

# Mathematica 11.3 Integration Test Results

Test results for the 108 problems in "3.2.3 u log(e (f (a+b x)^p (c+d x)^q)^r)^s.m"

Problem 16: Result more than twice size of optimal antiderivative.

$$\int (a + b x)^4 \operatorname{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]^2 dx$$

Optimal (type 4, 920 leaves, 32 steps):

$$\begin{aligned} & -\frac{a (b c - a d)^3 p q r^2 x}{5 d^3} + \frac{2 (b c - a d)^4 p q r^2 x}{25 d^4} + \frac{77 (b c - a d)^4 q^2 r^2 x}{150 d^4} + \\ & \frac{2 (b c - a d)^4 q (p + q) r^2 x}{5 d^4} - \frac{b (b c - a d)^3 p q r^2 x^2}{10 d^3} - \frac{(b c - a d)^3 p q r^2 (a + b x)^2}{25 b d^3} - \\ & \frac{77 (b c - a d)^3 q^2 r^2 (a + b x)^2}{300 b d^3} + \frac{16 (b c - a d)^2 p q r^2 (a + b x)^3}{225 b d^2} + \frac{47 (b c - a d)^2 q^2 r^2 (a + b x)^3}{450 b d^2} - \\ & \frac{9 (b c - a d) p q r^2 (a + b x)^4}{200 b d} - \frac{9 (b c - a d) q^2 r^2 (a + b x)^4}{200 b d} + \frac{2 p^2 r^2 (a + b x)^5}{125 b} + \\ & \frac{4 p q r^2 (a + b x)^5}{125 b} + \frac{2 q^2 r^2 (a + b x)^5}{125 b} - \frac{2 (b c - a d)^5 p q r^2 \operatorname{Log}[c + d x]}{25 b d^5} - \\ & \frac{137 (b c - a d)^5 q^2 r^2 \operatorname{Log}[c + d x]}{150 b d^5} - \frac{2 (b c - a d)^5 p q r^2 \operatorname{Log}\left[-\frac{d (a + b x)}{b c - a d}\right] \operatorname{Log}[c + d x]}{5 b d^5} - \\ & \frac{(b c - a d)^5 q^2 r^2 \operatorname{Log}[c + d x]^2}{5 b d^5} - \frac{2 (b c - a d)^4 q r (a + b x) \operatorname{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{5 b d^4} + \\ & \frac{(b c - a d)^3 q r (a + b x)^2 \operatorname{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{5 b d^3} - \\ & \frac{2 (b c - a d)^2 q r (a + b x)^3 \operatorname{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{15 b d^2} + \\ & \frac{(b c - a d) q r (a + b x)^4 \operatorname{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{10 b d} - \\ & \frac{2 p r (a + b x)^5 \operatorname{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{25 b} - \frac{2 q r (a + b x)^5 \operatorname{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{25 b} + \\ & \frac{2 (b c - a d)^5 q r \operatorname{Log}[c + d x] \operatorname{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]}{5 b d^5} + \\ & \frac{(a + b x)^5 \operatorname{Log}\left[e (f (a + b x)^p (c + d x)^q)^r\right]^2}{5 b} - \frac{2 (b c - a d)^5 p q r^2 \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]}{5 b d^5} \end{aligned}$$

Result (type 4, 2508 leaves):

$$\begin{aligned}
& \frac{2 a^5 p q r^2}{b} + \frac{2 a b^3 c^4 p q r^2}{5 d^4} - \frac{2 a^2 b^2 c^3 p q r^2}{d^3} + \frac{4 a^3 b c^2 p q r^2}{d^2} - \frac{4 a^4 c p q r^2}{d} + \\
& \frac{2}{25} a^4 p^2 r^2 x + \frac{197}{150} a^4 p q r^2 x + \frac{12 b^4 c^4 p q r^2 x}{25 d^4} - \frac{11 a b^3 c^3 p q r^2 x}{5 d^3} + \frac{59 a^2 b^2 c^2 p q r^2 x}{15 d^2} - \\
& \frac{101 a^3 b c p q r^2 x}{30 d} + 2 a^4 q^2 r^2 x + \frac{137 b^4 c^4 q^2 r^2 x}{150 d^4} - \frac{25 a b^3 c^3 q^2 r^2 x}{6 d^3} + \frac{22 a^2 b^2 c^2 q^2 r^2 x}{3 d^2} - \\
& \frac{6 a^3 b c q^2 r^2 x}{d} + \frac{4}{25} a^3 b p^2 r^2 x^2 + \frac{283}{300} a^3 b p q r^2 x^2 - \frac{7 b^4 c^3 p q r^2 x^2}{50 d^3} + \frac{19 a b^3 c^2 p q r^2 x^2}{30 d^2} - \\
& \frac{67 a^2 b^2 c p q r^2 x^2}{60 d} + a^3 b q^2 r^2 x^2 - \frac{77 b^4 c^3 q^2 r^2 x^2}{300 d^3} + \frac{13 a b^3 c^2 q^2 r^2 x^2}{12 d^2} - \frac{5 a^2 b^2 c q^2 r^2 x^2}{3 d} + \\
& \frac{4}{25} a^2 b^2 p^2 r^2 x^3 + \frac{257}{450} a^2 b^2 p q r^2 x^3 + \frac{16 b^4 c^2 p q r^2 x^3}{225 d^2} - \frac{29 a b^3 c p q r^2 x^3}{90 d} + \\
& \frac{4}{9} a^2 b^2 q^2 r^2 x^3 + \frac{47 b^4 c^2 q^2 r^2 x^3}{450 d^2} - \frac{7 a b^3 c q^2 r^2 x^3}{18 d} + \frac{2}{25} a b^3 p^2 r^2 x^4 + \frac{41}{200} a b^3 p q r^2 x^4 - \\
& \frac{9 b^4 c p q r^2 x^4}{200 d} + \frac{1}{8} a b^3 q^2 r^2 x^4 - \frac{9 b^4 c q^2 r^2 x^4}{200 d} + \frac{2}{125} b^4 p^2 r^2 x^5 + \frac{4}{125} b^4 p q r^2 x^5 + \\
& \frac{2}{125} b^4 q^2 r^2 x^5 - \frac{a^5 p^2 r^2 \text{Log}[a+b x]^2}{5 b} + \frac{2 a^5 p q r^2 \text{Log}[c+d x]}{b} - \frac{2 b^4 c^5 p q r^2 \text{Log}[c+d x]}{25 d^5} + \\
& \frac{2 a b^3 c^4 p q r^2 \text{Log}[c+d x]}{5 d^4} - \frac{4 a^2 b^2 c^3 p q r^2 \text{Log}[c+d x]}{5 d^3} + \frac{4 a^3 b c^2 p q r^2 \text{Log}[c+d x]}{5 d^2} - \\
& \frac{2 a^4 c p q r^2 \text{Log}[c+d x]}{5 d} - \frac{137 b^4 c^5 q^2 r^2 \text{Log}[c+d x]}{150 d^5} + \frac{25 a b^3 c^4 q^2 r^2 \text{Log}[c+d x]}{6 d^4} - \\
& \frac{22 a^2 b^2 c^3 q^2 r^2 \text{Log}[c+d x]}{3 d^3} + \frac{6 a^3 b c^2 q^2 r^2 \text{Log}[c+d x]}{d^2} - \frac{2 a^4 c q^2 r^2 \text{Log}[c+d x]}{d} - \\
& \frac{b^4 c^5 q^2 r^2 \text{Log}[c+d x]^2}{5 d^5} + \frac{a b^3 c^4 q^2 r^2 \text{Log}[c+d x]^2}{d^4} - \frac{2 a^2 b^2 c^3 q^2 r^2 \text{Log}[c+d x]^2}{d^3} + \\
& \frac{2 a^3 b c^2 q^2 r^2 \text{Log}[c+d x]^2}{d^2} - \frac{a^4 c q^2 r^2 \text{Log}[c+d x]^2}{d} - \frac{2 a^5 p r \text{Log}[e (f (a+b x)^p (c+d x)^q)^r]}{b} - \\
& \frac{2}{5} a^4 p r x \text{Log}[e (f (a+b x)^p (c+d x)^q)^r] - 2 a^4 q r x \text{Log}[e (f (a+b x)^p (c+d x)^q)^r] - \\
& \frac{2 b^4 c^4 q r x \text{Log}[e (f (a+b x)^p (c+d x)^q)^r]}{5 d^4} + \frac{2 a b^3 c^3 q r x \text{Log}[e (f (a+b x)^p (c+d x)^q)^r]}{d^3} - \\
& \frac{4 a^2 b^2 c^2 q r x \text{Log}[e (f (a+b x)^p (c+d x)^q)^r]}{d^2} + \frac{4 a^3 b c q r x \text{Log}[e (f (a+b x)^p (c+d x)^q)^r]}{d} - \\
& \frac{4}{5} a^3 b p r x^2 \text{Log}[e (f (a+b x)^p (c+d x)^q)^r] - 2 a^3 b q r x^2 \text{Log}[e (f (a+b x)^p (c+d x)^q)^r] + \\
& \frac{b^4 c^3 q r x^2 \text{Log}[e (f (a+b x)^p (c+d x)^q)^r]}{5 d^3} - \frac{a b^3 c^2 q r x^2 \text{Log}[e (f (a+b x)^p (c+d x)^q)^r]}{d^2} + \\
& \frac{2 a^2 b^2 c q r x^2 \text{Log}[e (f (a+b x)^p (c+d x)^q)^r]}{d} - \frac{4}{5} a^2 b^2 p r x^3 \text{Log}[e (f (a+b x)^p (c+d x)^q)^r] - \\
& \frac{4}{3} a^2 b^2 q r x^3 \text{Log}[e (f (a+b x)^p (c+d x)^q)^r] - \frac{2 b^4 c^2 q r x^3 \text{Log}[e (f (a+b x)^p (c+d x)^q)^r]}{15 d^2} +
\end{aligned}$$

$$\begin{aligned}
 & \frac{2 a b^3 c q r x^3 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]}{3 d} - \frac{2}{5} a b^3 p r x^4 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] - \\
 & \frac{1}{2} a b^3 q r x^4 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] + \frac{b^4 c q r x^4 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]}{10 d} - \\
 & \frac{2}{25} b^4 p r x^5 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] - \frac{2}{25} b^4 q r x^5 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] + \\
 & \frac{2 b^4 c^5 q r \operatorname{Log}[c+d x] \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]}{5 d^5} - \\
 & \frac{2 a b^3 c^4 q r \operatorname{Log}[c+d x] \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]}{d^4} + \\
 & \frac{4 a^2 b^2 c^3 q r \operatorname{Log}[c+d x] \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]}{d^3} - \\
 & \frac{4 a^3 b c^2 q r \operatorname{Log}[c+d x] \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]}{d^2} + \\
 & \frac{2 a^4 c q r \operatorname{Log}[c+d x] \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]}{d} + \\
 & a^4 x \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]^2 + 2 a^3 b x^2 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]^2 + \\
 & 2 a^2 b^2 x^3 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]^2 + a b^3 x^4 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]^2 + \\
 & \frac{1}{5} b^4 x^5 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]^2 + \frac{1}{150 b d^5} p r \operatorname{Log}[a+b x] \\
 & \left( a d\left(a^4 d^4(288 p-137 q)-60 b^4 c^4 q+270 a b^3 c^3 d q-470 a^2 b^2 c^2 d^2 q+385 a^3 b c d^3 q\right) r - \right. \\
 & \quad 60 b c\left(b^4 c^4-5 a b^3 c^3 d+10 a^2 b^2 c^2 d^2-10 a^3 b c d^3+5 a^4 d^4\right) q r \operatorname{Log}[c+d x] + \\
 & \quad \left. 60(b c-a d)^5 q r \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+60 a^5 d^5 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]\right) + \\
 & \frac{2(b c-a d)^5 p q r^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]}{5 b d^5}
 \end{aligned}$$

**Problem 17: Result more than twice size of optimal antiderivative.**

$$\int (a+b x)^3 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right]^2 dx$$

Optimal (type 4, 805 leaves, 28 steps):

$$\begin{aligned} & \frac{a (bc - ad)^2 pq r^2 x}{4 d^2} - \frac{(bc - ad)^3 pq r^2 x}{8 d^3} - \frac{13 (bc - ad)^3 q^2 r^2 x}{24 d^3} - \\ & \frac{(bc - ad)^3 q (p+q) r^2 x}{2 d^3} + \frac{b (bc - ad)^2 pq r^2 x^2}{8 d^2} + \frac{(bc - ad)^2 pq r^2 (a+bx)^2}{16 b d^2} + \\ & \frac{13 (bc - ad)^2 q^2 r^2 (a+bx)^2}{48 b d^2} - \frac{7 (bc - ad) pq r^2 (a+bx)^3}{72 b d} - \frac{7 (bc - ad) q^2 r^2 (a+bx)^3}{72 b d} + \\ & \frac{p^2 r^2 (a+bx)^4}{32 b} + \frac{pq r^2 (a+bx)^4}{16 b} + \frac{q^2 r^2 (a+bx)^4}{32 b} + \frac{(bc - ad)^4 pq r^2 \text{Log}[c+dx]}{8 b d^4} + \\ & \frac{25 (bc - ad)^4 q^2 r^2 \text{Log}[c+dx]}{24 b d^4} + \frac{(bc - ad)^4 pq r^2 \text{Log}\left[-\frac{d(a+bx)}{bc-ad}\right] \text{Log}[c+dx]}{2 b d^4} + \\ & \frac{(bc - ad)^4 q^2 r^2 \text{Log}[c+dx]^2}{4 b d^4} + \frac{(bc - ad)^3 qr (a+bx) \text{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]}{2 b d^3} - \\ & \frac{(bc - ad)^2 qr (a+bx)^2 \text{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]}{4 b d^2} + \\ & \frac{(bc - ad) qr (a+bx)^3 \text{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]}{6 b d} - \\ & \frac{pr (a+bx)^4 \text{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]}{8 b} - \frac{qr (a+bx)^4 \text{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]}{8 b} - \\ & \frac{(bc - ad)^4 qr \text{Log}[c+dx] \text{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]}{2 b d^4} + \\ & \frac{(a+bx)^4 \text{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]^2}{4 b} + \frac{(bc - ad)^4 pq r^2 \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{2 b d^4} \end{aligned}$$

Result (type 4, 1853 leaves):

$$\begin{aligned} & \frac{2 a^4 p q r^2}{b} - \frac{a b^2 c^3 p q r^2}{2 d^3} + \frac{2 a^2 b c^2 p q r^2}{d^2} - \frac{3 a^3 c p q r^2}{d} + \frac{1}{8} a^3 p^2 r^2 x + \frac{37}{24} a^3 p q r^2 x - \\ & \frac{5 b^3 c^3 p q r^2 x}{8 d^3} + \frac{9 a b^2 c^2 p q r^2 x}{4 d^2} - \frac{35 a^2 b c p q r^2 x}{12 d} + 2 a^3 q^2 r^2 x - \frac{25 b^3 c^3 q^2 r^2 x}{24 d^3} + \\ & \frac{11 a b^2 c^2 q^2 r^2 x}{3 d^2} - \frac{9 a^2 b c q^2 r^2 x}{2 d} + \frac{3}{16} a^2 b p^2 r^2 x^2 + \frac{41}{48} a^2 b p q r^2 x^2 + \frac{3 b^3 c^2 p q r^2 x^2}{16 d^2} - \\ & \frac{2 a b^2 c p q r^2 x^2}{3 d} + \frac{3}{4} a^2 b q^2 r^2 x^2 + \frac{13 b^3 c^2 q^2 r^2 x^2}{48 d^2} - \frac{5 a b^2 c q^2 r^2 x^2}{6 d} + \frac{1}{8} a b^2 p^2 r^2 x^3 + \\ & \frac{25}{72} a b^2 p q r^2 x^3 - \frac{7 b^3 c p q r^2 x^3}{72 d} + \frac{2}{9} a b^2 q^2 r^2 x^3 - \frac{7 b^3 c q^2 r^2 x^3}{72 d} + \frac{1}{32} b^3 p^2 r^2 x^4 + \\ & \frac{1}{16} b^3 p q r^2 x^4 + \frac{1}{32} b^3 q^2 r^2 x^4 - \frac{a^4 p^2 r^2 \text{Log}[a+bx]^2}{4 b} + \frac{2 a^4 p q r^2 \text{Log}[c+dx]}{b} + \\ & \frac{b^3 c^4 p q r^2 \text{Log}[c+dx]}{8 d^4} - \frac{a b^2 c^3 p q r^2 \text{Log}[c+dx]}{2 d^3} + \frac{3 a^2 b c^2 p q r^2 \text{Log}[c+dx]}{4 d^2} - \\ & \frac{a^3 c p q r^2 \text{Log}[c+dx]}{2 d} + \frac{25 b^3 c^4 q^2 r^2 \text{Log}[c+dx]}{24 d^4} - \frac{11 a b^2 c^3 q^2 r^2 \text{Log}[c+dx]}{3 d^3} + \\ & \frac{9 a^2 b c^2 q^2 r^2 \text{Log}[c+dx]}{2 d^2} - \frac{2 a^3 c q^2 r^2 \text{Log}[c+dx]}{d} + \frac{b^3 c^4 q^2 r^2 \text{Log}[c+dx]^2}{4 d^4} - \end{aligned}$$

$$\begin{aligned}
 & \frac{a b^2 c^3 q^2 r^2 \operatorname{Log}[c+dx]^2}{d^3} + \frac{3 a^2 b c^2 q^2 r^2 \operatorname{Log}[c+dx]^2}{2 d^2} - \frac{a^3 c q^2 r^2 \operatorname{Log}[c+dx]^2}{d} - \\
 & \frac{2 a^4 p r \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]}{b} - \frac{1}{2} a^3 p r x \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right] - \\
 & 2 a^3 q r x \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right] + \frac{b^3 c^3 q r x \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]}{2 d^3} - \\
 & \frac{2 a b^2 c^2 q r x \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]}{d^2} + \frac{3 a^2 b c q r x \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]}{d} - \\
 & \frac{3}{4} a^2 b p r x^2 \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right] - \frac{3}{2} a^2 b q r x^2 \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right] - \\
 & \frac{b^3 c^2 q r x^2 \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]}{4 d^2} + \frac{a b^2 c q r x^2 \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]}{d} - \\
 & \frac{1}{2} a b^2 p r x^3 \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right] - \frac{2}{3} a b^2 q r x^3 \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right] + \\
 & \frac{b^3 c q r x^3 \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]}{6 d} - \frac{1}{8} b^3 p r x^4 \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right] - \\
 & \frac{1}{8} b^3 q r x^4 \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right] - \frac{b^3 c^4 q r \operatorname{Log}[c+dx] \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]}{2 d^4} + \\
 & \frac{2 a b^2 c^3 q r \operatorname{Log}[c+dx] \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]}{d^3} - \\
 & \frac{3 a^2 b c^2 q r \operatorname{Log}[c+dx] \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]}{d^2} + \\
 & \frac{2 a^3 c q r \operatorname{Log}[c+dx] \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]}{d} + \\
 & a^3 x \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]^2 + \frac{3}{2} a^2 b x^2 \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]^2 + \\
 & a b^2 x^3 \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]^2 + \frac{1}{4} b^3 x^4 \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]^2 + \frac{1}{24 b d^4} \\
 & p r \operatorname{Log}[a+bx] \left( a d (5 a^3 d^3 (9 p - 5 q) + 12 b^3 c^3 q - 42 a b^2 c^2 d q + 52 a^2 b c d^2 q) r + 12 b c \right. \\
 & \quad \left. (b^3 c^3 - 4 a b^2 c^2 d + 6 a^2 b c d^2 - 4 a^3 d^3) q r \operatorname{Log}[c+dx] - 12 (b c - a d)^4 q r \operatorname{Log}\left[\frac{b (c+dx)}{b c - a d}\right] + \right. \\
 & \quad \left. 12 a^4 d^4 \operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right] \right) - \frac{(b c - a d)^4 p q r^2 \operatorname{PolyLog}\left[2, \frac{d (a+bx)}{-b c + a d}\right]}{2 b d^4}
 \end{aligned}$$

**Problem 23: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]^2}{(a+bx)^4} dx$$

Optimal (type 4, 764 leaves, 28 steps):

$$\begin{aligned}
 & - \frac{2 p^2 r^2}{27 b (a+b x)^3} - \frac{5 d p q r^2}{18 b (b c-a d) (a+b x)^2} + \frac{8 d^2 p q r^2}{9 b (b c-a d)^2 (a+b x)} - \\
 & \frac{d^2 q^2 r^2}{3 b (b c-a d)^2 (a+b x)} + \frac{2 d^3 p q r^2 \operatorname{Log}[a+b x]}{9 b (b c-a d)^3} - \frac{d^3 q^2 r^2 \operatorname{Log}[a+b x]}{b (b c-a d)^3} - \\
 & \frac{d^3 p q r^2 \operatorname{Log}[a+b x]^2}{3 b (b c-a d)^3} - \frac{2 d^3 p q r^2 \operatorname{Log}[c+d x]}{9 b (b c-a d)^3} + \frac{d^3 q^2 r^2 \operatorname{Log}[c+d x]}{b (b c-a d)^3} + \\
 & \frac{2 d^3 p q r^2 \operatorname{Log}\left[-\frac{d(a+b x)}{b c-a d}\right] \operatorname{Log}[c+d x]}{3 b (b c-a d)^3} + \frac{d^3 q^2 r^2 \operatorname{Log}[c+d x]^2}{3 b (b c-a d)^3} - \frac{2 d^3 q^2 r^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{3 b (b c-a d)^3} \\
 & \frac{2 p r \operatorname{Log}\left[e (f (a+b x)^p (c+d x)^q)^r\right]}{9 b (a+b x)^3} - \frac{d q r \operatorname{Log}\left[e (f (a+b x)^p (c+d x)^q)^r\right]}{3 b (b c-a d) (a+b x)^2} + \\
 & \frac{2 d^2 q r \operatorname{Log}\left[e (f (a+b x)^p (c+d x)^q)^r\right]}{3 b (b c-a d)^2 (a+b x)} + \frac{2 d^3 q r \operatorname{Log}[a+b x] \operatorname{Log}\left[e (f (a+b x)^p (c+d x)^q)^r\right]}{3 b (b c-a d)^3} - \\
 & \frac{2 d^3 q r \operatorname{Log}[c+d x] \operatorname{Log}\left[e (f (a+b x)^p (c+d x)^q)^r\right]}{3 b (b c-a d)^3} - \frac{\operatorname{Log}\left[e (f (a+b x)^p (c+d x)^q)^r\right]^2}{3 b (a+b x)^3} \\
 & \frac{2 d^3 q^2 r^2 \operatorname{PolyLog}\left[2, -\frac{d(a+b x)}{b c-a d}\right]}{3 b (b c-a d)^3} + \frac{2 d^3 p q r^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]}{3 b (b c-a d)^3}
 \end{aligned}$$

Result (type 4, 10507 leaves):

$$\begin{aligned}
 & - \frac{p^2 r^2 (6 \operatorname{Log}[a+b x] + 18 \operatorname{Log}[a+b x]^2 + 27 \operatorname{Log}[a+b x]^3)}{81 b (a+b x)^3 \operatorname{Log}[a+b x]} + \\
 & (q^2 r^2 (b^2 c^3 - 3 a b c^2 d + 3 a^2 c d^2 + 3 a^2 d^3 x + 3 a b d^3 x^2 + b^2 d^3 x^3) \operatorname{Log}[c+d x]^2) / \\
 & \left(3 (-b c+a d)^3 (a+b x)^3\right) - \frac{1}{3 b (a+b x)^3} \left(-p r \operatorname{Log}[a+b x] - \right. \\
 & \left. \operatorname{Log}\left[f (a+b x)^p (c+d x)^q\right] \left(r - \frac{r (-q \operatorname{Log}[c+d x] + \operatorname{Log}\left[f (a+b x)^p (c+d x)^q\right])}{\operatorname{Log}\left[f (a+b x)^p (c+d x)^q\right]}\right) + \right. \\
 & \left. \operatorname{Log}\left[e e^{r (-p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}\left[f (a+b x)^p (c+d x)^q\right])} (a+b x)^{p r}\right] \right. \\
 & \left. \left. (f (a+b x)^p (c+d x)^q)^{r - \frac{r (-q \operatorname{Log}[c+d x] + \operatorname{Log}\left[f (a+b x)^p (c+d x)^q\right])}{\operatorname{Log}\left[f (a+b x)^p (c+d x)^q\right]}}\right]^2 - \frac{1}{9 b (b c-a d)^2 (a+b x)} \right) \\
 & d^2 q r \left(-2 p r + 3 q r - 6 r (-p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}\left[f (a+b x)^p (c+d x)^q\right]) - \right. \\
 & \left. 6 \left(-p r \operatorname{Log}[a+b x] - r (-p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}\left[f (a+b x)^p (c+d x)^q\right]) - \right. \right. \\
 & \left. \left. \operatorname{Log}\left[f (a+b x)^p (c+d x)^q\right] \left(r - \frac{r (-q \operatorname{Log}[c+d x] + \operatorname{Log}\left[f (a+b x)^p (c+d x)^q\right])}{\operatorname{Log}\left[f (a+b x)^p (c+d x)^q\right]}\right) + \right. \right. \\
 & \left. \left. \operatorname{Log}\left[e e^{r (-p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}\left[f (a+b x)^p (c+d x)^q\right])} (a+b x)^{p r}\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( (f (a+bx)^p (c+dx)^q)^{r - \frac{r(-q \operatorname{Log}[c+dx] - \operatorname{Log}[f (a+bx)^p (c+dx)^q])}{\operatorname{Log}[f (a+bx)^p (c+dx)^q]}} \right) - \frac{1}{9b(bc-ad)^3} d^3 q r \operatorname{Log}[a+bx] \\
 & \left( -2pr + 9qr - 6r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f (a+bx)^p (c+dx)^q]) - \right. \\
 & 6 \left( -pr \operatorname{Log}[a+bx] - r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f (a+bx)^p (c+dx)^q]) - \right. \\
 & \operatorname{Log}[f (a+bx)^p (c+dx)^q] \left( r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f (a+bx)^p (c+dx)^q])}{\operatorname{Log}[f (a+bx)^p (c+dx)^q]} \right) + \\
 & \operatorname{Log}[e^{r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f (a+bx)^p (c+dx)^q])}] (a+bx)^{pr} \\
 & \left. \left. (f (a+bx)^p (c+dx)^q)^{r - \frac{r(-q \operatorname{Log}[c+dx] - \operatorname{Log}[f (a+bx)^p (c+dx)^q])}{\operatorname{Log}[f (a+bx)^p (c+dx)^q]}} \right) \right) + \frac{1}{9b(bc-ad)^3} d^3 q r \operatorname{Log}[c+dx] \\
 & \left( -2pr + 9qr - 6r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f (a+bx)^p (c+dx)^q]) - \right. \\
 & 6 \left( -pr \operatorname{Log}[a+bx] - r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f (a+bx)^p (c+dx)^q]) - \right. \\
 & \operatorname{Log}[f (a+bx)^p (c+dx)^q] \left( r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f (a+bx)^p (c+dx)^q])}{\operatorname{Log}[f (a+bx)^p (c+dx)^q]} \right) + \\
 & \operatorname{Log}[e^{r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f (a+bx)^p (c+dx)^q])}] (a+bx)^{pr} \\
 & \left. \left. (f (a+bx)^p (c+dx)^q)^{r - \frac{r(-q \operatorname{Log}[c+dx] - \operatorname{Log}[f (a+bx)^p (c+dx)^q])}{\operatorname{Log}[f (a+bx)^p (c+dx)^q]}} \right) \right) - \frac{1}{9b(bc-ad)(a+bx)^2} \\
 & dqr \left( pr + 3r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f (a+bx)^p (c+dx)^q]) + \right. \\
 & 3 \left( -pr \operatorname{Log}[a+bx] - r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f (a+bx)^p (c+dx)^q]) - \right. \\
 & \operatorname{Log}[f (a+bx)^p (c+dx)^q] \left( r - \frac{r(-q \operatorname{Log}[c+dx] + \operatorname{Log}[f (a+bx)^p (c+dx)^q])}{\operatorname{Log}[f (a+bx)^p (c+dx)^q]} \right) + \\
 & \operatorname{Log}[e^{r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f (a+bx)^p (c+dx)^q])}] (a+bx)^{pr} \\
 & \left. \left. (f (a+bx)^p (c+dx)^q)^{r - \frac{r(-q \operatorname{Log}[c+dx] - \operatorname{Log}[f (a+bx)^p (c+dx)^q])}{\operatorname{Log}[f (a+bx)^p (c+dx)^q]}} \right) \right) + \\
 & \operatorname{Log}[c+dx] \left( -\frac{d q^2 r^2}{3b(bc-ad)(a+bx)^2} + \frac{2 d^2 q^2 r^2}{3b(bc-ad)^2(a+bx)} + \right. \\
 & \frac{2 d^3 q^2 r^2 \operatorname{Log}[a+bx]}{3b(bc-ad)^3} - \frac{2 p q r^2 \operatorname{Log}[a+bx]}{3b(a+bx)^3} - \\
 & \frac{1}{9b(a+bx)^3} 2qr \left( pr + 3r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f (a+bx)^p (c+dx)^q]) + \right. \\
 & \left. 3 \left( -pr \operatorname{Log}[a+bx] - r(-p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}[f (a+bx)^p (c+dx)^q]) - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \log [f (a+bx)^p (c+dx)^q] \left( r - \frac{r (-q \log [c+dx] + \log [f (a+bx)^p (c+dx)^q])}{\log [f (a+bx)^p (c+dx)^q]} \right) + \right. \\
 & \left. \log [e e^{r (-p \log [a+bx] - q \log [c+dx] + \log [f (a+bx)^p (c+dx)^q])} (a+bx)^{pr} \right. \\
 & \left. \left. \left. \left. \left. (f (a+bx)^p (c+dx)^q)^{r - \frac{r (-q \log [c+dx] + \log [f (a+bx)^p (c+dx)^q])}{\log [f (a+bx)^p (c+dx)^q]}} \right) \right) \right) \right) - \frac{1}{3 (bc - ad)^3} \\
 & 8 a b^2 d^4 q^2 r^2 \left( \frac{c^3 \log [a+bx]^2}{2 (bc - ad)^4} + \frac{(3 a b^2 c^2 - 3 a^2 b c d + a^3 d^2) (1 + \log [a+bx])}{b^2 (bc - ad)^3 (ab + b^2 x)} - \right. \\
 & \frac{(3 a^2 b c - 2 a^3 d) (1 + 2 \log [a+bx])}{4 b^3 (bc - ad)^2 (a+bx)^2} + \\
 & \frac{a^3 (1 + 3 \log [a+bx])}{9 b^3 (bc - ad) (a+bx)^3} - \\
 & \left. \frac{c^3 \left( \log [a+bx] \log \left[ \frac{b(c+dx)}{bc-ad} \right] + \text{PolyLog} \left[ 2, \frac{d(a+bx)}{-bc+ad} \right] \right)}{(bc - ad)^4} \right) - \frac{1}{3 (bc - ad)^3} \\
 & 2 b^3 d^4 q^2 r^2 \left( - \frac{(4 a b^3 c^3 - 6 a^2 b^2 c^2 d + 4 a^3 b c d^2 - a^4 d^3) \log [a+bx]^2}{2 b^4 (bc - ad)^4} - \right. \\
 & \frac{(6 a^2 b^2 c^2 - 8 a^3 b c d + 3 a^4 d^2) (1 + \log [a+bx])}{b^3 (bc - ad)^3 (ab + b^2 x)} + \\
 & \frac{(4 a^3 b c - 3 a^4 d) (1 + 2 \log [a+bx])}{4 b^4 (bc - ad)^2 (a+bx)^2} - \frac{a^4 (1 + 3 \log [a+bx])}{9 b^4 (bc - ad) (a+bx)^3} + \\
 & \left. \frac{c^4 \left( \log [a+bx] \log \left[ \frac{b(c+dx)}{bc-ad} \right] + \text{PolyLog} \left[ 2, \frac{d(a+bx)}{-bc+ad} \right] \right)}{d (bc - ad)^4} \right) - \\
 & \frac{1}{(bc - ad)^3} 4 a^2 b d^4 q^2 r^2 \left( - \frac{c^2 d \log [a+bx]^2}{2 (bc - ad)^4} - \frac{b c^2 (1 + \log [a+bx])}{(bc - ad)^3 (ab + b^2 x)} + \right. \\
 & \frac{(2 a b c - a^2 d) (1 + 2 \log [a+bx])}{4 b^2 (bc - ad)^2 (a+bx)^2} - \frac{a^2 (1 + 3 \log [a+bx])}{9 b^2 (bc - ad) (a+bx)^3} + \\
 & \left. \frac{c^2 d \left( \log [a+bx] \log \left[ \frac{b(c+dx)}{bc-ad} \right] + \text{PolyLog} \left[ 2, \frac{d(a+bx)}{-bc+ad} \right] \right)}{(bc - ad)^4} \right) + \\
 & \frac{1}{3 (bc - ad)^3} 2 b^3 c^3 d p q r^2 \left( \frac{c d^2 \log [a+bx]^2}{2 (bc - ad)^4} + \frac{b c d (1 + \log [a+bx])}{(bc - ad)^3 (ab + b^2 x)} - \right. \\
 & \frac{c (1 + 2 \log [a+bx])}{4 (bc - ad)^2 (a+bx)^2} - \frac{a (1 + 3 \log [a+bx])}{9 b (-bc + ad) (a+bx)^3} - \\
 & \left. \frac{c d^2 \left( \log [a+bx] \log \left[ \frac{b(c+dx)}{bc-ad} \right] + \text{PolyLog} \left[ 2, \frac{d(a+bx)}{-bc+ad} \right] \right)}{(bc - ad)^4} \right) -
 \end{aligned}$$



$$\begin{aligned}
 & \frac{1}{(bc-ad)^3} 2ab^2c^2d^2pqr^2 \left( \frac{cd^2 \operatorname{Log}[a+bx]^2}{2(bc-ad)^4} + \frac{bcd(1+\operatorname{Log}[a+bx])}{(bc-ad)^3(ab+b^2x)} - \right. \\
 & \quad \frac{c(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^2(a+bx)^2} - \frac{a(1+3\operatorname{Log}[a+bx])}{9b(-bc+ad)(a+bx)^3} - \\
 & \quad \left. \frac{cd^2 \left( \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) + \\
 & \frac{1}{(bc-ad)^3} 2a^2bcd^3pqr^2 \left( \frac{cd^2 \operatorname{Log}[a+bx]^2}{2(bc-ad)^4} + \frac{bcd(1+\operatorname{Log}[a+bx])}{(bc-ad)^3(ab+b^2x)} - \right. \\
 & \quad \frac{c(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^2(a+bx)^2} - \frac{a(1+3\operatorname{Log}[a+bx])}{9b(-bc+ad)(a+bx)^3} - \\
 & \quad \left. \frac{cd^2 \left( \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) - \\
 & \frac{1}{3(bc-ad)^3} 2a^3d^4pqr^2 \left( \frac{cd^2 \operatorname{Log}[a+bx]^2}{2(bc-ad)^4} + \frac{bcd(1+\operatorname{Log}[a+bx])}{(bc-ad)^3(ab+b^2x)} - \right. \\
 & \quad \frac{c(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^2(a+bx)^2} - \frac{a(1+3\operatorname{Log}[a+bx])}{9b(-bc+ad)(a+bx)^3} - \\
 & \quad \left. \frac{cd^2 \left( \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) - \frac{1}{3(bc-ad)^3} \\
 & 8a^3d^4q^2r^2 \left( \frac{cd^2 \operatorname{Log}[a+bx]^2}{2(bc-ad)^4} + \frac{bcd(1+\operatorname{Log}[a+bx])}{(bc-ad)^3(ab+b^2x)} - \frac{c(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^2(a+bx)^2} - \right. \\
 & \quad \left. \frac{a(1+3\operatorname{Log}[a+bx])}{9b(-bc+ad)(a+bx)^3} - \frac{cd^2 \left( \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) + \\
 & \frac{1}{(bc-ad)^3} 2b^3c^3dpr^2 \left( -p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}\left[f(a+bx)^p(c+dx)^q\right] \right) \\
 & \left( \frac{cd^2 \operatorname{Log}[a+bx]^2}{2(bc-ad)^4} + \frac{bcd(1+\operatorname{Log}[a+bx])}{(bc-ad)^3(ab+b^2x)} - \frac{c(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^2(a+bx)^2} - \right. \\
 & \quad \left. \frac{a(1+3\operatorname{Log}[a+bx])}{9b(-bc+ad)(a+bx)^3} - \frac{cd^2 \left( \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) - \\
 & \frac{1}{(bc-ad)^3} 6a^2b^2c^2d^2pr^2 \left( -p \operatorname{Log}[a+bx] - q \operatorname{Log}[c+dx] + \operatorname{Log}\left[f(a+bx)^p(c+dx)^q\right] \right) \\
 & \left( \frac{cd^2 \operatorname{Log}[a+bx]^2}{2(bc-ad)^4} + \frac{bcd(1+\operatorname{Log}[a+bx])}{(bc-ad)^3(ab+b^2x)} - \frac{c(1+2\operatorname{Log}[a+bx])}{4(bc-ad)^2(a+bx)^2} - \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{a (1 + 3 \operatorname{Log}[a + b x])}{9 b (-b c + a d) (a + b x)^3} - \frac{c d^2 \left( \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^4} \right) + \\
 & \frac{1}{(b c - a d)^3} 6 a^2 b c d^3 p r^2 (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) \\
 & \left( \frac{c d^2 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^4} + \frac{b c d (1 + \operatorname{Log}[a + b x])}{(b c - a d)^3 (a b + b^2 x)} - \frac{c (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^2 (a + b x)^2} - \right. \\
 & \left. \frac{a (1 + 3 \operatorname{Log}[a + b x])}{9 b (-b c + a d) (a + b x)^3} - \frac{c d^2 \left( \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^4} \right) - \\
 & \frac{1}{(b c - a d)^3} 2 a^3 d^4 p r^2 (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) \\
 & \left( \frac{c d^2 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^4} + \frac{b c d (1 + \operatorname{Log}[a + b x])}{(b c - a d)^3 (a b + b^2 x)} - \frac{c (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^2 (a + b x)^2} - \frac{a (1 + 3 \operatorname{Log}[a + b x])}{9 b (-b c + a d) (a + b x)^3} - \right. \\
 & \left. \frac{c d^2 \left( \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^4} \right) + \frac{1}{(b c - a d)^3} \\
 & 2 b^3 c^3 d p r \left( -p r \operatorname{Log}[a + b x] - r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) - \right. \\
 & \left. \operatorname{Log}[f (a + b x)^p (c + d x)^q] \left( r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]} \right) \right) + \\
 & \operatorname{Log}\left[ e^{r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])} (a + b x)^{p r} \right. \\
 & \left. (f (a + b x)^p (c + d x)^q)^{r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]}} \right] \left( \frac{c d^2 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^4} + \right. \\
 & \frac{b c d (1 + \operatorname{Log}[a + b x])}{(b c - a d)^3 (a b + b^2 x)} - \frac{c (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^2 (a + b x)^2} - \frac{a (1 + 3 \operatorname{Log}[a + b x])}{9 b (-b c + a d) (a + b x)^3} - \\
 & \left. \frac{c d^2 \left( \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^4} \right) - \frac{1}{(b c - a d)^3} \\
 & 6 a b^2 c^2 d^2 p r \left( -p r \operatorname{Log}[a + b x] - r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q]) - \right. \\
 & \left. \operatorname{Log}[f (a + b x)^p (c + d x)^q] \left( r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]} \right) \right) + \\
 & \operatorname{Log}\left[ e^{r (-p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])} (a + b x)^{p r} \right. \\
 & \left. (f (a + b x)^p (c + d x)^q)^{r - \frac{r (-q \operatorname{Log}[c + d x] + \operatorname{Log}[f (a + b x)^p (c + d x)^q])}{\operatorname{Log}[f (a + b x)^p (c + d x)^q]}} \right] \left( \frac{c d^2 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^4} + \right. \\
 & \frac{b c d (1 + \operatorname{Log}[a + b x])}{(b c - a d)^3 (a b + b^2 x)} - \frac{c (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^2 (a + b x)^2} - \frac{a (1 + 3 \operatorname{Log}[a + b x])}{9 b (-b c + a d) (a + b x)^3} - \\
 & \left. \frac{c d^2 \left( \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^4} \right) - \frac{1}{(b c - a d)^3}
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{c d^2 \left( \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) + \frac{1}{(bc-ad)^3} \\
 6 a^2 b c d^3 p r & \left( -p r \text{Log}[a+bx] - r \left( -p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q] \right) - \right. \\
 & \text{Log}[f(a+bx)^p(c+dx)^q] \left( r - \frac{r(-q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q])}{\text{Log}[f(a+bx)^p(c+dx)^q]} \right) + \\
 & \text{Log}\left[ e^{e^{r(-p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q])}} (a+bx)^{pr} \right. \\
 & \left. \left. (f(a+bx)^p(c+dx)^q)^{r - \frac{r(-q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q])}{\text{Log}[f(a+bx)^p(c+dx)^q]}} \right) \right] \left( \frac{c d^2 \text{Log}[a+bx]^2}{2(bc-ad)^4} + \right. \\
 & \frac{b c d (1 + \text{Log}[a+bx])}{(bc-ad)^3 (ab+b^2x)} - \frac{c(1+2 \text{Log}[a+bx])}{4(bc-ad)^2 (a+bx)^2} - \frac{a(1+3 \text{Log}[a+bx])}{9b(-bc+ad)(a+bx)^3} - \\
 & \left. \left. \frac{c d^2 \left( \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) - \frac{1}{(bc-ad)^3} \right) \\
 2 a^3 d^4 p r & \left( -p r \text{Log}[a+bx] - r \left( -p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q] \right) - \right. \\
 & \text{Log}[f(a+bx)^p(c+dx)^q] \left( r - \frac{r(-q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q])}{\text{Log}[f(a+bx)^p(c+dx)^q]} \right) + \\
 & \text{Log}\left[ e^{e^{r(-p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q])}} (a+bx)^{pr} \right. \\
 & \left. \left. (f(a+bx)^p(c+dx)^q)^{r - \frac{r(-q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q])}{\text{Log}[f(a+bx)^p(c+dx)^q]}} \right) \right] \\
 & \left( \frac{c d^2 \text{Log}[a+bx]^2}{2(bc-ad)^4} + \frac{b c d (1 + \text{Log}[a+bx])}{(bc-ad)^3 (ab+b^2x)} - \frac{c(1+2 \text{Log}[a+bx])}{4(bc-ad)^2 (a+bx)^2} - \right. \\
 & \left. \frac{a(1+3 \text{Log}[a+bx])}{9b(-bc+ad)(a+bx)^3} - \frac{c d^2 \left( \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) + \\
 \frac{1}{3(bc-ad)^3} & 2 a b^2 c^3 d p q r^2 \left( -\frac{d^3 \text{Log}[a+bx]^2}{2(bc-ad)^4} - \frac{b d^2 (1 + \text{Log}[a+bx])}{(bc-ad)^3 (ab+b^2x)} + \right. \\
 & \frac{d(1+2 \text{Log}[a+bx])}{4(bc-ad)^2 (a+bx)^2} + \frac{1+3 \text{Log}[a+bx]}{9(-bc+ad)(a+bx)^3} + \\
 & \left. \left. \frac{d^3 \left( \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^4} \right) - \frac{1}{(bc-ad)^3} \right) \\
 2 a^2 b c^2 d^2 p q r^2 & \left( -\frac{d^3 \text{Log}[a+bx]^2}{2(bc-ad)^4} - \frac{b d^2 (1 + \text{Log}[a+bx])}{(bc-ad)^3 (ab+b^2x)} + \frac{d(1+2 \text{Log}[a+bx])}{4(bc-ad)^2 (a+bx)^2} + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{1 + 3 \operatorname{Log}[a + bx]}{9(-bc + ad)(a + bx)^3} + \frac{d^3 \left( \operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc - ad)^4} \right) + \frac{1}{(bc - ad)^3} \\
 2 a^3 c d^3 p q r^2 & \left( -\frac{d^3 \operatorname{Log}[a + bx]^2}{2(bc - ad)^4} - \frac{b d^2 (1 + \operatorname{Log}[a + bx])}{(bc - ad)^3 (a b + b^2 x)} + \frac{d (1 + 2 \operatorname{Log}[a + bx])}{4(bc - ad)^2 (a + bx)^2} + \right. \\
 & \left. \frac{1 + 3 \operatorname{Log}[a + bx]}{9(-bc + ad)(a + bx)^3} + \frac{d^3 \left( \operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc - ad)^4} \right) - \\
 \frac{1}{3 b (bc - ad)^3} 2 a^4 d^4 p q r^2 & \left( -\frac{d^3 \operatorname{Log}[a + bx]^2}{2(bc - ad)^4} - \frac{b d^2 (1 + \operatorname{Log}[a + bx])}{(bc - ad)^3 (a b + b^2 x)} + \frac{d (1 + 2 \operatorname{Log}[a + bx])}{4(bc - ad)^2 (a + bx)^2} + \right. \\
 & \left. \frac{1 + 3 \operatorname{Log}[a + bx]}{9(-bc + ad)(a + bx)^3} + \frac{d^3 \left( \operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc - ad)^4} \right) - \\
 \frac{1}{3 b (bc - ad)^3} 2 a^4 d^4 q^2 r^2 & \left( -\frac{d^3 \operatorname{Log}[a + bx]^2}{2(bc - ad)^4} - \frac{b d^2 (1 + \operatorname{Log}[a + bx])}{(bc - ad)^3 (a b + b^2 x)} + \frac{d (1 + 2 \operatorname{Log}[a + bx])}{4(bc - ad)^2 (a + bx)^2} + \right. \\
 & \left. \frac{1 + 3 \operatorname{Log}[a + bx]}{9(-bc + ad)(a + bx)^3} + \frac{d^3 \left( \operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc - ad)^4} \right) + \\
 \frac{1}{(bc - ad)^3} 2 b^3 c^4 p r^2 & (-p \operatorname{Log}[a + bx] - q \operatorname{Log}[c + dx] + \operatorname{Log}[f(a + bx)^p (c + dx)^q]) \\
 & \left( -\frac{d^3 \operatorname{Log}[a + bx]^2}{2(bc - ad)^4} - \frac{b d^2 (1 + \operatorname{Log}[a + bx])}{(bc - ad)^3 (a b + b^2 x)} + \frac{d (1 + 2 \operatorname{Log}[a + bx])}{4(bc - ad)^2 (a + bx)^2} + \right. \\
 & \left. \frac{1 + 3 \operatorname{Log}[a + bx]}{9(-bc + ad)(a + bx)^3} + \frac{d^3 \left( \operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc - ad)^4} \right) - \\
 \frac{1}{(bc - ad)^3} 6 a b^2 c^3 d p r^2 & (-p \operatorname{Log}[a + bx] - q \operatorname{Log}[c + dx] + \operatorname{Log}[f(a + bx)^p (c + dx)^q]) \\
 & \left( -\frac{d^3 \operatorname{Log}[a + bx]^2}{2(bc - ad)^4} - \frac{b d^2 (1 + \operatorname{Log}[a + bx])}{(bc - ad)^3 (a b + b^2 x)} + \frac{d (1 + 2 \operatorname{Log}[a + bx])}{4(bc - ad)^2 (a + bx)^2} + \right. \\
 & \left. \frac{1 + 3 \operatorname{Log}[a + bx]}{9(-bc + ad)(a + bx)^3} + \frac{d^3 \left( \operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc - ad)^4} \right) + \\
 \frac{1}{(bc - ad)^3} 6 a^2 b c^2 d^2 p r^2 & (-p \operatorname{Log}[a + bx] - q \operatorname{Log}[c + dx] + \operatorname{Log}[f(a + bx)^p (c + dx)^q]) \\
 & \left( -\frac{d^3 \operatorname{Log}[a + bx]^2}{2(bc - ad)^4} - \frac{b d^2 (1 + \operatorname{Log}[a + bx])}{(bc - ad)^3 (a b + b^2 x)} + \frac{d (1 + 2 \operatorname{Log}[a + bx])}{4(bc - ad)^2 (a + bx)^2} + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{1 + 3 \operatorname{Log}[a + b x]}{9 (-b c + a d) (a + b x)^3} + \frac{d^3 \left( \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^4} \right) - \\
 & \frac{1}{(b c - a d)^3} 2 a^3 c d^3 p r^2 \left( -p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right] \right) \\
 & \left( -\frac{d^3 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^4} - \frac{b d^2 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^3 (a b + b^2 x)} + \frac{d (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^2 (a + b x)^2} + \frac{1 + 3 \operatorname{Log}[a + b x]}{9 (-b c + a d) (a + b x)^3} + \right. \\
 & \left. \frac{d^3 \left( \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^4} \right) + \frac{1}{(b c - a d)^3} \\
 & 2 b^3 c^4 p r \left( -p r \operatorname{Log}[a + b x] - r \left( -p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right] \right) - \right. \\
 & \left. \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right] \left( r - \frac{r \left( -q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]\right)}{\operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]} \right) + \right. \\
 & \left. \operatorname{Log}\left[e^r \left( -p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right] \right) (a + b x)^{p r} \right. \right. \\
 & \left. \left. (f (a + b x)^p (c + d x)^q)^{r \frac{-r \left( -q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]\right)}{\operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]}} \right] \right) \\
 & \left( -\frac{d^3 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^4} - \frac{b d^2 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^3 (a b + b^2 x)} + \frac{d (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^2 (a + b x)^2} + \right. \\
 & \left. \frac{1 + 3 \operatorname{Log}[a + b x]}{9 (-b c + a d) (a + b x)^3} + \frac{d^3 \left( \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^4} \right) - \frac{1}{(b c - a d)^3} \\
 & 6 a b^2 c^3 d p r \left( -p r \operatorname{Log}[a + b x] - r \left( -p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right] \right) - \right. \\
 & \left. \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right] \left( r - \frac{r \left( -q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]\right)}{\operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]} \right) + \right. \\
 & \left. \operatorname{Log}\left[e^r \left( -p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right] \right) (a + b x)^{p r} \right. \right. \\
 & \left. \left. (f (a + b x)^p (c + d x)^q)^{r \frac{-r \left( -q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]\right)}{\operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]}} \right] \right) \\
 & \left( -\frac{d^3 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^4} - \frac{b d^2 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^3 (a b + b^2 x)} + \frac{d (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^2 (a + b x)^2} + \right. \\
 & \left. \frac{1 + 3 \operatorname{Log}[a + b x]}{9 (-b c + a d) (a + b x)^3} + \frac{d^3 \left( \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^4} \right) + \frac{1}{(b c - a d)^3} \\
 & 6 a^2 b c^2 d^2 p r \left( -p r \operatorname{Log}[a + b x] - r \left( -p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right] \right) - \right. \\
 & \left. \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right] \left( r - \frac{r \left( -q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]\right)}{\operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]} \right) + \right.
 \end{aligned}$$

$$\begin{aligned} & \text{Log} \left[ e^{r \left( -p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f (a+bx)^p (c+dx)^q] \right)} (a+bx)^{pr} \right. \\ & \quad \left. (f (a+bx)^p (c+dx)^q)^{r - \frac{r \left( -q \text{Log}[c+dx] + \text{Log}[f (a+bx)^p (c+dx)^q] \right)}{\text{Log}[f (a+bx)^p (c+dx)^q]}} \right] \\ & \left( -\frac{d^3 \text{Log}[a+bx]^2}{2 (bc-ad)^4} - \frac{bd^2 (1 + \text{Log}[a+bx])}{(bc-ad)^3 (ab+b^2x)} + \frac{d (1 + 2 \text{Log}[a+bx])}{4 (bc-ad)^2 (a+bx)^2} + \right. \\ & \quad \left. \frac{1 + 3 \text{Log}[a+bx]}{9 (-bc+ad) (a+bx)^3} + \frac{d^3 \left( \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(bc-ad)^4} \right) - \frac{1}{(bc-ad)^3} \\ & 2a^3 c d^3 p r \left( -p r \text{Log}[a+bx] - r \left( -p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f (a+bx)^p (c+dx)^q] \right) - \right. \\ & \quad \left. \text{Log}[f (a+bx)^p (c+dx)^q] \left( r - \frac{r \left( -q \text{Log}[c+dx] + \text{Log}[f (a+bx)^p (c+dx)^q] \right)}{\text{Log}[f (a+bx)^p (c+dx)^q]} \right) \right) + \\ & \quad \text{Log} \left[ e^{r \left( -p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f (a+bx)^p (c+dx)^q] \right)} (a+bx)^{pr} \right. \\ & \quad \left. (f (a+bx)^p (c+dx)^q)^{r - \frac{r \left( -q \text{Log}[c+dx] + \text{Log}[f (a+bx)^p (c+dx)^q] \right)}{\text{Log}[f (a+bx)^p (c+dx)^q]}} \right] \\ & \left( -\frac{d^3 \text{Log}[a+bx]^2}{2 (bc-ad)^4} - \frac{bd^2 (1 + \text{Log}[a+bx])}{(bc-ad)^3 (ab+b^2x)} + \frac{d (1 + 2 \text{Log}[a+bx])}{4 (bc-ad)^2 (a+bx)^2} + \right. \\ & \quad \left. \frac{1 + 3 \text{Log}[a+bx]}{9 (-bc+ad) (a+bx)^3} + \frac{d^3 \left( \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(bc-ad)^4} \right) \end{aligned}$$

**Problem 24: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Log} \left[ e \left( f (a+bx)^p (c+dx)^q \right)^r \right]^2}{(a+bx)^5} dx$$

Optimal (type 4, 884 leaves, 32 steps):

$$\begin{aligned}
 & - \frac{p^2 r^2}{32 b (a+bx)^4} - \frac{7 d p q r^2}{72 b (bc-ad)(a+bx)^3} + \frac{3 d^2 p q r^2}{16 b (bc-ad)^2 (a+bx)^2} - \\
 & \frac{d^2 q^2 r^2}{12 b (bc-ad)^2 (a+bx)^2} - \frac{5 d^3 p q r^2}{8 b (bc-ad)^3 (a+bx)} + \frac{5 d^3 q^2 r^2}{12 b (bc-ad)^3 (a+bx)} - \\
 & \frac{d^4 p q r^2 \text{Log}[a+bx]}{8 b (bc-ad)^4} + \frac{11 d^4 q^2 r^2 \text{Log}[a+bx]}{12 b (bc-ad)^4} + \frac{d^4 p q r^2 \text{Log}[a+bx]^2}{4 b (bc-ad)^4} + \frac{d^4 p q r^2 \text{Log}[c+dx]}{8 b (bc-ad)^4} - \\
 & \frac{11 d^4 q^2 r^2 \text{Log}[c+dx]}{12 b (bc-ad)^4} - \frac{d^4 p q r^2 \text{Log}\left[-\frac{d(a+bx)}{bc-ad}\right] \text{Log}[c+dx]}{2 b (bc-ad)^4} - \frac{d^4 q^2 r^2 \text{Log}[c+dx]^2}{4 b (bc-ad)^4} + \\
 & \frac{d^4 q^2 r^2 \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{2 b (bc-ad)^4} - \frac{p r \text{Log}\left[e(f(a+bx)^p(c+dx)^q)^r\right]}{8 b (a+bx)^4} - \\
 & \frac{d q r \text{Log}\left[e(f(a+bx)^p(c+dx)^q)^r\right]}{6 b (bc-ad)(a+bx)^3} + \frac{d^2 q r \text{Log}\left[e(f(a+bx)^p(c+dx)^q)^r\right]}{4 b (bc-ad)^2 (a+bx)^2} - \\
 & \frac{d^3 q r \text{Log}\left[e(f(a+bx)^p(c+dx)^q)^r\right]}{2 b (bc-ad)^3 (a+bx)} - \frac{d^4 q r \text{Log}[a+bx] \text{Log}\left[e(f(a+bx)^p(c+dx)^q)^r\right]}{2 b (bc-ad)^4} + \\
 & \frac{d^4 q r \text{Log}[c+dx] \text{Log}\left[e(f(a+bx)^p(c+dx)^q)^r\right]}{2 b (bc-ad)^4} - \frac{\text{Log}\left[e(f(a+bx)^p(c+dx)^q)^r\right]^2}{4 b (a+bx)^4} + \\
 & \frac{d^4 q^2 r^2 \text{PolyLog}\left[2, -\frac{d(a+bx)}{bc-ad}\right]}{2 b (bc-ad)^4} - \frac{d^4 p q r^2 \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{2 b (bc-ad)^4}
 \end{aligned}$$

Result (type 4, 14 321 leaves):

$$\begin{aligned}
 & - \frac{p^2 r^2 (8 \text{Log}[a+bx] + 32 \text{Log}[a+bx]^2 + 64 \text{Log}[a+bx]^3)}{256 b (a+bx)^4 \text{Log}[a+bx]} + \\
 & (q^2 r^2 (-b^3 c^4 + 4 a b^2 c^3 d - 6 a^2 b c^2 d^2 + 4 a^3 c d^3 + 4 a^3 d^4 x + 6 a^2 b d^4 x^2 + 4 a b^2 d^4 x^3 + b^3 d^4 x^4) \\
 & \text{Log}[c+dx]^2) / (4 (-bc+ad)^4 (a+bx)^4) - \frac{1}{4 b (a+bx)^4} \left( -p r \text{Log}[a+bx] - \right. \\
 & \left. \text{Log}\left[f(a+bx)^p(c+dx)^q\right] \left( r - \frac{r(-q \text{Log}[c+dx] + \text{Log}\left[f(a+bx)^p(c+dx)^q\right])}{\text{Log}\left[f(a+bx)^p(c+dx)^q\right]} \right) \right) + \\
 & \text{Log}\left[e^{e^{r(-p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}\left[f(a+bx)^p(c+dx)^q\right])}} (a+bx)^{p r} \right. \\
 & \left. \left( f(a+bx)^p(c+dx)^q \right)^{r - \frac{r(-q \text{Log}[c+dx] + \text{Log}\left[f(a+bx)^p(c+dx)^q\right])}{\text{Log}\left[f(a+bx)^p(c+dx)^q\right]}} \right]^2 - \frac{1}{48 b (bc-ad)^2 (a+bx)^2} \\
 & d^2 q r \left( -3 p r + 4 q r - 12 r (-p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}\left[f(a+bx)^p(c+dx)^q\right]) \right) - \\
 & 12 \left( -p r \text{Log}[a+bx] - r (-p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}\left[f(a+bx)^p(c+dx)^q\right]) \right) - \\
 & \text{Log}\left[f(a+bx)^p(c+dx)^q\right] \left( r - \frac{r(-q \text{Log}[c+dx] + \text{Log}\left[f(a+bx)^p(c+dx)^q\right])}{\text{Log}\left[f(a+bx)^p(c+dx)^q\right]} \right) +
 \end{aligned}$$





$$\begin{aligned}
 & \left( f (a+b x)^p (c+d x)^q \right)^{r - \frac{r (-q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q])}{\operatorname{Log}[f (a+b x)^p (c+d x)^q]}} \Bigg) + \\
 \operatorname{Log}[c+d x] & \left( - \frac{d q^2 r^2}{6 b (b c - a d) (a+b x)^3} + \frac{d^2 q^2 r^2}{4 b (b c - a d)^2 (a+b x)^2} - \right. \\
 & \frac{d^3 q^2 r^2}{2 b (b c - a d)^3 (a+b x)} - \\
 & \frac{d^4 q^2 r^2 \operatorname{Log}[a+b x]}{2 b (b c - a d)^4} - \frac{p q r^2 \operatorname{Log}[a+b x]}{2 b (a+b x)^4} - \\
 & \frac{1}{8 b (a+b x)^4} q r \left( p r + 4 r (-p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q]) + \right. \\
 & 4 \left( -p r \operatorname{Log}[a+b x] - r (-p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q]) - \right. \\
 & \left. \left. \operatorname{Log}[f (a+b x)^p (c+d x)^q] \left( r - \frac{r (-q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q])}{\operatorname{Log}[f (a+b x)^p (c+d x)^q]} \right) \right) + \right. \\
 & \left. \operatorname{Log}\left[ e e^{r (-p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q])} (a+b x)^{p r} \right. \right. \\
 & \left. \left. \left( f (a+b x)^p (c+d x)^q \right)^{r - \frac{r (-q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q])}{\operatorname{Log}[f (a+b x)^p (c+d x)^q]}} \right] \right) \Bigg) + \frac{1}{2 (b c - a d)^4} \\
 5 a b^3 d^5 q^2 r^2 & \left( \frac{c^4 \operatorname{Log}[a+b x]^2}{2 (b c - a d)^5} + \frac{(4 a b^3 c^3 - 6 a^2 b^2 c^2 d + 4 a^3 b c d^2 - a^4 d^3) (1 + \operatorname{Log}[a+b x])}{b^3 (b c - a d)^4 (a b + b^2 x)} - \right. \\
 & \frac{(6 a^2 b^2 c^2 - 8 a^3 b c d + 3 a^4 d^2) (1 + 2 \operatorname{Log}[a+b x])}{4 b^4 (b c - a d)^3 (a+b x)^2} + \\
 & \frac{(4 a^3 b c - 3 a^4 d) (1 + 3 \operatorname{Log}[a+b x])}{9 b^4 (b c - a d)^2 (a+b x)^3} - \\
 & \frac{a^4 (1 + 4 \operatorname{Log}[a+b x])}{16 b^4 (b c - a d) (a+b x)^4} - \\
 & \left. \frac{c^4 \left( \operatorname{Log}[a+b x] \operatorname{Log}\left[ \frac{b (c+d x)}{b c - a d} \right] + \operatorname{PolyLog}\left[ 2, \frac{d (a+b x)}{-b c + a d} \right] \right)}{(b c - a d)^5} \right) + \frac{1}{2 (b c - a d)^4} \\
 b^4 d^5 q^2 r^2 & \left( - \frac{1}{2 b^5 (b c - a d)^5} (5 a b^4 c^4 - 10 a^2 b^3 c^3 d + 10 a^3 b^2 c^2 d^2 - 5 a^4 b c d^3 + a^5 d^4) \operatorname{Log}[a+b x]^2 - \right. \\
 & \frac{(10 a^2 b^3 c^3 - 20 a^3 b^2 c^2 d + 15 a^4 b c d^2 - 4 a^5 d^3) (1 + \operatorname{Log}[a+b x])}{b^4 (b c - a d)^4 (a b + b^2 x)} + \\
 & \frac{(10 a^3 b^2 c^2 - 15 a^4 b c d + 6 a^5 d^2) (1 + 2 \operatorname{Log}[a+b x])}{4 b^5 (b c - a d)^3 (a+b x)^2} - \\
 & \left. \frac{(5 a^4 b c - 4 a^5 d) (1 + 3 \operatorname{Log}[a+b x])}{9 b^5 (b c - a d)^2 (a+b x)^3} + \frac{a^5 (1 + 4 \operatorname{Log}[a+b x])}{16 b^5 (b c - a d) (a+b x)^4} + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{c^5 \left( \text{Log}[a + b x] \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{d (b c - a d)^5} \right) + \\
 & \frac{1}{(b c - a d)^4} 5 a^2 b^2 d^5 q^2 r^2 \left( -\frac{c^3 d \text{Log}[a + b x]^2}{2 (b c - a d)^5} - \frac{b c^3 (1 + \text{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} + \right. \\
 & \quad \frac{(3 a b^2 c^2 - 3 a^2 b c d + a^3 d^2) (1 + 2 \text{Log}[a + b x])}{4 b^3 (b c - a d)^3 (a + b x)^2} - \\
 & \quad \frac{(3 a^2 b c - 2 a^3 d) (1 + 3 \text{Log}[a + b x])}{9 b^3 (b c - a d)^2 (a + b x)^3} + \frac{a^3 (1 + 4 \text{Log}[a + b x])}{16 b^3 (b c - a d) (a + b x)^4} + \\
 & \quad \left. \frac{c^3 d \left( \text{Log}[a + b x] \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^5} \right) + \frac{1}{(b c - a d)^4} \\
 & 5 a^3 b d^5 q^2 r^2 \left( \frac{c^2 d^2 \text{Log}[a + b x]^2}{2 (b c - a d)^5} + \frac{b c^2 d (1 + \text{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} - \frac{c^2 (1 + 2 \text{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} + \right. \\
 & \quad \frac{(2 a b c - a^2 d) (1 + 3 \text{Log}[a + b x])}{9 b^2 (b c - a d)^2 (a + b x)^3} - \frac{a^2 (1 + 4 \text{Log}[a + b x])}{16 b^2 (b c - a d) (a + b x)^4} - \\
 & \quad \left. \frac{c^2 d^2 \left( \text{Log}[a + b x] \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^5} \right) + \\
 & \frac{1}{2 (b c - a d)^4} b^4 c^4 d p q r^2 \left( -\frac{c d^3 \text{Log}[a + b x]^2}{2 (b c - a d)^5} - \frac{b c d^2 (1 + \text{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} + \right. \\
 & \quad \frac{c d (1 + 2 \text{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} - \frac{c (1 + 3 \text{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} - \frac{a (1 + 4 \text{Log}[a + b x])}{16 b (-b c + a d) (a + b x)^4} + \\
 & \quad \left. \frac{c d^3 \left( \text{Log}[a + b x] \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^5} \right) - \\
 & \frac{1}{(b c - a d)^4} 2 a b^3 c^3 d^2 p q r^2 \left( -\frac{c d^3 \text{Log}[a + b x]^2}{2 (b c - a d)^5} - \frac{b c d^2 (1 + \text{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} + \right. \\
 & \quad \frac{c d (1 + 2 \text{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} - \frac{c (1 + 3 \text{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} - \frac{a (1 + 4 \text{Log}[a + b x])}{16 b (-b c + a d) (a + b x)^4} + \\
 & \quad \left. \frac{c d^3 \left( \text{Log}[a + b x] \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^5} \right) + \\
 & \frac{1}{(b c - a d)^4} 3 a^2 b^2 c^2 d^3 p q r^2 \left( -\frac{c d^3 \text{Log}[a + b x]^2}{2 (b c - a d)^5} - \frac{b c d^2 (1 + \text{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} + \right. \\
 & \quad \frac{c d (1 + 2 \text{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} - \frac{c (1 + 3 \text{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} - \frac{a (1 + 4 \text{Log}[a + b x])}{16 b (-b c + a d) (a + b x)^4} +
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{c d^3 \left( \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^5} \right) - \\
 & \frac{1}{(bc-ad)^4} 2 a^3 b c d^4 p q r^2 \left( -\frac{c d^3 \text{Log}[a+bx]^2}{2 (bc-ad)^5} - \frac{b c d^2 (1 + \text{Log}[a+bx])}{(bc-ad)^4 (ab+b^2x)} + \right. \\
 & \frac{c d (1 + 2 \text{Log}[a+bx])}{4 (bc-ad)^3 (a+bx)^2} - \frac{c (1 + 3 \text{Log}[a+bx])}{9 (bc-ad)^2 (a+bx)^3} - \frac{a (1 + 4 \text{Log}[a+bx])}{16 b (-bc+ad) (a+bx)^4} + \\
 & \left. \frac{c d^3 \left( \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^5} \right) + \frac{1}{2 (bc-ad)^4} \\
 & a^4 d^5 p q r^2 \left( -\frac{c d^3 \text{Log}[a+bx]^2}{2 (bc-ad)^5} - \frac{b c d^2 (1 + \text{Log}[a+bx])}{(bc-ad)^4 (ab+b^2x)} + \frac{c d (1 + 2 \text{Log}[a+bx])}{4 (bc-ad)^3 (a+bx)^2} - \right. \\
 & \frac{c (1 + 3 \text{Log}[a+bx])}{9 (bc-ad)^2 (a+bx)^3} - \frac{a (1 + 4 \text{Log}[a+bx])}{16 b (-bc+ad) (a+bx)^4} + \\
 & \left. \frac{c d^3 \left( \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^5} \right) + \\
 & \frac{1}{2 (bc-ad)^4} 5 a^4 d^5 q^2 r^2 \left( -\frac{c d^3 \text{Log}[a+bx]^2}{2 (bc-ad)^5} - \frac{b c d^2 (1 + \text{Log}[a+bx])}{(bc-ad)^4 (ab+b^2x)} + \right. \\
 & \frac{c d (1 + 2 \text{Log}[a+bx])}{4 (bc-ad)^3 (a+bx)^2} - \frac{c (1 + 3 \text{Log}[a+bx])}{9 (bc-ad)^2 (a+bx)^3} - \frac{a (1 + 4 \text{Log}[a+bx])}{16 b (-bc+ad) (a+bx)^4} + \\
 & \left. \frac{c d^3 \left( \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^5} \right) + \frac{1}{(bc-ad)^4} \\
 & 2 b^4 c^4 d p r^2 \left( -p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q] \right) \\
 & \left( -\frac{c d^3 \text{Log}[a+bx]^2}{2 (bc-ad)^5} - \frac{b c d^2 (1 + \text{Log}[a+bx])}{(bc-ad)^4 (ab+b^2x)} + \frac{c d (1 + 2 \text{Log}[a+bx])}{4 (bc-ad)^3 (a+bx)^2} - \right. \\
 & \frac{c (1 + 3 \text{Log}[a+bx])}{9 (bc-ad)^2 (a+bx)^3} - \frac{a (1 + 4 \text{Log}[a+bx])}{16 b (-bc+ad) (a+bx)^4} + \\
 & \left. \frac{c d^3 \left( \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^5} \right) - \frac{1}{(bc-ad)^4} \\
 & 8 a b^3 c^3 d^2 p r^2 \left( -p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q] \right) \\
 & \left( -\frac{c d^3 \text{Log}[a+bx]^2}{2 (bc-ad)^5} - \frac{b c d^2 (1 + \text{Log}[a+bx])}{(bc-ad)^4 (ab+b^2x)} + \frac{c d (1 + 2 \text{Log}[a+bx])}{4 (bc-ad)^3 (a+bx)^2} - \right. \\
 & \frac{c (1 + 3 \text{Log}[a+bx])}{9 (bc-ad)^2 (a+bx)^3} - \frac{a (1 + 4 \text{Log}[a+bx])}{16 b (-bc+ad) (a+bx)^4} +
 \end{aligned}$$

$$\frac{c d^3 \left( \text{Log}[a + b x] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(bc-ad)^5} + \frac{1}{(bc-ad)^4}$$

$$12 a^2 b^2 c^2 d^3 p r^2 \left( -p \text{Log}[a + b x] - q \text{Log}[c + d x] + \text{Log}\left[f(a + b x)^p (c + d x)^q\right] \right)$$

$$\left( -\frac{c d^3 \text{Log}[a + b x]^2}{2 (bc-ad)^5} - \frac{b c d^2 (1 + \text{Log}[a + b x])}{(bc-ad)^4 (a b + b^2 x)} + \frac{c d (1 + 2 \text{Log}[a + b x])}{4 (bc-ad)^3 (a + b x)^2} - \frac{c (1 + 3 \text{Log}[a + b x])}{9 (bc-ad)^2 (a + b x)^3} - \frac{a (1 + 4 \text{Log}[a + b x])}{16 b (-bc + ad) (a + b x)^4} + \frac{c d^3 \left( \text{Log}[a + b x] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(bc-ad)^5} \right) -$$

$$\frac{1}{(bc-ad)^4} 8 a^3 b c d^4 p r^2 \left( -p \text{Log}[a + b x] - q \text{Log}[c + d x] + \text{Log}\left[f(a + b x)^p (c + d x)^q\right] \right)$$

$$\left( -\frac{c d^3 \text{Log}[a + b x]^2}{2 (bc-ad)^5} - \frac{b c d^2 (1 + \text{Log}[a + b x])}{(bc-ad)^4 (a b + b^2 x)} + \frac{c d (1 + 2 \text{Log}[a + b x])}{4 (bc-ad)^3 (a + b x)^2} - \frac{c (1 + 3 \text{Log}[a + b x])}{9 (bc-ad)^2 (a + b x)^3} - \frac{a (1 + 4 \text{Log}[a + b x])}{16 b (-bc + ad) (a + b x)^4} + \frac{c d^3 \left( \text{Log}[a + b x] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(bc-ad)^5} \right) +$$

$$\frac{1}{(bc-ad)^4} 2 a^4 d^5 p r^2 \left( -p \text{Log}[a + b x] - q \text{Log}[c + d x] + \text{Log}\left[f(a + b x)^p (c + d x)^q\right] \right)$$

$$\left( -\frac{c d^3 \text{Log}[a + b x]^2}{2 (bc-ad)^5} - \frac{b c d^2 (1 + \text{Log}[a + b x])}{(bc-ad)^4 (a b + b^2 x)} + \frac{c d (1 + 2 \text{Log}[a + b x])}{4 (bc-ad)^3 (a + b x)^2} - \frac{c (1 + 3 \text{Log}[a + b x])}{9 (bc-ad)^2 (a + b x)^3} - \frac{a (1 + 4 \text{Log}[a + b x])}{16 b (-bc + ad) (a + b x)^4} + \frac{c d^3 \left( \text{Log}[a + b x] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right)}{(bc-ad)^5} \right) + \frac{1}{(bc-ad)^4}$$

$$2 b^4 c^4 d p r \left( -p r \text{Log}[a + b x] - r \left( -p \text{Log}[a + b x] - q \text{Log}[c + d x] + \text{Log}\left[f(a + b x)^p (c + d x)^q\right] \right) - \right.$$

$$\left. \text{Log}\left[f(a + b x)^p (c + d x)^q\right] \left( r - \frac{r \left( -q \text{Log}[c + d x] + \text{Log}\left[f(a + b x)^p (c + d x)^q\right] \right)}{\text{Log}\left[f(a + b x)^p (c + d x)^q\right]} \right) + \right.$$

$$\left. \text{Log}\left[e^{r \left( -p \text{Log}[a + b x] - q \text{Log}[c + d x] + \text{Log}\left[f(a + b x)^p (c + d x)^q\right] \right)} (a + b x)^{p r} \right. \right.$$

$$\left. \left. (f(a + b x)^p (c + d x)^q)^{r \frac{-q \text{Log}[c + d x] + \text{Log}\left[f(a + b x)^p (c + d x)^q\right]}{\text{Log}\left[f(a + b x)^p (c + d x)^q\right]}} \right] \right)$$

$$\left( -\frac{c d^3 \text{Log}[a + b x]^2}{2 (bc-ad)^5} - \frac{b c d^2 (1 + \text{Log}[a + b x])}{(bc-ad)^4 (a b + b^2 x)} + \frac{c d (1 + 2 \text{Log}[a + b x])}{4 (bc-ad)^3 (a + b x)^2} - \frac{c (1 + 3 \text{Log}[a + b x])}{9 (bc-ad)^2 (a + b x)^3} - \frac{a (1 + 4 \text{Log}[a + b x])}{16 b (-bc + ad) (a + b x)^4} + \right.$$

$$\begin{aligned}
 & \left. \frac{c d^3 \left( \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^5} \right) - \frac{1}{(bc-ad)^4} \\
 8 a b^3 c^3 d^2 p r & \left( -p r \text{Log}[a+bx] - r \left( -p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q] \right) - \right. \\
 & \text{Log}[f(a+bx)^p(c+dx)^q] \left( r - \frac{r \left( -q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q] \right)}{\text{Log}[f(a+bx)^p(c+dx)^q]} \right) + \\
 & \text{Log}\left[ e^{e^{r \left( -p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q] \right)}} (a+bx)^{p r} \right. \\
 & \left. \left. \left( f(a+bx)^p(c+dx)^q \right)^{r - \frac{r \left( -q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q] \right)}{\text{Log}[f(a+bx)^p(c+dx)^q]}} \right) \right] \\
 & \left( -\frac{c d^3 \text{Log}[a+bx]^2}{2(bc-ad)^5} - \frac{b c d^2 (1 + \text{Log}[a+bx])}{(bc-ad)^4 (a+b^2x)} + \frac{c d (1 + 2 \text{Log}[a+bx])}{4(bc-ad)^3 (a+bx)^2} - \right. \\
 & \frac{c (1 + 3 \text{Log}[a+bx])}{9(bc-ad)^2 (a+bx)^3} - \frac{a (1 + 4 \text{Log}[a+bx])}{16b(-bc+ad)(a+bx)^4} + \\
 & \left. \frac{c d^3 \left( \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^5} \right) + \frac{1}{(bc-ad)^4} 12 a^2 b^2 c^2 d^3 p r \\
 & \left( -p r \text{Log}[a+bx] - r \left( -p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q] \right) - \right. \\
 & \text{Log}[f(a+bx)^p(c+dx)^q] \left( r - \frac{r \left( -q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q] \right)}{\text{Log}[f(a+bx)^p(c+dx)^q]} \right) + \\
 & \text{Log}\left[ e^{e^{r \left( -p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q] \right)}} (a+bx)^{p r} \right. \\
 & \left. \left. \left( f(a+bx)^p(c+dx)^q \right)^{r - \frac{r \left( -q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q] \right)}{\text{Log}[f(a+bx)^p(c+dx)^q]}} \right) \right] \\
 & \left( -\frac{c d^3 \text{Log}[a+bx]^2}{2(bc-ad)^5} - \frac{b c d^2 (1 + \text{Log}[a+bx])}{(bc-ad)^4 (a+b^2x)} + \frac{c d (1 + 2 \text{Log}[a+bx])}{4(bc-ad)^3 (a+bx)^2} - \right. \\
 & \frac{c (1 + 3 \text{Log}[a+bx])}{9(bc-ad)^2 (a+bx)^3} - \frac{a (1 + 4 \text{Log}[a+bx])}{16b(-bc+ad)(a+bx)^4} + \\
 & \left. \frac{c d^3 \left( \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^5} \right) - \frac{1}{(bc-ad)^4} \\
 8 a^3 b c d^4 p r & \left( -p r \text{Log}[a+bx] - r \left( -p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q] \right) - \right. \\
 & \text{Log}[f(a+bx)^p(c+dx)^q] \left( r - \frac{r \left( -q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q] \right)}{\text{Log}[f(a+bx)^p(c+dx)^q]} \right) + \\
 & \text{Log}\left[ e^{e^{r \left( -p \text{Log}[a+bx] - q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q] \right)}} (a+bx)^{p r} \right. \\
 & \left. \left. \left( f(a+bx)^p(c+dx)^q \right)^{r - \frac{r \left( -q \text{Log}[c+dx] + \text{Log}[f(a+bx)^p(c+dx)^q] \right)}{\text{Log}[f(a+bx)^p(c+dx)^q]}} \right) \right]
 \end{aligned}$$

$$\left( -\frac{c d^3 \operatorname{Log}[a+b x]^2}{2 (b c-a d)^5} - \frac{b c d^2 (1+\operatorname{Log}[a+b x])}{(b c-a d)^4 (a b+b^2 x)} + \frac{c d (1+2 \operatorname{Log}[a+b x])}{4 (b c-a d)^3 (a+b x)^2} - \frac{c (1+3 \operatorname{Log}[a+b x])}{9 (b c-a d)^2 (a+b x)^3} - \frac{a (1+4 \operatorname{Log}[a+b x])}{16 b (-b c+a d) (a+b x)^4} + \frac{c d^3 \left( \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)}{(b c-a d)^5} \right) + \frac{1}{(b c-a d)^4}$$

$$2 a^4 d^5 p r \left( -p r \operatorname{Log}[a+b x] - r (-p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q]) - \operatorname{Log}[f (a+b x)^p (c+d x)^q] \left( r - \frac{r (-q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q])}{\operatorname{Log}[f (a+b x)^p (c+d x)^q]} \right) + \operatorname{Log}\left[ e^{e^{r (-p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q])}} (a+b x)^{p r} (f (a+b x)^p (c+d x)^q)^{r - \frac{r (-q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q])}{\operatorname{Log}[f (a+b x)^p (c+d x)^q]}} \right] \right)$$

$$\left( -\frac{c d^3 \operatorname{Log}[a+b x]^2}{2 (b c-a d)^5} - \frac{b c d^2 (1+\operatorname{Log}[a+b x])}{(b c-a d)^4 (a b+b^2 x)} + \frac{c d (1+2 \operatorname{Log}[a+b x])}{4 (b c-a d)^3 (a+b x)^2} - \frac{c (1+3 \operatorname{Log}[a+b x])}{9 (b c-a d)^2 (a+b x)^3} - \frac{a (1+4 \operatorname{Log}[a+b x])}{16 b (-b c+a d) (a+b x)^4} + \frac{c d^3 \left( \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)}{(b c-a d)^5} \right) + \frac{1}{2 (b c-a d)^4}$$

$$a b^3 c^4 d p q r^2 \left( \frac{d^4 \operatorname{Log}[a+b x]^2}{2 (b c-a d)^5} + \frac{b d^3 (1+\operatorname{Log}[a+b x])}{(b c-a d)^4 (a b+b^2 x)} - \frac{d^2 (1+2 \operatorname{Log}[a+b x])}{4 (b c-a d)^3 (a+b x)^2} + \frac{d (1+3 \operatorname{Log}[a+b x])}{9 (b c-a d)^2 (a+b x)^3} + \frac{1+4 \operatorname{Log}[a+b x]}{16 (-b c+a d) (a+b x)^4} - \frac{d^4 \left( \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)}{(b c-a d)^5} \right) -$$

$$\frac{1}{(b c-a d)^4} 2 a^2 b^2 c^3 d^2 p q r^2 \left( \frac{d^4 \operatorname{Log}[a+b x]^2}{2 (b c-a d)^5} + \frac{b d^3 (1+\operatorname{Log}[a+b x])}{(b c-a d)^4 (a b+b^2 x)} - \frac{d^2 (1+2 \operatorname{Log}[a+b x])}{4 (b c-a d)^3 (a+b x)^2} + \frac{d (1+3 \operatorname{Log}[a+b x])}{9 (b c-a d)^2 (a+b x)^3} + \frac{1+4 \operatorname{Log}[a+b x]}{16 (-b c+a d) (a+b x)^4} - \frac{d^4 \left( \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)}{(b c-a d)^5} \right) +$$

$$\frac{1}{(b c-a d)^4} 3 a^3 b c^2 d^3 p q r^2 \left( \frac{d^4 \operatorname{Log}[a+b x]^2}{2 (b c-a d)^5} + \frac{b d^3 (1+\operatorname{Log}[a+b x])}{(b c-a d)^4 (a b+b^2 x)} -$$

$$\begin{aligned}
 & \frac{d^2 (1 + 2 \operatorname{Log}[a + bx])}{4 (bc - ad)^3 (a + bx)^2} + \frac{d (1 + 3 \operatorname{Log}[a + bx])}{9 (bc - ad)^2 (a + bx)^3} + \frac{1 + 4 \operatorname{Log}[a + bx]}{16 (-bc + ad) (a + bx)^4} - \\
 & \left. \frac{d^4 \left( \operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc - ad)^5} \right) - \frac{1}{(bc - ad)^4} \\
 2 a^4 c d^4 p q r^2 & \left( \frac{d^4 \operatorname{Log}[a + bx]^2}{2 (bc - ad)^5} + \frac{b d^3 (1 + \operatorname{Log}[a + bx])}{(bc - ad)^4 (a + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a + bx])}{4 (bc - ad)^3 (a + bx)^2} + \right. \\
 & \frac{d (1 + 3 \operatorname{Log}[a + bx])}{9 (bc - ad)^2 (a + bx)^3} + \frac{1 + 4 \operatorname{Log}[a + bx]}{16 (-bc + ad) (a + bx)^4} - \\
 & \left. \frac{d^4 \left( \operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc - ad)^5} \right) + \frac{1}{2 b (bc - ad)^4} \\
 a^5 d^5 p q r^2 & \left( \frac{d^4 \operatorname{Log}[a + bx]^2}{2 (bc - ad)^5} + \frac{b d^3 (1 + \operatorname{Log}[a + bx])}{(bc - ad)^4 (a + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a + bx])}{4 (bc - ad)^3 (a + bx)^2} + \right. \\
 & \frac{d (1 + 3 \operatorname{Log}[a + bx])}{9 (bc - ad)^2 (a + bx)^3} + \frac{1 + 4 \operatorname{Log}[a + bx]}{16 (-bc + ad) (a + bx)^4} - \\
 & \left. \frac{d^4 \left( \operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc - ad)^5} \right) + \frac{1}{2 b (bc - ad)^4} \\
 a^5 d^5 q^2 r^2 & \left( \frac{d^4 \operatorname{Log}[a + bx]^2}{2 (bc - ad)^5} + \frac{b d^3 (1 + \operatorname{Log}[a + bx])}{(bc - ad)^4 (a + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a + bx])}{4 (bc - ad)^3 (a + bx)^2} + \right. \\
 & \frac{d (1 + 3 \operatorname{Log}[a + bx])}{9 (bc - ad)^2 (a + bx)^3} + \frac{1 + 4 \operatorname{Log}[a + bx]}{16 (-bc + ad) (a + bx)^4} - \\
 & \left. \frac{d^4 \left( \operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc - ad)^5} \right) + \frac{1}{(bc - ad)^4} \\
 2 b^4 c^5 p r^2 & (-p \operatorname{Log}[a + bx] - q \operatorname{Log}[c + dx] + \operatorname{Log}[f(a + bx)^p (c + dx)^q]) \\
 & \left( \frac{d^4 \operatorname{Log}[a + bx]^2}{2 (bc - ad)^5} + \frac{b d^3 (1 + \operatorname{Log}[a + bx])}{(bc - ad)^4 (a + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a + bx])}{4 (bc - ad)^3 (a + bx)^2} + \frac{d (1 + 3 \operatorname{Log}[a + bx])}{9 (bc - ad)^2 (a + bx)^3} + \right. \\
 & \left. \frac{1 + 4 \operatorname{Log}[a + bx]}{16 (-bc + ad) (a + bx)^4} - \frac{d^4 \left( \operatorname{Log}[a + bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc - ad)^5} \right) - \\
 & \frac{1}{(bc - ad)^4} 8 a b^3 c^4 d p r^2 (-p \operatorname{Log}[a + bx] - q \operatorname{Log}[c + dx] + \operatorname{Log}[f(a + bx)^p (c + dx)^q]) \\
 & \left( \frac{d^4 \operatorname{Log}[a + bx]^2}{2 (bc - ad)^5} + \frac{b d^3 (1 + \operatorname{Log}[a + bx])}{(bc - ad)^4 (a + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a + bx])}{4 (bc - ad)^3 (a + bx)^2} + \frac{d (1 + 3 \operatorname{Log}[a + bx])}{9 (bc - ad)^2 (a + bx)^3} + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{1 + 4 \operatorname{Log}[a + b x]}{16 (-b c + a d) (a + b x)^4} - \frac{d^4 \left( \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^5} \right) + \\
 & \frac{1}{(b c - a d)^4} 12 a^2 b^2 c^3 d^2 p r^2 \left( -p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right] \right) \\
 & \left( \frac{d^4 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} + \frac{b d^3 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} + \frac{d (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} + \right. \\
 & \left. \frac{1 + 4 \operatorname{Log}[a + b x]}{16 (-b c + a d) (a + b x)^4} - \frac{d^4 \left( \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^5} \right) - \\
 & \frac{1}{(b c - a d)^4} 8 a^3 b c^2 d^3 p r^2 \left( -p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right] \right) \\
 & \left( \frac{d^4 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} + \frac{b d^3 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} + \frac{d (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} + \right. \\
 & \left. \frac{1 + 4 \operatorname{Log}[a + b x]}{16 (-b c + a d) (a + b x)^4} - \frac{d^4 \left( \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^5} \right) + \\
 & \frac{1}{(b c - a d)^4} 2 a^4 c d^4 p r^2 \left( -p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right] \right) \\
 & \left( \frac{d^4 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} + \frac{b d^3 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} + \frac{d (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} + \right. \\
 & \left. \frac{1 + 4 \operatorname{Log}[a + b x]}{16 (-b c + a d) (a + b x)^4} - \frac{d^4 \left( \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^5} \right) + \frac{1}{(b c - a d)^4} \\
 & 2 b^4 c^5 p r \left( -p r \operatorname{Log}[a + b x] - r \left( -p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right] \right) - \right. \\
 & \left. \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right] \left( r - \frac{r \left( -q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]\right)}{\operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]} \right) + \right. \\
 & \left. \operatorname{Log}\left[e^{r \left( -p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]\right)} (a + b x)^{p r} \right. \right. \\
 & \left. \left. (f (a + b x)^p (c + d x)^q)^{r - \frac{r \left( -q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]\right)}{\operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]}} \right) \right) \\
 & \left( \frac{d^4 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} + \frac{b d^3 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} + \right. \\
 & \frac{d (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} + \frac{1 + 4 \operatorname{Log}[a + b x]}{16 (-b c + a d) (a + b x)^4} - \\
 & \left. \frac{d^4 \left( \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)}{(b c - a d)^5} \right) - \frac{1}{(b c - a d)^4}
 \end{aligned}$$



$$\begin{aligned}
 & 8 a b^3 c^4 d p r \left( -p r \operatorname{Log}[a+b x] - r \left( -p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right] \right) - \right. \\
 & \quad \left. \operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right] \left( r - \frac{r \left( -q \operatorname{Log}[c+d x] + \operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right] \right)}{\operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right]} \right) + \right. \\
 & \quad \left. \operatorname{Log}\left[ e^{e^{r \left( -p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right] \right)}} (a+b x)^{p r} \right. \right. \\
 & \quad \left. \left. \left( f (a+b x)^p (c+d x)^q \right)^{r - \frac{r \left( -q \operatorname{Log}[c+d x] + \operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right] \right)}{\operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right]}} \right] \right) \\
 & \left( \frac{d^4 \operatorname{Log}[a+b x]^2}{2 (b c - a d)^5} + \frac{b d^3 (1 + \operatorname{Log}[a+b x])}{(b c - a d)^4 (a b + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a+b x])}{4 (b c - a d)^3 (a+b x)^2} + \frac{d (1 + 3 \operatorname{Log}[a+b x])}{9 (b c - a d)^2 (a+b x)^3} + \right. \\
 & \quad \left. \frac{1 + 4 \operatorname{Log}[a+b x]}{16 (-b c + a d) (a+b x)^4} - \frac{d^4 \left( \operatorname{Log}[a+b x] \operatorname{Log}\left[ \frac{b(c+d x)}{b c - a d} \right] + \operatorname{PolyLog}\left[ 2, \frac{d(a+b x)}{-b c + a d} \right] \right)}{(b c - a d)^5} \right) + \\
 & \frac{1}{(b c - a d)^4} 12 a^2 b^2 c^3 d^2 p r \left( -p r \operatorname{Log}[a+b x] - \right. \\
 & \quad r \left( -p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right] \right) - \\
 & \quad \operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right] \left( r - \frac{r \left( -q \operatorname{Log}[c+d x] + \operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right] \right)}{\operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right]} \right) + \\
 & \quad \operatorname{Log}\left[ e^{e^{r \left( -p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right] \right)}} (a+b x)^{p r} \right. \\
 & \quad \left. \left. \left( f (a+b x)^p (c+d x)^q \right)^{r - \frac{r \left( -q \operatorname{Log}[c+d x] + \operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right] \right)}{\operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right]}} \right] \right) \\
 & \left( \frac{d^4 \operatorname{Log}[a+b x]^2}{2 (b c - a d)^5} + \frac{b d^3 (1 + \operatorname{Log}[a+b x])}{(b c - a d)^4 (a b + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a+b x])}{4 (b c - a d)^3 (a+b x)^2} + \right. \\
 & \quad \frac{d (1 + 3 \operatorname{Log}[a+b x])}{9 (b c - a d)^2 (a+b x)^3} + \frac{1 + 4 \operatorname{Log}[a+b x]}{16 (-b c + a d) (a+b x)^4} - \\
 & \quad \left. \frac{d^4 \left( \operatorname{Log}[a+b x] \operatorname{Log}\left[ \frac{b(c+d x)}{b c - a d} \right] + \operatorname{PolyLog}\left[ 2, \frac{d(a+b x)}{-b c + a d} \right] \right)}{(b c - a d)^5} \right) - \frac{1}{(b c - a d)^4} \\
 & 8 a^3 b c^2 d^3 p r \left( -p r \operatorname{Log}[a+b x] - r \left( -p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right] \right) - \right. \\
 & \quad \operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right] \left( r - \frac{r \left( -q \operatorname{Log}[c+d x] + \operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right] \right)}{\operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right]} \right) + \\
 & \quad \operatorname{Log}\left[ e^{e^{r \left( -p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right] \right)}} (a+b x)^{p r} \right. \\
 & \quad \left. \left. \left( f (a+b x)^p (c+d x)^q \right)^{r - \frac{r \left( -q \operatorname{Log}[c+d x] + \operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right] \right)}{\operatorname{Log}\left[ f (a+b x)^p (c+d x)^q \right]}} \right] \right) \\
 & \left( \frac{d^4 \operatorname{Log}[a+b x]^2}{2 (b c - a d)^5} + \frac{b d^3 (1 + \operatorname{Log}[a+b x])}{(b c - a d)^4 (a b + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a+b x])}{4 (b c - a d)^3 (a+b x)^2} + \right.
 \end{aligned}$$

$$\frac{d (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} + \frac{1 + 4 \operatorname{Log}[a + b x]}{16 (-b c + a d) (a + b x)^4} - \frac{d^4 \left( \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^5} \Bigg) + \frac{1}{(bc-ad)^4} 2 a^4 c d^4 p r \left( -p r \operatorname{Log}[a + b x] - r \left( -p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right] \right) - \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right] \left( r - \frac{r \left( -q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]\right)}{\operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]} \right) + \operatorname{Log}\left[e e^{r \left( -p \operatorname{Log}[a + b x] - q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]\right)} (a + b x)^{p r} (f (a + b x)^p (c + d x)^q)^{r - \frac{r \left( -q \operatorname{Log}[c + d x] + \operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]\right)}{\operatorname{Log}\left[f (a + b x)^p (c + d x)^q\right]}} \right] \left( \frac{d^4 \operatorname{Log}[a + b x]^2}{2 (b c - a d)^5} + \frac{b d^3 (1 + \operatorname{Log}[a + b x])}{(b c - a d)^4 (a b + b^2 x)} - \frac{d^2 (1 + 2 \operatorname{Log}[a + b x])}{4 (b c - a d)^3 (a + b x)^2} + \frac{d (1 + 3 \operatorname{Log}[a + b x])}{9 (b c - a d)^2 (a + b x)^3} + \frac{1 + 4 \operatorname{Log}[a + b x]}{16 (-b c + a d) (a + b x)^4} - \frac{d^4 \left( \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{(bc-ad)^5} \right)$$

**Problem 40: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Log}\left[e \left(f (a + b x)^p (c + d x)^q\right)^r\right]^2}{(g + h x)^2} dx$$

Optimal (type 4, 832 leaves, 31 steps):

$$\begin{aligned} & \frac{2bpqr^2 \operatorname{Log}\left[-\frac{d(a+bx)}{bc-ad}\right] \operatorname{Log}[c+dx]}{h(bg-ah)} + \frac{2dpqr^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{h(dg-ch)} - \frac{1}{h(bg-ah)} 2bpr \\ & \operatorname{Log}[a+bx] \left( pr \operatorname{Log}[a+bx] + qr \operatorname{Log}[c+dx] - \operatorname{Log}\left[e(f(a+bx)^p(c+dx)^q)^r\right] \right) - \frac{1}{h(dg-ch)} \\ & \frac{2dqr \operatorname{Log}[c+dx] \left( pr \operatorname{Log}[a+bx] + qr \operatorname{Log}[c+dx] - \operatorname{Log}\left[e(f(a+bx)^p(c+dx)^q)^r\right] \right) -}{\operatorname{Log}\left[e(f(a+bx)^p(c+dx)^q)^r\right]^2} + \frac{1}{h(bg-ah)} 2bpr \\ & \left( pr \operatorname{Log}[a+bx] + qr \operatorname{Log}[c+dx] - \operatorname{Log}\left[e(f(a+bx)^p(c+dx)^q)^r\right] \right) \operatorname{Log}[g+hx] + \frac{1}{h(dg-ch)} \\ & \frac{2dqr \left( pr \operatorname{Log}[a+bx] + qr \operatorname{Log}[c+dx] - \operatorname{Log}\left[e(f(a+bx)^p(c+dx)^q)^r\right] \right) \operatorname{Log}[g+hx] -}{2dpqr^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right]} - \frac{2bpqr^2 \operatorname{Log}[c+dx] \operatorname{Log}\left[\frac{d(g+hx)}{dg-ch}\right]}{h(bg-ah)} \\ & \frac{2bp^2r^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[1 + \frac{bg-ah}{h(a+bx)}\right]}{h(bg-ah)} - \frac{2dq^2r^2 \operatorname{Log}[c+dx] \operatorname{Log}\left[1 + \frac{dg-ch}{h(c+dx)}\right]}{h(dg-ch)} + \\ & \frac{2bp^2r^2 \operatorname{PolyLog}\left[2, -\frac{bg-ah}{h(a+bx)}\right]}{h(bg-ah)} + \frac{2dpqr^2 \operatorname{PolyLog}\left[2, -\frac{d(a+bx)}{bc-ad}\right]}{h(dg-ch)} - \frac{2dpqr^2 \operatorname{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right]}{h(dg-ch)} + \\ & \frac{2dq^2r^2 \operatorname{PolyLog}\left[2, -\frac{dg-ch}{h(c+dx)}\right]}{h(dg-ch)} + \frac{2bpqr^2 \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{h(bg-ah)} - \frac{2bpqr^2 \operatorname{PolyLog}\left[2, -\frac{h(c+dx)}{dg-ch}\right]}{h(bg-ah)} \end{aligned}$$

Result (type 4, 2930 leaves):

$$\begin{aligned} & \frac{1}{h(-bg+ah)(-dg+ch)(g+hx)} \\ & \left( -bdg^2p^2r^2 \operatorname{Log}[a+bx]^2 + bcghp^2r^2 \operatorname{Log}[a+bx]^2 - bdghp^2r^2x \operatorname{Log}[a+bx]^2 + \right. \\ & \quad bc h^2 p^2 r^2 x \operatorname{Log}[a+bx]^2 - 2bdg^2pqr^2 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] + \\ & \quad 2adghpqr^2 \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] - 2bdghpqr^2x \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] + \\ & \quad 2adh^2pqr^2x \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] - bdg^2q^2r^2 \operatorname{Log}[c+dx]^2 + \\ & \quad adghq^2r^2 \operatorname{Log}[c+dx]^2 - bdghq^2r^2x \operatorname{Log}[c+dx]^2 + adh^2q^2r^2x \operatorname{Log}[c+dx]^2 + \\ & \quad 2bcghpqr^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] - 2adghpqr^2 \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] + \\ & \quad 2bch^2pqr^2x \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] - 2adh^2pqr^2x \operatorname{Log}[a+bx] \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] - \\ & \quad bcghpqr^2 \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right]^2 + adghpqr^2 \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right]^2 - bch^2pqr^2x \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right]^2 + \\ & \quad adh^2pqr^2x \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right]^2 + 2bcghpqr^2 \operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right] - \\ & \quad \left. 2adghpqr^2 \operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \operatorname{Log}\left[\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}\right] \right) + \end{aligned}$$

$$\begin{aligned}
 & 2 b c h^2 p q r^2 x \operatorname{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] \operatorname{Log}\left[\frac{(b g-a h)(c+d x)}{(d g-c h)(a+b x)}\right] - \\
 & 2 a d h^2 p q r^2 x \operatorname{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] \operatorname{Log}\left[\frac{(b g-a h)(c+d x)}{(d g-c h)(a+b x)}\right] + \\
 & 2 b c g h p q r^2 \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{(b g-a h)(c+d x)}{(d g-c h)(a+b x)}\right] - \\
 & 2 a d g h p q r^2 \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{(b g-a h)(c+d x)}{(d g-c h)(a+b x)}\right] + \\
 & 2 b c h^2 p q r^2 x \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{(b g-a h)(c+d x)}{(d g-c h)(a+b x)}\right] - \\
 & 2 a d h^2 p q r^2 x \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{(b g-a h)(c+d x)}{(d g-c h)(a+b x)}\right] - \\
 & b c g h p q r^2 \operatorname{Log}\left[\frac{(b g-a h)(c+d x)}{(d g-c h)(a+b x)}\right]^2 + a d g h p q r^2 \operatorname{Log}\left[\frac{(b g-a h)(c+d x)}{(d g-c h)(a+b x)}\right]^2 - \\
 & b c h^2 p q r^2 x \operatorname{Log}\left[\frac{(b g-a h)(c+d x)}{(d g-c h)(a+b x)}\right]^2 + a d h^2 p q r^2 x \operatorname{Log}\left[\frac{(b g-a h)(c+d x)}{(d g-c h)(a+b x)}\right]^2 + \\
 & 2 b d g^2 p r \operatorname{Log}[a+b x] \operatorname{Log}\left[e(f(a+b x)^p(c+d x)^q)^r\right] - \\
 & 2 b c g h p r \operatorname{Log}[a+b x] \operatorname{Log}\left[e(f(a+b x)^p(c+d x)^q)^r\right] + \\
 & 2 b d g h p r x \operatorname{Log}[a+b x] \operatorname{Log}\left[e(f(a+b x)^p(c+d x)^q)^r\right] - \\
 & 2 b c h^2 p r x \operatorname{Log}[a+b x] \operatorname{Log}\left[e(f(a+b x)^p(c+d x)^q)^r\right] + \\
 & 2 b d g^2 q r \operatorname{Log}[c+d x] \operatorname{Log}\left[e(f(a+b x)^p(c+d x)^q)^r\right] - \\
 & 2 a d g h q r \operatorname{Log}[c+d x] \operatorname{Log}\left[e(f(a+b x)^p(c+d x)^q)^r\right] + \\
 & 2 b d g h q r x \operatorname{Log}[c+d x] \operatorname{Log}\left[e(f(a+b x)^p(c+d x)^q)^r\right] - \\
 & 2 a d h^2 q r x \operatorname{Log}[c+d x] \operatorname{Log}\left[e(f(a+b x)^p(c+d x)^q)^r\right] - \\
 & b d g^2 \operatorname{Log}\left[e(f(a+b x)^p(c+d x)^q)^r\right]^2 + b c g h \operatorname{Log}\left[e(f(a+b x)^p(c+d x)^q)^r\right]^2 + \\
 & a d g h \operatorname{Log}\left[e(f(a+b x)^p(c+d x)^q)^r\right]^2 - a c h^2 \operatorname{Log}\left[e(f(a+b x)^p(c+d x)^q)^r\right]^2 - \\
 & 2 b d g^2 p q r^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + 2 a d g h p q r^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] - \\
 & 2 b d g h p q r^2 x \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + 2 a d h^2 p q r^2 x \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + \\
 & 2 b d g^2 p q r^2 \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] - \\
 & 2 b c g h p q r^2 \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + 2 b d g h p q r^2 x \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \\
 & \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] - 2 b c h^2 p q r^2 x \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] - \\
 & 2 b d g^2 p r \operatorname{Log}\left[e(f(a+b x)^p(c+d x)^q)^r\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + \\
 & 2 b c g h p r \operatorname{Log}\left[e(f(a+b x)^p(c+d x)^q)^r\right] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] -
 \end{aligned}$$

$$\begin{aligned}
 & 2 b d g h p r x \operatorname{Log}\left[e (f (a+b x)^p (c+d x)^q)^r\right] \operatorname{Log}\left[\frac{b (g+h x)}{b g-a h}\right] + \\
 & 2 b c h^2 p r x \operatorname{Log}\left[e (f (a+b x)^p (c+d x)^q)^r\right] \operatorname{Log}\left[\frac{b (g+h x)}{b g-a h}\right] + \\
 & 2 b d g^2 p q r^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d (g+h x)}{d g-c h}\right] - 2 a d g h p q r^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d (g+h x)}{d g-c h}\right] + \\
 & 2 b d g h p q r^2 x \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d (g+h x)}{d g-c h}\right] - 2 a d h^2 p q r^2 x \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{d (g+h x)}{d g-c h}\right] - \\
 & 2 b d g^2 p q r^2 \operatorname{Log}\left[\frac{h (c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{d (g+h x)}{d g-c h}\right] + \\
 & 2 b c g h p q r^2 \operatorname{Log}\left[\frac{h (c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{d (g+h x)}{d g-c h}\right] - 2 b d g h p q r^2 x \operatorname{Log}\left[\frac{h (c+d x)}{-d g+c h}\right] \\
 & \operatorname{Log}\left[\frac{d (g+h x)}{d g-c h}\right] + 2 b c h^2 p q r^2 x \operatorname{Log}\left[\frac{h (c+d x)}{-d g+c h}\right] \operatorname{Log}\left[\frac{d (g+h x)}{d g-c h}\right] - \\
 & 2 b d g^2 q r \operatorname{Log}\left[e (f (a+b x)^p (c+d x)^q)^r\right] \operatorname{Log}\left[\frac{d (g+h x)}{d g-c h}\right] + \\
 & 2 a d g h q r \operatorname{Log}\left[e (f (a+b x)^p (c+d x)^q)^r\right] \operatorname{Log}\left[\frac{d (g+h x)}{d g-c h}\right] - \\
 & 2 b d g h q r x \operatorname{Log}\left[e (f (a+b x)^p (c+d x)^q)^r\right] \operatorname{Log}\left[\frac{d (g+h x)}{d g-c h}\right] + \\
 & 2 a d h^2 q r x \operatorname{Log}\left[e (f (a+b x)^p (c+d x)^q)^r\right] \operatorname{Log}\left[\frac{d (g+h x)}{d g-c h}\right] + \\
 & 2 p (b c h p+a d h q-b d g (p+q)) r^2 (g+h x) \operatorname{PolyLog}\left[2, \frac{h (a+b x)}{-b g+a h}\right] + \\
 & 2 q (b c h p+a d h q-b d g (p+q)) r^2 (g+h x) \operatorname{PolyLog}\left[2, \frac{h (c+d x)}{-d g+c h}\right] + \\
 & 2 b c g h p q r^2 \operatorname{PolyLog}\left[2, \frac{b (c+d x)}{d (a+b x)}\right] - 2 a d g h p q r^2 \operatorname{PolyLog}\left[2, \frac{b (c+d x)}{d (a+b x)}\right] + \\
 & 2 b c h^2 p q r^2 x \operatorname{PolyLog}\left[2, \frac{b (c+d x)}{d (a+b x)}\right] - 2 a d h^2 p q r^2 x \operatorname{PolyLog}\left[2, \frac{b (c+d x)}{d (a+b x)}\right]
 \end{aligned}$$

**Problem 41: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Log}\left[e (f (a+b x)^p (c+d x)^q)^r\right]^2}{(g+h x)^3} dx$$

Optimal (type 4, 1304 leaves, 43 steps):

$$\begin{aligned}
 & - \frac{b d p q r^2 \operatorname{Log}[a+b x]}{h(b g-a h)(d g-c h)} + \frac{d p q r^2 \operatorname{Log}[a+b x]}{h(d g-c h)(g+h x)} - \frac{b p^2 r^2(a+b x) \operatorname{Log}[a+b x]}{(b g-a h)^2(g+h x)} - \\
 & \frac{b d p q r^2 \operatorname{Log}[c+d x]}{h(b g-a h)(d g-c h)} + \frac{b p q r^2 \operatorname{Log}[c+d x]}{h(b g-a h)(g+h x)} - \frac{d q^2 r^2(c+d x) \operatorname{Log}[c+d x]}{(d g-c h)^2(g+h x)} + \\
 & \frac{b^2 p q r^2 \operatorname{Log}\left[-\frac{d(a+b x)}{b c-a d}\right] \operatorname{Log}[c+d x]}{h(b g-a h)^2} + \frac{d^2 p q r^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]}{h(d g-c h)^2} - \\
 & \left( \frac{b p r(p r \operatorname{Log}[a+b x] + q r \operatorname{Log}[c+d x] - \operatorname{Log}[e(f(a+b x)^p(c+d x)^q)^r])}{(h(b g-a h)(g+h x))} - \right. \\
 & \left. \frac{d q r(p r \operatorname{Log}[a+b x] + q r \operatorname{Log}[c+d x] - \operatorname{Log}[e(f(a+b x)^p(c+d x)^q)^r])}{(h(d g-c h)(g+h x))} - \frac{1}{h(b g-a h)^2} b^2 p r \operatorname{Log}[a+b x] \right) \\
 & \left( p r \operatorname{Log}[a+b x] + q r \operatorname{Log}[c+d x] - \operatorname{Log}[e(f(a+b x)^p(c+d x)^q)^r] \right) - \frac{1}{h(d g-c h)^2} \\
 & \frac{d^2 q r \operatorname{Log}[c+d x] (p r \operatorname{Log}[a+b x] + q r \operatorname{Log}[c+d x] - \operatorname{Log}[e(f(a+b x)^p(c+d x)^q)^r]) - \operatorname{Log}[e(f(a+b x)^p(c+d x)^q)^r]^2}{2 h(g+h x)^2} + \frac{b^2 p^2 r^2 \operatorname{Log}[g+h x]}{h(b g-a h)^2} + \\
 & \frac{2 b d p q r^2 \operatorname{Log}[g+h x]}{h(b g-a h)(d g-c h)} + \frac{d^2 q^2 r^2 \operatorname{Log}[g+h x]}{h(d g-c h)^2} + \frac{1}{h(b g-a h)^2} \\
 & \frac{b^2 p r(p r \operatorname{Log}[a+b x] + q r \operatorname{Log}[c+d x] - \operatorname{Log}[e(f(a+b x)^p(c+d x)^q)^r]) \operatorname{Log}[g+h x] + \frac{1}{h(d g-c h)^2} d^2 q r(p r \operatorname{Log}[a+b x] + q r \operatorname{Log}[c+d x] - \operatorname{Log}[e(f(a+b x)^p(c+d x)^q)^r])}{h(d g-c h)^2} \\
 & \operatorname{Log}[g+h x] - \frac{d^2 p q r^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right]}{h(d g-c h)^2} - \frac{b^2 p q r^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[\frac{d(g+h x)}{d g-c h}\right]}{h(b g-a h)^2} - \\
 & \frac{b^2 p^2 r^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[1 + \frac{b g-a h}{h(a+b x)}\right]}{h(b g-a h)^2} - \frac{d^2 q^2 r^2 \operatorname{Log}[c+d x] \operatorname{Log}\left[1 + \frac{d g-c h}{h(c+d x)}\right]}{h(d g-c h)^2} + \\
 & \frac{b^2 p^2 r^2 \operatorname{PolyLog}\left[2, -\frac{b g-a h}{h(a+b x)}\right]}{h(b g-a h)^2} + \frac{d^2 p q r^2 \operatorname{PolyLog}\left[2, -\frac{d(a+b x)}{b c-a d}\right]}{h(d g-c h)^2} - \frac{d^2 p q r^2 \operatorname{PolyLog}\left[2, -\frac{h(a+b x)}{b g-a h}\right]}{h(d g-c h)^2} + \\
 & \frac{d^2 q^2 r^2 \operatorname{PolyLog}\left[2, -\frac{d g-c h}{h(c+d x)}\right]}{h(d g-c h)^2} + \frac{b^2 p q r^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]}{h(b g-a h)^2} - \frac{b^2 p q r^2 \operatorname{PolyLog}\left[2, -\frac{h(c+d x)}{d g-c h}\right]}{h(b g-a h)^2}
 \end{aligned}$$

Result (type 4, 15976 leaves):

$$\begin{aligned}
 & - \frac{1}{2 h(g+h x)^2} \left( -p r \operatorname{Log}[a+b x] - \right. \\
 & \left. \operatorname{Log}[f(a+b x)^p(c+d x)^q] \left( r - \frac{r(-q \operatorname{Log}[c+d x] + \operatorname{Log}[f(a+b x)^p(c+d x)^q])}{\operatorname{Log}[f(a+b x)^p(c+d x)^q]} \right) \right) + \\
 & \operatorname{Log}\left[ e^{e^{r(-p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}[f(a+b x)^p(c+d x)^q])}} (a+b x)^{p r} \right]
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( (f (a+b x))^p (c+d x)^q \right)^{r - \frac{r(-q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q])}{\operatorname{Log}[f (a+b x)^p (c+d x)^q]}} \right)^2 + \\
 & \frac{1}{h} p r \left( -p r \operatorname{Log}[a+b x] - \operatorname{Log}[f (a+b x)^p (c+d x)^q] \right. \\
 & \left. \left( r - \frac{r(-q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q])}{\operatorname{Log}[f (a+b x)^p (c+d x)^q]} \right) \right. \\
 & \left. \operatorname{Log}\left[ e^{e^{r(-p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q])}} (a+b x)^{p r} \right. \right. \\
 & \left. \left. (f (a+b x))^p (c+d x)^q \right)^{r - \frac{r(-q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q])}{\operatorname{Log}[f (a+b x)^p (c+d x)^q]}} \right] \\
 & \left( \frac{b^2 h (a+b x)}{(-b g + a h)^3 \left(1 - \frac{h(a+b x)}{-b g + a h}\right)} - \left( \frac{b^2 h^2 (a+b x)^2}{(-b g + a h)^4 \left(1 - \frac{h(a+b x)}{-b g + a h}\right)^2} + \frac{2 b^2 h (a+b x)}{(-b g + a h)^3 \left(1 - \frac{h(a+b x)}{-b g + a h}\right)} \right) \right. \\
 & \left. \operatorname{Log}[a+b x] - \frac{b^2 \operatorname{Log}\left[1 - \frac{h(a+b x)}{-b g + a h}\right]}{(-b g + a h)^2} \right) + \frac{1}{h} \\
 & q r^2 (-p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q]) \\
 & \left( \frac{d^2 h (c+d x)}{(-d g + c h)^3 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)} - \right. \\
 & \left. \left( \frac{d^2 h^2 (c+d x)^2}{(-d g + c h)^4 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)^2} + \frac{2 d^2 h (c+d x)}{(-d g + c h)^3 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)} \right) \operatorname{Log}[c+d x] - \frac{d^2 \operatorname{Log}\left[1 - \frac{h(c+d x)}{-d g + c h}\right]}{(-d g + c h)^2} \right) + \\
 & \frac{1}{h} q r \left( -p r \operatorname{Log}[a+b x] - r (-p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q]) - \right. \\
 & \left. \operatorname{Log}[f (a+b x)^p (c+d x)^q] \left( r - \frac{r(-q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q])}{\operatorname{Log}[f (a+b x)^p (c+d x)^q]} \right) \right. \\
 & \left. \operatorname{Log}\left[ e^{e^{r(-p \operatorname{Log}[a+b x] - q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q])}} (a+b x)^{p r} (f (a+b x))^p (c+d x)^q \right)^{r - \frac{r(-q \operatorname{Log}[c+d x] + \operatorname{Log}[f (a+b x)^p (c+d x)^q])}{\operatorname{Log}[f (a+b x)^p (c+d x)^q]}} \right] \\
 & \left( \frac{d^2 h (c+d x)}{(-d g + c h)^3 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)} - \left( \frac{d^2 h^2 (c+d x)^2}{(-d g + c h)^4 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)^2} + \frac{2 d^2 h (c+d x)}{(-d g + c h)^3 \left(1 - \frac{h(c+d x)}{-d g + c h}\right)} \right) \right. \\
 & \left. \operatorname{Log}[c+d x] - \frac{d^2 \operatorname{Log}\left[1 - \frac{h(c+d x)}{-d g + c h}\right]}{(-d g + c h)^2} \right) + \frac{1}{h} \\
 & p^2 r^2 \left( -\frac{1}{2} \left( \frac{b^2 h^2 (a+b x)^2}{(-b g + a h)^4 \left(1 - \frac{h(a+b x)}{-b g + a h}\right)^2} + \frac{2 b^2 h (a+b x)}{(-b g + a h)^3 \left(1 - \frac{h(a+b x)}{-b g + a h}\right)} \right) \operatorname{Log}[a+b x]^2 + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{b^2 \operatorname{Log}\left[1 - \frac{h(a+bx)}{-bg+ah}\right]}{(-bg+ah)^2} + \operatorname{Log}[a+bx] \left( \frac{b^2 h(a+bx)}{(-bg+ah)^3 \left(1 - \frac{h(a+bx)}{-bg+ah}\right)} - \frac{b^2 \operatorname{Log}\left[1 - \frac{h(a+bx)}{-bg+ah}\right]}{(-bg+ah)^2} \right) - \\
 & \left. \frac{b^2 \operatorname{PolyLog}\left[2, \frac{h(a+bx)}{-bg+ah}\right]}{(-bg+ah)^2} \right) + \frac{1}{h} \\
 q^2 r^2 & \left( -\frac{1}{2} \left( \frac{d^2 h^2 (c+dx)^2}{(-dg+ch)^4 \left(1 - \frac{h(c+dx)}{-dg+ch}\right)^2} + \frac{2 d^2 h (c+dx)}{(-dg+ch)^3 \left(1 - \frac{h(c+dx)}{-dg+ch}\right)} \right) \operatorname{Log}[c+dx]^2 + \right. \\
 & \frac{d^2 \operatorname{Log}\left[1 - \frac{h(c+dx)}{-dg+ch}\right]}{(-dg+ch)^2} + \operatorname{Log}[c+dx] \left( \frac{d^2 h (c+dx)}{(-dg+ch)^3 \left(1 - \frac{h(c+dx)}{-dg+ch}\right)} - \frac{d^2 \operatorname{Log}\left[1 - \frac{h(c+dx)}{-dg+ch}\right]}{(-dg+ch)^2} \right) - \\
 & \left. \frac{d^2 \operatorname{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right]}{(-dg+ch)^2} \right) + \\
 \frac{1}{g^2} p q r^2 & \left( \frac{1}{h} 2 \left( \operatorname{Log}[a+bx] \operatorname{Log}[c+dx] \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \frac{1}{2} \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \right) \right. \\
 & \left( -2 \operatorname{Log}[a+bx] + \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \right) \left( \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \operatorname{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) + \\
 & \operatorname{Log}\left[\frac{h(c+dx)}{-dg+ch}\right] \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left( -\operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \operatorname{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) \Big) + \\
 & \frac{1}{2} \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]^2 \left( \operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] + \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \right. \\
 & \left. \operatorname{Log}\left[-\frac{(-bc+ad)(g+hx)}{(-dg+ch)(a+bx)}\right] \right) + \left( \operatorname{Log}[c+dx] - \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \\
 & \operatorname{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right] + \left( \operatorname{Log}[a+bx] + \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \\
 & \operatorname{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right] + \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left( \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] - \right. \\
 & \left. \operatorname{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) - \operatorname{PolyLog}\left[3, -\frac{h(a+bx)}{bg-ah}\right] - \operatorname{PolyLog}\left[3, \right. \\
 & \left. \frac{h(c+dx)}{-dg+ch}\right] - \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right] + \operatorname{PolyLog}\left[3, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \Big) + \\
 h^2 & \left( \frac{1}{h} \left( \left( \frac{(bg-ah) \left( \frac{2abx}{(bg-ah)^2} + \frac{2a^2b(g+hx)}{(bg-ah)^3} \right)}{b(g+hx)} - \frac{(bg-ah)x \left( \frac{bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)^2} \right) \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \frac{a \left( \frac{-bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} \left( \text{Log}[a+bx] \text{Log}[c+dx] - \left( 2(-dg+ch)(a+bx) \right. \right. \\
 & \left. \left. \left( \frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \left( \frac{(bg-ah) \left( \frac{-bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} \right. \right. \right. \\
 & \left. \left. \left( (-dg+ch)(a+bx) \left( -\frac{(-bc+ad)x}{(-dg+ch)(a+bx)} + \frac{c(-bc+ad)(g+hx)}{(-dg+ch)^2(a+bx)} \right) \right) \right) / \right. \\
 & \left. \left( (-bc+ad)(g+hx) \right) \right) \text{Log} \left[ -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right] / \left( (bg-ah)(c+dx) \right) + \\
 & \left( -\frac{(bg-ah) \left( \frac{2abx}{(bg-ah)^2} + \frac{2a^2b(g+hx)}{(bg-ah)^3} \right)}{b(g+hx)} + \frac{(bg-ah)x \left( \frac{-bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)^2} + \right. \\
 & \left. \frac{a \left( \frac{-bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} - \frac{(-dg+ch) \left( \frac{-2cdx}{(-dg+ch)^2} - \frac{2c^2d(g+hx)}{(-dg+ch)^3} \right)}{d(g+hx)} + \right. \\
 & \left. \frac{(-dg+ch)x \left( -\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2} \right)}{d(g+hx)^2} - \frac{c \left( -\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2} \right)}{d(g+hx)} \right) \text{Log} \left[ \frac{h(c+dx)}{-dg+ch} \right] \\
 & \text{Log} \left[ -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right] + \frac{1}{2} \left( \frac{(bg-ah) \left( \frac{2abx}{(bg-ah)^2} + \frac{2a^2b(g+hx)}{(bg-ah)^3} \right)}{b(g+hx)} - \right. \\
 & \left. \frac{(bg-ah)x \left( \frac{-bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)^2} - \frac{a \left( \frac{-bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} + \right. \\
 & \left. \left( (-dg+ch)(a+bx) \left( \frac{2c(-bc+ad)x}{(-dg+ch)^2(a+bx)} - \frac{2c^2(-bc+ad)(g+hx)}{(-dg+ch)^3(a+bx)} \right) \right) / \right. \\
 & \left. \left( (-bc+ad)(g+hx) \right) - \left( (-dg+ch)x(a+bx) \right. \right. \\
 & \left. \left. \left( -\frac{(-bc+ad)x}{(-dg+ch)(a+bx)} + \frac{c(-bc+ad)(g+hx)}{(-dg+ch)^2(a+bx)} \right) \right) / \left( (-bc+ad)(g+hx)^2 \right) + \right. \\
 & \left. \frac{c(a+bx) \left( -\frac{(-bc+ad)x}{(-dg+ch)(a+bx)} + \frac{c(-bc+ad)(g+hx)}{(-dg+ch)^2(a+bx)} \right)}{(-bc+ad)(g+hx)} \right) \text{Log} \left[ -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right]^2 + \\
 & 2 \left( -\frac{(bg-ah) \left( \frac{-bx}{bg-ah} + \frac{ab(g+hx)}{(bg-ah)^2} \right)}{b(g+hx)} - \frac{(-dg+ch) \left( -\frac{dx}{-dg+ch} + \frac{cd(g+hx)}{(-dg+ch)^2} \right)}{d(g+hx)} \right) \\
 & \left( -\left( (-dg+ch)(a+bx) \left( \frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \right) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( -2 \operatorname{Log}[a+b x] + \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] \right) \left( \operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] - \operatorname{Log}\left[-\frac{d(g+h x)}{-d g+c h}\right] \right) + \\
 & \left( -\left( \left( 2(-d g+c h)^2(a+b x) \left( -\frac{c h(c+d x)}{(-d g+c h)^2} + \frac{c+d x}{-d g+c h} \right) \left( \frac{c(b g-a h)(c+d x)}{(-d g+c h)^2(a+b x)} + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{a(c+d x)}{(-d g+c h)(a+b x)} \right) \right) \right) / \left( h(b g-a h)(c+d x)^2 \right) + \\
 & \left( -\left( \left( (-d g+c h)(a+b x) \left( -\frac{2 c^2(b g-a h)(c+d x)}{(-d g+c h)^3(a+b x)} - \frac{2 a c(c+d x)}{(-d g+c h)^2(a+b x)} \right) \right) \right) / \right. \\
 & \quad \left. \left( (b g-a h)(c+d x) \right) - \frac{c(a+b x) \left( \frac{c(b g-a h)(c+d x)}{(-d g+c h)^2(a+b x)} + \frac{a(c+d x)}{(-d g+c h)(a+b x)} \right)}{(b g-a h)(c+d x)} - \right. \\
 & \quad \left. \left( a(-d g+c h)(a+b x) \left( \frac{c(b g-a h)(c+d x)}{(-d g+c h)^2(a+b x)} + \frac{a(c+d x)}{(-d g+c h)(a+b x)} \right) \right) \right) / \\
 & \quad \left( (b g-a h)^2(c+d x) \right) \operatorname{Log}\left[\frac{h(c+d x)}{-d g+c h}\right] + \\
 & \left( \frac{(-d g+c h) \left( \frac{2 c^2 h(c+d x)}{(-d g+c h)^3} - \frac{2 c(c+d x)}{(-d g+c h)^2} \right)}{h(c+d x)} + \frac{c \left( -\frac{c h(c+d x)}{(-d g+c h)^2} + \frac{c+d x}{-d g+c h} \right)}{h(c+d x)} - \right. \\
 & \quad \left. \frac{(-d g+c h) \left( -\frac{c h(c+d x)}{(-d g+c h)^2} + \frac{c+d x}{-d g+c h} \right)}{h^2(c+d x)} \right) \operatorname{Log}\left[-\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right] \\
 & \left( -\operatorname{Log}\left[\frac{b(g+h x)}{b g-a h}\right] + \operatorname{Log}\left[-\frac{d(g+h x)}{-d g+c h}\right] \right) + \frac{1}{2} \left( \left( 2(-d g+c h)^2(a+b x)^2 \right. \right. \\
 & \quad \left. \left. \left( \frac{c(b g-a h)(c+d x)}{(-d g+c h)^2(a+b x)} + \frac{a(c+d x)}{(-d g+c h)(a+b x)} \right)^2 \right) \right) / \left( (b g-a h)^2(c+d x)^2 \right) - \\
 & \left( 2(-d g+c h)(a+b x) \left( -\frac{2 c^2(b g-a h)(c+d x)}{(-d g+c h)^3(a+b x)} - \frac{2 a c(c+d x)}{(-d g+c h)^2(a+b x)} \right) \right. \\
 & \quad \left. \operatorname{Log}\left[-\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right] \right) / \left( (b g-a h)(c+d x) \right) - \\
 & \left( 2 c(a+b x) \left( \frac{c(b g-a h)(c+d x)}{(-d g+c h)^2(a+b x)} + \frac{a(c+d x)}{(-d g+c h)(a+b x)} \right) \right. \\
 & \quad \left. \operatorname{Log}\left[-\frac{(b g-a h)(c+d x)}{(-d g+c h)(a+b x)}\right] \right) / \left( (b g-a h)(c+d x) \right) - \\
 & \left( 2 a(-d g+c h)(a+b x) \left( \frac{c(b g-a h)(c+d x)}{(-d g+c h)^2(a+b x)} + \frac{a(c+d x)}{(-d g+c h)(a+b x)} \right) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left. \frac{(-dg+ch) \left( -\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \operatorname{Log}\left[1 - \frac{h(c+dx)}{-dg+ch}\right]}{h^2(c+dx)} \right) + \\
 & \left( (-dg+ch)^2 (a+bx)^2 \left( \frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \right)^2 \\
 & \operatorname{Log}\left[1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \Big/ \left( (bg-ah)^2(c+dx)^2 \right) + \\
 & \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \left( -\left( \left( (-dg+ch)(a+bx) \left( -\frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} - \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \left( \frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \right) \right) \Big/ \\
 & \quad \left( (bg-ah)(c+dx) \left( 1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right) \right) \Big) - \\
 & \left( (-dg+ch)(a+bx) \left( -\frac{2c^2(bg-ah)(c+dx)}{(-dg+ch)^3(a+bx)} - \frac{2ac(c+dx)}{(-dg+ch)^2(a+bx)} \right) \right) \\
 & \operatorname{Log}\left[1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \Big/ \left( (bg-ah)(c+dx) \right) - \\
 & \left( c(a+bx) \left( \frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \right) \\
 & \operatorname{Log}\left[1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \Big/ \left( (bg-ah)(c+dx) \right) - \\
 & \left( a(-dg+ch)(a+bx) \left( \frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \right) \\
 & \operatorname{Log}\left[1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \Big/ \left( (bg-ah)^2(c+dx) \right) \Big) + \\
 & \frac{(bg-ah) \left( -\frac{2a^2h(a+bx)}{(bg-ah)^3} - \frac{2a(a+bx)}{(bg-ah)^2} \right) \operatorname{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right]}{h(a+bx)} - \\
 & \frac{a \left( -\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \operatorname{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right]}{h(a+bx)} - \\
 & \frac{(bg-ah) \left( -\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \operatorname{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right]}{h^2(a+bx)} + \\
 & \left( \left( (-dg+ch)(a+bx) \left( -\frac{2c^2(bg-ah)(c+dx)}{(-dg+ch)^3(a+bx)} - \frac{2ac(c+dx)}{(-dg+ch)^2(a+bx)} \right) \right) \right) \Big/ \\
 & \left( (bg-ah)(c+dx) \right) + \frac{c(a+bx) \left( \frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right)}{(bg-ah)(c+dx)} +
 \end{aligned}$$

$$\begin{aligned}
 & \left( a (-dg + ch) (a + bx) \left( \frac{c (bg - ah) (c + dx)}{(-dg + ch)^2 (a + bx)} + \frac{a (c + dx)}{(-dg + ch) (a + bx)} \right) \right) / \\
 & \left( (bg - ah)^2 (c + dx) \right) \text{PolyLog}\left[2, -\frac{h (a + bx)}{bg - ah}\right] - \\
 & \frac{(-dg + ch) \left( \frac{2c^2 h (c + dx)}{(-dg + ch)^3} - \frac{2c (c + dx)}{(-dg + ch)^2} \right) \text{PolyLog}\left[2, \frac{h (c + dx)}{-dg + ch}\right]}{h (c + dx)} - \\
 & \frac{c \left( -\frac{ch (c + dx)}{(-dg + ch)^2} + \frac{c + dx}{-dg + ch} \right) \text{PolyLog}\left[2, \frac{h (c + dx)}{-dg + ch}\right]}{h (c + dx)} + \\
 & \frac{(-dg + ch) \left( -\frac{ch (c + dx)}{(-dg + ch)^2} + \frac{c + dx}{-dg + ch} \right) \text{PolyLog}\left[2, \frac{h (c + dx)}{-dg + ch}\right]}{h^2 (c + dx)} + \\
 & \left( - \left( \left( (-dg + ch) (a + bx) \left( -\frac{2c^2 (bg - ah) (c + dx)}{(-dg + ch)^3 (a + bx)} - \frac{2ac (c + dx)}{(-dg + ch)^2 (a + bx)} \right) \right) / \right. \right. \\
 & \left. \left. (bg - ah) (c + dx) \right) - \frac{c (a + bx) \left( \frac{c (bg - ah) (c + dx)}{(-dg + ch)^2 (a + bx)} + \frac{a (c + dx)}{(-dg + ch) (a + bx)} \right)}{(bg - ah) (c + dx)} - \right. \\
 & \left. \left( a (-dg + ch) (a + bx) \left( \frac{c (bg - ah) (c + dx)}{(-dg + ch)^2 (a + bx)} + \frac{a (c + dx)}{(-dg + ch) (a + bx)} \right) \right) / \right. \\
 & \left. \left( (bg - ah)^2 (c + dx) \right) \text{PolyLog}\left[2, \frac{h (c + dx)}{-dg + ch}\right] + \right. \\
 & \left( - \left( \left( (-dg + ch) (a + bx) \left( -\frac{2c^2 (bg - ah) (c + dx)}{(-dg + ch)^3 (a + bx)} - \frac{2ac (c + dx)}{(-dg + ch)^2 (a + bx)} \right) \right) / \right. \right. \\
 & \left. \left. (bg - ah) (c + dx) \right) - \frac{c (a + bx) \left( \frac{c (bg - ah) (c + dx)}{(-dg + ch)^2 (a + bx)} + \frac{a (c + dx)}{(-dg + ch) (a + bx)} \right)}{(bg - ah) (c + dx)} - \right. \\
 & \left. \left( a (-dg + ch) (a + bx) \left( \frac{c (bg - ah) (c + dx)}{(-dg + ch)^2 (a + bx)} + \frac{a (c + dx)}{(-dg + ch) (a + bx)} \right) \right) / \right. \\
 & \left. \left( (bg - ah)^2 (c + dx) \right) \right) \\
 & \left( \text{PolyLog}\left[2, \frac{b (c + dx)}{d (a + bx)}\right] - \text{PolyLog}\left[2, -\frac{(bg - ah) (c + dx)}{(-dg + ch) (a + bx)}\right] \right) - \\
 & \left( (-dg + ch) (a + bx) \left( -\frac{2c^2 (bg - ah) (c + dx)}{(-dg + ch)^3 (a + bx)} - \frac{2ac (c + dx)}{(-dg + ch)^2 (a + bx)} \right) \right. \\
 & \left. \text{PolyLog}\left[2, -\frac{(bg - ah) (c + dx)}{(-dg + ch) (a + bx)}\right] \right) / ((bg - ah) (c + dx)) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( c (a+b x) \left( \frac{c (b g-a h) (c+d x)}{(-d g+c h)^2 (a+b x)} + \frac{a (c+d x)}{(-d g+c h) (a+b x)} \right) \right. \\
 & \quad \left. \text{PolyLog}\left[2, -\frac{(b g-a h) (c+d x)}{(-d g+c h) (a+b x)}\right] \right) / \left( (b g-a h) (c+d x) - \right. \\
 & \left. \left( a (-d g+c h) (a+b x) \left( \frac{c (b g-a h) (c+d x)}{(-d g+c h)^2 (a+b x)} + \frac{a (c+d x)}{(-d g+c h) (a+b x)} \right) \right) \right. \\
 & \quad \left. \text{PolyLog}\left[2, -\frac{(b g-a h) (c+d x)}{(-d g+c h) (a+b x)}\right] \right) / \left( (b g-a h)^2 (c+d x) \right) \Bigg) - \\
 & \frac{1}{h^2} 2 \left( \frac{(b g-a h) \left( \frac{b x}{b g-a h} + \frac{a b (g+h x)}{(b g-a h)^2} \right) \text{Log}[a+b x] \text{Log}[c+d x]}{b (g+h x)} + \right. \\
 & \frac{1}{2} \left( \frac{(b g-a h) \left( \frac{b x}{b g-a h} + \frac{a b (g+h x)}{(b g-a h)^2} \right)}{b (g+h x)} + \frac{(-d g+c h) \left( -\frac{d x}{-d g+c h} + \frac{c d (g+h x)}{(-d g+c h)^2} \right)}{d (g+h x)} \right) \\
 & \quad \text{Log}\left[ \frac{h (c+d x)}{-d g+c h} \right] \left( -2 \text{Log}[a+b x] + \text{Log}\left[ \frac{h (c+d x)}{-d g+c h} \right] \right) + \\
 & \left( -\frac{(b g-a h) \left( \frac{b x}{b g-a h} + \frac{a b (g+h x)}{(b g-a h)^2} \right)}{b (g+h x)} - \frac{(-d g+c h) \left( -\frac{d x}{-d g+c h} + \frac{c d (g+h x)}{(-d g+c h)^2} \right)}{d (g+h x)} \right) \\
 & \quad \text{Log}\left[ \frac{h (c+d x)}{-d g+c h} \right] \text{Log}\left[ -\frac{(b g-a h) (c+d x)}{(-d g+c h) (a+b x)} \right] + \frac{1}{2} \left( \frac{(b g-a h) \left( \frac{b x}{b g-a h} + \frac{a b (g+h x)}{(b g-a h)^2} \right)}{b (g+h x)} + \right. \\
 & \quad \left. \left( (-d g+c h) (a+b x) \left( -\frac{(-b c+a d) x}{(-d g+c h) (a+b x)} + \frac{c (-b c+a d) (g+h x)}{(-d g+c h)^2 (a+b x)} \right) \right) / \right. \\
 & \quad \left. \left( (-b c+a d) (g+h x) \right) \right) \text{Log}\left[ -\frac{(b g-a h) (c+d x)}{(-d g+c h) (a+b x)} \right]^2 + \\
 & \frac{1}{2 h (c+d x)} (-d g+c h) \left( -\frac{c h (c+d x)}{(-d g+c h)^2} + \frac{c+d x}{-d g+c h} \right) \text{Log}\left[ \frac{h (c+d x)}{-d g+c h} \right] \\
 & \quad \left( \text{Log}\left[ \frac{b (g+h x)}{b g-a h} \right] - \text{Log}\left[ -\frac{d (g+h x)}{-d g+c h} \right] \right) + \frac{1}{2 h (c+d x)} \\
 & (-d g+c h) \left( -\frac{c h (c+d x)}{(-d g+c h)^2} + \frac{c+d x}{-d g+c h} \right) \left( -2 \text{Log}[a+b x] + \text{Log}\left[ \frac{h (c+d x)}{-d g+c h} \right] \right) \\
 & \quad \left( \text{Log}\left[ \frac{b (g+h x)}{b g-a h} \right] - \text{Log}\left[ -\frac{d (g+h x)}{-d g+c h} \right] \right) - \\
 & \left( (-d g+c h) (a+b x) \left( \frac{c (b g-a h) (c+d x)}{(-d g+c h)^2 (a+b x)} + \frac{a (c+d x)}{(-d g+c h) (a+b x)} \right) \right) \text{Log}\left[ \right.
 \end{aligned}$$

$$\begin{aligned}
& \frac{h(c+dx)}{-dg+ch} \left( -\operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \operatorname{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) \Big/ ((bg-ah)(c+dx)) + \\
& \frac{1}{h(c+dx)} (-dg+ch) \left( -\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \\
& \left( -\operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] + \operatorname{Log}\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) - \\
& \left( (-dg+ch)(a+bx) \left( \frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \operatorname{Log}\left[ \right. \right. \\
& \quad \left. \left. -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right] \left( \operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] + \operatorname{Log}\left[\frac{b(g+hx)}{bg-ah}\right] - \right. \right. \\
& \quad \left. \left. \operatorname{Log}\left[-\frac{(-bc+ad)(g+hx)}{(-dg+ch)(a+bx)}\right] \right) \right) \Big/ ((bg-ah)(c+dx)) + \frac{1}{h(a+bx)} \\
& (bg-ah) \left( -\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \left( \operatorname{Log}[c+dx] - \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \\
& \operatorname{Log}\left[1 + \frac{h(a+bx)}{bg-ah}\right] - \frac{1}{h(c+dx)} (-dg+ch) \left( -\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \\
& \left( \operatorname{Log}[a+bx] + \operatorname{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \operatorname{Log}\left[1 - \frac{h(c+dx)}{-dg+ch}\right] - \\
& \left( (-dg+ch)(a+bx) \left( \frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \operatorname{Log}\left[ \right. \right. \\
& \quad \left. \left. -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)} \right] \operatorname{Log}\left[1 + \frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \Big/ ((bg-ah)(c+dx)) + \\
& \frac{(bg-ah) \left( -\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah} \right) \operatorname{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right]}{h(a+bx)} + \left( (-dg+ch)(a+bx) \right. \\
& \quad \left. \left( \frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \operatorname{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right] \right) \Big/ \\
& ((bg-ah)(c+dx)) - \frac{(-dg+ch) \left( -\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch} \right) \operatorname{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right]}{h(c+dx)} - \\
& \left( (-dg+ch)(a+bx) \left( \frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \right. \\
& \quad \left. \operatorname{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right] \right) \Big/ ((bg-ah)(c+dx)) - \\
& \left( (-dg+ch)(a+bx) \left( \frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \left( \operatorname{PolyLog}\left[2, \right. \right. \right. \\
& \quad \left. \left. \frac{b(c+dx)}{d(a+bx)} \right] - \operatorname{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \right) \Big/ ((bg-ah)(c+dx)) -
\end{aligned}$$



$$\begin{aligned}
 & \left( (-d g + c h) (a + b x) \left( \frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \right. \\
 & \quad \left. \text{PolyLog}\left[2, -\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] \right) / ((b g - a h) (c + d x)) + \\
 & \frac{1}{h^3} 2 \left( \text{Log}[a + b x] \text{Log}[c + d x] \text{Log}\left[\frac{b (g + h x)}{b g - a h}\right] + \frac{1}{2} \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \right. \\
 & \quad \left( -2 \text{Log}[a + b x] + \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \right) \left( \text{Log}\left[\frac{b (g + h x)}{b g - a h}\right] - \text{Log}\left[-\frac{d (g + h x)}{-d g + c h}\right] \right) + \\
 & \quad \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \text{Log}\left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] \\
 & \quad \left( -\text{Log}\left[\frac{b (g + h x)}{b g - a h}\right] + \text{Log}\left[-\frac{d (g + h x)}{-d g + c h}\right] \right) + \frac{1}{2} \text{Log}\left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right]^2 \\
 & \quad \left( \text{Log}\left[\frac{-b c + a d}{d (a + b x)}\right] + \text{Log}\left[\frac{b (g + h x)}{b g - a h}\right] - \text{Log}\left[-\frac{(-b c + a d) (g + h x)}{(-d g + c h) (a + b x)}\right] \right) + \\
 & \quad \left( \text{Log}[c + d x] - \text{Log}\left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] \right) \text{PolyLog}\left[2, -\frac{h (a + b x)}{b g - a h}\right] + \\
 & \quad \left( \text{Log}[a + b x] + \text{Log}\left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] \right) \text{PolyLog}\left[2, \frac{h (c + d x)}{-d g + c h}\right] + \\
 & \quad \text{Log}\left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] \left( \text{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)}\right] - \text{PolyLog}\left[2, \right. \right. \\
 & \quad \left. \left. -\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] - \text{PolyLog}\left[3, -\frac{h (a + b x)}{b g - a h}\right] - \text{PolyLog}\left[3, \frac{h (c + d x)}{-d g + c h}\right] - \right. \\
 & \quad \left. \text{PolyLog}\left[3, \frac{b (c + d x)}{d (a + b x)}\right] + \text{PolyLog}\left[3, -\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] \right) \left. \right) + \\
 & 4 h \left( \frac{1}{h} \left( \frac{(b g - a h) \left( \frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right) \text{Log}[a + b x] \text{Log}[c + d x]}{b (g + h x)} + \right. \right. \\
 & \quad \left. \frac{1}{2} \left( \frac{(b g - a h) \left( \frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b (g + h x)} + \frac{(-d g + c h) \left( -\frac{d x}{-d g + c h} + \frac{c d (g + h x)}{(-d g + c h)^2} \right)}{d (g + h x)} \right) \right. \\
 & \quad \left. \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \left( -2 \text{Log}[a + b x] + \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \right) + \right. \\
 & \quad \left( -\frac{(b g - a h) \left( \frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b (g + h x)} - \frac{(-d g + c h) \left( -\frac{d x}{-d g + c h} + \frac{c d (g + h x)}{(-d g + c h)^2} \right)}{d (g + h x)} \right) \\
 & \quad \left. \text{Log}\left[\frac{h (c + d x)}{-d g + c h}\right] \text{Log}\left[-\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)}\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
& \frac{1}{2} \left( \frac{(b g - a h) \left( \frac{b x}{b g - a h} + \frac{a b (g + h x)}{(b g - a h)^2} \right)}{b (g + h x)} + \left( (-d g + c h) (a + b x) \right. \right. \\
& \quad \left. \left. \left( -\frac{(-b c + a d) x}{(-d g + c h) (a + b x)} + \frac{c (-b c + a d) (g + h x)}{(-d g + c h)^2 (a + b x)} \right) \right) / \left( (-b c + a d) (g + h x) \right) \right) \\
& \text{Log} \left[ -\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right]^2 + \frac{1}{2 h (c + d x)} (-d g + c h) \left( -\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \\
& \text{Log} \left[ \frac{h (c + d x)}{-d g + c h} \right] \left( \text{Log} \left[ \frac{b (g + h x)}{b g - a h} \right] - \text{Log} \left[ -\frac{d (g + h x)}{-d g + c h} \right] \right) + \\
& \frac{1}{2 h (c + d x)} (-d g + c h) \left( -\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \\
& \left( -2 \text{Log} [a + b x] + \text{Log} \left[ \frac{h (c + d x)}{-d g + c h} \right] \right) \left( \text{Log} \left[ \frac{b (g + h x)}{b g - a h} \right] - \text{Log} \left[ -\frac{d (g + h x)}{-d g + c h} \right] \right) - \\
& \left( (-d g + c h) (a + b x) \left( \frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \text{Log} \left[ \frac{h (c + d x)}{-d g + c h} \right] \right. \\
& \quad \left. \left( -\text{Log} \left[ \frac{b (g + h x)}{b g - a h} \right] + \text{Log} \left[ -\frac{d (g + h x)}{-d g + c h} \right] \right) \right) / \left( (b g - a h) (c + d x) \right) + \frac{1}{h (c + d x)} \\
& (-d g + c h) \left( -\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \text{Log} \left[ -\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right] \\
& \left( -\text{Log} \left[ \frac{b (g + h x)}{b g - a h} \right] + \text{Log} \left[ -\frac{d (g + h x)}{-d g + c h} \right] \right) - \left( (-d g + c h) (a + b x) \right. \\
& \quad \left. \left( \frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \text{Log} \left[ -\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right] \right. \\
& \quad \left. \left( \text{Log} \left[ \frac{-b c + a d}{d (a + b x)} \right] + \text{Log} \left[ \frac{b (g + h x)}{b g - a h} \right] - \text{Log} \left[ -\frac{(-b c + a d) (g + h x)}{(-d g + c h) (a + b x)} \right] \right) \right) / \\
& \left( (b g - a h) (c + d x) \right) + \frac{1}{h (a + b x)} (b g - a h) \left( -\frac{a h (a + b x)}{(b g - a h)^2} - \frac{a + b x}{b g - a h} \right) \\
& \left( \text{Log} [c + d x] - \text{Log} \left[ -\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right] \right) \text{Log} \left[ 1 + \frac{h (a + b x)}{b g - a h} \right] - \\
& \frac{1}{h (c + d x)} (-d g + c h) \left( -\frac{c h (c + d x)}{(-d g + c h)^2} + \frac{c + d x}{-d g + c h} \right) \\
& \left( \text{Log} [a + b x] + \text{Log} \left[ -\frac{(b g - a h) (c + d x)}{(-d g + c h) (a + b x)} \right] \right) \text{Log} \left[ 1 - \frac{h (c + d x)}{-d g + c h} \right] - \\
& \left( (-d g + c h) (a + b x) \left( \frac{c (b g - a h) (c + d x)}{(-d g + c h)^2 (a + b x)} + \frac{a (c + d x)}{(-d g + c h) (a + b x)} \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left. \log\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \log\left[1+\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]\right/ \\
 & \left( (bg-ah)(c+dx) + \frac{(bg-ah)\left(-\frac{ah(a+bx)}{(bg-ah)^2} - \frac{a+bx}{bg-ah}\right) \text{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right]}{h(a+bx)} + \right. \\
 & \left. \left( (-dg+ch)(a+bx) \left( \frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \right. \right. \\
 & \left. \left. \text{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right]\right) \right/ \left( (bg-ah)(c+dx) - \right. \\
 & \left. \frac{(-dg+ch)\left(-\frac{ch(c+dx)}{(-dg+ch)^2} + \frac{c+dx}{-dg+ch}\right) \text{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right]}{h(c+dx)} - \right. \\
 & \left. \left( (-dg+ch)(a+bx) \left( \frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \right. \right. \\
 & \left. \left. \text{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right]\right) \right/ \left( (bg-ah)(c+dx) - \right. \\
 & \left. \left( (-dg+ch)(a+bx) \left( \frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \right) \left( \text{PolyLog}\left[2, \right. \right. \right. \\
 & \left. \left. \left. \frac{b(c+dx)}{d(a+bx)}\right] - \text{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]\right) \right) \right/ \left( (bg-ah)(c+dx) - \right. \\
 & \left. \left( (-dg+ch)(a+bx) \left( \frac{c(bg-ah)(c+dx)}{(-dg+ch)^2(a+bx)} + \frac{a(c+dx)}{(-dg+ch)(a+bx)} \right) \right. \right. \\
 & \left. \left. \text{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]\right) \right/ \left( (bg-ah)(c+dx) \right) \right) - \\
 & \frac{1}{h^2} \left( \log[a+bx] \log[c+dx] \log\left[\frac{b(g+hx)}{bg-ah}\right] + \frac{1}{2} \log\left[\frac{h(c+dx)}{-dg+ch}\right] \right. \\
 & \left. \left( -2 \log[a+bx] + \log\left[\frac{h(c+dx)}{-dg+ch}\right] \right) \left( \log\left[\frac{b(g+hx)}{bg-ah}\right] - \log\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) \right) + \\
 & \log\left[\frac{h(c+dx)}{-dg+ch}\right] \log\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \\
 & \left( -\log\left[\frac{b(g+hx)}{bg-ah}\right] + \log\left[-\frac{d(g+hx)}{-dg+ch}\right] \right) + \frac{1}{2} \log\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]^2 \\
 & \left( \log\left[\frac{-bc+ad}{d(a+bx)}\right] + \log\left[\frac{b(g+hx)}{bg-ah}\right] - \log\left[-\frac{(-bc+ad)(g+hx)}{(-dg+ch)(a+bx)}\right] \right) + \\
 & \left( \log[c+dx] - \log\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \text{PolyLog}\left[2, -\frac{h(a+bx)}{bg-ah}\right] + \\
 & \left( \log[a+bx] + \log\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \right) \text{PolyLog}\left[2, \frac{h(c+dx)}{-dg+ch}\right] +
 \end{aligned}$$

$$\begin{aligned} & \text{Log}\left[-\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right] \\ & \left(\text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] - \text{PolyLog}\left[2, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]\right) - \\ & \text{PolyLog}\left[3, -\frac{h(a+bx)}{bg-ah}\right] - \text{PolyLog}\left[3, \frac{h(c+dx)}{-dg+ch}\right] - \\ & \left.\text{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right] + \text{PolyLog}\left[3, -\frac{(bg-ah)(c+dx)}{(-dg+ch)(a+bx)}\right]\right) \end{aligned}$$

**Problem 42: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Log}\left[e (f (a+bx)^p (c+dx)^q)^r\right]^2}{(g+hx)^4} dx$$

Optimal (type 4, 1957 leaves, 57 steps):

$$\begin{aligned} & -\frac{b^2 p^2 r^2}{3 h (b g - a h)^2 (g + h x)} - \frac{2 b d p q r^2}{3 h (b g - a h) (d g - c h) (g + h x)} - \\ & \frac{d^2 q^2 r^2}{3 h (d g - c h)^2 (g + h x)} - \frac{b^3 p^2 r^2 \text{Log}[a + b x]}{3 h (b g - a h)^3} - \frac{2 b d^2 p q r^2 \text{Log}[a + b x]}{3 h (b g - a h) (d g - c h)^2} - \\ & \frac{b^2 d p q r^2 \text{Log}[a + b x]}{3 h (b g - a h)^2 (d g - c h)} + \frac{b p^2 r^2 \text{Log}[a + b x]}{3 h (b g - a h) (g + h x)^2} + \frac{d p q r^2 \text{Log}[a + b x]}{3 h (d g - c h) (g + h x)^2} + \\ & \frac{2 d^2 p q r^2 \text{Log}[a + b x]}{3 h (d g - c h)^2 (g + h x)} - \frac{2 b^2 p^2 r^2 (a + b x) \text{Log}[a + b x]}{3 (b g - a h)^3 (g + h x)} - \frac{b d^2 p q r^2 \text{Log}[c + d x]}{3 h (b g - a h) (d g - c h)^2} - \\ & \frac{2 b^2 d p q r^2 \text{Log}[c + d x]}{3 h (b g - a h)^2 (d g - c h)} - \frac{d^3 q^2 r^2 \text{Log}[c + d x]}{3 h (d g - c h)^3} + \frac{b p q r^2 \text{Log}[c + d x]}{3 h (b g - a h) (g + h x)^2} + \\ & \frac{d q^2 r^2 \text{Log}[c + d x]}{3 h (d g - c h) (g + h x)^2} + \frac{2 b^2 p q r^2 \text{Log}[c + d x]}{3 h (b g - a h)^2 (g + h x)} - \frac{2 d^2 q^2 r^2 (c + d x) \text{Log}[c + d x]}{3 (d g - c h)^3 (g + h x)} + \\ & \frac{2 b^3 p q r^2 \text{Log}\left[-\frac{d(a+bx)}{bc-ad}\right] \text{Log}[c + d x]}{3 h (b g - a h)^3} + \frac{2 d^3 p q r^2 \text{Log}[a + b x] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right]}{3 h (d g - c h)^3} - \\ & \left(\frac{b p r (p r \text{Log}[a + b x] + q r \text{Log}[c + d x] - \text{Log}[e (f (a + b x)^p (c + d x)^q)^r])}{(3 h (b g - a h) (g + h x)^2)} - \right. \\ & \left. \frac{d q r (p r \text{Log}[a + b x] + q r \text{Log}[c + d x] - \text{Log}[e (f (a + b x)^p (c + d x)^q)^r])}{(3 h (d g - c h) (g + h x)^2)} - \right. \\ & \left. \frac{2 b^2 p r (p r \text{Log}[a + b x] + q r \text{Log}[c + d x] - \text{Log}[e (f (a + b x)^p (c + d x)^q)^r])}{(3 h (b g - a h)^2 (g + h x))} - \right. \\ & \left. \frac{2 d^2 q r (p r \text{Log}[a + b x] + q r \text{Log}[c + d x] - \text{Log}[e (f (a + b x)^p (c + d x)^q)^r])}{(3 h (d g - c h)^2 (g + h x))} \right) \end{aligned}$$

$$\begin{aligned}
 & \left( 3 h (d g - c h)^2 (g + h x) \right) - \frac{1}{3 h (b g - a h)^3} 2 b^3 p r \operatorname{Log}[a + b x] \\
 & \left( p r \operatorname{Log}[a + b x] + q r \operatorname{Log}[c + d x] - \operatorname{Log}\left[ e (f (a + b x)^p (c + d x)^q)^r \right] \right) - \frac{1}{3 h (d g - c h)^3} \\
 & 2 d^3 q r \operatorname{Log}[c + d x] \left( p r \operatorname{Log}[a + b x] + q r \operatorname{Log}[c + d x] - \operatorname{Log}\left[ e (f (a + b x)^p (c + d x)^q)^r \right] \right) - \\
 & \frac{\operatorname{Log}\left[ e (f (a + b x)^p (c + d x)^q)^r \right]^2}{3 h (g + h x)^3} + \frac{b^3 p^2 r^2 \operatorname{Log}[g + h x]}{h (b g - a h)^3} + \frac{b d^2 p q r^2 \operatorname{Log}[g + h x]}{h (b g - a h) (d g - c h)^2} + \\
 & \frac{b^2 d p q r^2 \operatorname{Log}[g + h x]}{h (b g - a h)^2 (d g - c h)} + \frac{d^3 q^2 r^2 \operatorname{Log}[g + h x]}{h (d g - c h)^3} + \frac{1}{3 h (b g - a h)^3} 2 b^3 p r \\
 & \left( p r \operatorname{Log}[a + b x] + q r \operatorname{Log}[c + d x] - \operatorname{Log}\left[ e (f (a + b x)^p (c + d x)^q)^r \right] \right) \operatorname{Log}[g + h x] + \frac{1}{3 h (d g - c h)^3} \\
 & 2 d^3 q r \left( p r \operatorname{Log}[a + b x] + q r \operatorname{Log}[c + d x] - \operatorname{Log}\left[ e (f (a + b x)^p (c + d x)^q)^r \right] \right) \operatorname{Log}[g + h x] - \\
 & \frac{2 d^3 p q r^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[ \frac{b(g+hx)}{bg-ah} \right]}{3 h (d g - c h)^3} - \frac{2 b^3 p q r^2 \operatorname{Log}[c + d x] \operatorname{Log}\left[ \frac{d(g+hx)}{dg-ch} \right]}{3 h (b g - a h)^3} - \\
 & \frac{2 b^3 p^2 r^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[ 1 + \frac{bg-ah}{h(a+bx)} \right]}{3 h (b g - a h)^3} - \frac{2 d^3 q^2 r^2 \operatorname{Log}[c + d x] \operatorname{Log}\left[ 1 + \frac{dg-ch}{h(c+dx)} \right]}{3 h (d g - c h)^3} + \\
 & \frac{2 b^3 p^2 r^2 \operatorname{PolyLog}\left[ 2, -\frac{bg-ah}{h(a+bx)} \right]}{3 h (b g - a h)^3} + \frac{2 d^3 p q r^2 \operatorname{PolyLog}\left[ 2, -\frac{d(a+bx)}{bc-ad} \right]}{3 h (d g - c h)^3} - \\
 & \frac{2 d^3 p q r^2 \operatorname{PolyLog}\left[ 2, -\frac{h(a+bx)}{bg-ah} \right]}{3 h (d g - c h)^3} + \frac{2 d^3 q^2 r^2 \operatorname{PolyLog}\left[ 2, -\frac{dg-ch}{h(c+dx)} \right]}{3 h (d g - c h)^3} + \\
 & \frac{2 b^3 p q r^2 \operatorname{PolyLog}\left[ 2, \frac{b(c+dx)}{bc-ad} \right]}{3 h (b g - a h)^3} - \frac{2 b^3 p q r^2 \operatorname{PolyLog}\left[ 2, -\frac{h(c+dx)}{dg-ch} \right]}{3 h (b g - a h)^3}
 \end{aligned}$$

Result (type 4, 47 110 leaves): Display of huge result suppressed!

**Problem 44: Result more than twice size of optimal antiderivative.**

$$\int \frac{\left( a + b \operatorname{Log}\left[ \frac{\sqrt{1-cx}}{\sqrt{1+cx}} \right] \right)^3}{1 - c^2 x^2} dx$$

Optimal (type 3, 37 leaves, 5 steps):

$$\frac{\left( a + b \operatorname{Log}\left[ \frac{\sqrt{1-cx}}{\sqrt{1+cx}} \right] \right)^4}{4 b c}$$

Result (type 3, 117 leaves):

$$-\frac{1}{4 c} \operatorname{Log}\left[ \frac{\sqrt{1-cx}}{\sqrt{1+cx}} \right] \left( 4 a^3 + 6 a^2 b \operatorname{Log}\left[ \frac{\sqrt{1-cx}}{\sqrt{1+cx}} \right] + 4 a b^2 \operatorname{Log}\left[ \frac{\sqrt{1-cx}}{\sqrt{1+cx}} \right]^2 + b^3 \operatorname{Log}\left[ \frac{\sqrt{1-cx}}{\sqrt{1+cx}} \right]^3 \right)$$

**Problem 45: Result more than twice size of optimal antiderivative.**

$$\int \frac{\left(a + b \operatorname{Log}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right)^2}{1 - c^2 x^2} dx$$

Optimal (type 3, 37 leaves, 5 steps):

$$\frac{\left(a + b \operatorname{Log}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]\right)^3}{3bc}$$

Result (type 3, 86 leaves):

$$\frac{\operatorname{Log}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right] \left(3a^2 + 3ab \operatorname{Log}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right] + b^2 \operatorname{Log}\left[\frac{\sqrt{1-cx}}{\sqrt{1+cx}}\right]^2\right)}{3c}$$

**Problem 51: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Log}\left[e \left(f (a + b x)^p (c + d x)^q\right)^r\right] \left(s + t \operatorname{Log}\left[i (g + h x)^n\right]\right)^2}{gk + hkx} dx$$

Optimal (type 4, 410 leaves, 11 steps):

$$\begin{aligned} & \frac{pr \operatorname{Log}\left[-\frac{h(a+bx)}{bg-ah}\right] \left(s + t \operatorname{Log}\left[i (g + h x)^n\right]\right)^3}{3hkn t} - \frac{qr \operatorname{Log}\left[-\frac{h(c+dx)}{dg-ch}\right] \left(s + t \operatorname{Log}\left[i (g + h x)^n\right]\right)^3}{3hkn t} + \\ & \frac{\operatorname{Log}\left[e \left(f (a + b x)^p (c + d x)^q\right)^r\right] \left(s + t \operatorname{Log}\left[i (g + h x)^n\right]\right)^3}{3hkn t} - \\ & \frac{pr \left(s + t \operatorname{Log}\left[i (g + h x)^n\right]\right)^2 \operatorname{PolyLog}\left[2, \frac{b(g+hx)}{bg-ah}\right]}{hk} - \\ & \frac{qr \left(s + t \operatorname{Log}\left[i (g + h x)^n\right]\right)^2 \operatorname{PolyLog}\left[2, \frac{d(g+hx)}{dg-ch}\right]}{hk} + \\ & \frac{2nprt \left(s + t \operatorname{Log}\left[i (g + h x)^n\right]\right) \operatorname{PolyLog}\left[3, \frac{b(g+hx)}{bg-ah}\right]}{hk} + \\ & \frac{2nqrt \left(s + t \operatorname{Log}\left[i (g + h x)^n\right]\right) \operatorname{PolyLog}\left[3, \frac{d(g+hx)}{dg-ch}\right]}{hk} - \\ & \frac{2n^2prt^2 \operatorname{PolyLog}\left[4, \frac{b(g+hx)}{bg-ah}\right]}{hk} - \frac{2n^2qrt^2 \operatorname{PolyLog}\left[4, \frac{d(g+hx)}{dg-ch}\right]}{hk} \end{aligned}$$

Result (type 4, 22 595 leaves): Display of huge result suppressed!

### Problem 56: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}[i (j (hx)^t)^u]^3 \text{Log}[e (f (a+bx)^p (c+dx)^q)^r]}{x} dx$$

Optimal (type 4, 328 leaves, 13 steps):

$$\begin{aligned} & - \frac{p r \text{Log}[i (j (hx)^t)^u]^4 \text{Log}[1 + \frac{bx}{a}]}{4 t u} + \frac{\text{Log}[i (j (hx)^t)^u]^4 \text{Log}[e (f (a+bx)^p (c+dx)^q)^r]}{4 t u} - \\ & \frac{q r \text{Log}[i (j (hx)^t)^u]^4 \text{Log}[1 + \frac{dx}{c}]}{4 t u} - p r \text{Log}[i (j (hx)^t)^u]^3 \text{PolyLog}[2, -\frac{bx}{a}] - \\ & q r \text{Log}[i (j (hx)^t)^u]^3 \text{PolyLog}[2, -\frac{dx}{c}] + 3 p r t u \text{Log}[i (j (hx)^t)^u]^2 \text{PolyLog}[3, -\frac{bx}{a}] + \\ & 3 q r t u \text{Log}[i (j (hx)^t)^u]^2 \text{PolyLog}[3, -\frac{dx}{c}] - 6 p r t^2 u^2 \text{Log}[i (j (hx)^t)^u] \text{PolyLog}[4, -\frac{bx}{a}] - \\ & 6 q r t^2 u^2 \text{Log}[i (j (hx)^t)^u] \text{PolyLog}[4, -\frac{dx}{c}] + \\ & 6 p r t^3 u^3 \text{PolyLog}[5, -\frac{bx}{a}] + 6 q r t^3 u^3 \text{PolyLog}[5, -\frac{dx}{c}] \end{aligned}$$

Result (type 4, 1241 leaves):

$$\begin{aligned}
& p r t^3 u^3 \operatorname{Log}[x] \operatorname{Log}[h x]^3 \operatorname{Log}[a+b x] - p r t^3 u^3 \operatorname{Log}[h x]^4 \operatorname{Log}[a+b x] - \\
& 3 p r t^2 u^2 \operatorname{Log}[x] \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}[a+b x] + \\
& 3 p r t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}[a+b x] + \\
& 3 p r t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}[a+b x] - \\
& 3 p r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}[a+b x] - \\
& p r \operatorname{Log}[x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{Log}[a+b x] + p r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{Log}[a+b x] + \\
& \frac{1}{4} p r t^3 u^3 \operatorname{Log}[h x]^4 \operatorname{Log}\left[1+\frac{b x}{a}\right] - p r t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}\left[1+\frac{b x}{a}\right] + \\
& \frac{3}{2} p r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}\left[1+\frac{b x}{a}\right] - p r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{Log}\left[1+\frac{b x}{a}\right] + \\
& q r t^3 u^3 \operatorname{Log}[x] \operatorname{Log}[h x]^3 \operatorname{Log}[c+d x] - q r t^3 u^3 \operatorname{Log}[h x]^4 \operatorname{Log}[c+d x] - \\
& 3 q r t^2 u^2 \operatorname{Log}[x] \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}[c+d x] + \\
& 3 q r t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}[c+d x] + \\
& 3 q r t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}[c+d x] - \\
& 3 q r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}[c+d x] - \\
& q r \operatorname{Log}[x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{Log}[c+d x] + q r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{Log}[c+d x] - \\
& t^3 u^3 \operatorname{Log}[x] \operatorname{Log}[h x]^3 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] + \\
& \frac{3}{4} t^3 u^3 \operatorname{Log}[h x]^4 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] + \\
& 3 t^2 u^2 \operatorname{Log}[x] \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] - \\
& 2 t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] - \\
& 3 t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] + \\
& \frac{3}{2} t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] + \\
& \operatorname{Log}[x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{Log}\left[e\left(f(a+b x)^p(c+d x)^q\right)^r\right] + \\
& \frac{1}{4} q r t^3 u^3 \operatorname{Log}[h x]^4 \operatorname{Log}\left[1+\frac{d x}{c}\right] - q r t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{Log}\left[1+\frac{d x}{c}\right] + \\
& \frac{3}{2} q r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{Log}\left[1+\frac{d x}{c}\right] - q r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{Log}\left[1+\frac{d x}{c}\right] - \\
& p r \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{PolyLog}\left[2,-\frac{b x}{a}\right] - q r \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^3 \operatorname{PolyLog}\left[2,-\frac{d x}{c}\right] + \\
& 3 p r t u \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{PolyLog}\left[3,-\frac{b x}{a}\right] + 3 q r t u \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right]^2 \operatorname{PolyLog}\left[3,-\frac{d x}{c}\right] - \\
& 6 p r t^2 u^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{PolyLog}\left[4,-\frac{b x}{a}\right] - 6 q r t^2 u^2 \operatorname{Log}\left[i\left(j(h x)^t\right)^u\right] \operatorname{PolyLog}\left[4,-\frac{d x}{c}\right] + \\
& 6 p r t^3 u^3 \operatorname{PolyLog}\left[5,-\frac{b x}{a}\right] + 6 q r t^3 u^3 \operatorname{PolyLog}\left[5,-\frac{d x}{c}\right]
\end{aligned}$$



**Problem 57: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Log}[i (j (hx)^t)^u]^2 \text{Log}[e (f (a+bx)^p (c+dx)^q)^r]}{x} dx$$

Optimal (type 4, 262 leaves, 11 steps):

$$\begin{aligned} & - \frac{p r \text{Log}[i (j (hx)^t)^u]^3 \text{Log}[1 + \frac{bx}{a}]}{3 t u} + \\ & \frac{\text{Log}[i (j (hx)^t)^u]^3 \text{Log}[e (f (a+bx)^p (c+dx)^q)^r]}{3 t u} - \frac{q r \text{Log}[i (j (hx)^t)^u]^3 \text{Log}[1 + \frac{dx}{c}]}{3 t u} - \\ & p r \text{Log}[i (j (hx)^t)^u]^2 \text{PolyLog}[2, -\frac{bx}{a}] - q r \text{Log}[i (j (hx)^t)^u]^2 \text{PolyLog}[2, -\frac{dx}{c}] + \\ & 2 p r t u \text{Log}[i (j (hx)^t)^u] \text{PolyLog}[3, -\frac{bx}{a}] + 2 q r t u \text{Log}[i (j (hx)^t)^u] \text{PolyLog}[3, -\frac{dx}{c}] - \\ & 2 p r t^2 u^2 \text{PolyLog}[4, -\frac{bx}{a}] - 2 q r t^2 u^2 \text{PolyLog}[4, -\frac{dx}{c}] \end{aligned}$$

Result (type 4, 839 leaves):

$$\begin{aligned}
 & -p r t^2 u^2 \operatorname{Log}[x] \operatorname{Log}[h x]^2 \operatorname{Log}[a+b x]+p r t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}[a+b x]+ \\
 & 2 p r t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{Log}[a+b x]- \\
 & 2 p r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{Log}[a+b x]-p r \operatorname{Log}[x] \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right]^2 \operatorname{Log}[a+b x]+ \\
 & p r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right]^2 \operatorname{Log}[a+b x]-\frac{1}{3} p r t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}\left[1+\frac{b x}{a}\right]+ \\
 & p r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{Log}\left[1+\frac{b x}{a}\right]-p r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right]^2 \operatorname{Log}\left[1+\frac{b x}{a}\right]- \\
 & q r t^2 u^2 \operatorname{Log}[x] \operatorname{Log}[h x]^2 \operatorname{Log}[c+d x]+q r t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}[c+d x]+ \\
 & 2 q r t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{Log}[c+d x]- \\
 & 2 q r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{Log}[c+d x]- \\
 & q r \operatorname{Log}[x] \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right]^2 \operatorname{Log}[c+d x]+q r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right]^2 \operatorname{Log}[c+d x]+ \\
 & t^2 u^2 \operatorname{Log}[x] \operatorname{Log}[h x]^2 \operatorname{Log}\left[e\left(f\left(a+b x\right)^p\left(c+d x\right)^q\right)^r\right]- \\
 & \frac{2}{3} t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}\left[e\left(f\left(a+b x\right)^p\left(c+d x\right)^q\right)^r\right]- \\
 & 2 t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{Log}\left[e\left(f\left(a+b x\right)^p\left(c+d x\right)^q\right)^r\right]+ \\
 & t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{Log}\left[e\left(f\left(a+b x\right)^p\left(c+d x\right)^q\right)^r\right]+ \\
 & \operatorname{Log}[x] \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right]^2 \operatorname{Log}\left[e\left(f\left(a+b x\right)^p\left(c+d x\right)^q\right)^r\right]-\frac{1}{3} q r t^2 u^2 \operatorname{Log}[h x]^3 \operatorname{Log}\left[1+\frac{d x}{c}\right]+ \\
 & q r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{Log}\left[1+\frac{d x}{c}\right]-q r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right]^2 \operatorname{Log}\left[1+\frac{d x}{c}\right]- \\
 & p r \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right]^2 \operatorname{PolyLog}\left[2,-\frac{b x}{a}\right]-q r \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right]^2 \operatorname{PolyLog}\left[2,-\frac{d x}{c}\right]+ \\
 & 2 p r t u \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{PolyLog}\left[3,-\frac{b x}{a}\right]+2 q r t u \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{PolyLog}\left[3,-\frac{d x}{c}\right]- \\
 & 2 p r t^2 u^2 \operatorname{PolyLog}\left[4,-\frac{b x}{a}\right]-2 q r t^2 u^2 \operatorname{PolyLog}\left[4,-\frac{d x}{c}\right]
 \end{aligned}$$

**Problem 58: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{Log}\left[e\left(f\left(a+b x\right)^p\left(c+d x\right)^q\right)^r\right]}{x} d x$$

Optimal (type 4, 194 leaves, 9 steps):

$$\begin{aligned}
 & -\frac{p r \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right]^2 \operatorname{Log}\left[1+\frac{b x}{a}\right]}{2 t u}+\frac{\operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right]^2 \operatorname{Log}\left[e\left(f\left(a+b x\right)^p\left(c+d x\right)^q\right)^r\right]}{2 t u}- \\
 & \frac{q r \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right]^2 \operatorname{Log}\left[1+\frac{d x}{c}\right]}{2 t u}-p r \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{PolyLog}\left[2,-\frac{b x}{a}\right]- \\
 & q r \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{PolyLog}\left[2,-\frac{d x}{c}\right]+p r t u \operatorname{PolyLog}\left[3,-\frac{b x}{a}\right]+q r t u \operatorname{PolyLog}\left[3,-\frac{d x}{c}\right]
 \end{aligned}$$

Result (type 4, 451 leaves):

$$\begin{aligned}
 & p r t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}[a+b x] - p r t u \operatorname{Log}[h x]^2 \operatorname{Log}[a+b x] - \\
 & p r \operatorname{Log}[x] \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{Log}[a+b x] + p r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{Log}[a+b x] + \\
 & \frac{1}{2} p r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[1+\frac{b x}{a}\right] - p r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{Log}\left[1+\frac{b x}{a}\right] + \\
 & q r t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}[c+d x] - q r t u \operatorname{Log}[h x]^2 \operatorname{Log}[c+d x] - \\
 & q r \operatorname{Log}[x] \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{Log}[c+d x] + q r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{Log}[c+d x] - \\
 & t u \operatorname{Log}[x] \operatorname{Log}[h x] \operatorname{Log}\left[e\left(f\left(a+b x\right)^p\left(c+d x\right)^q\right)^r\right] + \\
 & \frac{1}{2} t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[e\left(f\left(a+b x\right)^p\left(c+d x\right)^q\right)^r\right] + \\
 & \operatorname{Log}[x] \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{Log}\left[e\left(f\left(a+b x\right)^p\left(c+d x\right)^q\right)^r\right] + \frac{1}{2} q r t u \operatorname{Log}[h x]^2 \operatorname{Log}\left[1+\frac{d x}{c}\right] - \\
 & q r \operatorname{Log}[h x] \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{Log}\left[1+\frac{d x}{c}\right] - p r \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{PolyLog}\left[2,-\frac{b x}{a}\right] - \\
 & q r \operatorname{Log}\left[i\left(j\left(h x\right)^t\right)^u\right] \operatorname{PolyLog}\left[2,-\frac{d x}{c}\right] + p r t u \operatorname{PolyLog}\left[3,-\frac{b x}{a}\right] + q r t u \operatorname{PolyLog}\left[3,-\frac{d x}{c}\right]
 \end{aligned}$$

**Problem 67: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^3 \operatorname{Log}[h(f+g x)^m]}{(a+b x)(c+d x)} dx$$

Optimal (type 4, 620 leaves, 14 steps):

$$\begin{aligned}
 & \frac{m \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^4 \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right]}{4(b c-a d) n} + \frac{\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^4 \operatorname{Log}[h(f+g x)^m]}{4(b c-a d) n} - \\
 & \frac{m \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^4 \operatorname{Log}\left[1-\frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{4(b c-a d) n} + \frac{m \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^3 \operatorname{PolyLog}\left[2,\frac{d(a+b x)}{b(c+d x)}\right]}{b c-a d} - \\
 & \frac{m \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^3 \operatorname{PolyLog}\left[2,\frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{b c-a d} - \frac{3 m n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 \operatorname{PolyLog}\left[3,\frac{d(a+b x)}{b(c+d x)}\right]}{b c-a d} + \\
 & \frac{3 m n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 \operatorname{PolyLog}\left[3,\frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{b c-a d} + \\
 & \frac{6 m n^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{PolyLog}\left[4,\frac{d(a+b x)}{b(c+d x)}\right]}{b c-a d} - \frac{6 m n^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{PolyLog}\left[4,\frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{b c-a d} \\
 & \frac{6 m n^3 \operatorname{PolyLog}\left[5,\frac{d(a+b x)}{b(c+d x)}\right]}{b c-a d} + \frac{6 m n^3 \operatorname{PolyLog}\left[5,\frac{(d f-c g)(a+b x)}{(b f-a g)(c+d x)}\right]}{b c-a d}
 \end{aligned}$$

Result (type 4, 31 404 leaves): Display of huge result suppressed!

### Problem 68: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 \text{Log}[h(f+gx)^m]}{(a+bx)(c+dx)} dx$$

Optimal (type 4, 496 leaves, 12 steps):

$$\begin{aligned} & \frac{m \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^3 \text{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{3(bc-ad)n} + \frac{\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^3 \text{Log}[h(f+gx)^m]}{3(bc-ad)n} - \\ & \frac{m \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^3 \text{Log}\left[1 - \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{3(bc-ad)n} + \frac{m \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 \text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{bc-ad} - \\ & \frac{m \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 \text{PolyLog}\left[2, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{bc-ad} - \frac{2mn \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \text{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right]}{bc-ad} + \\ & \frac{2mn \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \text{PolyLog}\left[3, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{bc-ad} + \\ & \frac{2mn^2 \text{PolyLog}\left[4, \frac{d(a+bx)}{b(c+dx)}\right]}{bc-ad} - \frac{2mn^2 \text{PolyLog}\left[4, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{bc-ad} \end{aligned}$$

Result (type 4, 25557 leaves): Display of huge result suppressed!

### Problem 69: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \text{Log}[h(f+gx)^m]}{(a+bx)(c+dx)} dx$$

Optimal (type 4, 371 leaves, 10 steps):

$$\begin{aligned} & \frac{m \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 \text{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{2(bc-ad)n} + \frac{\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 \text{Log}[h(f+gx)^m]}{2(bc-ad)n} - \\ & \frac{m \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 \text{Log}\left[1 - \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{2(bc-ad)n} + \frac{m \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{bc-ad} - \\ & \frac{m \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \text{PolyLog}\left[2, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{bc-ad} - \\ & \frac{mn \text{PolyLog}\left[3, \frac{d(a+bx)}{b(c+dx)}\right]}{bc-ad} + \frac{mn \text{PolyLog}\left[3, \frac{(df-cg)(a+bx)}{(bf-ag)(c+dx)}\right]}{bc-ad} \end{aligned}$$

Result (type 4, 6704 leaves):

$$\frac{1}{2(bc-ad)} m \text{Log}\left[\frac{a+bx}{c+dx}\right] \left( n \text{Log}\left[\frac{a+bx}{c+dx}\right] + 2 \left( \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \text{Log}\left[\frac{a+bx}{c+dx}\right] \right) \right) \text{Log}[f+gx] -$$

$$\begin{aligned}
 & \frac{1}{-b c + a d} \operatorname{Log}[a + b x] \left( \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) (-m \operatorname{Log}[f + g x] + \operatorname{Log}[h (f + g x)^m]) + \\
 & \frac{1}{-b c + a d} \left( \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \operatorname{Log}[c + d x] (-m \operatorname{Log}[f + g x] + \operatorname{Log}[h (f + g x)^m]) + \\
 & \frac{1}{-b c + a d} b d g m \left( \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \\
 & \left( \frac{a^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{2 b^3 \left(-\frac{a}{b} + \frac{c}{d}\right) d \left(-\frac{a}{b} + \frac{f}{g}\right) g} + \frac{c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{2 b \left(-\frac{a}{b} + \frac{c}{d}\right) d^3 \left(-\frac{c}{d} + \frac{f}{g}\right) g} + \right. \\
 & \left( \frac{a^2 \operatorname{Log}[a + b x]}{b (b c - a d) (b f - a g)} + \frac{c^2 \operatorname{Log}[c + d x]}{d (b c - a d) (-d f + c g)} + \frac{f^2 \operatorname{Log}[f + g x]}{g (b f - a g) (d f - c g)} \right) \\
 & \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) - \\
 & \frac{c^2 \left( \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[1 - \frac{d \left(\frac{a+x}{b}\right)}{-c + \frac{a d}{b}}\right] + \operatorname{PolyLog}\left[2, \frac{d \left(\frac{a+x}{b}\right)}{-c + \frac{a d}{b}}\right] \right)}{b \left(-\frac{a}{b} + \frac{c}{d}\right) d^3 \left(-\frac{c}{d} + \frac{f}{g}\right) g} - \\
 & \frac{f^2 \left( \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[1 - \frac{g \left(\frac{a+x}{b}\right)}{-f + \frac{a g}{b}}\right] + \operatorname{PolyLog}\left[2, \frac{g \left(\frac{a+x}{b}\right)}{-f + \frac{a g}{b}}\right] \right)}{b d \left(\frac{c}{d} - \frac{f}{g}\right) \left(-\frac{a}{b} + \frac{f}{g}\right) g^3} - \\
 & \frac{a^2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[1 - \frac{b \left(\frac{c+x}{d}\right)}{-a + \frac{b c}{d}}\right] + \operatorname{PolyLog}\left[2, \frac{b \left(\frac{c+x}{d}\right)}{-a + \frac{b c}{d}}\right] \right)}{b^3 \left(-\frac{a}{b} + \frac{c}{d}\right) d \left(-\frac{a}{b} + \frac{f}{g}\right) g} + \\
 & \left. \frac{f^2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[1 - \frac{g \left(\frac{c+x}{d}\right)}{-f + \frac{c g}{d}}\right] + \operatorname{PolyLog}\left[2, \frac{g \left(\frac{c+x}{d}\right)}{-f + \frac{c g}{d}}\right] \right)}{b d \left(\frac{c}{d} - \frac{f}{g}\right) \left(-\frac{a}{b} + \frac{f}{g}\right) g^3} \right) + \\
 & \frac{1}{-b c + a d} b c g m \left( \operatorname{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \\
 & \left( -\frac{a \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{2 b^2 \left(-\frac{a}{b} + \frac{c}{d}\right) d \left(-\frac{a}{b} + \frac{f}{g}\right) g} - \frac{c \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{2 b \left(-\frac{a}{b} + \frac{c}{d}\right) d^2 \left(-\frac{c}{d} + \frac{f}{g}\right) g} + \right. \\
 & \left( (a (d f - c g) \operatorname{Log}[a + b x] + (-b c f + a c g) \operatorname{Log}[c + d x] + (b c - a d) f \operatorname{Log}[f + g x]) \right. \\
 & \left. \left. \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( (b c - a d) (b f - a g) (-d f + c g) \right) + \frac{c \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ 1 - \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{a d}{b}} \right] + \operatorname{PolyLog} \left[ 2, \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{a d}{b}} \right] \right)}{b \left( -\frac{a}{b} + \frac{c}{d} \right) d^2 \left( -\frac{c}{d} + \frac{f}{g} \right) g} + \\
 & \frac{f \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ 1 - \frac{g \left( \frac{a+x}{b} \right)}{-f + \frac{a g}{b}} \right] + \operatorname{PolyLog} \left[ 2, \frac{g \left( \frac{a+x}{b} \right)}{-f + \frac{a g}{b}} \right] \right)}{b d \left( \frac{c}{d} - \frac{f}{g} \right) \left( -\frac{a}{b} + \frac{f}{g} \right) g^2} + \\
 & \frac{a \left( \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} \left[ 1 - \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{b c}{d}} \right] + \operatorname{PolyLog} \left[ 2, \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{b c}{d}} \right] \right)}{b^2 \left( -\frac{a}{b} + \frac{c}{d} \right) d \left( -\frac{a}{b} + \frac{f}{g} \right) g} - \\
 & \left. \frac{f \left( \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} \left[ 1 - \frac{g \left( \frac{c+x}{d} \right)}{-f + \frac{c g}{d}} \right] + \operatorname{PolyLog} \left[ 2, \frac{g \left( \frac{c+x}{d} \right)}{-f + \frac{c g}{d}} \right] \right)}{b d \left( \frac{c}{d} - \frac{f}{g} \right) \left( -\frac{a}{b} + \frac{f}{g} \right) g^2} \right) + \\
 & \frac{1}{-b c + a d} a d g m \left( \operatorname{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - n \operatorname{Log} \left[ \frac{a + b x}{c + d x} \right] \right) \\
 & \left( -\frac{a \operatorname{Log} \left[ \frac{a}{b} + x \right]^2}{2 b^2 \left( -\frac{a}{b} + \frac{c}{d} \right) d \left( -\frac{a}{b} + \frac{f}{g} \right) g} - \frac{c \operatorname{Log} \left[ \frac{c}{d} + x \right]^2}{2 b \left( -\frac{a}{b} + \frac{c}{d} \right) d^2 \left( -\frac{c}{d} + \frac{f}{g} \right) g} + \right. \\
 & \left. \left( (a (d f - c g) \operatorname{Log} [a + b x] + (-b c f + a c g) \operatorname{Log} [c + d x] + (b c - a d) f \operatorname{Log} [f + g x] \right) \right. \\
 & \left. \left( -\operatorname{Log} \left[ \frac{a}{b} + x \right] + \operatorname{Log} \left[ \frac{c}{d} + x \right] + \operatorname{Log} \left[ \frac{a}{c + d x} + \frac{b x}{c + d x} \right] \right) \right) / \\
 & \left( (b c - a d) (b f - a g) (-d f + c g) \right) + \frac{c \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ 1 - \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{a d}{b}} \right] + \operatorname{PolyLog} \left[ 2, \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{a d}{b}} \right] \right)}{b \left( -\frac{a}{b} + \frac{c}{d} \right) d^2 \left( -\frac{c}{d} + \frac{f}{g} \right) g} + \\
 & \frac{f \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ 1 - \frac{g \left( \frac{a+x}{b} \right)}{-f + \frac{a g}{b}} \right] + \operatorname{PolyLog} \left[ 2, \frac{g \left( \frac{a+x}{b} \right)}{-f + \frac{a g}{b}} \right] \right)}{b d \left( \frac{c}{d} - \frac{f}{g} \right) \left( -\frac{a}{b} + \frac{f}{g} \right) g^2} + \\
 & \frac{a \left( \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} \left[ 1 - \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{b c}{d}} \right] + \operatorname{PolyLog} \left[ 2, \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{b c}{d}} \right] \right)}{b^2 \left( -\frac{a}{b} + \frac{c}{d} \right) d \left( -\frac{a}{b} + \frac{f}{g} \right) g} - \\
 & \left. \frac{f \left( \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} \left[ 1 - \frac{g \left( \frac{c+x}{d} \right)}{-f + \frac{c g}{d}} \right] + \operatorname{PolyLog} \left[ 2, \frac{g \left( \frac{c+x}{d} \right)}{-f + \frac{c g}{d}} \right] \right)}{b d \left( \frac{c}{d} - \frac{f}{g} \right) \left( -\frac{a}{b} + \frac{f}{g} \right) g^2} \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{-bc+ad} bcgn \left( -m \operatorname{Log}[f+gx] + \operatorname{Log}[h(f+gx)^m] \right) \\
 & \left( -\frac{a \operatorname{Log}\left[\frac{a}{b}+x\right]^2}{2b^2\left(-\frac{a}{b}+\frac{c}{d}\right)d\left(-\frac{a}{b}+\frac{f}{g}\right)g} - \frac{c \operatorname{Log}\left[\frac{c}{d}+x\right]^2}{2b\left(-\frac{a}{b}+\frac{c}{d}\right)d^2\left(-\frac{c}{d}+\frac{f}{g}\right)g} + \right. \\
 & \left. \left( (adf-cg) \operatorname{Log}[a+bx] + (-bcf+acg) \operatorname{Log}[c+dx] + (bc-ad) f \operatorname{Log}[f+gx] \right) \right. \\
 & \left. \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right) \right) / \\
 & \left( (bc-ad)(bf-ag)(-df+cg) \right) + \frac{c \left( \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[1 - \frac{d\left(\frac{a+x}{b}\right)}{-c+\frac{ad}{b}}\right] + \operatorname{PolyLog}\left[2, \frac{d\left(\frac{a+x}{b}\right)}{-c+\frac{ad}{b}}\right] \right)}{b\left(-\frac{a}{b}+\frac{c}{d}\right)d^2\left(-\frac{c}{d}+\frac{f}{g}\right)g} + \\
 & \frac{f \left( \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[1 - \frac{g\left(\frac{a+x}{b}\right)}{-f+\frac{ag}{b}}\right] + \operatorname{PolyLog}\left[2, \frac{g\left(\frac{a+x}{b}\right)}{-f+\frac{ag}{b}}\right] \right)}{bd\left(\frac{c}{d}-\frac{f}{g}\right)\left(-\frac{a}{b}+\frac{f}{g}\right)g^2} + \\
 & \frac{a \left( \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[1 - \frac{b\left(\frac{c+x}{d}\right)}{-a+\frac{bc}{d}}\right] + \operatorname{PolyLog}\left[2, \frac{b\left(\frac{c+x}{d}\right)}{-a+\frac{bc}{d}}\right] \right)}{b^2\left(-\frac{a}{b}+\frac{c}{d}\right)d\left(-\frac{a}{b}+\frac{f}{g}\right)g} - \\
 & \left. \frac{f \left( \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[1 - \frac{g\left(\frac{c+x}{d}\right)}{-f+\frac{cg}{d}}\right] + \operatorname{PolyLog}\left[2, \frac{g\left(\frac{c+x}{d}\right)}{-f+\frac{cg}{d}}\right] \right)}{bd\left(\frac{c}{d}-\frac{f}{g}\right)\left(-\frac{a}{b}+\frac{f}{g}\right)g^2} \right) + \\
 & \frac{1}{-bc+ad} adgn \left( -m \operatorname{Log}[f+gx] + \operatorname{Log}[h(f+gx)^m] \right) \\
 & \left( -\frac{a \operatorname{Log}\left[\frac{a}{b}+x\right]^2}{2b^2\left(-\frac{a}{b}+\frac{c}{d}\right)d\left(-\frac{a}{b}+\frac{f}{g}\right)g} - \frac{c \operatorname{Log}\left[\frac{c}{d}+x\right]^2}{2b\left(-\frac{a}{b}+\frac{c}{d}\right)d^2\left(-\frac{c}{d}+\frac{f}{g}\right)g} + \right. \\
 & \left. \left( (adf-cg) \operatorname{Log}[a+bx] + (-bcf+acg) \operatorname{Log}[c+dx] + (bc-ad) f \operatorname{Log}[f+gx] \right) \right. \\
 & \left. \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right) \right) / \\
 & \left( (bc-ad)(bf-ag)(-df+cg) \right) + \frac{c \left( \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[1 - \frac{d\left(\frac{a+x}{b}\right)}{-c+\frac{ad}{b}}\right] + \operatorname{PolyLog}\left[2, \frac{d\left(\frac{a+x}{b}\right)}{-c+\frac{ad}{b}}\right] \right)}{b\left(-\frac{a}{b}+\frac{c}{d}\right)d^2\left(-\frac{c}{d}+\frac{f}{g}\right)g} +
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{f \left( \text{Log} \left[ \frac{a}{b} + x \right] \text{Log} \left[ 1 - \frac{g \left( \frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right] + \text{PolyLog} \left[ 2, \frac{g \left( \frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right] \right)}{b d \left( \frac{c}{d} - \frac{f}{g} \right) \left( -\frac{a}{b} + \frac{f}{g} \right) g^2} + \right. \\
 & \frac{a \left( \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ 1 - \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] + \text{PolyLog} \left[ 2, \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] \right)}{b^2 \left( -\frac{a}{b} + \frac{c}{d} \right) d \left( -\frac{a}{b} + \frac{f}{g} \right) g} - \\
 & \left. \frac{f \left( \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ 1 - \frac{g \left( \frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right] + \text{PolyLog} \left[ 2, \frac{g \left( \frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right] \right)}{b d \left( \frac{c}{d} - \frac{f}{g} \right) \left( -\frac{a}{b} + \frac{f}{g} \right) g^2} \right) + \\
 & \frac{1}{-b c + a d} a c g m \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \\
 & \left( \frac{\text{Log} \left[ \frac{a}{b} + x \right]^2}{2 b \left( -\frac{a}{b} + \frac{c}{d} \right) d \left( -\frac{a}{b} + \frac{f}{g} \right) g} + \frac{\text{Log} \left[ \frac{c}{d} + x \right]^2}{2 b \left( -\frac{a}{b} + \frac{c}{d} \right) d \left( -\frac{c}{d} + \frac{f}{g} \right) g} + \right. \\
 & \left( (b (-d f + c g) \text{Log} [a + b x] + d (b f - a g) \text{Log} [c + d x] + (-b c + a d) g \text{Log} [f + g x]) \right. \\
 & \left. \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c + d x} + \frac{b x}{c + d x} \right] \right) \right) / \\
 & \left. \left( (b c - a d) (b f - a g) (-d f + c g) \right) - \frac{\text{Log} \left[ \frac{a}{b} + x \right] \text{Log} \left[ 1 - \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{ad}{b}} \right] + \text{PolyLog} \left[ 2, \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{ad}{b}} \right]}{b \left( -\frac{a}{b} + \frac{c}{d} \right) d \left( -\frac{c}{d} + \frac{f}{g} \right) g} - \right. \\
 & \frac{\text{Log} \left[ \frac{a}{b} + x \right] \text{Log} \left[ 1 - \frac{g \left( \frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right] + \text{PolyLog} \left[ 2, \frac{g \left( \frac{a+x}{b} \right)}{-f + \frac{ag}{b}} \right]}{b d \left( \frac{c}{d} - \frac{f}{g} \right) \left( -\frac{a}{b} + \frac{f}{g} \right) g} - \\
 & \frac{\text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ 1 - \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] + \text{PolyLog} \left[ 2, \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right]}{b \left( -\frac{a}{b} + \frac{c}{d} \right) d \left( -\frac{a}{b} + \frac{f}{g} \right) g} + \\
 & \left. \frac{\text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ 1 - \frac{g \left( \frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right] + \text{PolyLog} \left[ 2, \frac{g \left( \frac{c+x}{d} \right)}{-f + \frac{cg}{d}} \right]}{b d \left( \frac{c}{d} - \frac{f}{g} \right) \left( -\frac{a}{b} + \frac{f}{g} \right) g} \right) - \\
 & \frac{1}{-b c + a d} b c f n \left( -m \text{Log} [f + g x] + \text{Log} [h (f + g x)^m] \right)
 \end{aligned}$$



$$\left( \frac{\text{Log}\left[\frac{a}{b} + x\right]^2}{2b\left(-\frac{a}{b} + \frac{c}{d}\right)d\left(-\frac{a}{b} + \frac{f}{g}\right)g} + \frac{\text{Log}\left[\frac{c}{d} + x\right]^2}{2b\left(-\frac{a}{b} + \frac{c}{d}\right)d\left(-\frac{c}{d} + \frac{f}{g}\right)g} + \right.$$

$$\left. \left( (b(-df+cg)\text{Log}[a+bx] + d(bf-ag)\text{Log}[c+dx] + (-bc+ad)g\text{Log}[f+gx]) \right. \right.$$

$$\left. \left. \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right) \right) \right) /$$

$$\frac{\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[1 - \frac{d\left(\frac{a+x}{b}\right)}{-c + \frac{ad}{b}}\right] + \text{PolyLog}\left[2, \frac{d\left(\frac{a+x}{b}\right)}{-c + \frac{ad}{b}}\right]}{(bc-ad)(bf-ag)(-df+cg)g} -$$

$$\frac{\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[1 - \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right] + \text{PolyLog}\left[2, \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right]}{bd\left(\frac{c}{d} - \frac{f}{g}\right)\left(-\frac{a}{b} + \frac{f}{g}\right)g} -$$

$$\frac{\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[1 - \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{bc}{d}}\right] + \text{PolyLog}\left[2, \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{bc}{d}}\right]}{b\left(-\frac{a}{b} + \frac{c}{d}\right)d\left(-\frac{a}{b} + \frac{f}{g}\right)g} +$$

$$\left. \frac{\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[1 - \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right] + \text{PolyLog}\left[2, \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right]}{bd\left(\frac{c}{d} - \frac{f}{g}\right)\left(-\frac{a}{b} + \frac{f}{g}\right)g} \right) +$$

$$\frac{1}{-bc+ad} a d f n \left( -m \text{Log}[f+gx] + \text{Log}[h(f+gx)^m] \right)$$

$$\left( \frac{\text{Log}\left[\frac{a}{b} + x\right]^2}{2b\left(-\frac{a}{b} + \frac{c}{d}\right)d\left(-\frac{a}{b} + \frac{f}{g}\right)g} + \frac{\text{Log}\left[\frac{c}{d} + x\right]^2}{2b\left(-\frac{a}{b} + \frac{c}{d}\right)d\left(-\frac{c}{d} + \frac{f}{g}\right)g} + \right.$$

$$\left. \left( (b(-df+cg)\text{Log}[a+bx] + d(bf-ag)\text{Log}[c+dx] + (-bc+ad)g\text{Log}[f+gx]) \right. \right.$$

$$\left. \left. \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right) \right) \right) /$$

$$\frac{\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[1 - \frac{d\left(\frac{a+x}{b}\right)}{-c + \frac{ad}{b}}\right] + \text{PolyLog}\left[2, \frac{d\left(\frac{a+x}{b}\right)}{-c + \frac{ad}{b}}\right]}{(bc-ad)(bf-ag)(-df+cg)g} -$$

$$\frac{\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[1 - \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right] + \text{PolyLog}\left[2, \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right]}{bd\left(\frac{c}{d} - \frac{f}{g}\right)\left(-\frac{a}{b} + \frac{f}{g}\right)g} -$$

$$\begin{aligned}
 & \frac{\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[1 - \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{bc}{d}}\right] + \text{PolyLog}\left[2, \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{bc}{d}}\right]}{b\left(-\frac{a}{b} + \frac{c}{d}\right) d\left(-\frac{a}{b} + \frac{f}{g}\right) g} + \\
 & \left. \frac{\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[1 - \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right] + \text{PolyLog}\left[2, \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right]}{b d\left(\frac{c}{d} - \frac{f}{g}\right)\left(-\frac{a}{b} + \frac{f}{g}\right) g} \right) - \\
 & \frac{1}{2(b c - a d)} g m n \left( \frac{\text{Log}[f + g x] \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right]\right)^2}{g} + \right. \\
 & 2\left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right]\right) \\
 & \left. \frac{\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[1 - \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right] + \text{PolyLog}\left[2, \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right]}{g} - \right. \\
 & \left. \frac{\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[1 - \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right] + \text{PolyLog}\left[2, \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right]}{g} \right) + \frac{1}{g} \\
 & 2\left(\frac{1}{2} \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[1 - \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right] + \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right] - \right. \\
 & \text{PolyLog}\left[3, \frac{g\left(\frac{a+x}{b}\right)}{-f + \frac{ag}{b}}\right] + \frac{1}{g} \left(\frac{1}{2} \text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[1 - \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right] + \right. \\
 & \left. \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right] - \text{PolyLog}\left[3, \frac{g\left(\frac{c+x}{d}\right)}{-f + \frac{cg}{d}}\right] \right) - \\
 & \frac{1}{g} 2\left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \frac{1}{2} \text{Log}\left[\frac{dg\left(\frac{c+x}{d}\right)}{-df+cg}\right] \right. \\
 & \left. \left(-2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{dg\left(\frac{c+x}{d}\right)}{-df+cg}\right]\right) \left(\text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \text{Log}\left[-\frac{d(f+gx)}{-df+cg}\right]\right) + \right. \\
 & \left. \text{Log}\left[\frac{dg\left(\frac{c+x}{d}\right)}{-df+cg}\right] \text{Log}\left[-\frac{d(bf-ag)\left(\frac{c+x}{d}\right)}{b(-df+cg)\left(\frac{a}{b} + x\right)}\right] \left(-\text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] + \text{Log}\left[-\frac{d(f+gx)}{-df+cg}\right]\right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2} \operatorname{Log} \left[ -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right]^2 \left( \operatorname{Log} \left[ \frac{-b c + a d}{b d \left(\frac{a}{b} + x\right)} \right] + \operatorname{Log} \left[ \frac{b (f + g x)}{b f - a g} \right] - \right. \\
 & \left. \operatorname{Log} \left[ -\frac{(-b c + a d) (f + g x)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) + \left( \operatorname{Log} \left[ \frac{c}{d} + x \right] - \operatorname{Log} \left[ -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) \\
 & \operatorname{PolyLog} \left[ 2, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right] + \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] + \operatorname{Log} \left[ -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) \\
 & \operatorname{PolyLog} \left[ 2, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] + \operatorname{Log} \left[ -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \left( \operatorname{PolyLog} \left[ 2, \frac{c}{d} + x \right] - \right. \\
 & \left. \operatorname{PolyLog} \left[ 2, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right) - \operatorname{PolyLog} \left[ 3, -\frac{b g \left(\frac{a}{b} + x\right)}{b f - a g} \right] - \\
 & \left. \operatorname{PolyLog} \left[ 3, \frac{d g \left(\frac{c}{d} + x\right)}{-d f + c g} \right] - \operatorname{PolyLog} \left[ 3, \frac{c}{d} + x \right] + \operatorname{PolyLog} \left[ 3, -\frac{d (b f - a g) \left(\frac{c}{d} + x\right)}{b (-d f + c g) \left(\frac{a}{b} + x\right)} \right] \right)
 \end{aligned}$$

Problem 90: Unable to integrate problem.

$$\int \frac{\operatorname{Log} \left[ \frac{a}{a+b x} \right] \operatorname{Log} \left[ \frac{c x}{a+b x} \right]^2}{x (a+b x)} dx$$

Optimal (type 4, 82 leaves, 3 steps):

$$-\frac{\operatorname{Log} \left[ \frac{c x}{a+b x} \right]^2 \operatorname{PolyLog} \left[ 2, 1 - \frac{a}{a+b x} \right]}{a} + \frac{2 \operatorname{Log} \left[ \frac{c x}{a+b x} \right] \operatorname{PolyLog} \left[ 3, 1 - \frac{a}{a+b x} \right]}{a} - \frac{2 \operatorname{PolyLog} \left[ 4, 1 - \frac{a}{a+b x} \right]}{a}$$

Result (type 8, 36 leaves):

$$\int \frac{\operatorname{Log} \left[ \frac{a}{a+b x} \right] \operatorname{Log} \left[ \frac{c x}{a+b x} \right]^2}{x (a+b x)} dx$$

Problem 91: Unable to integrate problem.

$$\int \frac{\operatorname{Log} \left[ \frac{b c - a d}{b (c+d x)} \right] \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right]^2}{(c+d x) (a g + b g x)} dx$$

Optimal (type 4, 150 leaves, 3 steps):

$$\begin{aligned}
& - \frac{\text{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]^2 \text{PolyLog}\left[2, 1 - \frac{bc-ad}{b(c+dx)}\right]}{(bc-ad)g} + \\
& \frac{2 \text{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right] \text{PolyLog}\left[3, 1 - \frac{bc-ad}{b(c+dx)}\right]}{(bc-ad)g} - \frac{2 \text{PolyLog}\left[4, 1 - \frac{bc-ad}{b(c+dx)}\right]}{(bc-ad)g}
\end{aligned}$$

Result (type 8, 57 leaves):

$$\int \frac{\text{Log}\left[\frac{bc-ad}{b(c+dx)}\right] \text{Log}\left[\frac{e^{(a+bx)}}{c+dx}\right]^2}{(c+dx)(ag+bgx)} dx$$

**Problem 92: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 \text{Log}\left[\frac{bc-ad}{b(c+dx)}\right]}{(c+dx)(ag+bgx)} dx$$

Optimal (type 4, 160 leaves, 3 steps):

$$\begin{aligned}
& - \frac{\text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]^2 \text{PolyLog}\left[2, 1 - \frac{bc-ad}{b(c+dx)}\right]}{(bc-ad)g} + \\
& \frac{2n \text{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \text{PolyLog}\left[3, 1 - \frac{bc-ad}{b(c+dx)}\right]}{(bc-ad)g} - \frac{2n^2 \text{PolyLog}\left[4, 1 - \frac{bc-ad}{b(c+dx)}\right]}{(bc-ad)g}
\end{aligned}$$

Result (type 4, 785 leaves):

$$\begin{aligned}
 & \frac{1}{3 (b c - a d) g} \\
 & \left( \text{Log}\left[\frac{a+b x}{c+d x}\right] \left( 3 \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 - 3 n \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \text{Log}\left[\frac{a+b x}{c+d x}\right] + n^2 \text{Log}\left[\frac{a+b x}{c+d x}\right]^2 \right) \right. \\
 & \quad \left. \text{Log}\left[\frac{b c - a d}{b c + b d x}\right] + \frac{3}{2} \left( \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right] \right)^2 \right. \\
 & \quad \left( -\text{Log}\left[\frac{c}{d} + x\right]^2 - 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c+d x] + 2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[c+d x] + \right. \\
 & \quad \left. 2 \text{Log}\left[\frac{a+b x}{c+d x}\right] \text{Log}[c+d x] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + 2 \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) + \\
 & \quad n \left( \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) \\
 & \quad \left( \text{Log}\left[\frac{c}{d} + x\right]^3 + 3 \text{Log}\left[\frac{c}{d} + x\right]^2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] \right) + \right. \\
 & \quad \left. 3 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a+b x}{c+d x}\right] \right)^2 \text{Log}[c+d x] + 3 \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \right. \\
 & \quad \left. 6 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] + 3 \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) \right. \\
 & \quad \left. \left( \text{Log}\left[\frac{c}{d} + x\right]^2 - 2 \left( \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) \right) + 6 \text{Log}\left[\frac{c}{d} + x\right] \right. \\
 & \quad \left. \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] - 6 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c + a d}\right] - 6 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c - a d}\right] \right) - \\
 & \quad n^2 \left( \text{Log}\left[\frac{a+b x}{c+d x}\right]^3 \text{Log}\left[\frac{b c - a d}{b c + b d x}\right] + 3 \text{Log}\left[\frac{a+b x}{c+d x}\right]^2 \text{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right] - \right. \\
 & \quad \left. 6 \text{Log}\left[\frac{a+b x}{c+d x}\right] \text{PolyLog}\left[3, \frac{d(a+b x)}{b(c+d x)}\right] + 6 \text{PolyLog}\left[4, \frac{d(a+b x)}{b(c+d x)}\right] \right)
 \end{aligned}$$

### Problem 98: Unable to integrate problem.

$$\int \text{Log}\left[\frac{c(b+a x)^2}{x^2}\right]^3 dx$$

Optimal (type 4, 102 leaves, 5 steps):

$$\begin{aligned}
 & x \text{Log}\left[\frac{c(b+a x)^2}{x^2}\right]^3 - \frac{6 b \text{Log}\left[\frac{c(b+a x)^2}{x^2}\right]^2 \text{Log}\left[1 - \frac{a x}{b+a x}\right]}{a} + \\
 & \frac{24 b \text{Log}\left[\frac{c(b+a x)^2}{x^2}\right] \text{PolyLog}\left[2, \frac{a x}{b+a x}\right]}{a} + \frac{48 b \text{PolyLog}\left[3, \frac{a x}{b+a x}\right]}{a}
 \end{aligned}$$

Result (type 8, 17 leaves):

$$\int \text{Log}\left[\frac{c(b+a x)^2}{x^2}\right]^3 dx$$

### Problem 101: Unable to integrate problem.

$$\int \text{Log} \left[ \frac{c x^2}{(b + a x)^2} \right]^3 dx$$

Optimal (type 4, 98 leaves, 5 steps):

$$x \text{Log} \left[ \frac{c x^2}{(b + a x)^2} \right]^3 + \frac{6 b \text{Log} \left[ \frac{c x^2}{(b + a x)^2} \right]^2 \text{Log} \left[ \frac{b}{b + a x} \right]}{a} +$$

$$\frac{24 b \text{Log} \left[ \frac{c x^2}{(b + a x)^2} \right] \text{PolyLog} \left[ 2, \frac{a x}{b + a x} \right]}{a} - \frac{48 b \text{PolyLog} \left[ 3, \frac{a x}{b + a x} \right]}{a}$$

Result (type 8, 17 leaves):

$$\int \text{Log} \left[ \frac{c x^2}{(b + a x)^2} \right]^3 dx$$

### Problem 102: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{PolyLog} \left[ 2, 1 + \frac{b c - a d}{d (a + b x)} \right]}{(a + b x) (c + d x)} dx$$

Optimal (type 4, 35 leaves, 1 step):

$$- \frac{\text{PolyLog} \left[ 3, 1 + \frac{b c - a d}{d (a + b x)} \right]}{b c - a d}$$

Result (type 4, 1037 leaves):

$$\begin{aligned}
 & \frac{(\text{Log}[a+bx] - \text{Log}[c+dx]) \text{PolyLog}\left[2, \frac{bc}{d(a+bx)} + \frac{bx}{a+bx}\right]}{bc - ad} - \\
 & \frac{1}{6bc - 6ad} \left( -3 \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] + 3 \text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] + \right. \\
 & 2 \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right]^3 - 3 \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}[a+bx] + 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a+bx] + \\
 & 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \text{Log}[a+bx] + 6 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \text{Log}[a+bx] + \\
 & 6 \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right]^2 \text{Log}[a+bx] + 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a+bx]^2 + 6 \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \text{Log}[a+bx]^2 - \\
 & 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 3 \text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] - \\
 & 6 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 9 \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}[c+dx] - \\
 & 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[c+dx] + 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \text{Log}[c+dx] - \\
 & 6 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \text{Log}[c+dx] - 12 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a+bx] \text{Log}[c+dx] - \\
 & 12 \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \text{Log}[a+bx] \text{Log}[c+dx] + 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c+dx]^2 + \\
 & 6 \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \text{Log}[c+dx]^2 - 9 \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \\
 & 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \\
 & 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a+bx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c+dx] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
 & 6 \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] - \text{Log}[a+bx] + \text{Log}[c+dx] \right) \\
 & \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 6 \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \right) \\
 & \left. \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - 6 \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - 6 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right)
 \end{aligned}$$

**Problem 103: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \text{Log}\left[\frac{e(c+dx)}{a+bx}\right]}{(a+bx)(c+dx)} dx$$

Optimal (type 4, 85 leaves, 2 steps):

$$\frac{\text{Log}\left[\frac{e(c+dx)}{a+bx}\right] \text{PolyLog}\left[2, 1 + \frac{bc-ad}{d(a+bx)}\right]}{bc-ad} - \frac{\text{PolyLog}\left[3, 1 + \frac{bc-ad}{d(a+bx)}\right]}{bc-ad}$$

Result (type 4, 617 leaves):

$$\begin{aligned} & \frac{1}{6(bc-ad)} \left( 2 \text{Log}\left[\frac{a}{b} + x\right]^3 + 3 \text{Log}\left[\frac{c}{d} + x\right]^2 \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) + \right. \\ & 3 \text{Log}\left[\frac{a}{b} + x\right]^2 \left( -\text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + 6 \left( \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \right) \\ & \left. \left( \text{Log}[a+bx] - \text{Log}[c+dx] \right) \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{e(c+dx)}{a+bx}\right] \right) + \right. \\ & 6 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 3 \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{e(c+dx)}{a+bx}\right] \right) \\ & \left. \left( \text{Log}\left[\frac{a}{b} + x\right]^2 - 2 \left( \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) \right) - \\ & 6 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - 3 \left( \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \right) \\ & \left( \text{Log}\left[\frac{a}{b} + x\right]^2 + \text{Log}\left[\frac{c}{d} + x\right]^2 - 2 \left( \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) - \\ & 2 \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) - \\ & 6 \left( \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - \right. \\ & \left. 2 \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] \right) - 6 \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] + 6 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \end{aligned}$$

**Problem 104: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2}{a+bx} dx$$

Optimal (type 4, 140 leaves, 4 steps):

$$\frac{\text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2}{b} - \frac{2 \text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{b} + \frac{2 \text{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right]}{b}$$

Result (type 4, 363 leaves):



$$\begin{aligned} & \frac{1}{3b} \left( \text{Log}\left[\frac{a}{b} + x\right]^3 + 3 \text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 3 \text{Log}\left[\frac{a}{b} + x\right]^2 \left( -\text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) \right) + \\ & 3 \text{Log}[a+bx] \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \right)^2 + \\ & 6 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 6 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - \\ & 3 \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \right) \\ & \left( \text{Log}\left[\frac{a}{b} + x\right]^2 - 2 \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) - \\ & 6 \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - 6 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \end{aligned}$$

### Problem 105: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[\frac{e(c+dx)}{a+bx}\right] \text{Log}\left[\frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)}\right]}{(a+bx)(c+dx)} dx$$

Optimal (type 4, 109 leaves, 2 steps):

$$\frac{\text{Log}\left[\frac{e(c+dx)}{a+bx}\right] \text{PolyLog}\left[2, 1 + \frac{(bc-ad)(e+fx)}{(de-cf)(a+bx)}\right]}{bc-ad} - \frac{\text{PolyLog}\left[3, 1 + \frac{(bc-ad)(e+fx)}{(de-cf)(a+bx)}\right]}{bc-ad}$$

Result (type 4, 1681 leaves):

$$\begin{aligned} & -\frac{1}{6bc-6ad} \left( -2 \text{Log}\left[\frac{a}{b} + x\right]^3 + 3 \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}[a+bx] - 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a+bx] + \right. \\ & 3 \text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}[a+bx] + 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] - \\ & 3 \text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 3 \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\ & 3 \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[\frac{e(c+dx)}{a+bx}\right] + 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a+bx] \text{Log}\left[\frac{e(c+dx)}{a+bx}\right] - \\ & 6 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a+bx] \text{Log}\left[\frac{e(c+dx)}{a+bx}\right] + 6 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \text{Log}\left[\frac{e(c+dx)}{a+bx}\right] + \\ & 3 \text{Log}[a+bx] \text{Log}\left[\frac{e(c+dx)}{a+bx}\right]^2 + 3 \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2 - \\ & 3 \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}[e+fx] + 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[e+fx] - \\ & 3 \text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}[e+fx] - 6 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{e(c+dx)}{a+bx}\right] \text{Log}[e+fx] + \\ & 6 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{e(c+dx)}{a+bx}\right] \text{Log}[e+fx] - 3 \text{Log}\left[\frac{e(c+dx)}{a+bx}\right]^2 \text{Log}[e+fx] + \end{aligned}$$

$$\begin{aligned}
& 3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(e+fx)}{be-af}\right] - 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \operatorname{Log}\left[\frac{b(e+fx)}{be-af}\right] + \\
& 3 \operatorname{Log}\left[\frac{f(c+dx)}{-de+cf}\right]^2 \operatorname{Log}\left[\frac{b(e+fx)}{be-af}\right] + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{e(c+dx)}{a+bx}\right] \operatorname{Log}\left[\frac{b(e+fx)}{be-af}\right] - \\
& 6 \operatorname{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \operatorname{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \operatorname{Log}\left[\frac{b(e+fx)}{be-af}\right] + \\
& 3 \operatorname{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2 \operatorname{Log}\left[\frac{b(e+fx)}{be-af}\right] - 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(e+fx)}{de-cf}\right] + \\
& 3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(e+fx)}{de-cf}\right] + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \operatorname{Log}\left[\frac{d(e+fx)}{de-cf}\right] - \\
& 3 \operatorname{Log}\left[\frac{f(c+dx)}{-de+cf}\right]^2 \operatorname{Log}\left[\frac{d(e+fx)}{de-cf}\right] - 6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{e(c+dx)}{a+bx}\right] \operatorname{Log}\left[\frac{d(e+fx)}{de-cf}\right] + \\
& 6 \operatorname{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \operatorname{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \operatorname{Log}\left[\frac{d(e+fx)}{de-cf}\right] + \\
& 3 \operatorname{Log}\left[\frac{e(c+dx)}{a+bx}\right]^2 \operatorname{Log}\left[\frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)}\right] - \\
& 3 \operatorname{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2 \operatorname{Log}\left[\frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)}\right] + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + \\
& 6 \left( \operatorname{Log}\left[\frac{e(c+dx)}{a+bx}\right] - \operatorname{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \right) \operatorname{PolyLog}\left[2, \frac{f(a+bx)}{-be+af}\right] + \\
& 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 6 \operatorname{Log}\left[\frac{e(c+dx)}{a+bx}\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - \\
& 6 \operatorname{Log}\left[\frac{e(c+dx)}{a+bx}\right] \operatorname{PolyLog}\left[2, \frac{f(c+dx)}{-de+cf}\right] + 6 \operatorname{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \\
& \operatorname{PolyLog}\left[2, \frac{f(c+dx)}{-de+cf}\right] + 6 \operatorname{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] - \\
& 6 \operatorname{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \operatorname{PolyLog}\left[2, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] - 6 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - \\
& 6 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right] + 6 \operatorname{PolyLog}\left[3, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]
\end{aligned}$$

**Problem 106: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2}{(a+bx)(e+fx)} dx$$

Optimal (type 4, 204 leaves, 4 steps):

$$\frac{\text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2 \text{Log}\left[1 - \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{be-af} - \frac{2 \text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \text{PolyLog}\left[2, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{be-af} + \frac{2 \text{PolyLog}\left[3, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{be-af}$$

Result (type 4, 1636 leaves):

$$\begin{aligned}
 & \frac{1}{3be-3af} \left( -2 \text{Log}\left[\frac{a}{b}+x\right]^3 + 3 \text{Log}\left[\frac{a}{b}+x\right]^2 \text{Log}[a+bx] - 6 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{c}{d}+x\right] \text{Log}[a+bx] + \right. \\
 & 3 \text{Log}\left[\frac{c}{d}+x\right]^2 \text{Log}[a+bx] + 6 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] - \\
 & 3 \text{Log}\left[\frac{c}{d}+x\right]^2 \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 3 \text{Log}\left[\frac{a}{b}+x\right]^2 \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \\
 & 3 \text{Log}\left[\frac{a}{b}+x\right]^2 \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] + 6 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}[a+bx] \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] - \\
 & 6 \text{Log}\left[\frac{c}{d}+x\right] \text{Log}[a+bx] \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] + \\
 & 6 \text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] + \\
 & 3 \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right]^2 + 3 \text{Log}[a+bx] \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right]^2 - \\
 & 3 \text{Log}\left[\frac{a}{b}+x\right]^2 \text{Log}[e+fx] + 6 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{c}{d}+x\right] \text{Log}[e+fx] - \\
 & 3 \text{Log}\left[\frac{c}{d}+x\right]^2 \text{Log}[e+fx] - 6 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \text{Log}[e+fx] + \\
 & 6 \text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \text{Log}[e+fx] - \\
 & 3 \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right]^2 \text{Log}[e+fx] + 3 \text{Log}\left[\frac{a}{b}+x\right]^2 \text{Log}\left[\frac{b(e+fx)}{be-af}\right] - \\
 & 6 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \text{Log}\left[\frac{b(e+fx)}{be-af}\right] + 3 \text{Log}\left[\frac{f(c+dx)}{-de+cf}\right]^2 \text{Log}\left[\frac{b(e+fx)}{be-af}\right] + \\
 & 6 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \text{Log}\left[\frac{b(e+fx)}{be-af}\right] - \\
 & 6 \text{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \text{Log}\left[\frac{b(e+fx)}{be-af}\right] + \\
 & 3 \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right]^2 \text{Log}\left[\frac{b(e+fx)}{be-af}\right] - 6 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] + \\
 & 3 \text{Log}\left[\frac{c}{d}+x\right]^2 \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] + 6 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] - \\
 & 3 \text{Log}\left[\frac{f(c+dx)}{-de+cf}\right]^2 \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] - 6 \text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] +
 \end{aligned}$$

$$\begin{aligned}
 & 6 \operatorname{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \operatorname{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \operatorname{Log}\left[\frac{d(e+fx)}{de-cf}\right] - \\
 & 3 \operatorname{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right]^2 \operatorname{Log}\left[\frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)}\right] + \\
 & 6 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 6 \left( \operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \right) \\
 & \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 6 \operatorname{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] - \\
 & 6 \operatorname{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \operatorname{PolyLog}\left[2, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] - 6 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - \\
 & 6 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right] + 6 \operatorname{PolyLog}\left[3, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]
 \end{aligned}$$

**Problem 107: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2}{e+fx} dx$$

Optimal (type 4, 322 leaves, 9 steps):

$$\begin{aligned}
 & -\frac{\operatorname{Log}\left[-\frac{bc-ad}{d(a+bx)}\right] \operatorname{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2}{f} + \frac{\operatorname{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2 \operatorname{Log}\left[1-\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{f} - \\
 & \frac{2 \operatorname{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{f} + \frac{2 \operatorname{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \operatorname{PolyLog}\left[2, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{f} + \\
 & \frac{2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right]}{f} - \frac{2 \operatorname{PolyLog}\left[3, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{f}
 \end{aligned}$$

Result (type 4, 1080 leaves):

$$\begin{aligned}
 & \frac{1}{f} \left( -\operatorname{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] \operatorname{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right]^2 + \right. \\
 & \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}[e+fx] - 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[e+fx] + \\
 & \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}[e+fx] + 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \operatorname{Log}[e+fx] - \\
 & 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \operatorname{Log}[e+fx] + \operatorname{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right]^2 \operatorname{Log}[e+fx] - \\
 & \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(e+fx)}{be-af}\right] + 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \operatorname{Log}\left[\frac{b(e+fx)}{be-af}\right] - \\
 & \operatorname{Log}\left[\frac{f(c+dx)}{-de+cf}\right]^2 \operatorname{Log}\left[\frac{b(e+fx)}{be-af}\right] - 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \operatorname{Log}\left[\frac{b(e+fx)}{be-af}\right] + \\
 & 2 \operatorname{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \operatorname{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \operatorname{Log}\left[\frac{b(e+fx)}{be-af}\right] - \\
 & \operatorname{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right]^2 \operatorname{Log}\left[\frac{b(e+fx)}{be-af}\right] + 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(e+fx)}{de-cf}\right] - \\
 & \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(e+fx)}{de-cf}\right] - 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \operatorname{Log}\left[\frac{d(e+fx)}{de-cf}\right] + \\
 & \operatorname{Log}\left[\frac{f(c+dx)}{-de+cf}\right]^2 \operatorname{Log}\left[\frac{d(e+fx)}{de-cf}\right] + 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \operatorname{Log}\left[\frac{d(e+fx)}{de-cf}\right] - \\
 & 2 \operatorname{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \operatorname{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \operatorname{Log}\left[\frac{d(e+fx)}{de-cf}\right] + \\
 & \operatorname{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right]^2 \operatorname{Log}\left[\frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)}\right] - \\
 & 2 \operatorname{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] + \\
 & 2 \operatorname{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \operatorname{PolyLog}\left[2, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] + \\
 & \left. 2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right] - 2 \operatorname{PolyLog}\left[3, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \right)
 \end{aligned}$$

**Problem 108: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \operatorname{Log}\left[\frac{b(e+fx)}{be-af}\right]}{(a+bx)(c+dx)} dx$$

Optimal (type 4, 433 leaves, 10 steps):

$$\begin{aligned}
& - \frac{\text{Log}\left[-\frac{bc-ad}{d(a+bx)}\right] \text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2}{2(bc-ad)} - \frac{\text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2 \text{Log}\left[\frac{b(e+fx)}{be-af}\right]}{2(bc-ad)} + \\
& \frac{\text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]^2 \text{Log}\left[1 - \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{2(bc-ad)} - \frac{\text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{bc-ad} + \\
& \frac{\text{Log}\left[\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right] \text{PolyLog}\left[2, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{bc-ad} + \frac{\text{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right]}{bc-ad} - \frac{\text{PolyLog}\left[3, \frac{(be-af)(c+dx)}{(de-cf)(a+bx)}\right]}{bc-ad}
\end{aligned}$$

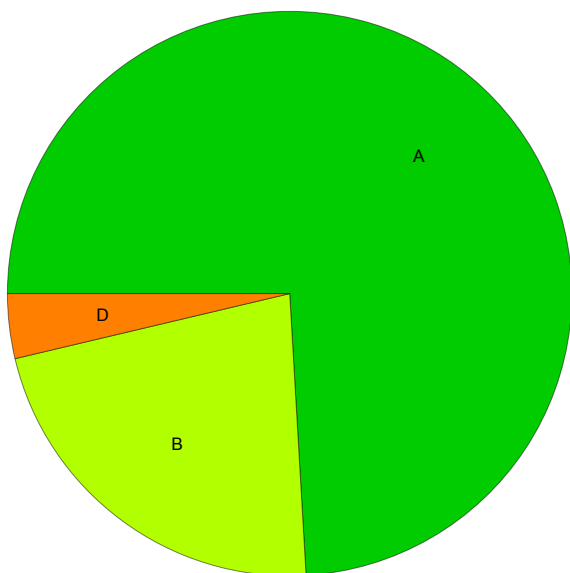
Result (type 4, 1855 leaves):

$$\begin{aligned}
& \frac{1}{2(bc-ad)} \left( 2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{e}{f} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \right. \\
& 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{e}{f} + x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - 2 \left( \text{Log}[a+bx] - \text{Log}[c+dx] \right) \\
& \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \right) \left( \text{Log}\left[\frac{e}{f} + x\right] - \text{Log}\left[\frac{b(e+fx)}{be-af}\right] \right) + \\
& \left( \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] - \text{Log}\left[\frac{f(a+bx)}{-be+af}\right] \right) \text{Log}\left[\frac{b(e+fx)}{be-af}\right] \left( -2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{b(e+fx)}{be-af}\right] \right) + \\
& \text{Log}\left[\frac{a}{b} + x\right]^2 \left( -\text{Log}\left[\frac{e}{f} + x\right] + \text{Log}\left[\frac{b(e+fx)}{be-af}\right] \right) + \\
& \left( \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \text{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \right) \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] \left( -2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] \right) + \\
& \text{Log}\left[\frac{c}{d} + x\right]^2 \left( -\text{Log}\left[\frac{e}{f} + x\right] + \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] \right) + \\
& 2 \left( -\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{Log}\left[\frac{f(c+dx)}{-de+cf}\right] \right) \text{Log}\left[\frac{d(e+fx)}{de-cf}\right] \text{Log}\left[\frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)}\right] + \\
& \left( \text{Log}\left[\frac{-be+af}{f(a+bx)}\right] + \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] - \text{Log}\left[\frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)}\right] \right) \text{Log}\left[\frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)}\right]^2 + \\
& 2 \left( -\text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{Log}\left[\frac{f(a+bx)}{-be+af}\right] \right) \text{Log}\left[\frac{b(e+fx)}{be-af}\right] \text{Log}\left[\frac{(bc-ad)(e+fx)}{(be-af)(c+dx)}\right] + \\
& \left( \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{Log}\left[\frac{-de+cf}{f(c+dx)}\right] - \text{Log}\left[\frac{(de-cf)(a+bx)}{(be-af)(c+dx)}\right] \right) \text{Log}\left[\frac{(bc-ad)(e+fx)}{(be-af)(c+dx)}\right]^2 + \\
& 2 \left( \text{Log}\left[\frac{e}{f} + x\right] - \text{Log}\left[\frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)}\right] \right) \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + \\
& 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{f(a+bx)}{-be+af}\right] + 2 \left( \text{Log}\left[\frac{e}{f} + x\right] - \text{Log}\left[\frac{(bc-ad)(e+fx)}{(be-af)(c+dx)}\right] \right) \\
& \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + \left( \text{Log}\left[\frac{e}{f} + x\right] - \text{Log}\left[\frac{b(e+fx)}{be-af}\right] \right) \\
& \left( \text{Log}\left[\frac{a}{b} + x\right]^2 + \text{Log}\left[\frac{c}{d} + x\right]^2 - 2 \left( \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) - \right.
\end{aligned}$$

$$\begin{aligned}
 & 2 \left( \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d(a+bx)}{-bc+ad} \right] + \text{PolyLog} \left[ 2, \frac{b(c+dx)}{bc-ad} \right] \right) + \\
 & 2 \text{Log} \left[ \frac{c}{d} + x \right] \text{PolyLog} \left[ 2, \frac{f(c+dx)}{-de+cf} \right] + 2 \left( \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{(bc-ad)(e+fx)}{(be-af)(c+dx)} \right] \right) \\
 & \text{PolyLog} \left[ 2, \frac{b(e+fx)}{be-af} \right] + 2 \left( \text{Log} \left[ \frac{a}{b} + x \right] - \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{(-be+af)(c+dx)}{(-de+cf)(a+bx)} \right] \right) \\
 & \left( \text{Log} \left[ \frac{e}{f} + x \right] \left( \text{Log} \left[ \frac{f(a+bx)}{-be+af} \right] - \text{Log} \left[ \frac{f(c+dx)}{-de+cf} \right] \right) + \right. \\
 & \quad \left. \text{PolyLog} \left[ 2, \frac{b(e+fx)}{be-af} \right] - \text{PolyLog} \left[ 2, \frac{d(e+fx)}{de-cf} \right] \right) + \\
 & 2 \left( \text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)} \right] \right) \text{PolyLog} \left[ 2, \frac{d(e+fx)}{de-cf} \right] + \\
 & 2 \text{Log} \left[ \frac{(-bc+ad)(e+fx)}{(de-cf)(a+bx)} \right] \left( \text{PolyLog} \left[ 2, \frac{b(e+fx)}{f(a+bx)} \right] - \text{PolyLog} \left[ 2, -\frac{(bc-ad)(e+fx)}{(de-cf)(a+bx)} \right] \right) + \\
 & 2 \text{Log} \left[ \frac{(bc-ad)(e+fx)}{(be-af)(c+dx)} \right] \left( \text{PolyLog} \left[ 2, \frac{d(e+fx)}{f(c+dx)} \right] - \text{PolyLog} \left[ 2, \frac{(bc-ad)(e+fx)}{(be-af)(c+dx)} \right] \right) - \\
 & 2 \text{PolyLog} \left[ 3, \frac{d(a+bx)}{-bc+ad} \right] - 2 \text{PolyLog} \left[ 3, \frac{f(a+bx)}{-be+af} \right] - 2 \text{PolyLog} \left[ 3, \frac{b(c+dx)}{bc-ad} \right] - \\
 & 2 \text{PolyLog} \left[ 3, \frac{f(c+dx)}{-de+cf} \right] - 2 \text{PolyLog} \left[ 3, \frac{b(e+fx)}{be-af} \right] - 2 \text{PolyLog} \left[ 3, \frac{d(e+fx)}{de-cf} \right] - \\
 & 2 \text{PolyLog} \left[ 3, \frac{b(e+fx)}{f(a+bx)} \right] + 2 \text{PolyLog} \left[ 3, -\frac{(bc-ad)(e+fx)}{(de-cf)(a+bx)} \right] - \\
 & 2 \text{PolyLog} \left[ 3, \frac{d(e+fx)}{f(c+dx)} \right] + 2 \text{PolyLog} \left[ 3, \frac{(bc-ad)(e+fx)}{(be-af)(c+dx)} \right]
 \end{aligned}$$

## Summary of Integration Test Results

108 integration problems



- A - 80 optimal antiderivatives
- B - 24 more than twice size of optimal antiderivatives
- C - 0 unnecessarily complex antiderivatives
- D - 4 unable to integrate problems
- E - 0 integration timeouts