{c^2 d^2 - e^2}} + \\ & \frac{2 i b^2 c (e^2 f - d^2 h) \operatorname{ArcSin}[c x] \operatorname{Log}\left[1 - \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^2 \sqrt{c^2 d^2 - e^2}} - \frac{2 b^2 c (e^2 f - d^2 h) \operatorname{PolyLog}\left[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^2 \sqrt{c^2 d^2 - e^2}} + \frac{2 b^2 c (e^2 f - d^2 h) \operatorname{PolyLog}\left[2, \frac{i e e^{i \operatorname{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^2 \sqrt{c^2 d^2 - e^2}} \end{aligned}$$

Result (type 8, 35 leaves):

$$\int \frac{(e f + 2 d h x + e h x^2) (a + b \operatorname{ArcSin}[c x])^2}{(d + e x)^2} dx$$

### Problem 121: Unable to integrate problem.

$$\int \frac{(e f + 2 d h x + e h x^2)^2 (a + b \operatorname{ArcSin}[c x])^2}{(d + e x)^2} dx$$

Optimal (type 4, 920 leaves, 32 steps):

$$\begin{aligned}
& -\frac{4 b^2 h^2 x}{9 c^2} - \frac{2 b^2 h (2 e^2 f - d^2 h) x}{e^2} - \frac{b^2 d h^2 x^2}{2 e} - \frac{2}{27} b^2 h^2 x^3 + \frac{a b h (4 e^2 h + c^2 (36 e^2 f - 25 d^2 h)) \sqrt{1 - c^2 x^2}}{9 c^3 e^2} + \\
& \frac{5 a b d h^2 (d + e x) \sqrt{1 - c^2 x^2}}{9 c e^2} + \frac{2 a b h^2 (d + e x)^2 \sqrt{1 - c^2 x^2}}{9 c e^2} - \frac{a b d (2 c^2 d^2 + 3 e^2) h^2 \text{ArcSin}[c x]}{3 c^2 e^3} + \frac{4 b^2 h^2 \sqrt{1 - c^2 x^2} \text{ArcSin}[c x]}{9 c^3} + \\
& \frac{2 b^2 h (2 e^2 f - d^2 h) \sqrt{1 - c^2 x^2} \text{ArcSin}[c x]}{c e^2} + \frac{b^2 d h^2 x \sqrt{1 - c^2 x^2} \text{ArcSin}[c x]}{c e} + \frac{2 b^2 h^2 x^2 \sqrt{1 - c^2 x^2} \text{ArcSin}[c x]}{9 c} - \\
& \frac{b^2 d^3 h^2 \text{ArcSin}[c x]^2}{3 e^3} - \frac{b^2 d h^2 \text{ArcSin}[c x]^2}{2 c^2 e} + \frac{2 h (e^2 f - d^2 h) x (a + b \text{ArcSin}[c x])^2}{e^2} - \frac{(e^2 f - d^2 h)^2 (a + b \text{ArcSin}[c x])^2}{e^3 (d + e x)} + \\
& \frac{h^2 (d + e x)^3 (a + b \text{ArcSin}[c x])^2}{3 e^3} + \frac{2 a b c (e^2 f - d^2 h)^2 \text{ArcTan}\left[\frac{e + c^2 d x}{\sqrt{c^2 d^2 - e^2} \sqrt{1 - c^2 x^2}}\right]}{e^3 \sqrt{c^2 d^2 - e^2}} - \frac{2 i b^2 c (e^2 f - d^2 h)^2 \text{ArcSin}[c x] \text{Log}\left[1 - \frac{i e e^{i \text{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^3 \sqrt{c^2 d^2 - e^2}} + \\
& \frac{2 i b^2 c (e^2 f - d^2 h)^2 \text{ArcSin}[c x] \text{Log}\left[1 - \frac{i e e^{i \text{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^3 \sqrt{c^2 d^2 - e^2}} - \frac{2 b^2 c (e^2 f - d^2 h)^2 \text{PolyLog}\left[2, \frac{i e e^{i \text{ArcSin}[c x]}}{c d - \sqrt{c^2 d^2 - e^2}}\right]}{e^3 \sqrt{c^2 d^2 - e^2}} + \frac{2 b^2 c (e^2 f - d^2 h)^2 \text{PolyLog}\left[2, \frac{i e e^{i \text{ArcSin}[c x]}}{c d + \sqrt{c^2 d^2 - e^2}}\right]}{e^3 \sqrt{c^2 d^2 - e^2}}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{(e f + 2 d h x + e h x^2)^2 (a + b \text{ArcSin}[c x])^2}{(d + e x)^2} dx$$

**Problem 135:** Result more than twice size of optimal antiderivative.

$$\int \frac{\text{ArcSin}[a + b x]^2}{x} dx$$

Optimal (type 4, 271 leaves, 11 steps):

$$\begin{aligned}
& -\frac{1}{3} i \text{ArcSin}[a + b x]^3 + \text{ArcSin}[a + b x]^2 \text{Log}\left[1 - \frac{e^{i \text{ArcSin}[a+b x]}}{i a - \sqrt{1 - a^2}}\right] + \\
& \text{ArcSin}[a + b x]^2 \text{Log}\left[1 - \frac{e^{i \text{ArcSin}[a+b x]}}{i a + \sqrt{1 - a^2}}\right] - 2 i \text{ArcSin}[a + b x] \text{PolyLog}\left[2, \frac{e^{i \text{ArcSin}[a+b x]}}{i a - \sqrt{1 - a^2}}\right] - \\
& 2 i \text{ArcSin}[a + b x] \text{PolyLog}\left[2, \frac{e^{i \text{ArcSin}[a+b x]}}{i a + \sqrt{1 - a^2}}\right] + 2 \text{PolyLog}\left[3, \frac{e^{i \text{ArcSin}[a+b x]}}{i a - \sqrt{1 - a^2}}\right] + 2 \text{PolyLog}\left[3, \frac{e^{i \text{ArcSin}[a+b x]}}{i a + \sqrt{1 - a^2}}\right]
\end{aligned}$$

Result (type 4, 1014 leaves):

$$\begin{aligned}
& -\frac{1}{3} \operatorname{ArcSin}[a+b x]^3 + 8 \operatorname{ArcSin}\left[\frac{\sqrt{1-a}}{\sqrt{2}}\right] \operatorname{ArcSin}[a+b x] \operatorname{ArcTan}\left[\frac{(1+a) \operatorname{Cot}\left[\frac{1}{4}(\pi+2 \operatorname{ArcSin}[a+b x])\right]}{\sqrt{-1+a^2}}\right] - \\
& 8 i \operatorname{ArcSin}\left[\frac{\sqrt{1-a}}{\sqrt{2}}\right] \operatorname{ArcSin}[a+b x] \operatorname{ArcTan}\left[\frac{(1+a) \left(\cos \left[\frac{1}{2} \operatorname{ArcSin}[a+b x]\right]-\sin \left[\frac{1}{2} \operatorname{ArcSin}[a+b x]\right]\right)}{\sqrt{-1+a^2} \left(\cos \left[\frac{1}{2} \operatorname{ArcSin}[a+b x]\right]+\sin \left[\frac{1}{2} \operatorname{ArcSin}[a+b x]\right]\right)}\right] - \\
& \pi \operatorname{ArcSin}[a+b x] \operatorname{Log}\left[1+i\left(-a+\sqrt{-1+a^2}\right) e^{-i \operatorname{ArcSin}[a+b x]}\right]+4 \operatorname{ArcSin}\left[\frac{\sqrt{1-a}}{\sqrt{2}}\right] \operatorname{ArcSin}[a+b x] \operatorname{Log}\left[1+i\left(-a+\sqrt{-1+a^2}\right) e^{-i \operatorname{ArcSin}[a+b x]}\right]+ \\
& \operatorname{ArcSin}[a+b x]^2 \operatorname{Log}\left[1+i\left(-a+\sqrt{-1+a^2}\right) e^{-i \operatorname{ArcSin}[a+b x]}\right]-\pi \operatorname{ArcSin}[a+b x] \operatorname{Log}\left[1-i\left(a+\sqrt{-1+a^2}\right) e^{-i \operatorname{ArcSin}[a+b x]}\right]- \\
& 4 \operatorname{ArcSin}\left[\frac{\sqrt{1-a}}{\sqrt{2}}\right] \operatorname{ArcSin}[a+b x] \operatorname{Log}\left[1-i\left(a+\sqrt{-1+a^2}\right) e^{-i \operatorname{ArcSin}[a+b x]}\right]+ \\
& \operatorname{ArcSin}[a+b x]^2 \operatorname{Log}\left[1-i\left(a+\sqrt{-1+a^2}\right) e^{-i \operatorname{ArcSin}[a+b x]}\right]+\operatorname{ArcSin}[a+b x]^2 \operatorname{Log}\left[1+\frac{e^{i \operatorname{ArcSin}[a+b x]}}{-i a+\sqrt{1-a^2}}\right]+ \\
& \operatorname{ArcSin}[a+b x]^2 \operatorname{Log}\left[1-\frac{e^{i \operatorname{ArcSin}[a+b x]}}{i a+\sqrt{1-a^2}}\right]+\pi \operatorname{ArcSin}[a+b x] \operatorname{Log}\left[1+\left(a+\sqrt{-1+a^2}\right)\left(-a-b x-i \sqrt{1-(a+b x)^2}\right)\right]+ \\
& 4 \operatorname{ArcSin}\left[\frac{\sqrt{1-a}}{\sqrt{2}}\right] \operatorname{ArcSin}[a+b x] \operatorname{Log}\left[1+\left(a+\sqrt{-1+a^2}\right)\left(-a-b x-i \sqrt{1-(a+b x)^2}\right)\right]- \\
& \operatorname{ArcSin}[a+b x]^2 \operatorname{Log}\left[1+\left(a+\sqrt{-1+a^2}\right)\left(-a-b x-i \sqrt{1-(a+b x)^2}\right)\right]+\pi \operatorname{ArcSin}[a+b x] \operatorname{Log}\left[1+\left(-a+\sqrt{-1+a^2}\right)\left(a+b x+i \sqrt{1-(a+b x)^2}\right)\right]- \\
& 4 \operatorname{ArcSin}\left[\frac{\sqrt{1-a}}{\sqrt{2}}\right] \operatorname{ArcSin}[a+b x] \operatorname{Log}\left[1+\left(-a+\sqrt{-1+a^2}\right)\left(a+b x+i \sqrt{1-(a+b x)^2}\right)\right]- \\
& \operatorname{ArcSin}[a+b x]^2 \operatorname{Log}\left[1+\left(-a+\sqrt{-1+a^2}\right)\left(a+b x+i \sqrt{1-(a+b x)^2}\right)\right]-2 i \operatorname{ArcSin}[a+b x] \operatorname{PolyLog}\left[2,-\frac{e^{i \operatorname{ArcSin}[a+b x]}}{-i a+\sqrt{1-a^2}}\right]- \\
& 2 i \operatorname{ArcSin}[a+b x] \operatorname{PolyLog}\left[2,\frac{e^{i \operatorname{ArcSin}[a+b x]}}{i a+\sqrt{1-a^2}}\right]+2 \operatorname{PolyLog}\left[3,-\frac{e^{i \operatorname{ArcSin}[a+b x]}}{-i a+\sqrt{1-a^2}}\right]+2 \operatorname{PolyLog}\left[3,\frac{e^{i \operatorname{ArcSin}[a+b x]}}{i a+\sqrt{1-a^2}}\right]
\end{aligned}$$

**Problem 136: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{ArcSin}[a+b x]^2}{x^2} dx$$

Optimal (type 4, 230 leaves, 11 steps):

$$\begin{aligned}
 & -\frac{\text{ArcSin}[a+b x]^2}{x} - \frac{2 b \text{ArcSin}[a+b x] \text{Log}\left[1-\frac{e^{i \text{ArcSin}[a+b x]}}{i a-\sqrt{1-a^2}}\right]}{\sqrt{1-a^2}} + \\
 & \frac{2 b \text{ArcSin}[a+b x] \text{Log}\left[1-\frac{e^{i \text{ArcSin}[a+b x]}}{i a+\sqrt{1-a^2}}\right]}{\sqrt{1-a^2}} + \frac{2 \frac{i}{2} b \text{PolyLog}\left[2, \frac{e^{i \text{ArcSin}[a+b x]}}{i a-\sqrt{1-a^2}}\right]}{\sqrt{1-a^2}} - \frac{2 \frac{i}{2} b \text{PolyLog}\left[2, \frac{e^{i \text{ArcSin}[a+b x]}}{i a+\sqrt{1-a^2}}\right]}{\sqrt{1-a^2}}
 \end{aligned}$$

Result (type 4, 789 leaves) :

$$\begin{aligned}
& - \frac{\text{ArcSin}[a + b x]^2}{x} + \frac{2 b \pi \text{ArcTan}\left[\frac{1-a \tan\left[\frac{1}{2} \text{ArcSin}[a+b x]\right]}{\sqrt{-1+a^2}}\right]}{\sqrt{-1+a^2}} + \frac{1}{\sqrt{1-a^2}} \\
& 2 b \left( -2 \text{ArcCos}[a] \text{ArcTanh}\left[\frac{(1+a) \cot\left[\frac{1}{4} (\pi+2 \text{ArcSin}[a+b x])\right]}{\sqrt{1-a^2}}\right] - (\pi-2 \text{ArcSin}[a+b x]) \text{ArcTanh}\left[\frac{(-1+a) \tan\left[\frac{1}{4} (\pi+2 \text{ArcSin}[a+b x])\right]}{\sqrt{1-a^2}}\right] + \right. \\
& \left. \left( \text{ArcCos}[a] - 2 i \left( \text{ArcTanh}\left[\frac{(1+a) \cot\left[\frac{1}{4} (\pi+2 \text{ArcSin}[a+b x])\right]}{\sqrt{1-a^2}}\right] + \text{ArcTanh}\left[\frac{(-1+a) \tan\left[\frac{1}{4} (\pi+2 \text{ArcSin}[a+b x])\right]}{\sqrt{1-a^2}}\right] \right) \right) \right. \\
& \left. \text{Log}\left[\frac{\sqrt{1-a^2} e^{\frac{1}{4} i (\pi-2 \text{ArcSin}[a+b x])}}{\sqrt{2} \sqrt{b x}}\right] + \right. \\
& \left. \left( \text{ArcCos}[a] + 2 i \text{ArcTanh}\left[\frac{(1+a) \cot\left[\frac{1}{4} (\pi+2 \text{ArcSin}[a+b x])\right]}{\sqrt{1-a^2}}\right] + 2 i \text{ArcTanh}\left[\frac{(-1+a) \tan\left[\frac{1}{4} (\pi+2 \text{ArcSin}[a+b x])\right]}{\sqrt{1-a^2}}\right] \right) \right. \\
& \left. \text{Log}\left[\frac{\left(\frac{1}{2}-\frac{i}{2}\right) \sqrt{1-a^2} e^{\frac{1}{2} i \text{ArcSin}[a+b x]}}{\sqrt{b x}}\right] - \left( \text{ArcCos}[a] - 2 i \text{ArcTanh}\left[\frac{(1+a) \cot\left[\frac{1}{4} (\pi+2 \text{ArcSin}[a+b x])\right]}{\sqrt{1-a^2}}\right] \right) \text{Log}\left[ \right. \right. \\
& \left. \left. - \frac{(-1+a) \left(i+\frac{i}{2} a+\sqrt{1-a^2}\right) \left(-\frac{i}{2}+\cot\left[\frac{1}{4} (\pi+2 \text{ArcSin}[a+b x])\right]\right)}{1-a+\sqrt{1-a^2} \cot\left[\frac{1}{4} (\pi+2 \text{ArcSin}[a+b x])\right]} \right. - \left( \text{ArcCos}[a] + 2 i \text{ArcTanh}\left[\frac{(1+a) \cot\left[\frac{1}{4} (\pi+2 \text{ArcSin}[a+b x])\right]}{\sqrt{1-a^2}}\right] \right) \right. \\
& \left. \text{Log}\left[-\frac{(-1+a) \left(-\frac{i}{2}-\frac{i}{2} a+\sqrt{1-a^2}\right) \left(\frac{i}{2}+\cot\left[\frac{1}{4} (\pi+2 \text{ArcSin}[a+b x])\right]\right)}{1-a+\sqrt{1-a^2} \cot\left[\frac{1}{4} (\pi+2 \text{ArcSin}[a+b x])\right]}\right] + \right. \\
& \left. \left. i \left( -\text{PolyLog}\left[2, \frac{\left(a-\frac{i}{2} \sqrt{1-a^2}\right) \left(-1+a+\sqrt{1-a^2}\right) \cot\left[\frac{1}{4} (\pi+2 \text{ArcSin}[a+b x])\right]}{1-a+\sqrt{1-a^2} \cot\left[\frac{1}{4} (\pi+2 \text{ArcSin}[a+b x])\right]}\right] + \right. \right. \right. \\
& \left. \left. \left. \text{PolyLog}\left[2, \frac{\left(a+\frac{i}{2} \sqrt{1-a^2}\right) \left(-1+a+\sqrt{1-a^2}\right) \cot\left[\frac{1}{4} (\pi+2 \text{ArcSin}[a+b x])\right]}{1-a+\sqrt{1-a^2} \cot\left[\frac{1}{4} (\pi+2 \text{ArcSin}[a+b x])\right]}\right] \right) \right)
\end{aligned}$$

Problem 137: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{ArcSin}[a+b x]^2}{x^3} dx$$

Optimal (type 4, 272 leaves, 14 steps):

$$\begin{aligned}
& - \frac{b \sqrt{1 - (a + b x)^2} \operatorname{ArcSin}[a + b x]}{(1 - a^2) x} - \frac{\operatorname{ArcSin}[a + b x]^2}{2 x^2} - \frac{i a b^2 \operatorname{ArcSin}[a + b x] \operatorname{Log}\left[1 + \frac{i e^{i \operatorname{ArcSin}[a+b x]}}{a - \sqrt{-1+a^2}}\right]}{(-1 + a^2)^{3/2}} + \\
& \frac{i a b^2 \operatorname{ArcSin}[a + b x] \operatorname{Log}\left[1 + \frac{i e^{i \operatorname{ArcSin}[a+b x]}}{a + \sqrt{-1+a^2}}\right]}{(-1 + a^2)^{3/2}} + \frac{b^2 \operatorname{Log}[x]}{1 - a^2} - \frac{a b^2 \operatorname{PolyLog}\left[2, - \frac{i e^{i \operatorname{ArcSin}[a+b x]}}{a - \sqrt{-1+a^2}}\right]}{(-1 + a^2)^{3/2}} + \frac{a b^2 \operatorname{PolyLog}\left[2, - \frac{i e^{i \operatorname{ArcSin}[a+b x]}}{a + \sqrt{-1+a^2}}\right]}{(-1 + a^2)^{3/2}}
\end{aligned}$$

Result (type 4, 859 leaves):

$$\begin{aligned}
& \frac{b \sqrt{1 - (a + b x)^2} \operatorname{ArcSin}[a + b x]}{(-1 + a) (1 + a) x} - \frac{\operatorname{ArcSin}[a + b x]^2}{2 x^2} + \frac{b^2 \operatorname{Log}\left[-\frac{b x}{a}\right]}{1 - a^2} - \\
& \frac{1}{-1 + a^2} a b^2 \left( \frac{\pi \operatorname{ArcTan}\left[\frac{1-a \operatorname{Tan}\left[\frac{1}{2} \operatorname{ArcSin}[a+b x]\right]}{\sqrt{-1+a^2}}\right]}{\sqrt{-1+a^2}} + \frac{1}{\sqrt{1-a^2}} \left( -2 \operatorname{ArcCos}[a] \operatorname{ArcTanh}\left[\frac{(1+a) \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a+b x])\right]}{\sqrt{1-a^2}}\right] - (\pi - 2 \operatorname{ArcSin}[a+b x]) \right. \right. \\
& \left. \left. \operatorname{ArcTanh}\left[\frac{(-1+a) \operatorname{Tan}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a+b x])\right]}{\sqrt{1-a^2}}\right] + \left( \operatorname{ArcCos}[a] - 2 \operatorname{ArcTanh}\left[\frac{(1+a) \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a+b x])\right]}{\sqrt{1-a^2}}\right] + \operatorname{ArcTanh}\left[\frac{(-1+a) \operatorname{Tan}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a+b x])\right]}{\sqrt{1-a^2}}\right] \right) \operatorname{Log}\left[\frac{(-1)^{1/4} \sqrt{1-a^2} e^{-\frac{1}{2} i \operatorname{ArcSin}[a+b x]}}{\sqrt{2} \sqrt{b x}}\right] + \right. \\
& \left. \left( \operatorname{ArcCos}[a] + 2 \operatorname{ArcTanh}\left[\frac{(1+a) \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a+b x])\right]}{\sqrt{1-a^2}}\right] + 2 \operatorname{ArcTanh}\left[\frac{(-1+a) \operatorname{Tan}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a+b x])\right]}{\sqrt{1-a^2}}\right] \right) \operatorname{Log}\left[\frac{\left(\frac{1}{2} - \frac{i}{2}\right) \sqrt{1-a^2} e^{\frac{1}{2} i \operatorname{ArcSin}[a+b x]}}{\sqrt{b x}}\right] - \left( \operatorname{ArcCos}[a] - 2 \operatorname{ArcTanh}\left[\frac{(1+a) \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a+b x])\right]}{\sqrt{1-a^2}}\right] \right) \right. \\
& \left. \operatorname{Log}\left[-\frac{(-1+a) \left(i + i a + \sqrt{1-a^2}\right) \left(-i + \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a+b x])\right]\right)}{1 - a + \sqrt{1-a^2} \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a+b x])\right]}\right] - \left( \operatorname{ArcCos}[a] + \right. \right. \\
& \left. \left. 2 \operatorname{ArcTanh}\left[\frac{(1+a) \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a+b x])\right]}{\sqrt{1-a^2}}\right]\right) \operatorname{Log}\left[-\frac{(-1+a) \left(-i - i a + \sqrt{1-a^2}\right) \left(i + \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a+b x])\right]\right)}{1 - a + \sqrt{1-a^2} \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a+b x])\right]}\right] + \right. \\
& \left. i \left( -\operatorname{PolyLog}\left[2, \frac{\left(a - i \sqrt{1-a^2}\right) \left(-1 + a + \sqrt{1-a^2} \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a+b x])\right]\right)}{1 - a + \sqrt{1-a^2} \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a+b x])\right]}\right] + \right. \right. \\
& \left. \left. \operatorname{PolyLog}\left[2, \frac{\left(a + i \sqrt{1-a^2}\right) \left(-1 + a + \sqrt{1-a^2} \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a+b x])\right]\right)}{1 - a + \sqrt{1-a^2} \operatorname{Cot}\left[\frac{1}{4} (\pi + 2 \operatorname{ArcSin}[a+b x])\right]}\right]\right)\right)
\end{aligned}$$

### Problem 141: Unable to integrate problem.

$$\int \frac{\text{ArcSin}[a+b x]^3}{x} dx$$

Optimal (type 4, 365 leaves, 13 steps):

$$\begin{aligned} & -\frac{1}{4} i \text{ArcSin}[a+b x]^4 + \text{ArcSin}[a+b x]^3 \text{Log}\left[1 - \frac{e^{i \text{ArcSin}[a+b x]}}{i a - \sqrt{1-a^2}}\right] + \text{ArcSin}[a+b x]^3 \text{Log}\left[1 - \frac{e^{i \text{ArcSin}[a+b x]}}{i a + \sqrt{1-a^2}}\right] - \\ & 3 i \text{ArcSin}[a+b x]^2 \text{PolyLog}\left[2, \frac{e^{i \text{ArcSin}[a+b x]}}{i a - \sqrt{1-a^2}}\right] - 3 i \text{ArcSin}[a+b x]^2 \text{PolyLog}\left[2, \frac{e^{i \text{ArcSin}[a+b x]}}{i a + \sqrt{1-a^2}}\right] + 6 \text{ArcSin}[a+b x] \text{PolyLog}\left[3, \frac{e^{i \text{ArcSin}[a+b x]}}{i a - \sqrt{1-a^2}}\right] + \\ & 6 \text{ArcSin}[a+b x] \text{PolyLog}\left[3, \frac{e^{i \text{ArcSin}[a+b x]}}{i a + \sqrt{1-a^2}}\right] + 6 i \text{PolyLog}\left[4, \frac{e^{i \text{ArcSin}[a+b x]}}{i a - \sqrt{1-a^2}}\right] + 6 i \text{PolyLog}\left[4, \frac{e^{i \text{ArcSin}[a+b x]}}{i a + \sqrt{1-a^2}}\right] \end{aligned}$$

Result (type 8, 14 leaves):

$$\int \frac{\text{ArcSin}[a+b x]^3}{x} dx$$

### Problem 142: Unable to integrate problem.

$$\int \frac{\text{ArcSin}[a+b x]^3}{x^2} dx$$

Optimal (type 4, 316 leaves, 13 steps):

$$\begin{aligned} & -\frac{\text{ArcSin}[a+b x]^3}{x} + \frac{3 i b \text{ArcSin}[a+b x]^2 \text{Log}\left[1 + \frac{i e^{i \text{ArcSin}[a+b x]}}{a - \sqrt{-1+a^2}}\right]}{\sqrt{-1+a^2}} - \\ & \frac{3 i b \text{ArcSin}[a+b x]^2 \text{Log}\left[1 + \frac{i e^{i \text{ArcSin}[a+b x]}}{a + \sqrt{-1+a^2}}\right]}{\sqrt{-1+a^2}} + \frac{6 b \text{ArcSin}[a+b x] \text{PolyLog}\left[2, -\frac{i e^{i \text{ArcSin}[a+b x]}}{a - \sqrt{-1+a^2}}\right]}{\sqrt{-1+a^2}} - \\ & \frac{6 b \text{ArcSin}[a+b x] \text{PolyLog}\left[2, -\frac{i e^{i \text{ArcSin}[a+b x]}}{a + \sqrt{-1+a^2}}\right]}{\sqrt{-1+a^2}} + \frac{6 i b \text{PolyLog}\left[3, -\frac{i e^{i \text{ArcSin}[a+b x]}}{a - \sqrt{-1+a^2}}\right]}{\sqrt{-1+a^2}} - \frac{6 i b \text{PolyLog}\left[3, -\frac{i e^{i \text{ArcSin}[a+b x]}}{a + \sqrt{-1+a^2}}\right]}{\sqrt{-1+a^2}} \end{aligned}$$

Result (type 8, 14 leaves):

$$\int \frac{\text{ArcSin}[a+b x]^3}{x^2} dx$$

### Problem 173: Unable to integrate problem.

$$\int x^2 (a + b \operatorname{ArcSin}[c + d x])^n dx$$

Optimal (type 4, 611 leaves, 22 steps):

$$\begin{aligned}
& -\frac{i e^{-\frac{ia}{b}} (a + b \operatorname{ArcSin}[c + d x])^n \left(-\frac{i(a+b \operatorname{ArcSin}[c+d x])}{b}\right)^{-n} \operatorname{Gamma}[1+n, -\frac{i(a+b \operatorname{ArcSin}[c+d x])}{b}]}{8 d^3} - \\
& + \frac{i c^2 e^{-\frac{ia}{b}} (a + b \operatorname{ArcSin}[c + d x])^n \left(-\frac{i(a+b \operatorname{ArcSin}[c+d x])}{b}\right)^{-n} \operatorname{Gamma}[1+n, -\frac{i(a+b \operatorname{ArcSin}[c+d x])}{b}]}{2 d^3} + \\
& + \frac{i e^{\frac{ia}{b}} (a + b \operatorname{ArcSin}[c + d x])^n \left(\frac{i(a+b \operatorname{ArcSin}[c+d x])}{b}\right)^{-n} \operatorname{Gamma}[1+n, \frac{i(a+b \operatorname{ArcSin}[c+d x])}{b}]}{8 d^3} + \\
& + \frac{i c^2 e^{\frac{ia}{b}} (a + b \operatorname{ArcSin}[c + d x])^n \left(\frac{i(a+b \operatorname{ArcSin}[c+d x])}{b}\right)^{-n} \operatorname{Gamma}[1+n, \frac{i(a+b \operatorname{ArcSin}[c+d x])}{b}]}{2 d^3} + \\
& + \frac{2^{-2-n} c e^{-\frac{2ia}{b}} (a + b \operatorname{ArcSin}[c + d x])^n \left(-\frac{i(a+b \operatorname{ArcSin}[c+d x])}{b}\right)^{-n} \operatorname{Gamma}[1+n, -\frac{2i(a+b \operatorname{ArcSin}[c+d x])}{b}]}{d^3} + \\
& + \frac{2^{-2-n} c e^{\frac{2ia}{b}} (a + b \operatorname{ArcSin}[c + d x])^n \left(\frac{i(a+b \operatorname{ArcSin}[c+d x])}{b}\right)^{-n} \operatorname{Gamma}[1+n, \frac{2i(a+b \operatorname{ArcSin}[c+d x])}{b}]}{d^3} + \\
& - \frac{i 3^{-1-n} e^{-\frac{3ia}{b}} (a + b \operatorname{ArcSin}[c + d x])^n \left(-\frac{i(a+b \operatorname{ArcSin}[c+d x])}{b}\right)^{-n} \operatorname{Gamma}[1+n, -\frac{3i(a+b \operatorname{ArcSin}[c+d x])}{b}]}{8 d^3} - \\
& - \frac{i 3^{-1-n} e^{\frac{3ia}{b}} (a + b \operatorname{ArcSin}[c + d x])^n \left(\frac{i(a+b \operatorname{ArcSin}[c+d x])}{b}\right)^{-n} \operatorname{Gamma}[1+n, \frac{3i(a+b \operatorname{ArcSin}[c+d x])}{b}]}{8 d^3}
\end{aligned}$$

Result (type 8, 18 leaves):

$$\int x^2 (a + b \operatorname{ArcSin}[c + d x])^n dx$$

### Problem 205: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[c + d x])^3}{(c e + d e x)^4} dx$$

Optimal (type 4, 291 leaves, 16 steps):

$$\begin{aligned}
& -\frac{b^2 (a + b \operatorname{ArcSin}[c + d x])}{d e^4 (c + d x)} - \frac{b \sqrt{1 - (c + d x)^2} (a + b \operatorname{ArcSin}[c + d x])^2}{2 d e^4 (c + d x)^2} - \frac{(a + b \operatorname{ArcSin}[c + d x])^3}{3 d e^4 (c + d x)^3} \\
& - \frac{b (a + b \operatorname{ArcSin}[c + d x])^2 \operatorname{ArcTanh}[e^{i \operatorname{ArcSin}[c+d x]}]}{d e^4} - \frac{b^3 \operatorname{ArcTanh}[\sqrt{1 - (c + d x)^2}]}{d e^4} + \frac{i b^2 (a + b \operatorname{ArcSin}[c + d x]) \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c+d x]}]}{d e^4} \\
& - \frac{i b^2 (a + b \operatorname{ArcSin}[c + d x]) \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c+d x]}]}{d e^4} - \frac{b^3 \operatorname{PolyLog}[3, -e^{i \operatorname{ArcSin}[c+d x]}]}{d e^4} + \frac{b^3 \operatorname{PolyLog}[3, e^{i \operatorname{ArcSin}[c+d x]}]}{d e^4}
\end{aligned}$$

Result (type 4, 732 leaves):

$$\begin{aligned}
& -\frac{a^3}{3 d e^4 (c + d x)^3} - \frac{a^2 b \sqrt{1 - c^2 - 2 c d x - d^2 x^2}}{2 d e^4 (c + d x)^2} - \frac{a^2 b \operatorname{ArcSin}[c + d x]}{d e^4 (c + d x)^3} + \\
& \frac{a^2 b \operatorname{Log}[c + d x]}{2 d e^4} - \frac{a^2 b \operatorname{Log}[1 + \sqrt{1 - c^2 - 2 c d x - d^2 x^2}]}{2 d e^4} + \frac{1}{8 d e^4} a b^2 \left( 8 i \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c+d x]}] - \right. \\
& \frac{1}{(c + d x)^3} 2 \left( 2 + 4 \operatorname{ArcSin}[c + d x]^2 - 2 \operatorname{Cos}[2 \operatorname{ArcSin}[c + d x]] - 3 (c + d x) \operatorname{ArcSin}[c + d x] \operatorname{Log}[1 - e^{i \operatorname{ArcSin}[c+d x]}] + \right. \\
& 3 (c + d x) \operatorname{ArcSin}[c + d x] \operatorname{Log}[1 + e^{i \operatorname{ArcSin}[c+d x]}] + 4 i (c + d x)^3 \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c+d x]}] + 2 \operatorname{ArcSin}[c + d x] \operatorname{Sin}[2 \operatorname{ArcSin}[c + d x]] + \\
& \left. \operatorname{ArcSin}[c + d x] \operatorname{Log}[1 - e^{i \operatorname{ArcSin}[c+d x]}] \operatorname{Sin}[3 \operatorname{ArcSin}[c + d x]] - \operatorname{ArcSin}[c + d x] \operatorname{Log}[1 + e^{i \operatorname{ArcSin}[c+d x]}] \operatorname{Sin}[3 \operatorname{ArcSin}[c + d x]] \right) + \\
& \frac{1}{48 d e^4} b^3 \left( -24 \operatorname{ArcSin}[c + d x] \operatorname{Cot}\left[\frac{1}{2} \operatorname{ArcSin}[c + d x]\right] - 4 \operatorname{ArcSin}[c + d x]^3 \operatorname{Cot}\left[\frac{1}{2} \operatorname{ArcSin}[c + d x]\right] - 6 \operatorname{ArcSin}[c + d x]^2 \operatorname{Csc}\left[\frac{1}{2} \operatorname{ArcSin}[c + d x]\right]^2 - \right. \\
& (c + d x) \operatorname{ArcSin}[c + d x]^3 \operatorname{Csc}\left[\frac{1}{2} \operatorname{ArcSin}[c + d x]\right]^4 + 24 \operatorname{ArcSin}[c + d x]^2 \operatorname{Log}[1 - e^{i \operatorname{ArcSin}[c+d x]}] - 24 \operatorname{ArcSin}[c + d x]^2 \operatorname{Log}[1 + e^{i \operatorname{ArcSin}[c+d x]}] + \\
& 48 \operatorname{Log}\left[\operatorname{Tan}\left[\frac{1}{2} \operatorname{ArcSin}[c + d x]\right]\right] + 48 i \operatorname{ArcSin}[c + d x] \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c+d x]}] - 48 i \operatorname{ArcSin}[c + d x] \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c+d x]}] - \\
& 48 \operatorname{PolyLog}[3, -e^{i \operatorname{ArcSin}[c+d x]}] + 48 \operatorname{PolyLog}[3, e^{i \operatorname{ArcSin}[c+d x]}] + 6 \operatorname{ArcSin}[c + d x]^2 \operatorname{Sec}\left[\frac{1}{2} \operatorname{ArcSin}[c + d x]\right]^2 - \\
& \left. \frac{16 \operatorname{ArcSin}[c + d x]^3 \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSin}[c + d x]\right]^4}{(c + d x)^3} - 24 \operatorname{ArcSin}[c + d x] \operatorname{Tan}\left[\frac{1}{2} \operatorname{ArcSin}[c + d x]\right] - 4 \operatorname{ArcSin}[c + d x]^3 \operatorname{Tan}\left[\frac{1}{2} \operatorname{ArcSin}[c + d x]\right] \right)
\end{aligned}$$

Problem 210: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[c + d x])^4}{c e + d e x} dx$$

Optimal (type 4, 202 leaves, 10 steps):

$$\begin{aligned}
& - \frac{\frac{i}{5} (a + b \operatorname{ArcSin}[c + d x])^5}{b d e} + \frac{(a + b \operatorname{ArcSin}[c + d x])^4 \operatorname{Log}[1 - e^{2i \operatorname{ArcSin}[c+d x]}]}{d e} - \\
& \frac{2 i b (a + b \operatorname{ArcSin}[c + d x])^3 \operatorname{PolyLog}[2, e^{2i \operatorname{ArcSin}[c+d x]}]}{d e} + \frac{3 b^2 (a + b \operatorname{ArcSin}[c + d x])^2 \operatorname{PolyLog}[3, e^{2i \operatorname{ArcSin}[c+d x]}]}{d e} + \\
& \frac{3 i b^3 (a + b \operatorname{ArcSin}[c + d x]) \operatorname{PolyLog}[4, e^{2i \operatorname{ArcSin}[c+d x]}]}{d e} - \frac{3 b^4 \operatorname{PolyLog}[5, e^{2i \operatorname{ArcSin}[c+d x]}]}{2 d e}
\end{aligned}$$

Result (type 4, 439 leaves):

$$\begin{aligned}
& \frac{1}{16 d e} \left( 16 a^4 \operatorname{Log}[c + d x] + 64 a^3 b \left( \operatorname{ArcSin}[c + d x] \operatorname{Log}[1 - e^{2i \operatorname{ArcSin}[c+d x]}] - \frac{1}{2} i (\operatorname{ArcSin}[c + d x]^2 + \operatorname{PolyLog}[2, e^{2i \operatorname{ArcSin}[c+d x]}]) \right) + \right. \\
& 4 a^2 b^2 (-i \pi^3 + 8 i \operatorname{ArcSin}[c + d x]^3 + 24 \operatorname{ArcSin}[c + d x]^2 \operatorname{Log}[1 - e^{-2i \operatorname{ArcSin}[c+d x]}] + \\
& 24 i \operatorname{ArcSin}[c + d x] \operatorname{PolyLog}[2, e^{-2i \operatorname{ArcSin}[c+d x]}] + 12 \operatorname{PolyLog}[3, e^{-2i \operatorname{ArcSin}[c+d x]}]) - \\
& i a b^3 (\pi^4 - 16 \operatorname{ArcSin}[c + d x]^4 + 64 i \operatorname{ArcSin}[c + d x]^3 \operatorname{Log}[1 - e^{-2i \operatorname{ArcSin}[c+d x]}] - 96 \operatorname{ArcSin}[c + d x]^2 \operatorname{PolyLog}[2, e^{-2i \operatorname{ArcSin}[c+d x]}] + \\
& 96 i \operatorname{ArcSin}[c + d x] \operatorname{PolyLog}[3, e^{-2i \operatorname{ArcSin}[c+d x]}] + 48 \operatorname{PolyLog}[4, e^{-2i \operatorname{ArcSin}[c+d x]}]) + \\
& 16 b^4 \left( -\frac{i \pi^5}{160} + \frac{1}{5} i \operatorname{ArcSin}[c + d x]^5 + \operatorname{ArcSin}[c + d x]^4 \operatorname{Log}[1 - e^{-2i \operatorname{ArcSin}[c+d x]}] + 2 i \operatorname{ArcSin}[c + d x]^3 \operatorname{PolyLog}[2, e^{-2i \operatorname{ArcSin}[c+d x]}] + \right. \\
& \left. 3 \operatorname{ArcSin}[c + d x]^2 \operatorname{PolyLog}[3, e^{-2i \operatorname{ArcSin}[c+d x]}] - 3 i \operatorname{ArcSin}[c + d x] \operatorname{PolyLog}[4, e^{-2i \operatorname{ArcSin}[c+d x]}] - \frac{3}{2} \operatorname{PolyLog}[5, e^{-2i \operatorname{ArcSin}[c+d x]}] \right)
\end{aligned}$$

### Problem 211: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcSin}[c + d x])^4}{(c e + d e x)^2} dx$$

Optimal (type 4, 270 leaves, 13 steps):

$$\begin{aligned}
& - \frac{(a + b \operatorname{ArcSin}[c + d x])^4}{d e^2 (c + d x)} - \frac{8 b (a + b \operatorname{ArcSin}[c + d x])^3 \operatorname{ArcTanh}[e^{i \operatorname{ArcSin}[c+d x]}]}{d e^2} + \frac{12 i b^2 (a + b \operatorname{ArcSin}[c + d x])^2 \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c+d x]}]}{d e^2} - \\
& \frac{12 i b^2 (a + b \operatorname{ArcSin}[c + d x])^2 \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c+d x]}]}{d e^2} - \frac{24 b^3 (a + b \operatorname{ArcSin}[c + d x]) \operatorname{PolyLog}[3, -e^{i \operatorname{ArcSin}[c+d x]}]}{d e^2} + \\
& \frac{24 b^3 (a + b \operatorname{ArcSin}[c + d x]) \operatorname{PolyLog}[3, e^{i \operatorname{ArcSin}[c+d x]}]}{d e^2} - \frac{24 i b^4 \operatorname{PolyLog}[4, -e^{i \operatorname{ArcSin}[c+d x]}]}{d e^2} + \frac{24 i b^4 \operatorname{PolyLog}[4, e^{i \operatorname{ArcSin}[c+d x]}]}{d e^2}
\end{aligned}$$

Result (type 4, 575 leaves):

$$\begin{aligned}
& \frac{1}{d e^2} \left( -\frac{a^4}{c + d x} - 4 a^3 b \left( \frac{\text{ArcSin}[c + d x]}{c + d x} + \log \left[ \frac{1}{2} (c + d x) \csc \left[ \frac{1}{2} \text{ArcSin}[c + d x] \right] \right] - \log \left[ \sin \left[ \frac{1}{2} \text{ArcSin}[c + d x] \right] \right] \right) + \right. \\
& 6 a^2 b^2 \left( \text{ArcSin}[c + d x] \left( -\frac{\text{ArcSin}[c + d x]}{c + d x} + 2 \log \left[ 1 - e^{i \text{ArcSin}[c+d x]} \right] - 2 \log \left[ 1 + e^{i \text{ArcSin}[c+d x]} \right] \right) + \right. \\
& 2 i \text{PolyLog}[2, -e^{i \text{ArcSin}[c+d x]}] - 2 i \text{PolyLog}[2, e^{i \text{ArcSin}[c+d x]}] \Big) + \\
& 4 a b^3 \left( -\frac{\text{ArcSin}[c + d x]^3}{c + d x} + 3 \text{ArcSin}[c + d x]^2 \log \left[ 1 - e^{i \text{ArcSin}[c+d x]} \right] - 3 \text{ArcSin}[c + d x]^2 \log \left[ 1 + e^{i \text{ArcSin}[c+d x]} \right] + 6 i \text{ArcSin}[c + d x] \right. \\
& \text{PolyLog}[2, -e^{i \text{ArcSin}[c+d x]}] - 6 i \text{ArcSin}[c + d x] \text{PolyLog}[2, e^{i \text{ArcSin}[c+d x]}] - 6 \text{PolyLog}[3, -e^{i \text{ArcSin}[c+d x]}] + 6 \text{PolyLog}[3, e^{i \text{ArcSin}[c+d x]}] \Big) + \\
& b^4 \left( -\frac{i \pi^4}{2} + i \text{ArcSin}[c + d x]^4 - \frac{\text{ArcSin}[c + d x]^4}{c + d x} + 4 \text{ArcSin}[c + d x]^3 \log \left[ 1 - e^{-i \text{ArcSin}[c+d x]} \right] - 4 \text{ArcSin}[c + d x]^3 \log \left[ 1 + e^{i \text{ArcSin}[c+d x]} \right] + \right. \\
& 12 i \text{ArcSin}[c + d x]^2 \text{PolyLog}[2, e^{-i \text{ArcSin}[c+d x]}] + 12 i \text{ArcSin}[c + d x]^2 \text{PolyLog}[2, -e^{i \text{ArcSin}[c+d x]}] + \\
& 24 \text{ArcSin}[c + d x] \text{PolyLog}[3, e^{-i \text{ArcSin}[c+d x]}] - 24 \text{ArcSin}[c + d x] \text{PolyLog}[3, -e^{i \text{ArcSin}[c+d x]}] - \\
& \left. 24 i \text{PolyLog}[4, e^{-i \text{ArcSin}[c+d x]}] - 24 i \text{PolyLog}[4, -e^{i \text{ArcSin}[c+d x]}] \right)
\end{aligned}$$

**Problem 213:** Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \text{ArcSin}[c + d x])^4}{(c e + d e x)^4} dx$$

Optimal (type 4, 439 leaves, 21 steps):

$$\begin{aligned}
& \frac{2 b^2 (a + b \text{ArcSin}[c + d x])^2}{d e^4 (c + d x)} - \frac{2 b \sqrt{1 - (c + d x)^2} (a + b \text{ArcSin}[c + d x])^3}{3 d e^4 (c + d x)^2} - \frac{(a + b \text{ArcSin}[c + d x])^4}{3 d e^4 (c + d x)^3} \\
& \frac{8 b^3 (a + b \text{ArcSin}[c + d x]) \text{ArcTanh}[e^{i \text{ArcSin}[c+d x]}]}{d e^4} - \frac{4 b (a + b \text{ArcSin}[c + d x])^3 \text{ArcTanh}[e^{i \text{ArcSin}[c+d x]}]}{3 d e^4} + \\
& \frac{4 i b^4 \text{PolyLog}[2, -e^{i \text{ArcSin}[c+d x]}]}{d e^4} + \frac{2 i b^2 (a + b \text{ArcSin}[c + d x])^2 \text{PolyLog}[2, -e^{i \text{ArcSin}[c+d x]}]}{d e^4} - \frac{4 i b^4 \text{PolyLog}[2, e^{i \text{ArcSin}[c+d x]}]}{d e^4} - \\
& \frac{2 i b^2 (a + b \text{ArcSin}[c + d x])^2 \text{PolyLog}[2, e^{i \text{ArcSin}[c+d x]}]}{d e^4} - \frac{4 b^3 (a + b \text{ArcSin}[c + d x]) \text{PolyLog}[3, -e^{i \text{ArcSin}[c+d x]}]}{d e^4} + \\
& \frac{4 b^3 (a + b \text{ArcSin}[c + d x]) \text{PolyLog}[3, e^{i \text{ArcSin}[c+d x]}]}{d e^4} - \frac{4 i b^4 \text{PolyLog}[4, -e^{i \text{ArcSin}[c+d x]}]}{d e^4} + \frac{4 i b^4 \text{PolyLog}[4, e^{i \text{ArcSin}[c+d x]}]}{d e^4}
\end{aligned}$$

Result (type 4, 1274 leaves):

$$\begin{aligned}
& -\frac{a^4}{3 d e^4 (c + d x)^3} + \frac{1}{4 d e^4} a^2 b^2 \left( 8 i \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c + d x]}] - \right. \\
& \quad \frac{1}{(c + d x)^3} 2 \left( 2 + 4 \operatorname{ArcSin}[c + d x]^2 - 2 \cos[2 \operatorname{ArcSin}[c + d x]] - 3 (c + d x) \operatorname{ArcSin}[c + d x] \log[1 - e^{i \operatorname{ArcSin}[c + d x]}] + \right. \\
& \quad \left. 3 (c + d x) \operatorname{ArcSin}[c + d x] \log[1 + e^{i \operatorname{ArcSin}[c + d x]}] + 4 i (c + d x)^3 \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c + d x]}] + 2 \operatorname{ArcSin}[c + d x] \sin[2 \operatorname{ArcSin}[c + d x]] + \right. \\
& \quad \left. \operatorname{ArcSin}[c + d x] \log[1 - e^{i \operatorname{ArcSin}[c + d x]}] \sin[3 \operatorname{ArcSin}[c + d x]] - \operatorname{ArcSin}[c + d x] \log[1 + e^{i \operatorname{ArcSin}[c + d x]}] \sin[3 \operatorname{ArcSin}[c + d x]] \right) + \\
& \quad \frac{1}{12 d e^4} a b^3 \left( -24 \operatorname{ArcSin}[c + d x] \cot[\frac{1}{2} \operatorname{ArcSin}[c + d x]] - 4 \operatorname{ArcSin}[c + d x]^3 \cot[\frac{1}{2} \operatorname{ArcSin}[c + d x]] - 6 \operatorname{ArcSin}[c + d x]^2 \csc[\frac{1}{2} \operatorname{ArcSin}[c + d x]]^2 - \right. \\
& \quad \left. (c + d x) \operatorname{ArcSin}[c + d x]^3 \csc[\frac{1}{2} \operatorname{ArcSin}[c + d x]]^4 + 24 \operatorname{ArcSin}[c + d x]^2 \log[1 - e^{i \operatorname{ArcSin}[c + d x]}] - 24 \operatorname{ArcSin}[c + d x]^2 \log[1 + e^{i \operatorname{ArcSin}[c + d x]}] + \right. \\
& \quad 48 \log[\tan[\frac{1}{2} \operatorname{ArcSin}[c + d x]]] + 48 i \operatorname{ArcSin}[c + d x] \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c + d x]}] - 48 i \operatorname{ArcSin}[c + d x] \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c + d x]}] - \\
& \quad 48 \operatorname{PolyLog}[3, -e^{i \operatorname{ArcSin}[c + d x]}] + 48 \operatorname{PolyLog}[3, e^{i \operatorname{ArcSin}[c + d x]}] + 6 \operatorname{ArcSin}[c + d x]^2 \sec[\frac{1}{2} \operatorname{ArcSin}[c + d x]]^2 - \\
& \quad \left. \frac{16 \operatorname{ArcSin}[c + d x]^3 \sin[\frac{1}{2} \operatorname{ArcSin}[c + d x]]^4}{(c + d x)^3} - 24 \operatorname{ArcSin}[c + d x] \tan[\frac{1}{2} \operatorname{ArcSin}[c + d x]] - 4 \operatorname{ArcSin}[c + d x]^3 \tan[\frac{1}{2} \operatorname{ArcSin}[c + d x]] \right) + \\
& \quad \frac{1}{24 d e^4} b^4 \left( -2 i \pi^4 + 4 i \operatorname{ArcSin}[c + d x]^4 - 24 \operatorname{ArcSin}[c + d x]^2 \cot[\frac{1}{2} \operatorname{ArcSin}[c + d x]] - 2 \operatorname{ArcSin}[c + d x]^4 \cot[\frac{1}{2} \operatorname{ArcSin}[c + d x]] - \right. \\
& \quad 4 \operatorname{ArcSin}[c + d x]^3 \csc[\frac{1}{2} \operatorname{ArcSin}[c + d x]]^2 - \frac{1}{2} (c + d x) \operatorname{ArcSin}[c + d x]^4 \csc[\frac{1}{2} \operatorname{ArcSin}[c + d x]]^4 + 16 \operatorname{ArcSin}[c + d x]^3 \log[1 - e^{-i \operatorname{ArcSin}[c + d x]}] + \\
& \quad 96 \operatorname{ArcSin}[c + d x] \log[1 - e^{i \operatorname{ArcSin}[c + d x]}] - 96 \operatorname{ArcSin}[c + d x] \log[1 + e^{i \operatorname{ArcSin}[c + d x]}] - 16 \operatorname{ArcSin}[c + d x]^3 \log[1 + e^{i \operatorname{ArcSin}[c + d x]}] + \\
& \quad 48 i \operatorname{ArcSin}[c + d x]^2 \operatorname{PolyLog}[2, e^{-i \operatorname{ArcSin}[c + d x]}] + 48 i (2 + \operatorname{ArcSin}[c + d x]^2) \operatorname{PolyLog}[2, -e^{i \operatorname{ArcSin}[c + d x]}] - \\
& \quad 96 i \operatorname{PolyLog}[2, e^{i \operatorname{ArcSin}[c + d x]}] + 96 \operatorname{ArcSin}[c + d x] \operatorname{PolyLog}[3, e^{-i \operatorname{ArcSin}[c + d x]}] - 96 \operatorname{ArcSin}[c + d x] \operatorname{PolyLog}[3, -e^{i \operatorname{ArcSin}[c + d x]}] - \\
& \quad 96 i \operatorname{PolyLog}[4, e^{-i \operatorname{ArcSin}[c + d x]}] - 96 i \operatorname{PolyLog}[4, -e^{i \operatorname{ArcSin}[c + d x]}] + 4 \operatorname{ArcSin}[c + d x]^3 \sec[\frac{1}{2} \operatorname{ArcSin}[c + d x]]^2 - \\
& \quad \left. \frac{8 \operatorname{ArcSin}[c + d x]^4 \sin[\frac{1}{2} \operatorname{ArcSin}[c + d x]]^4}{(c + d x)^3} - 24 \operatorname{ArcSin}[c + d x]^2 \tan[\frac{1}{2} \operatorname{ArcSin}[c + d x]] - 2 \operatorname{ArcSin}[c + d x]^4 \tan[\frac{1}{2} \operatorname{ArcSin}[c + d x]] \right) + \\
& \quad \frac{1}{d e^4} 4 a^3 b \left( -\frac{1}{12} \operatorname{ArcSin}[c + d x] \cot[\frac{1}{2} \operatorname{ArcSin}[c + d x]] - \frac{1}{24} \csc[\frac{1}{2} \operatorname{ArcSin}[c + d x]]^2 - \frac{1}{24} \operatorname{ArcSin}[c + d x] \cot[\frac{1}{2} \operatorname{ArcSin}[c + d x]] \right. \\
& \quad \left. \csc[\frac{1}{2} \operatorname{ArcSin}[c + d x]]^2 - \frac{1}{6} \log[\cos[\frac{1}{2} \operatorname{ArcSin}[c + d x]]] + \frac{1}{6} \log[\sin[\frac{1}{2} \operatorname{ArcSin}[c + d x]]] + \frac{1}{24} \sec[\frac{1}{2} \operatorname{ArcSin}[c + d x]]^2 - \right)
\end{aligned}$$

$$\frac{1}{12} \operatorname{ArcSin}[c + d x] \operatorname{Tan}\left[\frac{1}{2} \operatorname{ArcSin}[c + d x]\right] - \frac{1}{24} \operatorname{ArcSin}[c + d x] \operatorname{Sec}\left[\frac{1}{2} \operatorname{ArcSin}[c + d x]\right]^2 \operatorname{Tan}\left[\frac{1}{2} \operatorname{ArcSin}[c + d x]\right]$$

**Problem 214:** Result more than twice size of optimal antiderivative.

$$\int (a + b \operatorname{ArcSin}[c + d x])^5 dx$$

Optimal (type 3, 164 leaves, 8 steps):

$$\begin{aligned} & 120 a b^4 x + \frac{120 b^5 \sqrt{1 - (c + d x)^2}}{d} + \frac{120 b^5 (c + d x) \operatorname{ArcSin}[c + d x]}{d} - \frac{60 b^3 \sqrt{1 - (c + d x)^2} (a + b \operatorname{ArcSin}[c + d x])^2}{d} - \\ & \frac{20 b^2 (c + d x) (a + b \operatorname{ArcSin}[c + d x])^3}{d} + \frac{5 b \sqrt{1 - (c + d x)^2} (a + b \operatorname{ArcSin}[c + d x])^4}{d} + \frac{(c + d x) (a + b \operatorname{ArcSin}[c + d x])^5}{d} \end{aligned}$$

Result (type 3, 332 leaves):

$$\begin{aligned} & \frac{1}{d} \left( a (a^4 - 20 a^2 b^2 + 120 b^4) (c + d x) + 5 b (a^4 - 12 a^2 b^2 + 24 b^4) \sqrt{1 - (c + d x)^2} + \right. \\ & 5 b \left( a^4 (c + d x) - 12 a^2 b^2 (c + d x) + 24 b^4 (c + d x) + 4 a^3 b \sqrt{1 - (c + d x)^2} - 24 a b^3 \sqrt{1 - (c + d x)^2} \right) \operatorname{ArcSin}[c + d x] - \\ & 10 b^2 \left( -a^3 (c + d x) + 6 a b^2 (c + d x) - 3 a^2 b \sqrt{1 - (c + d x)^2} + 6 b^3 \sqrt{1 - (c + d x)^2} \right) \operatorname{ArcSin}[c + d x]^2 - \\ & 10 b^3 \left( -a^2 (c + d x) + 2 b^2 (c + d x) - 2 a b \sqrt{1 - (c + d x)^2} \right) \operatorname{ArcSin}[c + d x]^3 + \\ & \left. 5 b^4 \left( a c + a d x + b \sqrt{1 - (c + d x)^2} \right) \operatorname{ArcSin}[c + d x]^4 + b^5 (c + d x) \operatorname{ArcSin}[c + d x]^5 \right) \end{aligned}$$

**Problem 292:** Result more than twice size of optimal antiderivative.

$$\int (c e + d e x)^{5/2} (a + b \operatorname{ArcSin}[c + d x])^2 dx$$

Optimal (type 5, 130 leaves, 3 steps):

$$\begin{aligned} & \frac{2 (e (c + d x))^{7/2} (a + b \operatorname{ArcSin}[c + d x])^2}{7 d e} - \frac{8 b (e (c + d x))^{9/2} (a + b \operatorname{ArcSin}[c + d x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{9}{4}, \frac{13}{4}, (c + d x)^2\right]}{63 d e^2} + \\ & \frac{16 b^2 (e (c + d x))^{11/2} \operatorname{HypergeometricPFQ}\left[\left\{1, \frac{11}{4}, \frac{11}{4}\right\}, \left\{\frac{13}{4}, \frac{15}{4}\right\}, (c + d x)^2\right]}{693 d e^3} \end{aligned}$$

Result (type 5, 328 leaves):

$$\begin{aligned}
& \frac{1}{6174 d} \\
& \left( e (c + d x) \right)^{5/2} \left( 1764 a^2 (c + d x) + 168 a b \left( 21 (c + d x) \operatorname{ArcSin}[c + d x] + \left( -2 \sqrt{c + d x} (-5 + 2 (c + d x)^2 + 3 (c + d x)^4) + 10 (c + d x) \sqrt{1 - \frac{1}{(c + d x)^2}} \right. \right. \right. \\
& \left. \left. \left. \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{1}{\sqrt{c + d x}}\right], -1] \right) \right) \Big/ \left( (c + d x)^{5/2} \sqrt{1 - (c + d x)^2} \right) + \\
& \frac{1}{(c + d x)^2} b^2 \left( -1336 (c + d x) + 1932 \sqrt{1 - (c + d x)^2} \operatorname{ArcSin}[c + d x] + 1323 (c + d x) \operatorname{ArcSin}[c + d x]^2 - \right. \\
& 252 \operatorname{ArcSin}[c + d x] \cos[3 \operatorname{ArcSin}[c + d x]] - 1680 \sqrt{1 - (c + d x)^2} \operatorname{ArcSin}[c + d x] \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{5}{4}, (c + d x)^2\right] + \\
& \left. \frac{210 \sqrt{2} \pi (c + d x) \operatorname{HypergeometricPFQ}\left[\left\{\frac{3}{4}, \frac{3}{4}, 1\right\}, \left\{\frac{5}{4}, \frac{7}{4}\right\}, (c + d x)^2\right]}{\Gamma\left[\frac{5}{4}\right] \Gamma\left[\frac{7}{4}\right]} \right. \\
& \left. \left. \left. 72 \sin[3 \operatorname{ArcSin}[c + d x]] - 441 \operatorname{ArcSin}[c + d x]^2 \sin[3 \operatorname{ArcSin}[c + d x]] \right) \right)
\end{aligned}$$

Problem 294: Result more than twice size of optimal antiderivative.

$$\int \sqrt{c e + d e x} (a + b \operatorname{ArcSin}[c + d x])^2 dx$$

Optimal (type 5, 130 leaves, 3 steps):

$$\begin{aligned}
& \frac{2 (e (c + d x))^{3/2} (a + b \operatorname{ArcSin}[c + d x])^2}{3 d e} - \frac{8 b (e (c + d x))^{5/2} (a + b \operatorname{ArcSin}[c + d x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{5}{4}, \frac{9}{4}, (c + d x)^2\right]}{15 d e^2} + \\
& \frac{16 b^2 (e (c + d x))^{7/2} \operatorname{HypergeometricPFQ}\left[\left\{1, \frac{7}{4}, \frac{7}{4}\right\}, \left\{\frac{9}{4}, \frac{11}{4}\right\}, (c + d x)^2\right]}{105 d e^3}
\end{aligned}$$

Result (type 5, 267 leaves):

$$\left( \frac{1}{27 d} \sqrt{e(c+dx)} \right) \left( 18 a^2 (c+dx) + 36 a b (c+dx) \operatorname{ArcSin}[c+dx] + 24 b^2 \sqrt{1 - (c+dx)^2} \operatorname{ArcSin}[c+dx] + 2 b^2 (c+dx) (-8 + 9 \operatorname{ArcSin}[c+dx]^2) - \frac{12 a b \left( 2 \sqrt{c+dx} \left( -1 + (c+dx)^2 \right) - 2 (c+dx) \sqrt{1 - \frac{1}{(c+dx)^2}} \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{1}{\sqrt{c+dx}}\right], -1] \right)}{\sqrt{c+dx} \sqrt{1 - (c+dx)^2}} - 24 b^2 \sqrt{1 - (c+dx)^2} \right. \\ \left. \operatorname{ArcSin}[c+dx] \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{5}{4}, (c+dx)^2\right] + \frac{3 \sqrt{2} b^2 \pi (c+dx) \operatorname{HypergeometricPFQ}\left[\left\{\frac{3}{4}, \frac{3}{4}, 1\right\}, \left\{\frac{5}{4}, \frac{7}{4}\right\}, (c+dx)^2\right]}{\Gamma\left[\frac{5}{4}\right] \Gamma\left[\frac{7}{4}\right]} \right)$$

**Problem 299: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \operatorname{ArcSin}[c+dx])^2}{(c e + d e x)^{9/2}} dx$$

Optimal (type 5, 130 leaves, 3 steps):

$$\begin{aligned} & -\frac{2 (a + b \operatorname{ArcSin}[c+dx])^2}{7 d e (e(c+dx))^{7/2}} - \frac{8 b (a + b \operatorname{ArcSin}[c+dx]) \operatorname{Hypergeometric2F1}\left[-\frac{5}{4}, \frac{1}{2}, -\frac{1}{4}, (c+dx)^2\right]}{35 d e^2 (e(c+dx))^{5/2}} - \\ & \frac{16 b^2 \operatorname{HypergeometricPFQ}\left[\left\{-\frac{3}{4}, -\frac{3}{4}, 1\right\}, \left\{-\frac{1}{4}, \frac{1}{4}\right\}, (c+dx)^2\right]}{105 d e^3 (e(c+dx))^{3/2}} \end{aligned}$$

Result (type 5, 299 leaves):

$$\begin{aligned}
& \frac{1}{420 d (e (c + d x))^{9/2}} \left( -120 a^2 (c + d x) + 48 a b \left( -5 (c + d x) \operatorname{ArcSin}[c + d x] + \right. \right. \\
& \quad \left. \left. 2 (c + d x)^{9/2} \left( -\frac{\sqrt{1 - (c + d x)^2} (1 + 3 (c + d x)^2)}{(c + d x)^{5/2}} - 3 \operatorname{EllipticE}[\operatorname{ArcSin}[\sqrt{c + d x}], -1] + 3 \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{c + d x}], -1] \right) \right) + \right. \\
& \quad \left. b^2 (c + d x) \left( \frac{9 \sqrt{2} \pi (c + d x)^6 \operatorname{HypergeometricPFQ}[\{1, \frac{5}{4}, \frac{5}{4}\}, \{\frac{7}{4}, \frac{9}{4}\}, (c + d x)^2]}{\operatorname{Gamma}[\frac{7}{4}] \operatorname{Gamma}[\frac{9}{4}]} - \right. \right. \\
& \quad \left. \left. 4 \left( -46 + 30 \operatorname{ArcSin}[c + d x]^2 + 64 \cos[2 \operatorname{ArcSin}[c + d x]] - 18 \cos[4 \operatorname{ArcSin}[c + d x]] + 24 (c + d x)^5 \sqrt{1 - (c + d x)^2} \operatorname{ArcSin}[c + d x] \right. \right. \right. \\
& \quad \left. \left. \left. \operatorname{Hypergeometric2F1}[1, \frac{5}{4}, \frac{7}{4}, (c + d x)^2] + 30 \operatorname{ArcSin}[c + d x] \sin[2 \operatorname{ArcSin}[c + d x]] - 9 \operatorname{ArcSin}[c + d x] \sin[4 \operatorname{ArcSin}[c + d x]] \right) \right) \right)
\end{aligned}$$

**Problem 300: Attempted integration timed out after 120 seconds.**

$$\int \sqrt{c e + d e x} (a + b \operatorname{ArcSin}[c + d x])^3 dx$$

Optimal (type 9, 81 leaves, 2 steps):

$$\frac{2 (e (c + d x))^{3/2} (a + b \operatorname{ArcSin}[c + d x])^3}{3 d e} - \frac{2 b \operatorname{Unintegrable}[\frac{(e (c + d x))^{3/2} (a + b \operatorname{ArcSin}[c + d x])^2}{\sqrt{1 - (c + d x)^2}}, x]}{e}$$

Result (type 1, 1 leaves):

???

**Problem 304: Attempted integration timed out after 120 seconds.**

$$\int \sqrt{c e + d e x} (a + b \operatorname{ArcSin}[c + d x])^4 dx$$

Optimal (type 9, 83 leaves, 2 steps):

$$\frac{2 (e (c + d x))^{3/2} (a + b \operatorname{ArcSin}[c + d x])^4}{3 d e} - \frac{8 b \operatorname{Unintegrable}[\frac{(e (c + d x))^{3/2} (a + b \operatorname{ArcSin}[c + d x])^3}{\sqrt{1 - (c + d x)^2}}, x]}{3 e}$$

Result (type 1, 1 leaves):

???

### Problem 310: Unable to integrate problem.

$$\int (c e + d e x)^m (a + b \operatorname{ArcSin}[c + d x])^2 dx$$

Optimal (type 5, 183 leaves, 3 steps):

$$\frac{(e(c + d x))^{1+m} (a + b \operatorname{ArcSin}[c + d x])^2}{d e (1 + m)} - \frac{2 b (e(c + d x))^{2+m} (a + b \operatorname{ArcSin}[c + d x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2+m}{2}, \frac{4+m}{2}, (c + d x)^2\right]}{d e^2 (1 + m) (2 + m)} + \frac{2 b^2 (e(c + d x))^{3+m} \operatorname{HypergeometricPFQ}\left[\left\{1, \frac{3}{2} + \frac{m}{2}, \frac{3}{2} + \frac{m}{2}\right\}, \left\{2 + \frac{m}{2}, \frac{5}{2} + \frac{m}{2}\right\}, (c + d x)^2\right]}{d e^3 (1 + m) (2 + m) (3 + m)}$$

Result (type 8, 25 leaves):

$$\int (c e + d e x)^m (a + b \operatorname{ArcSin}[c + d x])^2 dx$$

### Problem 352: Result unnecessarily involves imaginary or complex numbers.

$$\int x^6 (a + b \operatorname{ArcSin}[c x^2]) dx$$

Optimal (type 4, 86 leaves, 5 steps):

$$\frac{10 b x \sqrt{1 - c^2 x^4}}{147 c^3} + \frac{2 b x^5 \sqrt{1 - c^2 x^4}}{49 c} + \frac{1}{7} x^7 (a + b \operatorname{ArcSin}[c x^2]) - \frac{10 b \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{c} x], -1]}{147 c^{7/2}}$$

Result (type 4, 82 leaves):

$$\frac{1}{147} \left( 21 a x^7 + \frac{2 b x \sqrt{1 - c^2 x^4} (5 + 3 c^2 x^4)}{c^3} + 21 b x^7 \operatorname{ArcSin}[c x^2] - \frac{10 i b \operatorname{EllipticF}[i \operatorname{ArcSinh}[\sqrt{-c} x], -1]}{(-c)^{7/2}} \right)$$

### Problem 353: Result unnecessarily involves imaginary or complex numbers.

$$\int x^4 (a + b \operatorname{ArcSin}[c x^2]) dx$$

Optimal (type 4, 83 leaves, 7 steps):

$$\frac{2 b x^3 \sqrt{1 - c^2 x^4}}{25 c} + \frac{1}{5} x^5 (a + b \operatorname{ArcSin}[c x^2]) - \frac{6 b \operatorname{EllipticE}[\operatorname{ArcSin}[\sqrt{c} x], -1]}{25 c^{5/2}} + \frac{6 b \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{c} x], -1]}{25 c^{5/2}}$$

Result (type 4, 93 leaves) :

$$\frac{1}{25} \left( 5 a x^5 + \frac{2 b x^3 \sqrt{1 - c^2 x^4}}{c} + 5 b x^5 \operatorname{ArcSin}[c x^2] + \frac{6 i b \left( \operatorname{EllipticE}[i \operatorname{ArcSinh}[\sqrt{-c} x], -1] - \operatorname{EllipticF}[i \operatorname{ArcSinh}[\sqrt{-c} x], -1] \right)}{(-c)^{5/2}} \right)$$

Problem 354: Result unnecessarily involves imaginary or complex numbers.

$$\int x^2 (a + b \operatorname{ArcSin}[c x^2]) dx$$

Optimal (type 4, 61 leaves, 4 steps) :

$$\frac{2 b x \sqrt{1 - c^2 x^4}}{9 c} + \frac{1}{3} x^3 (a + b \operatorname{ArcSin}[c x^2]) - \frac{2 b \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{c} x], -1]}{9 c^{3/2}}$$

Result (type 4, 72 leaves) :

$$\frac{1}{9} \left( 3 a x^3 + \frac{2 b x \sqrt{1 - c^2 x^4}}{c} + 3 b x^3 \operatorname{ArcSin}[c x^2] - \frac{2 i b \operatorname{EllipticF}[i \operatorname{ArcSinh}[\sqrt{-c} x], -1]}{(-c)^{3/2}} \right)$$

Problem 355: Result unnecessarily involves imaginary or complex numbers.

$$\int (a + b \operatorname{ArcSin}[c x^2]) dx$$

Optimal (type 4, 49 leaves, 7 steps) :

$$a x + b x \operatorname{ArcSin}[c x^2] - \frac{2 b \operatorname{EllipticE}[\operatorname{ArcSin}[\sqrt{c} x], -1]}{\sqrt{c}} + \frac{2 b \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{c} x], -1]}{\sqrt{c}}$$

Result (type 4, 61 leaves) :

$$a x + b x \operatorname{ArcSin}[c x^2] - \frac{2 i b c \left( \operatorname{EllipticE}[i \operatorname{ArcSinh}[\sqrt{-c} x], -1] - \operatorname{EllipticF}[i \operatorname{ArcSinh}[\sqrt{-c} x], -1] \right)}{(-c)^{3/2}}$$

Problem 356: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{ArcSin}[c x^2]}{x^2} dx$$

Optimal (type 4, 34 leaves, 3 steps) :

$$-\frac{a + b \operatorname{ArcSin}[c x^2]}{x} + 2 b \sqrt{-c} \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{-c} x], -1]$$

Result (type 4, 44 leaves) :

$$-\frac{a + b \operatorname{ArcSin}[c x^2] - 2 i b \sqrt{-c} x \operatorname{EllipticF}[i \operatorname{ArcSinh}[\sqrt{-c} x], -1]}{x}$$

**Problem 357:** Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{ArcSin}[c x^2]}{x^4} dx$$

Optimal (type 4, 81 leaves, 7 steps) :

$$-\frac{2 b c \sqrt{1 - c^2 x^4}}{3 x} - \frac{a + b \operatorname{ArcSin}[c x^2]}{3 x^3} - \frac{2}{3} b c^{3/2} \operatorname{EllipticE}[\operatorname{ArcSin}[\sqrt{c} x], -1] + \frac{2}{3} b c^{3/2} \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{c} x], -1]$$

Result (type 4, 91 leaves) :

$$\frac{1}{3} \left( -\frac{a}{x^3} - \frac{2 b c \sqrt{1 - c^2 x^4}}{x} - \frac{b \operatorname{ArcSin}[c x^2]}{x^3} + 2 i b (-c)^{3/2} \left( \operatorname{EllipticE}[i \operatorname{ArcSinh}[\sqrt{-c} x], -1] - \operatorname{EllipticF}[i \operatorname{ArcSinh}[\sqrt{-c} x], -1] \right) \right)$$

**Problem 358:** Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{ArcSin}[c x^2]}{x^6} dx$$

Optimal (type 4, 61 leaves, 4 steps) :

$$-\frac{2 b c \sqrt{1 - c^2 x^4}}{15 x^3} - \frac{a + b \operatorname{ArcSin}[c x^2]}{5 x^5} + \frac{2}{15} b c^{5/2} \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{c} x], -1]$$

Result (type 4, 72 leaves) :

$$-\frac{3 a + 2 b c x^2 \sqrt{1 - c^2 x^4} + 3 b \operatorname{ArcSin}[c x^2] - 2 i b (-c)^{5/2} x^5 \operatorname{EllipticF}[i \operatorname{ArcSinh}[\sqrt{-c} x], -1]}{15 x^5}$$

**Problem 359:** Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{ArcSin}[c x^2]}{x^8} dx$$

Optimal (type 4, 106 leaves, 8 steps) :

$$-\frac{2 b c \sqrt{1-c^2 x^4}}{35 x^5} - \frac{6 b c^3 \sqrt{1-c^2 x^4}}{35 x} - \frac{a+b \operatorname{ArcSin}[c x^2]}{7 x^7} - \frac{6}{35} b c^{7/2} \operatorname{EllipticE}[\operatorname{ArcSin}[\sqrt{c} x], -1] + \frac{6}{35} b c^{7/2} \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{c} x], -1]$$

Result (type 4, 100 leaves):

$$\frac{1}{35} \left( -\frac{5 a}{x^7} - \frac{2 b \sqrt{1-c^2 x^4} (c+3 c^3 x^4)}{x^5} - \frac{5 b \operatorname{ArcSin}[c x^2]}{x^7} + 6 i b (-c)^{7/2} \left( \operatorname{EllipticE}[i \operatorname{ArcSinh}[\sqrt{-c} x], -1] - \operatorname{EllipticF}[i \operatorname{ArcSinh}[\sqrt{-c} x], -1] \right) \right)$$

Problem 373: Result more than twice size of optimal antiderivative.

$$\int \left( a + b \operatorname{ArcSin}\left[\frac{c}{x}\right] \right) dx$$

Optimal (type 3, 31 leaves, 6 steps):

$$a x + b x \operatorname{ArcCsc}\left[\frac{x}{c}\right] + b c \operatorname{ArcTanh}\left[\sqrt{1-\frac{c^2}{x^2}}\right]$$

Result (type 3, 89 leaves):

$$a x + b x \operatorname{ArcSin}\left[\frac{c}{x}\right] + \frac{b c \sqrt{-c^2+x^2} \left(-\operatorname{Log}\left[1-\frac{x}{\sqrt{-c^2+x^2}}\right] + \operatorname{Log}\left[1+\frac{x}{\sqrt{-c^2+x^2}}\right]\right)}{2 \sqrt{1-\frac{c^2}{x^2}} x}$$

Problem 383: Result more than twice size of optimal antiderivative.

$$\int \frac{a+b \operatorname{ArcSin}[c x^n]}{x} dx$$

Optimal (type 4, 75 leaves, 7 steps):

$$-\frac{i b \operatorname{ArcSin}[c x^n]^2}{2 n} + \frac{b \operatorname{ArcSin}[c x^n] \operatorname{Log}\left[1-e^{2 i \operatorname{ArcSin}[c x^n]}\right]}{n} + a \operatorname{Log}[x] - \frac{i b \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}[c x^n]}]}{2 n}$$

Result (type 4, 157 leaves):

$$\begin{aligned} & a \operatorname{Log}[x] + b \operatorname{ArcSin}[c x^n] \operatorname{Log}[x] - \frac{1}{\sqrt{-c^2}} b c \left( \operatorname{Log}[x] \operatorname{Log}\left[\sqrt{-c^2} x^n + \sqrt{1 - c^2 x^{2n}}\right] + \frac{1}{n} \right. \\ & \quad \left. \pm \left( \frac{1}{2} \operatorname{ArcSinh}\left[\sqrt{-c^2} x^n\right] \operatorname{Log}\left[1 - e^{-2 \operatorname{ArcSinh}\left[\sqrt{-c^2} x^n\right]}\right] - \frac{1}{2} \operatorname{Im}\left(-\operatorname{ArcSinh}\left[\sqrt{-c^2} x^n\right]^2 + \operatorname{PolyLog}[2, e^{-2 \operatorname{ArcSinh}\left[\sqrt{-c^2} x^n\right]}]\right)\right) \right) \end{aligned}$$

Problem 389: Unable to integrate problem.

$$\int \frac{a + b \operatorname{ArcSin}[c + d x^2]}{x} dx$$

Optimal (type 4, 214 leaves, 12 steps):

$$\begin{aligned} & -\frac{1}{4} \operatorname{Im} b \operatorname{ArcSin}[c + d x^2]^2 + \frac{1}{2} b \operatorname{ArcSin}[c + d x^2] \operatorname{Log}\left[1 - \frac{e^{i \operatorname{ArcSin}[c+d x^2]}}{\operatorname{Im} c - \sqrt{1 - c^2}}\right] + \\ & \frac{1}{2} b \operatorname{ArcSin}[c + d x^2] \operatorname{Log}\left[1 - \frac{e^{i \operatorname{ArcSin}[c+d x^2]}}{\operatorname{Im} c + \sqrt{1 - c^2}}\right] + a \operatorname{Log}[x] - \frac{1}{2} \operatorname{Im} b \operatorname{PolyLog}[2, \frac{e^{i \operatorname{ArcSin}[c+d x^2]}}{\operatorname{Im} c - \sqrt{1 - c^2}}] - \frac{1}{2} \operatorname{Im} b \operatorname{PolyLog}[2, \frac{e^{i \operatorname{ArcSin}[c+d x^2]}}{\operatorname{Im} c + \sqrt{1 - c^2}}] \end{aligned}$$

Result (type 8, 18 leaves):

$$\int \frac{a + b \operatorname{ArcSin}[c + d x^2]}{x} dx$$

Problem 393: Result unnecessarily involves imaginary or complex numbers.

$$\int x^4 (a + b \operatorname{ArcSin}[c + d x^2]) dx$$

Optimal (type 4, 336 leaves, 8 steps):

$$\begin{aligned} & -\frac{16 b c x \sqrt{1 - c^2 - 2 c d x^2 - d^2 x^4}}{75 d^2} + \frac{2 b x^3 \sqrt{1 - c^2 - 2 c d x^2 - d^2 x^4}}{25 d} + \frac{1}{5} x^5 (a + b \operatorname{ArcSin}[c + d x^2]) - \\ & \frac{2 b \sqrt{1 - c} (1 + c) (9 + 23 c^2) \sqrt{1 - \frac{d x^2}{1 - c}} \sqrt{1 + \frac{d x^2}{1 + c}} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} x}{\sqrt{1 - c}}\right], -\frac{1 - c}{1 + c}\right]}{75 d^{5/2} \sqrt{1 - c^2 - 2 c d x^2 - d^2 x^4}} + \\ & \frac{2 b \sqrt{1 - c} (1 + c) (9 + 8 c + 15 c^2) \sqrt{1 - \frac{d x^2}{1 - c}} \sqrt{1 + \frac{d x^2}{1 + c}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} x}{\sqrt{1 - c}}\right], -\frac{1 - c}{1 + c}\right]}{75 d^{5/2} \sqrt{1 - c^2 - 2 c d x^2 - d^2 x^4}} \end{aligned}$$

Result (type 4, 349 leaves):

$$\begin{aligned}
& \frac{1}{75 d^2 \sqrt{\frac{d}{1+c}} \sqrt{1-c^2-2 c d x^2-d^2 x^4}} \left( \sqrt{\frac{d}{1+c}} x \right. \\
& \left( 15 a d^2 x^4 \sqrt{1-c^2-2 c d x^2-d^2 x^4} + 2 b (-8 c + 8 c^3 + 3 d x^2 + 13 c^2 d x^2 + 2 c d^2 x^4 - 3 d^3 x^6) + 15 b d^2 x^4 \sqrt{1-c^2-2 c d x^2-d^2 x^4} \operatorname{ArcSin}[c+d x^2] \right) + \\
& 2 \pm b (-9 + 9 c - 23 c^2 + 23 c^3) \sqrt{\frac{-1+c+d x^2}{-1+c}} \sqrt{\frac{1+c+d x^2}{1+c}} \operatorname{EllipticE}[\pm \operatorname{ArcSinh}\left[\sqrt{\frac{d}{1+c}} x\right], \frac{1+c}{-1+c}] - \\
& \left. 2 \pm b (-9 + 17 c - 23 c^2 + 15 c^3) \sqrt{\frac{-1+c+d x^2}{-1+c}} \sqrt{\frac{1+c+d x^2}{1+c}} \operatorname{EllipticF}[\pm \operatorname{ArcSinh}\left[\sqrt{\frac{d}{1+c}} x\right], \frac{1+c}{-1+c}] \right)
\end{aligned}$$

**Problem 394: Result unnecessarily involves imaginary or complex numbers.**

$$\int x^2 (a + b \operatorname{ArcSin}[c + d x^2]) dx$$

Optimal (type 4, 287 leaves, 7 steps):

$$\begin{aligned}
& \frac{2 b x \sqrt{1-c^2-2 c d x^2-d^2 x^4}}{9 d} + \frac{1}{3} x^3 (a + b \operatorname{ArcSin}[c + d x^2]) + \frac{8 b \sqrt{1-c} c (1+c) \sqrt{1-\frac{d x^2}{1-c}} \sqrt{1+\frac{d x^2}{1+c}} \operatorname{EllipticE}[\operatorname{ArcSin}\left[\frac{\sqrt{d} x}{\sqrt{1-c}}\right], -\frac{1-c}{1+c}]}{9 d^{3/2} \sqrt{1-c^2-2 c d x^2-d^2 x^4}} - \\
& \frac{2 b \sqrt{1-c} (1+c) (1+3 c) \sqrt{1-\frac{d x^2}{1-c}} \sqrt{1+\frac{d x^2}{1+c}} \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\sqrt{d} x}{\sqrt{1-c}}\right], -\frac{1-c}{1+c}]}{9 d^{3/2} \sqrt{1-c^2-2 c d x^2-d^2 x^4}}
\end{aligned}$$

Result (type 4, 307 leaves):

$$\begin{aligned}
& \left( \sqrt{\frac{d}{1+c}} x \left( 3 a d x^2 \sqrt{1-c^2-2 c d x^2-d^2 x^4} - 2 b (-1+c^2+2 c d x^2+d^2 x^4) + 3 b d x^2 \sqrt{1-c^2-2 c d x^2-d^2 x^4} \operatorname{ArcSin}[c+d x^2] \right) - \right. \\
& \left. 8 \pm b (-1+c) c \sqrt{\frac{-1+c+d x^2}{-1+c}} \sqrt{\frac{1+c+d x^2}{1+c}} \operatorname{EllipticE}[\pm \operatorname{ArcSinh}\left[\sqrt{\frac{d}{1+c}} x\right], \frac{1+c}{-1+c}] + \right. \\
& \left. 2 \pm b (1-4 c+3 c^2) \sqrt{\frac{-1+c+d x^2}{-1+c}} \sqrt{\frac{1+c+d x^2}{1+c}} \operatorname{EllipticF}[\pm \operatorname{ArcSinh}\left[\sqrt{\frac{d}{1+c}} x\right], \frac{1+c}{-1+c}] \right) / \left( 9 d \sqrt{\frac{d}{1+c}} \sqrt{1-c^2-2 c d x^2-d^2 x^4} \right)
\end{aligned}$$

**Problem 395: Result unnecessarily involves imaginary or complex numbers.**

$$\int (a + b \operatorname{ArcSin}[c + d x^2]) dx$$

Optimal (type 4, 237 leaves, 7 steps):

$$\begin{aligned} a x + b x \operatorname{ArcSin}[c + d x^2] - & \frac{2 b \sqrt{1-c} (1+c) \sqrt{1-\frac{d x^2}{1-c}} \sqrt{1+\frac{d x^2}{1+c}} \operatorname{EllipticE}[\operatorname{ArcSin}\left[\frac{\sqrt{d} x}{\sqrt{1-c}}\right], -\frac{1-c}{1+c}]}{\sqrt{d} \sqrt{1-c^2-2 c d x^2-d^2 x^4}} + \\ & \frac{2 b \sqrt{1-c} (1+c) \sqrt{1-\frac{d x^2}{1-c}} \sqrt{1+\frac{d x^2}{1+c}} \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\sqrt{d} x}{\sqrt{1-c}}\right], -\frac{1-c}{1+c}]}{\sqrt{d} \sqrt{1-c^2-2 c d x^2-d^2 x^4}} \end{aligned}$$

Result (type 4, 155 leaves):

$$\begin{aligned} a x + b x \operatorname{ArcSin}[c + d x^2] + & \\ & \left( 2 \pm b (-1+c) \sqrt{\frac{-1+c+d x^2}{-1+c}} \sqrt{\frac{1+c+d x^2}{1+c}} \left( \operatorname{EllipticE}\left[\pm \operatorname{ArcSinh}\left[\sqrt{\frac{d}{1+c}} x\right], \frac{1+c}{-1+c}\right] - \operatorname{EllipticF}\left[\pm \operatorname{ArcSinh}\left[\sqrt{\frac{d}{1+c}} x\right], \frac{1+c}{-1+c}\right] \right) \right) / \\ & \left( \sqrt{\frac{d}{1+c}} \sqrt{1-c^2-2 c d x^2-d^2 x^4} \right) \end{aligned}$$

**Problem 396: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{a + b \operatorname{ArcSin}[c + d x^2]}{x^2} dx$$

Optimal (type 4, 126 leaves, 4 steps):

$$- \frac{a + b \operatorname{ArcSin}[c + d x^2]}{x} + \frac{2 b \sqrt{1-c} \sqrt{d} \sqrt{1-\frac{d x^2}{1-c}} \sqrt{1+\frac{d x^2}{1+c}} \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\sqrt{d} x}{\sqrt{1-c}}\right], -\frac{1-c}{1+c}]}{\sqrt{1-c^2-2 c d x^2-d^2 x^4}}$$

Result (type 4, 140 leaves):

$$-\frac{a}{x} - \frac{b \operatorname{ArcSin}[c + d x^2]}{x} - \frac{2 i b d \sqrt{1 - \frac{d x^2}{-1-c}} \sqrt{1 - \frac{d x^2}{1-c}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{d}{-1-c}} x\right], \frac{-1-c}{1-c}\right]}{\sqrt{-\frac{d}{-1-c}} \sqrt{1 - c^2 - 2 c d x^2 - d^2 x^4}}$$

Problem 397: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{ArcSin}[c + d x^2]}{x^4} dx$$

Optimal (type 4, 284 leaves, 8 steps):

$$\begin{aligned} & -\frac{2 b d \sqrt{1 - c^2 - 2 c d x^2 - d^2 x^4}}{3 (1 - c^2) x} - \frac{a + b \operatorname{ArcSin}[c + d x^2]}{3 x^3} \\ & + \frac{2 b d^{3/2} \sqrt{1 - \frac{d x^2}{1-c}} \sqrt{1 + \frac{d x^2}{1+c}} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} x}{\sqrt{1-c}}\right], -\frac{1-c}{1+c}\right]}{3 \sqrt{1-c} \sqrt{1 - c^2 - 2 c d x^2 - d^2 x^4}} + \frac{2 b d^{3/2} \sqrt{1 - \frac{d x^2}{1-c}} \sqrt{1 + \frac{d x^2}{1+c}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d} x}{\sqrt{1-c}}\right], -\frac{1-c}{1+c}\right]}{3 \sqrt{1-c} \sqrt{1 - c^2 - 2 c d x^2 - d^2 x^4}} \end{aligned}$$

Result (type 4, 243 leaves):

$$\begin{aligned} & -\frac{a}{3 x^3} + \frac{2 b d \sqrt{1 - c^2 - 2 c d x^2 - d^2 x^4}}{3 (-1 + c^2) x} - \frac{b \operatorname{ArcSin}[c + d x^2]}{3 x^3} + \\ & \left( 2 i b (1 - c) d^2 \sqrt{1 - \frac{d x^2}{-1-c}} \sqrt{1 - \frac{d x^2}{1-c}} \left( \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{d}{-1-c}} x\right], \frac{-1-c}{1-c}\right] - \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{d}{-1-c}} x\right], \frac{-1-c}{1-c}\right] \right) \right) / \\ & \left( 3 (-1 + c) (1 + c) \sqrt{-\frac{d}{-1-c}} \sqrt{1 - c^2 - 2 c d x^2 - d^2 x^4} \right) \end{aligned}$$

Problem 398: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{ArcSin}[c + d x^2]}{x^6} dx$$

Optimal (type 4, 355 leaves, 8 steps):

$$\begin{aligned}
& - \frac{2 b d \sqrt{1 - c^2 - 2 c d x^2 - d^2 x^4}}{15 (1 - c^2) x^3} - \frac{8 b c d^2 \sqrt{1 - c^2 - 2 c d x^2 - d^2 x^4}}{15 (1 - c^2)^2 x} - \frac{a + b \operatorname{ArcSin}[c + d x^2]}{5 x^5} \\
& + \frac{8 b c d^{5/2} \sqrt{1 - \frac{d x^2}{1-c}} \sqrt{1 + \frac{d x^2}{1+c}} \operatorname{EllipticE}[\operatorname{ArcSin}\left[\frac{\sqrt{d} x}{\sqrt{1-c}}\right], -\frac{1-c}{1+c}] + 2 b (1+3 c) d^{5/2} \sqrt{1 - \frac{d x^2}{1-c}} \sqrt{1 + \frac{d x^2}{1+c}} \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\sqrt{d} x}{\sqrt{1-c}}\right], -\frac{1-c}{1+c}]}{15 \sqrt{1-c} (1-c^2) \sqrt{1 - c^2 - 2 c d x^2 - d^2 x^4}}
\end{aligned}$$

Result (type 4, 370 leaves):

$$\begin{aligned}
& \frac{1}{15 (-1 + c^2)^2 \sqrt{\frac{d}{1+c}} x^5 \sqrt{1 - c^2 - 2 c d x^2 - d^2 x^4}} \\
& \left( \sqrt{\frac{d}{1+c}} \left( -3 a (-1 + c^2)^2 \sqrt{1 - c^2 - 2 c d x^2 - d^2 x^4} + 2 b d x^2 (-1 - c^4 + 2 c^3 d x^2 + d^2 x^4 + c^2 (2 + 7 d^2 x^4)) + c (-2 d x^2 + 4 d^3 x^6) \right) - \right. \\
& \left. 3 b (-1 + c^2)^2 \sqrt{1 - c^2 - 2 c d x^2 - d^2 x^4} \operatorname{ArcSin}[c + d x^2] \right) + \\
& 8 i b (-1 + c) c d^3 x^5 \sqrt{\frac{-1 + c + d x^2}{-1 + c}} \sqrt{\frac{1 + c + d x^2}{1 + c}} \operatorname{EllipticE}[i \operatorname{ArcSinh}\left[\sqrt{\frac{d}{1+c}} x\right], \frac{1+c}{-1+c}] - \\
& 2 i b (1 - 4 c + 3 c^2) d^3 x^5 \sqrt{\frac{-1 + c + d x^2}{-1 + c}} \sqrt{\frac{1 + c + d x^2}{1 + c}} \operatorname{EllipticF}[i \operatorname{ArcSinh}\left[\sqrt{\frac{d}{1+c}} x\right], \frac{1+c}{-1+c}]
\end{aligned}$$

### Problem 432: Unable to integrate problem.

$$\int \frac{\left(a + b \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right)^3}{1 - c^2 x^2} dx$$

Optimal (type 4, 275 leaves, 8 steps):

$$\begin{aligned}
& \frac{i \left(a + b \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right)^4}{4 b c} - \frac{\left(a + b \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right)^3 \operatorname{Log}\left[1 - e^{-2 i \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]}\right]}{c} + \frac{3 i b \left(a + b \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right)^2 \operatorname{PolyLog}[2, e^{2 i \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]}]}{2 c} - \\
& \frac{3 b^2 \left(a + b \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right) \operatorname{PolyLog}[3, e^{2 i \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]}]}{2 c} - \frac{3 i b^3 \operatorname{PolyLog}[4, e^{2 i \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]}]}{4 c}
\end{aligned}$$

Result (type 8, 42 leaves) :

$$\int \frac{\left(a + b \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right)^3}{1 - c^2 x^2} dx$$

Problem 433: Unable to integrate problem.

$$\int \frac{\left(a + b \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right)^2}{1 - c^2 x^2} dx$$

Optimal (type 4, 205 leaves, 7 steps) :

$$\begin{aligned} & \frac{i \left(a + b \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right)^3}{3bc} - \frac{\left(a + b \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right)^2 \operatorname{Log}\left[1 - e^{2i \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]}\right]}{c} + \\ & \frac{i b \left(a + b \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right) \operatorname{PolyLog}\left[2, e^{2i \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]}\right]}{c} - \frac{b^2 \operatorname{PolyLog}\left[3, e^{2i \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]}\right]}{2c} \end{aligned}$$

Result (type 8, 42 leaves) :

$$\int \frac{\left(a + b \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right)^2}{1 - c^2 x^2} dx$$

Problem 434: Unable to integrate problem.

$$\int \frac{a + b \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]}{1 - c^2 x^2} dx$$

Optimal (type 4, 141 leaves, 6 steps) :

$$\begin{aligned} & \frac{i \left(a + b \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right)^2}{2bc} - \frac{\left(a + b \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right) \operatorname{Log}\left[1 - e^{2i \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]}\right]}{c} + \frac{i b \operatorname{PolyLog}\left[2, e^{2i \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]}\right]}{2c} \end{aligned}$$

Result (type 8, 40 leaves) :

$$\int \frac{a + b \operatorname{ArcSin}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]}{1 - c^2 x^2} dx$$

Problem 438: Attempted integration timed out after 120 seconds.

$$\int \operatorname{ArcSin}[c e^{ax}] dx$$

Optimal (type 4, 84 leaves, 6 steps):

$$-\frac{\frac{i}{2} \operatorname{ArcSin}[c e^{ax}]^2}{2b} + \frac{\operatorname{ArcSin}[c e^{ax}] \operatorname{Log}[1 - e^{2i} \operatorname{ArcSin}[c e^{ax}]]}{b} - \frac{\frac{i}{2} \operatorname{PolyLog}[2, e^{2i} \operatorname{ArcSin}[c e^{ax}]]}{2b}$$

Result (type 1, 1 leaves):

???

Problem 467: Result more than twice size of optimal antiderivative.

$$\int \frac{e^{\operatorname{ArcSin}[ax]}}{(1 - a^2 x^2)^{3/2}} dx$$

Optimal (type 5, 45 leaves, 4 steps):

$$\left(\frac{4}{5} - \frac{8i}{5}\right) e^{(1+2i) \operatorname{ArcSin}[ax]} \operatorname{Hypergeometric2F1}\left[1 - \frac{i}{2}, 2, 2 - \frac{i}{2}, -e^{2i} \operatorname{ArcSin}[ax]\right]$$

a

Result (type 5, 101 leaves):

$$\begin{aligned} & \frac{1}{a} \left( \frac{2}{5} + \frac{i}{5} \right) e^{\operatorname{ArcSin}[ax]} \\ & \left( \frac{(2-i)a}{\sqrt{1-a^2 x^2}} - (1+2i) \operatorname{Hypergeometric2F1}\left[-\frac{i}{2}, 1, 1 - \frac{i}{2}, -e^{2i} \operatorname{ArcSin}[ax]\right] + e^{2i} \operatorname{ArcSin}[ax] \operatorname{Hypergeometric2F1}\left[1, 1 - \frac{i}{2}, 2 - \frac{i}{2}, -e^{2i} \operatorname{ArcSin}[ax]\right] \right) \end{aligned}$$

Problem 469: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \operatorname{ArcSin}\left[\frac{c}{a + bx}\right] dx$$

Optimal (type 3, 47 leaves, 6 steps):

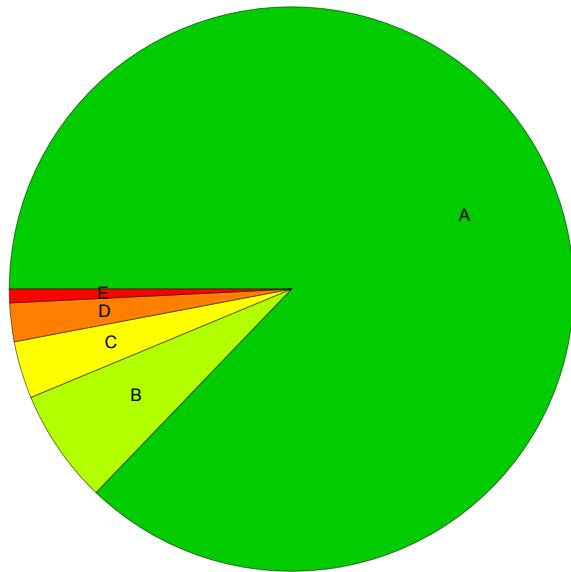
$$\frac{(a + b x) \operatorname{ArcCsc} \left[ \frac{a}{c} + \frac{b x}{c} \right]}{b} + \frac{c \operatorname{ArcTanh} \left[ \sqrt{1 - \frac{c^2}{(a+b x)^2}} \right]}{b}$$

Result (type 3, 166 leaves):

$$x \operatorname{ArcSin} \left[ \frac{c}{a + b x} \right] + \\ \left( (a + b x) \sqrt{\frac{a^2 - c^2 + 2 a b x + b^2 x^2}{(a + b x)^2}} \left( \frac{2 b^2 \left( -\frac{i}{2} c + \sqrt{a^2 - c^2 + 2 a b x + b^2 x^2} \right)}{a (a + b x)} \operatorname{Log} \left[ -\frac{2 b^2 \left( -\frac{i}{2} c + \sqrt{a^2 - c^2 + 2 a b x + b^2 x^2} \right)}{a (a + b x)} \right] + c \operatorname{Log} \left[ a + b x + \sqrt{a^2 - c^2 + 2 a b x + b^2 x^2} \right] \right) \right) / \\ \left( b \sqrt{a^2 - c^2 + 2 a b x + b^2 x^2} \right)$$

## Summary of Integration Test Results

1404 integration problems



A - 1224 optimal antiderivatives

B - 92 more than twice size of optimal antiderivatives

C - 46 unnecessarily complex antiderivatives

D - 31 unable to integrate problems

E - 11 integration timeouts