

Mathematica 11.3 Integration Test Results

Test results for the 174 problems in "5.5.1 u (a+b arcsec(c x))^n.m"

Problem 25: Result more than twice size of optimal antiderivative.

$$\int x^2 (a + b \operatorname{ArcSec}[c x])^3 dx$$

Optimal (type 4, 236 leaves, 11 steps):

$$\begin{aligned} & \frac{b^2 x (a + b \operatorname{ArcSec}[c x])}{c^2} - \frac{b \sqrt{1 - \frac{1}{c^2 x^2}} x^2 (a + b \operatorname{ArcSec}[c x])^2}{2 c} + \\ & \frac{1}{3} x^3 (a + b \operatorname{ArcSec}[c x])^3 + \frac{i b (a + b \operatorname{ArcSec}[c x])^2 \operatorname{ArcTan}[e^{i \operatorname{ArcSec}[c x]}]}{c^3} - \\ & \frac{b^3 \operatorname{ArcTanh}\left[\sqrt{1 - \frac{1}{c^2 x^2}}\right]}{c^3} - \frac{i b^2 (a + b \operatorname{ArcSec}[c x]) \operatorname{PolyLog}[2, -i e^{i \operatorname{ArcSec}[c x]}]}{c^3} + \\ & \frac{i b^2 (a + b \operatorname{ArcSec}[c x]) \operatorname{PolyLog}[2, i e^{i \operatorname{ArcSec}[c x]}]}{c^3} + \\ & \frac{b^3 \operatorname{PolyLog}[3, -i e^{i \operatorname{ArcSec}[c x]}]}{c^3} - \frac{b^3 \operatorname{PolyLog}[3, i e^{i \operatorname{ArcSec}[c x]}]}{c^3} \end{aligned}$$

Result (type 4, 775 leaves):

$$\begin{aligned}
 & \frac{1}{6 c^3} \left(6 a b^2 c x - 3 a^2 b c^2 \sqrt{1 - \frac{1}{c^2 x^2}} x^2 + 2 a^3 c^3 x^3 + \right. \\
 & 6 b^3 c x \operatorname{ArcSec}[c x] - 6 a b^2 c^2 \sqrt{1 - \frac{1}{c^2 x^2}} x^2 \operatorname{ArcSec}[c x] + 6 a^2 b c^3 x^3 \operatorname{ArcSec}[c x] - \\
 & 3 b^3 c^2 \sqrt{1 - \frac{1}{c^2 x^2}} x^2 \operatorname{ArcSec}[c x]^2 + 6 a b^2 c^3 x^3 \operatorname{ArcSec}[c x]^2 + 2 b^3 c^3 x^3 \operatorname{ArcSec}[c x]^3 - \\
 & 6 a b^2 \operatorname{ArcSec}[c x] \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSec}[c x]}\right] - 3 b^3 \operatorname{ArcSec}[c x]^2 \operatorname{Log}\left[1 - i e^{i \operatorname{ArcSec}[c x]}\right] + \\
 & 6 a b^2 \operatorname{ArcSec}[c x] \operatorname{Log}\left[1 + i e^{i \operatorname{ArcSec}[c x]}\right] + 3 b^3 \operatorname{ArcSec}[c x]^2 \operatorname{Log}\left[1 + i e^{i \operatorname{ArcSec}[c x]}\right] - \\
 & 3 b^3 \pi \operatorname{ArcSec}[c x] \operatorname{Log}\left[\left(-\frac{1}{2} - \frac{i}{2}\right) e^{-\frac{1}{2} i \operatorname{ArcSec}[c x]} \left(-i + e^{i \operatorname{ArcSec}[c x]}\right)\right] + \\
 & 3 b^3 \operatorname{ArcSec}[c x]^2 \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) e^{-\frac{1}{2} i \operatorname{ArcSec}[c x]} \left(-i + e^{i \operatorname{ArcSec}[c x]}\right)\right] - \\
 & 3 b^3 \pi \operatorname{ArcSec}[c x] \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSec}[c x]} \left(\left(1 + i\right) + \left(1 - i\right) e^{i \operatorname{ArcSec}[c x]}\right)\right] - \\
 & 3 b^3 \operatorname{ArcSec}[c x]^2 \operatorname{Log}\left[\frac{1}{2} e^{-\frac{1}{2} i \operatorname{ArcSec}[c x]} \left(\left(1 + i\right) + \left(1 - i\right) e^{i \operatorname{ArcSec}[c x]}\right)\right] - \\
 & 3 a^2 b \operatorname{Log}\left[\left(1 + \sqrt{1 - \frac{1}{c^2 x^2}}\right) x\right] + 6 b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSec}[c x]\right] - \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSec}[c x]\right]\right] - \\
 & 3 b^3 \operatorname{ArcSec}[c x]^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSec}[c x]\right] - \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSec}[c x]\right]\right] + \\
 & 3 b^3 \pi \operatorname{ArcSec}[c x] \operatorname{Log}\left[-\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSec}[c x]\right] + \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSec}[c x]\right]\right] - \\
 & 6 b^3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSec}[c x]\right] + \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSec}[c x]\right]\right] + \\
 & 3 b^3 \pi \operatorname{ArcSec}[c x] \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSec}[c x]\right] + \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSec}[c x]\right]\right] + \\
 & 3 b^3 \operatorname{ArcSec}[c x]^2 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} \operatorname{ArcSec}[c x]\right] + \operatorname{Sin}\left[\frac{1}{2} \operatorname{ArcSec}[c x]\right]\right] - \\
 & 6 i b^2 (a + b \operatorname{ArcSec}[c x]) \operatorname{PolyLog}\left[2, -i e^{i \operatorname{ArcSec}[c x]}\right] + \\
 & 6 i b^2 (a + b \operatorname{ArcSec}[c x]) \operatorname{PolyLog}\left[2, i e^{i \operatorname{ArcSec}[c x]}\right] + \\
 & \left. 6 b^3 \operatorname{PolyLog}\left[3, -i e^{i \operatorname{ArcSec}[c x]}\right] - 6 b^3 \operatorname{PolyLog}\left[3, i e^{i \operatorname{ArcSec}[c x]}\right]\right)
 \end{aligned}$$

Problem 63: Result unnecessarily involves imaginary or complex numbers.

$$\int (d + e x)^{3/2} (a + b \operatorname{ArcSec}[c x]) dx$$

Optimal (type 4, 372 leaves, 22 steps):

$$\frac{4 b e \sqrt{d+e x} \left(1-c^2 x^2\right)}{15 c^3 \sqrt{1-\frac{1}{c^2 x^2}} x} + \frac{2 (d+e x)^{5/2} (a+b \operatorname{ArcSec}[c x])}{5 e} +$$

$$\frac{28 b d \sqrt{d+e x} \sqrt{1-c^2 x^2} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{1-c x}}{\sqrt{2}}\right], \frac{2 e}{c d+e}\right]}{15 c^2 \sqrt{1-\frac{1}{c^2 x^2}} x \sqrt{\frac{c(d+e x)}{c d+e}}} +$$

$$\left(4 b \left(2 c^2 d^2+e^2\right) \sqrt{\frac{c(d+e x)}{c d+e}} \sqrt{1-c^2 x^2} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{1-c x}}{\sqrt{2}}\right], \frac{2 e}{c d+e}\right]\right) /$$

$$\left(15 c^4 \sqrt{1-\frac{1}{c^2 x^2}} x \sqrt{d+e x}\right) + \frac{4 b d^3 \sqrt{\frac{c(d+e x)}{c d+e}} \sqrt{1-c^2 x^2} \operatorname{EllipticPi}\left[2, \operatorname{ArcSin}\left[\frac{\sqrt{1-c x}}{\sqrt{2}}\right], \frac{2 e}{c d+e}\right]}{5 c e \sqrt{1-\frac{1}{c^2 x^2}} x \sqrt{d+e x}}$$

Result (type 4, 333 leaves):

$$\frac{1}{15}$$

$$\left(-\frac{4 b e \sqrt{1-\frac{1}{c^2 x^2}} x \sqrt{d+e x}}{c} + \frac{6 a (d+e x)^{5/2}}{e} + \frac{6 b (d+e x)^{5/2} \operatorname{ArcSec}[c x]}{e} + \left(4 i b \sqrt{\frac{e(1+c x)}{-c d+e}}\right.\right.$$

$$\left.\left. \sqrt{\frac{e-c e x}{c d+e}} \left(-7 c d (c d-e) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{c}{c d+e}} \sqrt{d+e x}\right], \frac{c d+e}{c d-e}\right] + \right.\right.$$

$$\left.\left. (9 c^2 d^2-7 c d e+e^2) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{c}{c d+e}} \sqrt{d+e x}\right], \frac{c d+e}{c d-e}\right] - \right.\right.$$

$$\left.\left. 3 c^2 d^2 \operatorname{EllipticPi}\left[1+\frac{e}{c d}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{c}{c d+e}} \sqrt{d+e x}\right], \frac{c d+e}{c d-e}\right]\right)\right) /$$

$$\left(c^3 e \sqrt{-\frac{c}{c d+e}} \sqrt{1-\frac{1}{c^2 x^2}} x\right)$$

Problem 64: Result unnecessarily involves imaginary or complex numbers.

$$\int \sqrt{d+e x} (a+b \operatorname{ArcSec}[c x]) dx$$

Optimal (type 4, 315 leaves, 15 steps):

$$\frac{2 (d + e x)^{3/2} (a + b \operatorname{ArcSec}[c x])}{3 e} + \frac{4 b \sqrt{d + e x} \sqrt{1 - c^2 x^2} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{1 - c x}}{\sqrt{2}}\right], \frac{2 e}{c d + e}\right]}{3 c^2 \sqrt{1 - \frac{1}{c^2 x^2}} x \sqrt{\frac{c (d + e x)}{c d + e}}} +$$

$$\frac{4 b d \sqrt{\frac{c (d + e x)}{c d + e}} \sqrt{1 - c^2 x^2} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{1 - c x}}{\sqrt{2}}\right], \frac{2 e}{c d + e}\right]}{3 c^2 \sqrt{1 - \frac{1}{c^2 x^2}} x \sqrt{d + e x}} +$$

$$\frac{4 b d^2 \sqrt{\frac{c (d + e x)}{c d + e}} \sqrt{1 - c^2 x^2} \operatorname{EllipticPi}\left[2, \operatorname{ArcSin}\left[\frac{\sqrt{1 - c x}}{\sqrt{2}}\right], \frac{2 e}{c d + e}\right]}{3 c e \sqrt{1 - \frac{1}{c^2 x^2}} x \sqrt{d + e x}}$$

Result (type 4, 277 leaves):

$$\frac{1}{3 e} 2 \left(a (d + e x)^{3/2} + b (d + e x)^{3/2} \operatorname{ArcSec}[c x] + \left(2 i b \sqrt{\frac{e (1 + c x)}{-c d + e}} \right. \right.$$

$$\left. \sqrt{\frac{e - c e x}{c d + e}} \left((-c d + e) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{c}{c d + e}} \sqrt{d + e x}\right], \frac{c d + e}{c d - e}\right] + \right. \right.$$

$$\left. (2 c d - e) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{c}{c d + e}} \sqrt{d + e x}\right], \frac{c d + e}{c d - e}\right] - c d \operatorname{EllipticPi}\left[1 + \frac{e}{c d}, \right. \right.$$

$$\left. \left. i \operatorname{ArcSinh}\left[\sqrt{-\frac{c}{c d + e}} \sqrt{d + e x}\right], \frac{c d + e}{c d - e}\right] \right) \Big/ \left(c^2 \sqrt{-\frac{c}{c d + e}} \sqrt{1 - \frac{1}{c^2 x^2}} x \right)$$

Problem 65: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{ArcSec}[c x]}{\sqrt{d + e x}} dx$$

Optimal (type 4, 212 leaves, 9 steps):

$$\frac{2 \sqrt{d+e x} (a+b \operatorname{ArcSec}[c x])}{e} + \frac{4 b \sqrt{\frac{c(d+e x)}{c d+e}} \sqrt{1-c^2 x^2} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{1-c x}}{\sqrt{2}}\right], \frac{2 e}{c d+e}\right]}{c^2 \sqrt{1-\frac{1}{c^2 x^2}} x \sqrt{d+e x}} +$$

$$\frac{4 b d \sqrt{\frac{c(d+e x)}{c d+e}} \sqrt{1-c^2 x^2} \operatorname{EllipticPi}\left[2, \operatorname{ArcSin}\left[\frac{\sqrt{1-c x}}{\sqrt{2}}\right], \frac{2 e}{c d+e}\right]}{c e \sqrt{1-\frac{1}{c^2 x^2}} x \sqrt{d+e x}}$$

Result (type 4, 212 leaves):

$$\frac{1}{e} \left(a \sqrt{d+e x} + b \sqrt{d+e x} \operatorname{ArcSec}[c x] + \left(2 i b \sqrt{\frac{e(1+c x)}{-c d+e}} \sqrt{\frac{e-c e x}{c d+e}} \right. \right.$$

$$\left. \left(\operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{c}{c d+e}} \sqrt{d+e x}\right], \frac{c d+e}{c d-e}\right] - \operatorname{EllipticPi}\left[1+\frac{e}{c d}, \right. \right. \right.$$

$$\left. \left. i \operatorname{ArcSinh}\left[\sqrt{-\frac{c}{c d+e}} \sqrt{d+e x}\right], \frac{c d+e}{c d-e}\right] \right) \right) / \left(c \sqrt{-\frac{c}{c d+e}} \sqrt{1-\frac{1}{c^2 x^2}} x \right)$$

Problem 67: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a+b \operatorname{ArcSec}[c x]}{(d+e x)^{5/2}} dx$$

Optimal (type 4, 298 leaves, 12 steps):

$$-\frac{4 b e (1-c^2 x^2)}{3 c d (c^2 d^2 - e^2) \sqrt{1-\frac{1}{c^2 x^2}} x \sqrt{d+e x}} - \frac{2 (a+b \operatorname{ArcSec}[c x])}{3 e (d+e x)^{3/2}} +$$

$$\frac{4 b \sqrt{d+e x} \sqrt{1-c^2 x^2} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{1-c x}}{\sqrt{2}}\right], \frac{2 e}{c d+e}\right]}{3 d (c^2 d^2 - e^2) \sqrt{1-\frac{1}{c^2 x^2}} x \sqrt{\frac{c(d+e x)}{c d+e}}}$$

$$-\frac{4 b \sqrt{\frac{c(d+e x)}{c d+e}} \sqrt{1-c^2 x^2} \operatorname{EllipticPi}\left[2, \operatorname{ArcSin}\left[\frac{\sqrt{1-c x}}{\sqrt{2}}\right], \frac{2 e}{c d+e}\right]}{3 c d e \sqrt{1-\frac{1}{c^2 x^2}} x \sqrt{d+e x}}$$

Result (type 4, 326 leaves):

$$\frac{1}{3e} \left(-\frac{a}{(d+ex)^{3/2}} + \frac{2bce^2 \sqrt{1 - \frac{1}{c^2 x^2}} x}{(c^2 d^3 - de^2) \sqrt{d+ex}} - \frac{b \operatorname{ArcSec}[cx]}{(d+ex)^{3/2}} - \right. \\ \left. \left(2ib \sqrt{\frac{e(1+cx)}{-cd+e}} \sqrt{\frac{e-cex}{cd+e}} \left(-cd \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{c}{cd+e}} \sqrt{d+ex} \right], \frac{cd+e}{cd-e} \right] + \right. \right. \right. \\ \left. \left. \left. cd \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{c}{cd+e}} \sqrt{d+ex} \right], \frac{cd+e}{cd-e} \right] + \right. \right. \right. \\ \left. \left. \left. (cd+e) \operatorname{EllipticPi}\left[1 + \frac{e}{cd}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{c}{cd+e}} \sqrt{d+ex} \right], \frac{cd+e}{cd-e} \right] \right) \right) \right) / \\ \left(d^2 \left(-\frac{c}{cd+e} \right)^{3/2} (cd+e)^2 \sqrt{1 - \frac{1}{c^2 x^2}} x \right)$$

Problem 68: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a + b \operatorname{ArcSec}[cx]}{(d+ex)^{7/2}} dx$$

Optimal (type 4, 540 leaves, 19 steps):

$$\begin{aligned}
 & - \frac{4 b e (1 - c^2 x^2)}{15 c d (c^2 d^2 - e^2) \sqrt{1 - \frac{1}{c^2 x^2}} x (d + e x)^{3/2}} - \frac{16 b c e (1 - c^2 x^2)}{15 (c^2 d^2 - e^2)^2 \sqrt{1 - \frac{1}{c^2 x^2}} x \sqrt{d + e x}} \\
 & \frac{4 b e (1 - c^2 x^2)}{5 c d^2 (c^2 d^2 - e^2) \sqrt{1 - \frac{1}{c^2 x^2}} x \sqrt{d + e x}} - \frac{2 (a + b \operatorname{ArcSec}[c x])}{5 e (d + e x)^{5/2}} + \\
 & \left(4 b (7 c^2 d^2 - 3 e^2) \sqrt{d + e x} \sqrt{1 - c^2 x^2} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{1 - c x}}{\sqrt{2}}\right], \frac{2 e}{c d + e}\right] \right) / \\
 & \left(15 (c^2 d^3 - d e^2)^2 \sqrt{1 - \frac{1}{c^2 x^2}} x \sqrt{\frac{c (d + e x)}{c d + e}} \right) - \\
 & \frac{4 b \sqrt{\frac{c (d + e x)}{c d + e}} \sqrt{1 - c^2 x^2} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{1 - c x}}{\sqrt{2}}\right], \frac{2 e}{c d + e}\right]}{15 d (c^2 d^2 - e^2) \sqrt{1 - \frac{1}{c^2 x^2}} x \sqrt{d + e x}} - \\
 & \frac{4 b \sqrt{\frac{c (d + e x)}{c d + e}} \sqrt{1 - c^2 x^2} \operatorname{EllipticPi}\left[2, \operatorname{ArcSin}\left[\frac{\sqrt{1 - c x}}{\sqrt{2}}\right], \frac{2 e}{c d + e}\right]}{5 c d^2 e \sqrt{1 - \frac{1}{c^2 x^2}} x \sqrt{d + e x}}
 \end{aligned}$$

Result (type 4, 407 leaves):

$$\frac{1}{15 e} \left(-\frac{3 a}{(d+e x)^{5/2}} + \frac{2 b c e^2 \sqrt{1-\frac{1}{c^2 x^2}} x \left(-e^2(4 d+3 e x)+c^2 d^2(8 d+7 e x)\right)}{\left(c^2 d^3-d e^2\right)^2(d+e x)^{3/2}} - \frac{3 b \operatorname{ArcSec}[c x]}{(d+e x)^{5/2}} + \left(2 i b \sqrt{\frac{e(1+c x)}{-c d+e}} \sqrt{\frac{e-c e x}{c d+e}} \right. \right. \\ \left. \left(c d\left(7 c^2 d^2-3 e^2\right) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{c}{c d+e}} \sqrt{d+e x}\right], \frac{c d+e}{c d-e}\right] - \right. \right. \\ \left. c d\left(6 c^2 d^2-c d e-3 e^2\right) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{-\frac{c}{c d+e}} \sqrt{d+e x}\right], \frac{c d+e}{c d-e}\right] - \right. \\ \left. \left. 3(c d-e)(c d+e)^2 \operatorname{EllipticPi}\left[1+\frac{e}{c d}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{c}{c d+e}} \sqrt{d+e x}\right], \frac{c d+e}{c d-e}\right]\right) \right) / \\ \left(d^3(c d-e)\left(-\frac{c}{c d+e}\right)^{3/2}(c d+e)^3 \sqrt{1-\frac{1}{c^2 x^2}} x \right)$$

Problem 96: Result more than twice size of optimal antiderivative.

$$\int \frac{x^5 (a+b \operatorname{ArcSec}[c x])}{(d+e x^2)^2} dx$$

Optimal (type 4, 608 leaves, 31 steps):

$$\begin{aligned}
 & -\frac{b \sqrt{1 - \frac{1}{c^2 x^2}} x}{2 c e^2} + \frac{d (a + b \operatorname{ArcSec}[c x])}{2 e^2 \left(e + \frac{d}{x^2} \right)} + \frac{x^2 (a + b \operatorname{ArcSec}[c x])}{2 e^2} + \frac{b d \operatorname{ArcTan}\left[\frac{\sqrt{c^2 d + e}}{c \sqrt{e} \sqrt{1 - \frac{1}{c^2 x^2}} x} \right]}{2 e^{5/2} \sqrt{c^2 d + e}} - \\
 & \frac{d (a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 - \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} - \sqrt{c^2 d + e}} \right]}{e^3} - \frac{d (a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 + \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} - \sqrt{c^2 d + e}} \right]}{e^3} - \\
 & \frac{d (a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 - \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} + \sqrt{c^2 d + e}} \right]}{e^3} - \frac{d (a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 + \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} + \sqrt{c^2 d + e}} \right]}{e^3} + \\
 & \frac{2 d (a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 + e^{2 i \operatorname{ArcSec}[c x]} \right]}{e^3} + \frac{i b d \operatorname{PolyLog}\left[2, -\frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} - \sqrt{c^2 d + e}} \right]}{e^3} + \\
 & \frac{i b d \operatorname{PolyLog}\left[2, \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} - \sqrt{c^2 d + e}} \right]}{e^3} + \frac{i b d \operatorname{PolyLog}\left[2, -\frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} + \sqrt{c^2 d + e}} \right]}{e^3} + \\
 & \frac{i b d \operatorname{PolyLog}\left[2, \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} + \sqrt{c^2 d + e}} \right]}{e^3} - \frac{i b d \operatorname{PolyLog}\left[2, -e^{2 i \operatorname{ArcSec}[c x]} \right]}{e^3}
 \end{aligned}$$

Result (type 4, 1362 leaves):

$$\frac{a x^2}{2 e^2} - \frac{a d^2}{2 e^3 (d + e x^2)} - \frac{a d \operatorname{Log}[d + e x^2]}{e^3} + b \left(\frac{x \left(-\sqrt{1 - \frac{1}{c^2 x^2}} + c x \operatorname{ArcSec}[c x] \right)}{2 c e^2} + \frac{1}{4 e^{5/2}} \right)$$

$$\left(i d^{3/2} \left(-\frac{\operatorname{ArcSec}[c x]}{i \sqrt{d} \sqrt{e} + e x} + \frac{i \left(\frac{\operatorname{ArcSin}\left[\frac{1}{c x} \right]}{\sqrt{e}} - \frac{\operatorname{Log}\left[\frac{2 \sqrt{d} \sqrt{e} \left(\sqrt{e} + c \left(i c \sqrt{d} - \sqrt{-c^2 d - e} \sqrt{1 - \frac{1}{c^2 x^2}} \right) x \right]}{\sqrt{-c^2 d - e} \left(\sqrt{d} - i \sqrt{e} x \right)} \right]}{\sqrt{-c^2 d - e}} \right)}{\sqrt{d}} \right) - \frac{1}{4 e^{5/2}} \right)$$

$$\begin{aligned}
 & \left(\frac{i d^{3/2}}{-i \sqrt{d} \sqrt{e} + e x} - \frac{\operatorname{ArcSec}[c x]}{\sqrt{d}} - \frac{i \left(\frac{\operatorname{ArcSin}\left[\frac{1}{c x}\right]}{\sqrt{e}} - \frac{\operatorname{Log}\left[\frac{2 \sqrt{d} \sqrt{e} \left(-\sqrt{e}-c\left(i c \sqrt{d}+\sqrt{-c^2 d-e}\right) \sqrt{1-\frac{1}{c^2 x^2}}\right) x}{\sqrt{-c^2 d-e} \left(\sqrt{d}+i \sqrt{e} x\right)}\right]}{\sqrt{-c^2 d-e}} \right)}{\sqrt{d}} \right) - \\
 & \frac{1}{2 e^3} i d \left(8 \operatorname{ArcSin}\left[\frac{\sqrt{1+\frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}}\right] \operatorname{ArcTan}\left[\frac{\left(i c \sqrt{d}+\sqrt{e}\right) \operatorname{Tan}\left[\frac{1}{2} \operatorname{ArcSec}[c x]\right]}{\sqrt{c^2 d+e}}\right] - \right. \\
 & 2 i \operatorname{ArcSec}[c x] \operatorname{Log}\left[1+\frac{i\left(\sqrt{e}-\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] - \\
 & 4 i \operatorname{ArcSin}\left[\frac{\sqrt{1+\frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}}\right] \operatorname{Log}\left[1+\frac{i\left(\sqrt{e}-\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] - \\
 & 2 i \operatorname{ArcSec}[c x] \operatorname{Log}\left[1+\frac{i\left(\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] + \\
 & 4 i \operatorname{ArcSin}\left[\frac{\sqrt{1+\frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}}\right] \operatorname{Log}\left[1+\frac{i\left(\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] + \\
 & 2 i \operatorname{ArcSec}[c x] \operatorname{Log}\left[1+e^{2 i \operatorname{ArcSec}[c x]}\right] - 2 \operatorname{PolyLog}\left[2, \frac{i\left(-\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] - \\
 & \left. 2 \operatorname{PolyLog}\left[2, -\frac{i\left(\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] + \operatorname{PolyLog}\left[2, -e^{2 i \operatorname{ArcSec}[c x]}\right] \right) - \\
 & \frac{1}{2 e^3} i d \left(8 \operatorname{ArcSin}\left[\frac{\sqrt{1-\frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}}\right] \operatorname{ArcTan}\left[\frac{\left(-i c \sqrt{d}+\sqrt{e}\right) \operatorname{Tan}\left[\frac{1}{2} \operatorname{ArcSec}[c x]\right]}{\sqrt{c^2 d+e}}\right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 i \operatorname{ArcSec}[c x] \operatorname{Log}\left[1 + \frac{i\left(-\sqrt{e} + \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] - \\
 & 4 i \operatorname{ArcSin}\left[\frac{\sqrt{1 - \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}}\right] \operatorname{Log}\left[1 + \frac{i\left(-\sqrt{e} + \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] - \\
 & 2 i \operatorname{ArcSec}[c x] \operatorname{Log}\left[1 - \frac{i\left(\sqrt{e} + \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] + \\
 & 4 i \operatorname{ArcSin}\left[\frac{\sqrt{1 - \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}}\right] \operatorname{Log}\left[1 - \frac{i\left(\sqrt{e} + \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] + \\
 & 2 i \operatorname{ArcSec}[c x] \operatorname{Log}\left[1 + e^{2 i \operatorname{ArcSec}[c x]}\right] - 2 \operatorname{PolyLog}\left[2, \frac{i\left(\sqrt{e} - \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] - \\
 & \left. \left. \left. 2 \operatorname{PolyLog}\left[2, \frac{i\left(\sqrt{e} + \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] + \operatorname{PolyLog}\left[2, -e^{2 i \operatorname{ArcSec}[c x]}\right]\right)\right)\right)
 \end{aligned}$$

Problem 97: Result more than twice size of optimal antiderivative.

$$\int \frac{x^3 (a + b \operatorname{ArcSec}[c x])}{(d + e x^2)^2} dx$$

Optimal (type 4, 570 leaves, 29 steps):

$$\begin{aligned}
 & - \frac{a + b \operatorname{ArcSec}[c x]}{2 e \left(e + \frac{d}{x^2} \right)} - \frac{b \operatorname{ArcTan}\left[\frac{\sqrt{c^2 d + e}}{c \sqrt{e} \sqrt{1 - \frac{1}{c^2 x^2}} x} \right]}{2 e^{3/2} \sqrt{c^2 d + e}} + \frac{(a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 - \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} - \sqrt{c^2 d + e}} \right]}{2 e^2} + \\
 & \frac{(a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 + \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} - \sqrt{c^2 d + e}} \right]}{2 e^2} + \frac{(a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 - \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} + \sqrt{c^2 d + e}} \right]}{2 e^2} + \\
 & \frac{(a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 + \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} + \sqrt{c^2 d + e}} \right]}{2 e^2} - \frac{(a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 + e^{2 i \operatorname{ArcSec}[c x]} \right]}{e^2} - \\
 & \frac{i b \operatorname{PolyLog}\left[2, -\frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} - \sqrt{c^2 d + e}} \right]}{2 e^2} - \frac{i b \operatorname{PolyLog}\left[2, \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} - \sqrt{c^2 d + e}} \right]}{2 e^2} - \\
 & \frac{i b \operatorname{PolyLog}\left[2, -\frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} + \sqrt{c^2 d + e}} \right]}{2 e^2} - \frac{i b \operatorname{PolyLog}\left[2, \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} + \sqrt{c^2 d + e}} \right]}{2 e^2} + \frac{i b \operatorname{PolyLog}\left[2, -e^{2 i \operatorname{ArcSec}[c x]} \right]}{2 e^2}
 \end{aligned}$$

Result (type 4, 1213 leaves):

$$\begin{aligned}
 & \frac{1}{4 e^2} \left(\frac{2 a d}{d + e x^2} + \frac{b \sqrt{d} \operatorname{ArcSec}[c x]}{\sqrt{d} - i \sqrt{e} x} + \frac{b \sqrt{d} \operatorname{ArcSec}[c x]}{\sqrt{d} + i \sqrt{e} x} + 2 b \operatorname{ArcSin}\left[\frac{1}{c x} \right] + \right. \\
 & 8 i b \operatorname{ArcSin}\left[\frac{\sqrt{1 - \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}} \right] \operatorname{ArcTan}\left[\frac{(-i c \sqrt{d} + \sqrt{e}) \operatorname{Tan}\left[\frac{1}{2} \operatorname{ArcSec}[c x] \right]}{\sqrt{c^2 d + e}} \right] + \\
 & 8 i b \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}} \right] \operatorname{ArcTan}\left[\frac{(i c \sqrt{d} + \sqrt{e}) \operatorname{Tan}\left[\frac{1}{2} \operatorname{ArcSec}[c x] \right]}{\sqrt{c^2 d + e}} \right] + \\
 & 2 b \operatorname{ArcSec}[c x] \operatorname{Log}\left[1 + \frac{i (\sqrt{e} - \sqrt{c^2 d + e}) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}} \right] + \\
 & 4 b \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}} \right] \operatorname{Log}\left[1 + \frac{i (\sqrt{e} - \sqrt{c^2 d + e}) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}} \right] + \\
 & 2 b \operatorname{ArcSec}[c x] \operatorname{Log}\left[1 + \frac{i (-\sqrt{e} + \sqrt{c^2 d + e}) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}} \right] +
 \end{aligned}$$

$$\begin{aligned}
 & 4 b \operatorname{ArcSin}\left[\frac{\sqrt{1-\frac{i\sqrt{e}}{c\sqrt{d}}}}{\sqrt{2}}\right] \operatorname{Log}\left[1+\frac{i\left(-\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]+ \\
 & 2 b \operatorname{ArcSec}[c x] \operatorname{Log}\left[1-\frac{i\left(\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]- \\
 & 4 b \operatorname{ArcSin}\left[\frac{\sqrt{1-\frac{i\sqrt{e}}{c\sqrt{d}}}}{\sqrt{2}}\right] \operatorname{Log}\left[1-\frac{i\left(\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]+ \\
 & 2 b \operatorname{ArcSec}[c x] \operatorname{Log}\left[1+\frac{i\left(\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]- \\
 & 4 b \operatorname{ArcSin}\left[\frac{\sqrt{1+\frac{i\sqrt{e}}{c\sqrt{d}}}}{\sqrt{2}}\right] \operatorname{Log}\left[1+\frac{i\left(\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]- \\
 & 4 b \operatorname{ArcSec}[c x] \operatorname{Log}\left[1+e^{2 i \operatorname{ArcSec}[c x]}\right]-\frac{b \sqrt{e} \operatorname{Log}\left[\frac{2 \sqrt{d} \sqrt{e}\left(\sqrt{e}+c\left(i c \sqrt{d}-\sqrt{-c^2 d-e}\right) \sqrt{1-\frac{1}{c^2 x^2}}\right) x}{\sqrt{-c^2 d-e}\left(\sqrt{d}-i \sqrt{e} x\right)}\right]}{\sqrt{-c^2 d-e}}- \\
 & \frac{b \sqrt{e} \operatorname{Log}\left[\frac{2 \sqrt{d} \sqrt{e}\left(-\sqrt{e}+c\left(i c \sqrt{d}+\sqrt{-c^2 d-e}\right) \sqrt{1-\frac{1}{c^2 x^2}}\right) x}{\sqrt{-c^2 d-e}\left(\sqrt{d}+i \sqrt{e} x\right)}\right]}{\sqrt{-c^2 d-e}}+ \\
 & 2 a \operatorname{Log}[d+e x^2]-2 i b \operatorname{PolyLog}\left[2, \frac{i\left(\sqrt{e}-\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]- \\
 & 2 i b \operatorname{PolyLog}\left[2, \frac{i\left(-\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]- \\
 & 2 i b \operatorname{PolyLog}\left[2, -\frac{i\left(\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]- \\
 & \left. 2 i b \operatorname{PolyLog}\left[2, \frac{i\left(\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]+2 i b \operatorname{PolyLog}\left[2, -e^{2 i \operatorname{ArcSec}[c x]}\right]\right]
 \end{aligned}$$

Problem 98: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{x(a+b \operatorname{ArcSec}[c x])}{(d+e x^2)^2} dx$$

Optimal (type 3, 131 leaves, 7 steps):

$$-\frac{a+b \operatorname{ArcSec}[c x]}{2 e(d+e x^2)} + \frac{b c x \operatorname{ArcTan}\left[\frac{\sqrt{-1+c^2 x^2}}{\sqrt{c^2 d+e}}\right]}{2 d e \sqrt{c^2 x^2}} - \frac{b c x \operatorname{ArcTan}\left[\frac{\sqrt{e} \sqrt{-1+c^2 x^2}}{\sqrt{c^2 d+e}}\right]}{2 d \sqrt{e} \sqrt{c^2 d+e} \sqrt{c^2 x^2}}$$

Result (type 3, 286 leaves):

$$\frac{1}{4 e} \left(-\frac{2 a}{d+e x^2} - \frac{2 b \operatorname{ArcSec}[c x]}{d+e x^2} - \frac{2 b \operatorname{ArcSin}\left[\frac{1}{c x}\right]}{d} + \frac{b \sqrt{e} \operatorname{Log}\left[\frac{4 i d e+4 c d \sqrt{e}\left(c \sqrt{d}-i \sqrt{-c^2 d-e} \sqrt{1-\frac{1}{c^2 x^2}}\right) x}{b \sqrt{-c^2 d-e}\left(\sqrt{d}+i \sqrt{e} x\right)}\right]}{d \sqrt{-c^2 d-e}} + \frac{b \sqrt{e} \operatorname{Log}\left[\frac{-4 i d e+4 c d \sqrt{e}\left(c \sqrt{d}+i \sqrt{-c^2 d-e} \sqrt{1-\frac{1}{c^2 x^2}}\right) x}{b \sqrt{-c^2 d-e}\left(\sqrt{d}-i \sqrt{e} x\right)}\right]}{d \sqrt{-c^2 d-e}} \right)$$

Problem 99: Result more than twice size of optimal antiderivative.

$$\int \frac{a+b \operatorname{ArcSec}[c x]}{x(d+e x^2)^2} dx$$

Optimal (type 4, 546 leaves, 24 steps):

$$\begin{aligned}
 & - \frac{e (a + b \operatorname{ArcSec}[c x])}{2 d^2 \left(e + \frac{d}{x^2} \right)} + \frac{i (a + b \operatorname{ArcSec}[c x])^2}{2 b d^2} - \frac{b \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{c^2 d + e}}{c \sqrt{e} \sqrt{1 - \frac{1}{c^2 x^2}}} \right]}{2 d^2 \sqrt{c^2 d + e}} - \\
 & \frac{(a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 - \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} - \sqrt{c^2 d + e}} \right]}{2 d^2} - \frac{(a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 + \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} - \sqrt{c^2 d + e}} \right]}{2 d^2} - \\
 & \frac{(a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 - \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} + \sqrt{c^2 d + e}} \right]}{2 d^2} - \frac{(a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 + \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} + \sqrt{c^2 d + e}} \right]}{2 d^2} + \\
 & \frac{i b \operatorname{PolyLog}\left[2, -\frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} - \sqrt{c^2 d + e}} \right]}{2 d^2} + \frac{i b \operatorname{PolyLog}\left[2, \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} - \sqrt{c^2 d + e}} \right]}{2 d^2} + \\
 & \frac{i b \operatorname{PolyLog}\left[2, -\frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} + \sqrt{c^2 d + e}} \right]}{2 d^2} + \frac{i b \operatorname{PolyLog}\left[2, \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} + \sqrt{c^2 d + e}} \right]}{2 d^2}
 \end{aligned}$$

Result (type 4, 1190 leaves):

$$\begin{aligned}
 & \frac{1}{4 d^2} \left(\frac{2 a d}{d + e x^2} + \frac{b \sqrt{d} \operatorname{ArcSec}[c x]}{\sqrt{d} - i \sqrt{e} x} + \frac{b \sqrt{d} \operatorname{ArcSec}[c x]}{\sqrt{d} + i \sqrt{e} x} + 2 i b \operatorname{ArcSec}[c x]^2 + 2 b \operatorname{ArcSin}\left[\frac{1}{c x} \right] - \right. \\
 & 8 i b \operatorname{ArcSin}\left[\frac{\sqrt{1 - \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}} \right] \operatorname{ArcTan}\left[\frac{(-i c \sqrt{d} + \sqrt{e}) \operatorname{Tan}\left[\frac{1}{2} \operatorname{ArcSec}[c x] \right]}{\sqrt{c^2 d + e}} \right] - \\
 & 8 i b \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}} \right] \operatorname{ArcTan}\left[\frac{(i c \sqrt{d} + \sqrt{e}) \operatorname{Tan}\left[\frac{1}{2} \operatorname{ArcSec}[c x] \right]}{\sqrt{c^2 d + e}} \right] - \\
 & 2 b \operatorname{ArcSec}[c x] \operatorname{Log}\left[1 + \frac{i (\sqrt{e} - \sqrt{c^2 d + e}) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}} \right] - \\
 & 4 b \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}} \right] \operatorname{Log}\left[1 + \frac{i (\sqrt{e} - \sqrt{c^2 d + e}) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}} \right] - \\
 & 2 b \operatorname{ArcSec}[c x] \operatorname{Log}\left[1 + \frac{i (-\sqrt{e} + \sqrt{c^2 d + e}) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}} \right] -
 \end{aligned}$$

$$\begin{aligned}
 & 4 b \operatorname{ArcSin}\left[\frac{\sqrt{1-\frac{i\sqrt{e}}{c\sqrt{d}}}}{\sqrt{2}}\right] \operatorname{Log}\left[1+\frac{i\left(-\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]- \\
 & 2 b \operatorname{ArcSec}[c x] \operatorname{Log}\left[1-\frac{i\left(\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]+ \\
 & 4 b \operatorname{ArcSin}\left[\frac{\sqrt{1-\frac{i\sqrt{e}}{c\sqrt{d}}}}{\sqrt{2}}\right] \operatorname{Log}\left[1-\frac{i\left(\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]- \\
 & 2 b \operatorname{ArcSec}[c x] \operatorname{Log}\left[1+\frac{i\left(\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]+ \\
 & 4 b \operatorname{ArcSin}\left[\frac{\sqrt{1+\frac{i\sqrt{e}}{c\sqrt{d}}}}{\sqrt{2}}\right] \operatorname{Log}\left[1+\frac{i\left(\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]+ \\
 & \frac{b \sqrt{e} \operatorname{Log}\left[\frac{2 \sqrt{d} \sqrt{e}\left(\sqrt{e}+c\left(i c \sqrt{d}-\sqrt{-c^2 d-e} \sqrt{1-\frac{1}{c^2 x^2}}\right) x\right)}{\sqrt{-c^2 d-e}\left(\sqrt{d}-i \sqrt{e} x\right)}\right]}{\sqrt{-c^2 d-e}}- \\
 & \frac{b \sqrt{e} \operatorname{Log}\left[\frac{2 \sqrt{d} \sqrt{e}\left(-\sqrt{e}+c\left(i c \sqrt{d}+\sqrt{-c^2 d-e} \sqrt{1-\frac{1}{c^2 x^2}}\right) x\right)}{\sqrt{-c^2 d-e}\left(\sqrt{d}+i \sqrt{e} x\right)}\right]}{\sqrt{-c^2 d-e}}- \\
 & 2 a \operatorname{Log}[d+e x^2]+2 i b \operatorname{PolyLog}\left[2, \frac{i\left(\sqrt{e}-\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]+ \\
 & 2 i b \operatorname{PolyLog}\left[2, \frac{i\left(-\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]+ \\
 & 2 i b \operatorname{PolyLog}\left[2, -\frac{i\left(\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]+ \\
 & \left. 2 i b \operatorname{PolyLog}\left[2, \frac{i\left(\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right]\right)
 \end{aligned}$$

Problem 104: Result more than twice size of optimal antiderivative.

$$\int \frac{x^5 (a + b \operatorname{ArcSec}[cx])}{(d + ex^2)^3} dx$$

Optimal (type 4, 707 leaves, 33 steps):

$$\begin{aligned} & -\frac{bcd\sqrt{1-\frac{1}{c^2x^2}}}{8e^2(c^2d+e)\left(e+\frac{d}{x^2}\right)x} - \frac{a+b\operatorname{ArcSec}[cx]}{4e\left(e+\frac{d}{x^2}\right)^2} - \frac{a+b\operatorname{ArcSec}[cx]}{2e^2\left(e+\frac{d}{x^2}\right)} - \frac{b\operatorname{ArcTan}\left[\frac{\sqrt{c^2d+e}}{c\sqrt{e}\sqrt{1-\frac{1}{c^2x^2}}}\right]}{2e^{5/2}\sqrt{c^2d+e}} \\ & + \frac{b(c^2d+2e)\operatorname{ArcTan}\left[\frac{\sqrt{c^2d+e}}{c\sqrt{e}\sqrt{1-\frac{1}{c^2x^2}}}\right]}{8e^{5/2}(c^2d+e)^{3/2}} + \frac{(a+b\operatorname{ArcSec}[cx])\operatorname{Log}\left[1-\frac{c\sqrt{-d}e^{i\operatorname{ArcSec}[cx]}}{\sqrt{e}-\sqrt{c^2d+e}}\right]}{2e^3} + \\ & + \frac{(a+b\operatorname{ArcSec}[cx])\operatorname{Log}\left[1+\frac{c\sqrt{-d}e^{i\operatorname{ArcSec}[cx]}}{\sqrt{e}+\sqrt{c^2d+e}}\right]}{2e^3} + \frac{(a+b\operatorname{ArcSec}[cx])\operatorname{Log}\left[1-\frac{c\sqrt{-d}e^{i\operatorname{ArcSec}[cx]}}{\sqrt{e}+\sqrt{c^2d+e}}\right]}{2e^3} + \\ & - \frac{(a+b\operatorname{ArcSec}[cx])\operatorname{Log}\left[1+\frac{c\sqrt{-d}e^{i\operatorname{ArcSec}[cx]}}{\sqrt{e}+\sqrt{c^2d+e}}\right]}{2e^3} - \frac{(a+b\operatorname{ArcSec}[cx])\operatorname{Log}\left[1+e^{2i\operatorname{ArcSec}[cx]}\right]}{e^3} \\ & - \frac{i b \operatorname{PolyLog}\left[2, -\frac{c\sqrt{-d}e^{i\operatorname{ArcSec}[cx]}}{\sqrt{e}-\sqrt{c^2d+e}}\right]}{2e^3} - \frac{i b \operatorname{PolyLog}\left[2, \frac{c\sqrt{-d}e^{i\operatorname{ArcSec}[cx]}}{\sqrt{e}-\sqrt{c^2d+e}}\right]}{2e^3} \\ & - \frac{i b \operatorname{PolyLog}\left[2, -\frac{c\sqrt{-d}e^{i\operatorname{ArcSec}[cx]}}{\sqrt{e}+\sqrt{c^2d+e}}\right]}{2e^3} - \frac{i b \operatorname{PolyLog}\left[2, \frac{c\sqrt{-d}e^{i\operatorname{ArcSec}[cx]}}{\sqrt{e}+\sqrt{c^2d+e}}\right]}{2e^3} + \frac{i b \operatorname{PolyLog}\left[2, -e^{2i\operatorname{ArcSec}[cx]}\right]}{2e^3} \end{aligned}$$

Result (type 4, 1805 leaves):

$$\begin{aligned} & -\frac{ad^2}{4e^3(d+ex^2)^2} + \frac{ad}{e^3(d+ex^2)} + \frac{a\operatorname{Log}[d+ex^2]}{2e^3} + \\ & b \left(-\frac{1}{16e^{5/2}} - 7i\sqrt{d} - \frac{\operatorname{ArcSec}[cx]}{i\sqrt{d}\sqrt{e+ex}} + \frac{i \left(\frac{\operatorname{ArcSin}\left[\frac{1}{cx}\right]}{\sqrt{e}} - \frac{\operatorname{Log}\left[\frac{2\sqrt{d}\sqrt{e}\left(\sqrt{e+c}\left(i c\sqrt{d}-\sqrt{-c^2d-e}\sqrt{1-\frac{1}{c^2x^2}}\right)x\right)}{\sqrt{-c^2d-e}\left(\sqrt{d}-i\sqrt{e}x\right)}\right]}{\sqrt{-c^2d-e}}\right)}{\sqrt{d}} \right) + \frac{1}{16e^{5/2}} \end{aligned}$$

$$\begin{aligned}
 & 2 i \operatorname{ArcSec}[c x] \operatorname{Log}\left[1 + \frac{i\left(\sqrt{e} - \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] - \\
 & 4 i \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}}\right] \operatorname{Log}\left[1 + \frac{i\left(\sqrt{e} - \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] - \\
 & 2 i \operatorname{ArcSec}[c x] \operatorname{Log}\left[1 + \frac{i\left(\sqrt{e} + \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] + \\
 & 4 i \operatorname{ArcSin}\left[\frac{\sqrt{1 + \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}}\right] \operatorname{Log}\left[1 + \frac{i\left(\sqrt{e} + \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] + \\
 & 2 i \operatorname{ArcSec}[c x] \operatorname{Log}\left[1 + e^{2 i \operatorname{ArcSec}[c x]}\right] - 2 \operatorname{PolyLog}\left[2, \frac{i\left(-\sqrt{e} + \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] - \\
 & \left. 2 \operatorname{PolyLog}\left[2, -\frac{i\left(\sqrt{e} + \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] + \operatorname{PolyLog}\left[2, -e^{2 i \operatorname{ArcSec}[c x]}\right]\right] + \\
 & \frac{1}{4 e^3} i \left(8 \operatorname{ArcSin}\left[\frac{\sqrt{1 - \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}}\right] \operatorname{ArcTan}\left[\frac{\left(-i c \sqrt{d} + \sqrt{e}\right) \operatorname{Tan}\left[\frac{1}{2} \operatorname{ArcSec}[c x]\right]}{\sqrt{c^2 d + e}}\right] - \right. \\
 & 2 i \operatorname{ArcSec}[c x] \operatorname{Log}\left[1 + \frac{i\left(-\sqrt{e} + \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] - \\
 & 4 i \operatorname{ArcSin}\left[\frac{\sqrt{1 - \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}}\right] \operatorname{Log}\left[1 + \frac{i\left(-\sqrt{e} + \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] - \\
 & 2 i \operatorname{ArcSec}[c x] \operatorname{Log}\left[1 - \frac{i\left(\sqrt{e} + \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] + \\
 & 4 i \operatorname{ArcSin}\left[\frac{\sqrt{1 - \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}}\right] \operatorname{Log}\left[1 - \frac{i\left(\sqrt{e} + \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] + \\
 & \left. 2 i \operatorname{ArcSec}[c x] \operatorname{Log}\left[1 + e^{2 i \operatorname{ArcSec}[c x]}\right] - 2 \operatorname{PolyLog}\left[2, \frac{i\left(\sqrt{e} - \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] - \right.
 \end{aligned}$$

$$2 \operatorname{PolyLog}\left[2, \frac{i \left(\sqrt{e} + \sqrt{c^2 d + e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] + \operatorname{PolyLog}\left[2, -e^{2 i \operatorname{ArcSec}[c x]}\right]$$

Problem 105: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{x^3 (a + b \operatorname{ArcSec}[c x])}{(d + e x^2)^3} dx$$

Optimal (type 3, 157 leaves, 6 steps):

$$\frac{b c x \sqrt{-1 + c^2 x^2}}{8 e (c^2 d + e) \sqrt{c^2 x^2} (d + e x^2)} + \frac{x^4 (a + b \operatorname{ArcSec}[c x])}{4 d (d + e x^2)^2} - \frac{b c (c^2 d + 2 e) x \operatorname{ArcTan}\left[\frac{\sqrt{e} \sqrt{-1 + c^2 x^2}}{\sqrt{c^2 d + e}}\right]}{8 d e^{3/2} (c^2 d + e)^{3/2} \sqrt{c^2 x^2}}$$

Result (type 3, 389 leaves):

$$\begin{aligned}
 & -\frac{1}{16 e^2} \left(-\frac{4 a d}{(d+e x^2)^2} + \frac{8 a}{d+e x^2} - \frac{2 b c e \sqrt{1-\frac{1}{c^2 x^2}} x}{(c^2 d+e)(d+e x^2)} + \right. \\
 & \quad \frac{4 b (d+2 e x^2) \operatorname{ArcSec}[c x]}{(d+e x^2)^2} + \frac{4 b \operatorname{ArcSin}\left[\frac{1}{c x}\right]}{d} + \frac{1}{d(-c^2 d-e)^{3/2}} \\
 & \quad \left. b \sqrt{e} (c^2 d+2 e) \operatorname{Log}\left[-\left(\left(16 d \sqrt{-c^2 d-e} e^{3/2} \left(\sqrt{e}+c\left(i c \sqrt{d}-\sqrt{-c^2 d-e} \sqrt{1-\frac{1}{c^2 x^2}}\right) x\right)\right) / \right.\right.\right. \\
 & \quad \left. \left. \left. \left(b\left(c^2 d+2 e\right)\left(i \sqrt{d}+\sqrt{e} x\right)\right)\right)\right] + \frac{1}{d(-c^2 d-e)^{3/2}} \right. \\
 & \quad \left. b \sqrt{e} (c^2 d+2 e) \operatorname{Log}\left[\left(16 i d \sqrt{-c^2 d-e} e^{3/2} \left(-\sqrt{e}+c\left(i c \sqrt{d}+\sqrt{-c^2 d-e} \sqrt{1-\frac{1}{c^2 x^2}}\right) x\right)\right) / \right.\right. \\
 & \quad \left. \left. \left. \left(b\left(c^2 d+2 e\right)\left(\sqrt{d}+i \sqrt{e} x\right)\right)\right)\right] \right)
 \end{aligned}$$

Problem 106: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x (a+b \operatorname{ArcSec}[c x])}{(d+e x^2)^3} dx$$

Optimal (type 3, 193 leaves, 8 steps):

$$\begin{aligned}
 & -\frac{b c x \sqrt{-1+c^2 x^2}}{8 d (c^2 d+e) \sqrt{c^2 x^2} (d+e x^2)} - \frac{a+b \operatorname{ArcSec}[c x]}{4 e (d+e x^2)^2} + \\
 & \quad \frac{b c x \operatorname{ArcTan}\left[\sqrt{-1+c^2 x^2}\right]}{4 d^2 e \sqrt{c^2 x^2}} - \frac{b c (3 c^2 d+2 e) x \operatorname{ArcTan}\left[\frac{\sqrt{e} \sqrt{-1+c^2 x^2}}{\sqrt{c^2 d+e}}\right]}{8 d^2 \sqrt{e} (c^2 d+e)^{3/2} \sqrt{c^2 x^2}}
 \end{aligned}$$

Result (type 3, 386 leaves):

$$\frac{1}{16} \left(-\frac{4a}{e(d+ex^2)^2} - \frac{2bc\sqrt{1-\frac{1}{c^2x^2}}x}{d(c^2d+e)(d+ex^2)} - \frac{4b\text{ArcSec}[cx]}{e(d+ex^2)^2} - \frac{4b\text{ArcSin}\left[\frac{1}{cx}\right]}{d^2e} - \right.$$

$$\left. \left(b(3c^2d+2e) \text{Log}\left[-\left(\left(16d^2\sqrt{-c^2d-e}\sqrt{e}\left(\sqrt{e}+c\left(i c\sqrt{d}-\sqrt{-c^2d-e}\sqrt{1-\frac{1}{c^2x^2}}\right)x\right)\right)\right] \right) \right] \right) / \left(d^2(-c^2d-e)^{3/2}\sqrt{e} \right) -$$

$$\left. \left(b(3c^2d+2e) \left(i\sqrt{d} + \sqrt{e}x \right) \right) \right] \right) / \left(d^2(-c^2d-e)^{3/2}\sqrt{e} \right) -$$

$$\left(b(3c^2d+2e) \text{Log}\left[\left(16id^2\sqrt{-c^2d-e}\sqrt{e}\left(-\sqrt{e}+c\left(i c\sqrt{d}+\sqrt{-c^2d-e}\sqrt{1-\frac{1}{c^2x^2}}\right)x\right)\right)\right] \right) / \left(d^2(-c^2d-e)^{3/2}\sqrt{e} \right) \right)$$

Problem 107: Result more than twice size of optimal antiderivative.

$$\int \frac{a+b\text{ArcSec}[cx]}{x(d+ex^2)^3} dx$$

Optimal (type 4, 685 leaves, 28 steps):

$$\frac{b c e \sqrt{1 - \frac{1}{c^2 x^2}}}{8 d^2 (c^2 d + e) \left(e + \frac{d}{x^2}\right) x} + \frac{e^2 (a + b \operatorname{ArcSec}[c x])}{4 d^3 \left(e + \frac{d}{x^2}\right)^2} - \frac{e (a + b \operatorname{ArcSec}[c x])}{d^3 \left(e + \frac{d}{x^2}\right)} + \frac{i (a + b \operatorname{ArcSec}[c x])^2}{2 b d^3} -$$

$$\frac{b \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{c^2 d + e}}{c \sqrt{e} \sqrt{1 - \frac{1}{c^2 x^2}} x}\right]}{d^3 \sqrt{c^2 d + e}} + \frac{b \sqrt{e} (c^2 d + 2 e) \operatorname{ArcTan}\left[\frac{\sqrt{c^2 d + e}}{c \sqrt{e} \sqrt{1 - \frac{1}{c^2 x^2}} x}\right]}{8 d^3 (c^2 d + e)^{3/2}} -$$

$$\frac{(a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 - \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} - \sqrt{c^2 d + e}}\right]}{2 d^3} - \frac{(a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 + \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} - \sqrt{c^2 d + e}}\right]}{2 d^3} -$$

$$\frac{(a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 - \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} + \sqrt{c^2 d + e}}\right]}{2 d^3} - \frac{(a + b \operatorname{ArcSec}[c x]) \operatorname{Log}\left[1 + \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} + \sqrt{c^2 d + e}}\right]}{2 d^3} +$$

$$\frac{i b \operatorname{PolyLog}\left[2, -\frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} - \sqrt{c^2 d + e}}\right]}{2 d^3} + \frac{i b \operatorname{PolyLog}\left[2, \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} - \sqrt{c^2 d + e}}\right]}{2 d^3} +$$

$$\frac{i b \operatorname{PolyLog}\left[2, -\frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} + \sqrt{c^2 d + e}}\right]}{2 d^3} + \frac{i b \operatorname{PolyLog}\left[2, \frac{c \sqrt{-d} e^{i \operatorname{ArcSec}[c x]}}{\sqrt{e} + \sqrt{c^2 d + e}}\right]}{2 d^3}$$

Result (type 4, 1871 leaves):

$$\frac{a}{4 d (d + e x^2)^2} + \frac{a}{2 d^2 (d + e x^2)} + \frac{a \operatorname{Log}[x]}{d^3} - \frac{a \operatorname{Log}[d + e x^2]}{2 d^3} +$$

$$b \left(-\frac{1}{16 d^{5/2}} - 5 i \sqrt{e} \left(-\frac{\operatorname{ArcSec}[c x]}{i \sqrt{d} \sqrt{e} + e x} + \frac{i \left(\frac{\operatorname{ArcSin}\left[\frac{1}{c x}\right]}{\sqrt{e}} - \frac{\operatorname{Log}\left[\frac{2 \sqrt{d} \sqrt{e} \left(\sqrt{e} + c \left(i c \sqrt{d} - \sqrt{-c^2 d - e} \sqrt{1 - \frac{1}{c^2 x^2}}\right) x\right)}{\sqrt{-c^2 d - e} \left(\sqrt{d} - i \sqrt{e} x\right)}\right]}{\sqrt{-c^2 d - e}} \right)}{\sqrt{d}} \right) \right) + \frac{1}{16 d^{5/2}}$$

$$\begin{aligned}
 & \frac{1}{4 d^3} i \left(8 \operatorname{ArcSin} \left[\frac{\sqrt{1 + \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}} \right] \operatorname{ArcTan} \left[\frac{(i c \sqrt{d} + \sqrt{e}) \operatorname{Tan} \left[\frac{1}{2} \operatorname{ArcSec} [c x] \right]}{\sqrt{c^2 d + e}} \right] - \right. \\
 & 2 i \operatorname{ArcSec} [c x] \operatorname{Log} \left[1 + \frac{i (\sqrt{e} - \sqrt{c^2 d + e}) e^{i \operatorname{ArcSec} [c x]}}{c \sqrt{d}} \right] - \\
 & 4 i \operatorname{ArcSin} \left[\frac{\sqrt{1 + \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}} \right] \operatorname{Log} \left[1 + \frac{i (\sqrt{e} - \sqrt{c^2 d + e}) e^{i \operatorname{ArcSec} [c x]}}{c \sqrt{d}} \right] - \\
 & 2 i \operatorname{ArcSec} [c x] \operatorname{Log} \left[1 + \frac{i (\sqrt{e} + \sqrt{c^2 d + e}) e^{i \operatorname{ArcSec} [c x]}}{c \sqrt{d}} \right] + \\
 & 4 i \operatorname{ArcSin} \left[\frac{\sqrt{1 + \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}} \right] \operatorname{Log} \left[1 + \frac{i (\sqrt{e} + \sqrt{c^2 d + e}) e^{i \operatorname{ArcSec} [c x]}}{c \sqrt{d}} \right] + \\
 & 2 i \operatorname{ArcSec} [c x] \operatorname{Log} \left[1 + e^{2 i \operatorname{ArcSec} [c x]} \right] - 2 \operatorname{PolyLog} \left[2, \frac{i (-\sqrt{e} + \sqrt{c^2 d + e}) e^{i \operatorname{ArcSec} [c x]}}{c \sqrt{d}} \right] - \\
 & \left. 2 \operatorname{PolyLog} \left[2, -\frac{i (\sqrt{e} + \sqrt{c^2 d + e}) e^{i \operatorname{ArcSec} [c x]}}{c \sqrt{d}} \right] + \operatorname{PolyLog} \left[2, -e^{2 i \operatorname{ArcSec} [c x]} \right] \right) - \\
 & \frac{1}{4 d^3} i \left(8 \operatorname{ArcSin} \left[\frac{\sqrt{1 - \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}} \right] \operatorname{ArcTan} \left[\frac{(-i c \sqrt{d} + \sqrt{e}) \operatorname{Tan} \left[\frac{1}{2} \operatorname{ArcSec} [c x] \right]}{\sqrt{c^2 d + e}} \right] - \right. \\
 & 2 i \operatorname{ArcSec} [c x] \operatorname{Log} \left[1 + \frac{i (-\sqrt{e} + \sqrt{c^2 d + e}) e^{i \operatorname{ArcSec} [c x]}}{c \sqrt{d}} \right] - \\
 & 4 i \operatorname{ArcSin} \left[\frac{\sqrt{1 - \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}} \right] \operatorname{Log} \left[1 + \frac{i (-\sqrt{e} + \sqrt{c^2 d + e}) e^{i \operatorname{ArcSec} [c x]}}{c \sqrt{d}} \right] - \\
 & 2 i \operatorname{ArcSec} [c x] \operatorname{Log} \left[1 - \frac{i (\sqrt{e} + \sqrt{c^2 d + e}) e^{i \operatorname{ArcSec} [c x]}}{c \sqrt{d}} \right] + \\
 & \left. 4 i \operatorname{ArcSin} \left[\frac{\sqrt{1 - \frac{i \sqrt{e}}{c \sqrt{d}}}}{\sqrt{2}} \right] \operatorname{Log} \left[1 - \frac{i (\sqrt{e} + \sqrt{c^2 d + e}) e^{i \operatorname{ArcSec} [c x]}}{c \sqrt{d}} \right] + \right)
 \end{aligned}$$

$$\left. \begin{aligned}
 & 2 \operatorname{ArcSec}[c x] \operatorname{Log}\left[1 + e^{2 i \operatorname{ArcSec}[c x]}\right] - 2 \operatorname{PolyLog}\left[2, \frac{i\left(\sqrt{e}-\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] - \\
 & 2 \operatorname{PolyLog}\left[2, \frac{i\left(\sqrt{e}+\sqrt{c^2 d+e}\right) e^{i \operatorname{ArcSec}[c x]}}{c \sqrt{d}}\right] + \operatorname{PolyLog}\left[2, -e^{2 i \operatorname{ArcSec}[c x]}\right]
 \end{aligned} \right\}$$

Problem 111: Result unnecessarily involves higher level functions.

$$\int x^5 \sqrt{d+e x^2} (a+b \operatorname{ArcSec}[c x]) dx$$

Optimal (type 3, 403 leaves, 12 steps):

$$\begin{aligned}
 & \frac{b\left(23 c^4 d^2+12 c^2 d e-75 e^2\right) x \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}{1680 c^5 e^2 \sqrt{c^2 x^2}} + \\
 & \frac{b\left(29 c^2 d-25 e\right) x \sqrt{-1+c^2 x^2}\left(d+e x^2\right)^{3 / 2}}{840 c^3 e^2 \sqrt{c^2 x^2}} - \frac{b x \sqrt{-1+c^2 x^2}\left(d+e x^2\right)^{5 / 2}}{42 c e^2 \sqrt{c^2 x^2}} + \\
 & \frac{d^2\left(d+e x^2\right)^{3 / 2}(a+b \operatorname{ArcSec}[c x])}{3 e^3} - \frac{2 d\left(d+e x^2\right)^{5 / 2}(a+b \operatorname{ArcSec}[c x])}{5 e^3} + \\
 & \frac{\left(d+e x^2\right)^{7 / 2}(a+b \operatorname{ArcSec}[c x])}{7 e^3} + \frac{8 b c d^{7 / 2} x \operatorname{ArcTan}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d} \sqrt{-1+c^2 x^2}}\right]}{105 e^3 \sqrt{c^2 x^2}} - \\
 & \frac{b\left(105 c^6 d^3-35 c^4 d^2 e+63 c^2 d e^2+75 e^3\right) x \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{-1+c^2 x^2}}{c \sqrt{d+e x^2}}\right]}{1680 c^6 e^{5 / 2} \sqrt{c^2 x^2}}
 \end{aligned}$$

Result (type 6, 706 leaves):

$$\begin{aligned}
 & - \left(\left(b d \sqrt{1 - \frac{1}{c^2 x^2}} x^3 \left((105 c^6 d^3 - 35 c^4 d^2 e + 63 c^2 d e^2 + 75 e^3) \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d} \right] \right. \right. \right. \\
 & \quad \left. \left(c^2 d \operatorname{AppellF1} \left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] - e \operatorname{AppellF1} \left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] \right) + \right. \\
 & \quad \left. 4 \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] \right. \\
 & \quad \left. \left((35 c^6 d^2 e^2 x^2 - 63 c^4 d e^3 x^2 - 75 c^2 e^4 x^2 + c^8 d^3 (128 d - 105 e x^2)) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d} \right] + 32 c^8 d^3 x^2 \left(-e \operatorname{AppellF1} \left[2, \frac{1}{2}, \frac{3}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 3, c^2 x^2, -\frac{e x^2}{d} \right] + c^2 d \operatorname{AppellF1} \left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d} \right] \right) \right) \right) \Bigg/ \\
 & \left(840 c^5 e^2 (-1 + c^2 x^2) \sqrt{d + e x^2} \left(-4 c^2 e x^2 \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] + \right. \right. \\
 & \quad \left. c^2 d \operatorname{AppellF1} \left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] - e \operatorname{AppellF1} \left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] \right) \\
 & \quad \left(4 d \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d} \right] + x^2 \right. \\
 & \quad \left. \left. \left(-e \operatorname{AppellF1} \left[2, \frac{1}{2}, \frac{3}{2}, 3, c^2 x^2, -\frac{e x^2}{d} \right] + c^2 d \operatorname{AppellF1} \left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d} \right] \right) \right) \right) \Bigg) + \\
 & \frac{1}{1680 c^5 e^3} \sqrt{d + e x^2} \left(16 a c^5 (8 d^3 - 4 d^2 e x^2 + 3 d e^2 x^4 + 15 e^3 x^6) - \right. \\
 & \quad b e \sqrt{1 - \frac{1}{c^2 x^2}} x \\
 & \quad \left. (75 e^2 + 2 c^2 e (19 d + 25 e x^2) + c^4 (-41 d^2 + 22 d e x^2 + 40 e^2 x^4)) + \right. \\
 & \quad \left. 16 b c^5 (8 d^3 - 4 d^2 e x^2 + 3 d e^2 x^4 + 15 e^3 x^6) \operatorname{ArcSec}[c x] \right)
 \end{aligned}$$

Problem 112: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int x^3 \sqrt{d + e x^2} (a + b \operatorname{ArcSec}[c x]) dx$$

Optimal (type 3, 294 leaves, 11 steps):

$$\begin{aligned}
 & - \frac{b(c^2 d + 9 e) x \sqrt{-1 + c^2 x^2} \sqrt{d + e x^2}}{120 c^3 e \sqrt{c^2 x^2}} - \frac{b x \sqrt{-1 + c^2 x^2} (d + e x^2)^{3/2}}{20 c e \sqrt{c^2 x^2}} \\
 & \frac{d(d + e x^2)^{3/2} (a + b \operatorname{ArcSec}[c x])}{3 e^2} + \frac{(d + e x^2)^{5/2} (a + b \operatorname{ArcSec}[c x])}{5 e^2} \\
 & \frac{2 b c d^{5/2} x \operatorname{ArcTan}\left[\frac{\sqrt{d + e x^2}}{\sqrt{d} \sqrt{-1 + c^2 x^2}}\right]}{15 e^2 \sqrt{c^2 x^2}} + \frac{b(15 c^4 d^2 - 10 c^2 d e - 9 e^2) x \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{-1 + c^2 x^2}}{c \sqrt{d + e x^2}}\right]}{120 c^4 e^{3/2} \sqrt{c^2 x^2}}
 \end{aligned}$$

Result (type 6, 628 leaves):

$$\begin{aligned}
 & \left(b d \sqrt{1 - \frac{1}{c^2 x^2}} x^3 \left((15 c^4 d^2 - 10 c^2 d e - 9 e^2) \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right] \right. \right. \\
 & \quad \left. \left(c^2 d \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] - e \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] \right) + \right. \\
 & \quad \left. 4 \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] \right. \\
 & \quad \left. \left((10 c^4 d e^2 x^2 + 9 c^2 e^3 x^2 + c^6 d^2 (16 d - 15 e x^2)) \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right] + \right. \right. \\
 & \quad \left. \left. 4 c^6 d^2 x^2 \left(-e \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. c^2 d \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] \right) \right) \right) \right) / \\
 & \left(60 c^3 e (-1 + c^2 x^2) \sqrt{d + e x^2} \left(-4 c^2 e x^2 \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] + \right. \right. \\
 & \quad \left. c^2 d \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] - e \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] \right) \\
 & \quad \left(4 d \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right] + \right. \\
 & \quad \left. x^2 \left(-e \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] + c^2 d \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] \right) \right) \right) + \\
 & \frac{1}{120 c^3 e^2} \sqrt{d + e x^2} \left(8 a c^3 (-2 d^2 + d e x^2 + 3 e^2 x^4) - b e \sqrt{1 - \frac{1}{c^2 x^2}} x (9 e + c^2 (7 d + 6 e x^2)) + \right. \\
 & \quad \left. 8 b c^3 (-2 d^2 + d e x^2 + 3 e^2 x^4) \operatorname{ArcSec}[c x] \right)
 \end{aligned}$$

Problem 113: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int x \sqrt{d+e x^2} (a+b \operatorname{ArcSec}[c x]) dx$$

Optimal (type 3, 195 leaves, 9 steps):

$$\begin{aligned} & -\frac{b x \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}{6 c \sqrt{c^2 x^2}} + \frac{(d+e x^2)^{3/2} (a+b \operatorname{ArcSec}[c x])}{3 e} + \\ & \frac{b c d^{3/2} x \operatorname{ArcTan}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d} \sqrt{-1+c^2 x^2}}\right]}{3 e \sqrt{c^2 x^2}} - \frac{b (3 c^2 d+e) x \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{-1+c^2 x^2}}{c \sqrt{d+e x^2}}\right]}{6 c^2 \sqrt{e} \sqrt{c^2 x^2}} \end{aligned}$$

Result (type 6, 548 leaves):

$$\begin{aligned} & -\left(\left(b d \sqrt{1-\frac{1}{c^2 x^2}} x^3 \left((3 c^2 d+e) \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right]\right.\right.\right. \\ & \quad \left.\left.\left(c^2 d \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right]-e \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right]\right)\right.\right. \\ & \quad \left.\left.2 \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right]\left((-2 c^2 e^2 x^2+2 c^4 d(2 d-3 e x^2))\right.\right.\right. \\ & \quad \left.\left.\operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right]+c^4 d x^2\left(-e \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2},\right.\right.\right. \\ & \quad \left.\left.\left.3, c^2 x^2, -\frac{e x^2}{d}\right]+c^2 d \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right]\right)\right)\right)\left.\right)\left.\right) / \\ & \left(3 c(-1+c^2 x^2) \sqrt{d+e x^2}\left(-4 c^2 e x^2 \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right]+\right.\right. \\ & \quad \left.\left.c^2 d \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right]-e \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right]\right)\right) \\ & \left(4 d \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right]+x^2\right. \\ & \quad \left.\left(-e \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right]+c^2 d \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right]\right)\right)\left.\right)\left.\right) + \\ & \frac{1}{6 c e} \sqrt{d+e x^2}\left(-b e \sqrt{1-\frac{1}{c^2 x^2}} x+2 a c(d+e x^2)+\right. \\ & \quad \left.2 b c(d+e x^2) \operatorname{ArcSec}[c x]\right) \end{aligned}$$

Problem 119: Unable to integrate problem.

$$\int \frac{\sqrt{d+ex^2} (a+b \operatorname{ArcSec}[cx])}{x^4} dx$$

Optimal (type 4, 328 leaves, 11 steps):

$$\begin{aligned} & \frac{2bc(c^2d+2e)\sqrt{-1+c^2x^2}\sqrt{d+ex^2}}{9d\sqrt{c^2x^2}} + \\ & \frac{bc\sqrt{-1+c^2x^2}\sqrt{d+ex^2}}{9x^2\sqrt{c^2x^2}} - \frac{(d+ex^2)^{3/2}(a+b \operatorname{ArcSec}[cx])}{3dx^3} - \\ & \left(2bc^2(c^2d+2e)x\sqrt{1-c^2x^2}\sqrt{d+ex^2} \operatorname{EllipticE}[\operatorname{ArcSin}[cx], -\frac{e}{c^2d}] \right) / \\ & \left(9d\sqrt{c^2x^2}\sqrt{-1+c^2x^2}\sqrt{1+\frac{ex^2}{d}} \right) + \\ & \left(b(c^2d+e)(2c^2d+3e)x\sqrt{1-c^2x^2}\sqrt{1+\frac{ex^2}{d}} \operatorname{EllipticF}[\operatorname{ArcSin}[cx], -\frac{e}{c^2d}] \right) / \\ & \left(9d\sqrt{c^2x^2}\sqrt{-1+c^2x^2}\sqrt{d+ex^2} \right) \end{aligned}$$

Result (type 8, 25 leaves):

$$\int \frac{\sqrt{d+ex^2} (a+b \operatorname{ArcSec}[cx])}{x^4} dx$$

Problem 120: Unable to integrate problem.

$$\int \frac{\sqrt{d+ex^2} (a+b \operatorname{ArcSec}[cx])}{x^6} dx$$

Optimal (type 4, 453 leaves, 12 steps):

$$\begin{aligned}
 & \frac{bc (24c^4d^2 + 19c^2de - 31e^2) \sqrt{-1+c^2x^2} \sqrt{d+ex^2}}{225d^2 \sqrt{c^2x^2}} + \\
 & \frac{bc (12c^2d - e) \sqrt{-1+c^2x^2} \sqrt{d+ex^2}}{225dx^2 \sqrt{c^2x^2}} + \frac{bc \sqrt{-1+c^2x^2} (d+ex^2)^{3/2}}{25dx^4 \sqrt{c^2x^2}} - \\
 & \frac{(d+ex^2)^{3/2} (a+b \operatorname{ArcSec}[cx])}{5dx^5} + \frac{2e (d+ex^2)^{3/2} (a+b \operatorname{ArcSec}[cx])}{15d^2x^3} - \\
 & \left(bc^2 (24c^4d^2 + 19c^2de - 31e^2) x \sqrt{1-c^2x^2} \sqrt{d+ex^2} \operatorname{EllipticE} \left[\operatorname{ArcSin}[cx], -\frac{e}{c^2d} \right] \right) / \\
 & \left(225d^2 \sqrt{c^2x^2} \sqrt{-1+c^2x^2} \sqrt{1+\frac{ex^2}{d}} \right) + \\
 & \left(b(c^2d+e) (24c^4d^2 + 7c^2de - 30e^2) x \sqrt{1-c^2x^2} \sqrt{1+\frac{ex^2}{d}} \operatorname{EllipticF} \left[\operatorname{ArcSin}[cx], -\frac{e}{c^2d} \right] \right) / \\
 & \left(225d^2 \sqrt{c^2x^2} \sqrt{-1+c^2x^2} \sqrt{d+ex^2} \right)
 \end{aligned}$$

Result (type 8, 25 leaves):

$$\int \frac{\sqrt{d+ex^2} (a+b \operatorname{ArcSec}[cx])}{x^6} dx$$

Problem 121: Result unnecessarily involves higher level functions.

$$\int x^3 (d+ex^2)^{3/2} (a+b \operatorname{ArcSec}[cx]) dx$$

Optimal (type 3, 374 leaves, 12 steps):

$$\begin{aligned}
 & \frac{b (3c^4d^2 - 38c^2de - 25e^2) x \sqrt{-1+c^2x^2} \sqrt{d+ex^2}}{560c^5e \sqrt{c^2x^2}} - \\
 & \frac{b (13c^2d + 25e) x \sqrt{-1+c^2x^2} (d+ex^2)^{3/2}}{840c^3e \sqrt{c^2x^2}} - \frac{bx \sqrt{-1+c^2x^2} (d+ex^2)^{5/2}}{42ce \sqrt{c^2x^2}} - \\
 & \frac{d (d+ex^2)^{5/2} (a+b \operatorname{ArcSec}[cx])}{5e^2} + \frac{(d+ex^2)^{7/2} (a+b \operatorname{ArcSec}[cx])}{7e^2} - \\
 & \frac{2bc d^{7/2} x \operatorname{ArcTan} \left[\frac{\sqrt{d+ex^2}}{\sqrt{d} \sqrt{-1+c^2x^2}} \right]}{35e^2 \sqrt{c^2x^2}} + \frac{b (35c^6d^3 - 35c^4d^2e - 63c^2de^2 - 25e^3) x \operatorname{ArcTanh} \left[\frac{\sqrt{e} \sqrt{-1+c^2x^2}}{c \sqrt{d+ex^2}} \right]}{560c^6e^{3/2} \sqrt{c^2x^2}}
 \end{aligned}$$

Result (type 6, 679 leaves):

$$\begin{aligned}
 & \left(b d \sqrt{1 - \frac{1}{c^2 x^2}} x^3 \left((35 c^6 d^3 - 35 c^4 d^2 e - 63 c^2 d e^2 - 25 e^3) \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right] \right. \right. \\
 & \quad \left. \left(c^2 d \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] - e \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] \right) + \right. \\
 & \quad \left. 4 \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] \right. \\
 & \quad \left. \left((35 c^6 d^2 e^2 x^2 + 63 c^4 d e^3 x^2 + 25 c^2 e^4 x^2 + c^8 d^3 (32 d - 35 e x^2)) \operatorname{AppellF1}\left[1, \frac{1}{2}, \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right] + 8 c^8 d^3 x^2 \left(-e \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] + \right. \right. \\
 & \quad \left. \left. c^2 d \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] \right) \right) \right) \Bigg/ \\
 & \left(280 c^5 e (-1 + c^2 x^2) \sqrt{d + e x^2} \left(-4 c^2 e x^2 \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] + \right. \right. \\
 & \quad \left. c^2 d \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] - e \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] \right) \\
 & \quad \left(4 d \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right] + \right. \\
 & \quad \left. x^2 \left(-e \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] + c^2 d \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] \right) \right) \Bigg) - \\
 & \frac{1}{1680 c^5 e^2} \sqrt{d + e x^2} \left(48 a c^5 (2 d - 5 e x^2) (d + e x^2)^2 + \right. \\
 & \quad \left. b e \sqrt{1 - \frac{1}{c^2 x^2}} x (75 e^2 + 2 c^2 e (82 d + 25 e x^2) + c^4 (57 d^2 + 106 d e x^2 + 40 e^2 x^4)) + \right. \\
 & \quad \left. 48 b c^5 (2 d - 5 e x^2) (d + e x^2)^2 \operatorname{ArcSec}[c x] \right)
 \end{aligned}$$

Problem 122: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int x (d + e x^2)^{3/2} (a + b \operatorname{ArcSec}[c x]) dx$$

Optimal (type 3, 262 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{b (7 c^2 d + 3 e) x \sqrt{-1 + c^2 x^2} \sqrt{d + e x^2}}{40 c^3 \sqrt{c^2 x^2}} - \frac{b x \sqrt{-1 + c^2 x^2} (d + e x^2)^{3/2}}{20 c \sqrt{c^2 x^2}} + \\
 & \frac{(d + e x^2)^{5/2} (a + b \operatorname{ArcSec}[c x])}{5 e} + \frac{b c d^{5/2} x \operatorname{ArcTan}\left[\frac{\sqrt{d + e x^2}}{\sqrt{d} \sqrt{-1 + c^2 x^2}}\right]}{5 e \sqrt{c^2 x^2}} - \\
 & \frac{b (15 c^4 d^2 + 10 c^2 d e + 3 e^2) x \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{-1 + c^2 x^2}}{c \sqrt{d + e x^2}}\right]}{40 c^4 \sqrt{e} \sqrt{c^2 x^2}}
 \end{aligned}$$

Result (type 6, 604 leaves):

$$\begin{aligned}
 & \left(b d \sqrt{1 - \frac{1}{c^2 x^2}} x^3 \left(- (15 c^4 d^2 + 10 c^2 d e + 3 e^2) \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right] \right. \right. \\
 & \quad \left. \left(c^2 d \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] - e \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] \right) + \right. \\
 & \quad \left. \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] \left((40 c^4 d e^2 x^2 + 12 c^2 e^3 x^2 + 4 c^6 d^2 (-8 d + 15 e x^2)) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right] + 8 c^6 d^2 x^2 \left(e \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] - \right. \right. \right. \\
 & \quad \left. \left. \left. c^2 d \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] \right) \right) \right) \right) / \\
 & \left(20 c^3 (-1 + c^2 x^2) \sqrt{d + e x^2} \left(-4 c^2 e x^2 \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] + \right. \right. \\
 & \quad \left. c^2 d \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] - e \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] \right) \\
 & \left(4 d \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right] + \right. \\
 & \quad \left. x^2 \left(-e \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] + c^2 d \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] \right) \right) \right) + \\
 & \frac{1}{40 c^3 e} \sqrt{d + e x^2} \left(8 a c^3 (d + e x^2)^2 - b e \sqrt{1 - \frac{1}{c^2 x^2}} x (3 e + c^2 (9 d + 2 e x^2)) + \right. \\
 & \quad \left. 8 b c^3 (d + e x^2)^2 \operatorname{ArcSec}[c x] \right)
 \end{aligned}$$

Problem 129: Unable to integrate problem.

$$\int \frac{(d + e x^2)^{3/2} (a + b \operatorname{ArcSec}[c x])}{x^6} dx$$

Optimal (type 4, 416 leaves, 12 steps):

$$\frac{bc(8c^4d^2 + 23c^2de + 23e^2)\sqrt{-1+c^2x^2}\sqrt{d+ex^2}}{75d\sqrt{c^2x^2}} + \frac{4bc(c^2d+2e)\sqrt{-1+c^2x^2}\sqrt{d+ex^2}}{75x^2\sqrt{c^2x^2}} +$$

$$\frac{bc\sqrt{-1+c^2x^2}(d+ex^2)^{3/2}}{25x^4\sqrt{c^2x^2}} - \frac{(d+ex^2)^{5/2}(a+b\text{ArcSec}[cx])}{5dx^5} -$$

$$\left(bc^2(8c^4d^2 + 23c^2de + 23e^2)x\sqrt{1-c^2x^2}\sqrt{d+ex^2}\text{EllipticE}\left[\text{ArcSin}[cx], -\frac{e}{c^2d}\right] \right) /$$

$$\left(75d\sqrt{c^2x^2}\sqrt{-1+c^2x^2}\sqrt{1+\frac{ex^2}{d}} \right) +$$

$$\left(b(c^2d+e)(8c^4d^2 + 19c^2de + 15e^2)x\sqrt{1-c^2x^2}\sqrt{1+\frac{ex^2}{d}}\text{EllipticF}\left[\text{ArcSin}[cx], -\frac{e}{c^2d}\right] \right) /$$

$$\left(75d\sqrt{c^2x^2}\sqrt{-1+c^2x^2}\sqrt{d+ex^2} \right)$$

Result (type 8, 25 leaves):

$$\int \frac{(d+ex^2)^{3/2}(a+b\text{ArcSec}[cx])}{x^6} dx$$

Problem 130: Unable to integrate problem.

$$\int \frac{(d+ex^2)^{3/2}(a+b\text{ArcSec}[cx])}{x^8} dx$$

Optimal (type 4, 554 leaves, 13 steps):

$$\begin{aligned}
 & \frac{bc (240 c^6 d^3 + 528 c^4 d^2 e + 193 c^2 d e^2 - 247 e^3) \sqrt{-1 + c^2 x^2} \sqrt{d + e x^2}}{3675 d^2 \sqrt{c^2 x^2}} + \\
 & \frac{bc (120 c^4 d^2 + 159 c^2 d e - 37 e^2) \sqrt{-1 + c^2 x^2} \sqrt{d + e x^2}}{3675 d x^2 \sqrt{c^2 x^2}} + \\
 & \frac{bc (30 c^2 d + 11 e) \sqrt{-1 + c^2 x^2} (d + e x^2)^{3/2}}{1225 d x^4 \sqrt{c^2 x^2}} + \frac{bc \sqrt{-1 + c^2 x^2} (d + e x^2)^{5/2}}{49 d x^6 \sqrt{c^2 x^2}} - \\
 & \frac{(d + e x^2)^{5/2} (a + b \operatorname{ArcSec}[c x])}{7 d x^7} + \frac{2 e (d + e x^2)^{5/2} (a + b \operatorname{ArcSec}[c x])}{35 d^2 x^5} - \\
 & \left(bc^2 (240 c^6 d^3 + 528 c^4 d^2 e + 193 c^2 d e^2 - 247 e^3) x \sqrt{1 - c^2 x^2} \sqrt{d + e x^2} \right. \\
 & \quad \left. \operatorname{EllipticE}\left[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}\right] \right) / \left(3675 d^2 \sqrt{c^2 x^2} \sqrt{-1 + c^2 x^2} \sqrt{1 + \frac{e x^2}{d}} \right) + \\
 & \left(2 b (c^2 d + e) (120 c^6 d^3 + 204 c^4 d^2 e + 17 c^2 d e^2 - 105 e^3) x \sqrt{1 - c^2 x^2} \sqrt{1 + \frac{e x^2}{d}} \right. \\
 & \quad \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}\right] \right) / \left(3675 d^2 \sqrt{c^2 x^2} \sqrt{-1 + c^2 x^2} \sqrt{d + e x^2} \right)
 \end{aligned}$$

Result (type 8, 25 leaves):

$$\int \frac{(d + e x^2)^{3/2} (a + b \operatorname{ArcSec}[c x])}{x^8} dx$$

Problem 131: Result unnecessarily involves higher level functions.

$$\int \frac{x^5 (a + b \operatorname{ArcSec}[c x])}{\sqrt{d + e x^2}} dx$$

Optimal (type 3, 321 leaves, 11 steps):

$$\begin{aligned}
 & \frac{b (19 c^2 d - 9 e) x \sqrt{-1 + c^2 x^2} \sqrt{d + e x^2}}{120 c^3 e^2 \sqrt{c^2 x^2}} - \frac{b x \sqrt{-1 + c^2 x^2} (d + e x^2)^{3/2}}{20 c e^2 \sqrt{c^2 x^2}} + \\
 & \frac{d^2 \sqrt{d + e x^2} (a + b \operatorname{ArcSec}[c x])}{e^3} - \frac{2 d (d + e x^2)^{3/2} (a + b \operatorname{ArcSec}[c x])}{3 e^3} + \\
 & \frac{(d + e x^2)^{5/2} (a + b \operatorname{ArcSec}[c x])}{5 e^3} + \frac{8 b c d^{5/2} x \operatorname{ArcTan}\left[\frac{\sqrt{d + e x^2}}{\sqrt{d} \sqrt{-1 + c^2 x^2}}\right]}{15 e^3 \sqrt{c^2 x^2}} - \\
 & \frac{b (45 c^4 d^2 - 10 c^2 d e + 9 e^2) x \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{-1 + c^2 x^2}}{c \sqrt{d + e x^2}}\right]}{120 c^4 e^{5/2} \sqrt{c^2 x^2}}
 \end{aligned}$$

Result (type 6, 629 leaves):

$$\begin{aligned}
 & - \left(\left(b d \sqrt{1 - \frac{1}{c^2 x^2}} x^3 \left((45 c^4 d^2 - 10 c^2 d e + 9 e^2) \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d} \right] \right. \right. \right. \\
 & \quad \left. \left. \left(c^2 d \operatorname{AppellF1} \left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] - e \operatorname{AppellF1} \left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] \right) + \right. \right. \\
 & \quad \left. \left. 4 \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] \left((10 c^4 d e^2 x^2 - 9 c^2 e^3 x^2 + c^6 d^2 (64 d - 45 e x^2)) \right) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d} \right] + 16 c^6 d^2 x^2 \left(-e \operatorname{AppellF1} \left[2, \frac{1}{2}, \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. 3, c^2 x^2, -\frac{e x^2}{d} \right] + c^2 d \operatorname{AppellF1} \left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d} \right] \right) \right) \right) \Bigg/ \\
 & \left(60 c^3 e^2 (-1 + c^2 x^2) \sqrt{d + e x^2} \left(-4 c^2 e x^2 \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] + \right. \right. \\
 & \quad \left. \left. c^2 d \operatorname{AppellF1} \left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] - e \operatorname{AppellF1} \left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] \right) \right) \\
 & \left(4 d \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d} \right] + x^2 \right. \\
 & \quad \left. \left(-e \operatorname{AppellF1} \left[2, \frac{1}{2}, \frac{3}{2}, 3, c^2 x^2, -\frac{e x^2}{d} \right] + c^2 d \operatorname{AppellF1} \left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d} \right] \right) \right) \Bigg) + \\
 & \frac{1}{120 c^3 e^3} \sqrt{d + e x^2} \left(8 a c^3 (8 d^2 - 4 d e x^2 + 3 e^2 x^4) + b e \sqrt{1 - \frac{1}{c^2 x^2}} x \right. \\
 & \quad \left. (-9 e + c^2 (13 d - 6 e x^2)) + \right. \\
 & \quad \left. 8 b c^3 (8 d^2 - 4 d e x^2 + 3 e^2 x^4) \operatorname{ArcSec}[c x] \right)
 \end{aligned}$$

Problem 132: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{x^3 (a + b \operatorname{ArcSec}[c x])}{\sqrt{d + e x^2}} dx$$

Optimal (type 3, 225 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{b x \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}{6 c e \sqrt{c^2 x^2}} - \frac{d \sqrt{d+e x^2} (a+b \operatorname{ArcSec}[c x])}{e^2} + \frac{(d+e x^2)^{3/2} (a+b \operatorname{ArcSec}[c x])}{3 e^2} \\
 & \frac{2 b c d^{3/2} x \operatorname{ArcTan}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d} \sqrt{-1+c^2 x^2}}\right]}{3 e^2 \sqrt{c^2 x^2}} + \frac{b (3 c^2 d - e) x \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{-1+c^2 x^2}}{c \sqrt{d+e x^2}}\right]}{6 c^2 e^{3/2} \sqrt{c^2 x^2}}
 \end{aligned}$$

Result (type 6, 555 leaves):

$$\begin{aligned}
 & \left(b d \sqrt{1 - \frac{1}{c^2 x^2}} x^3 \right. \\
 & \left((3 c^2 d - e) \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right] \left(c^2 d \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] - \right. \right. \\
 & \quad \left. \left. e \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] \right) + 4 \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] \right. \\
 & \left. \left((c^2 e^2 x^2 + c^4 d (4 d - 3 e x^2)) \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right] + c^4 d x^2 \left(-e \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \quad \left. \left. \left. 2, \frac{1}{2}, \frac{3}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] + c^2 d \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] \right) \right) \right) / \\
 & \left(3 c e (-1+c^2 x^2) \sqrt{d+e x^2} \left(-4 c^2 e x^2 \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] + \right. \right. \\
 & \quad \left. \left. c^2 d \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] - e \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] \right) \right. \\
 & \left. \left(4 d \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right] + \right. \right. \\
 & \quad \left. \left. x^2 \left(-e \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] + c^2 d \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] \right) \right) \right) - \\
 & \frac{1}{6 c e^2} \sqrt{d+e x^2} \left(4 a c d + b e \sqrt{1 - \frac{1}{c^2 x^2}} x - 2 a c e x^2 + 2 b c (2 d - e x^2) \operatorname{ArcSec}[c x] \right)
 \end{aligned}$$

Problem 133: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{x (a + b \operatorname{ArcSec}[c x])}{\sqrt{d+e x^2}} dx$$

Optimal (type 3, 132 leaves, 9 steps):

$$\frac{\sqrt{d+e x^2} (a + b \operatorname{ArcSec}[c x])}{e} + \frac{b c \sqrt{d} x \operatorname{ArcTan}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d} \sqrt{-1+c^2 x^2}}\right]}{e \sqrt{c^2 x^2}} - \frac{b x \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{-1+c^2 x^2}}{c \sqrt{d+e x^2}}\right]}{\sqrt{e} \sqrt{c^2 x^2}}$$

Result (type 6, 271 leaves):

$$\left(3 b (c^2 d + e) \sqrt{1 - \frac{1}{c^2 x^2}} \sqrt{d + e x^2} \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}, 1, \frac{3}{2}, \frac{e - c^2 e x^2}{c^2 d + e}, 1 - c^2 x^2\right] \right) /$$

$$\left(c e x \left(-3 (c^2 d + e) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}, 1, \frac{3}{2}, \frac{e - c^2 e x^2}{c^2 d + e}, 1 - c^2 x^2\right] + \right. \right.$$

$$\left. (-1 + c^2 x^2) \left(2 (c^2 d + e) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}, 2, \frac{5}{2}, \frac{e - c^2 e x^2}{c^2 d + e}, 1 - c^2 x^2\right] - \right. \right.$$

$$\left. \left. e \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{2}, 1, \frac{5}{2}, \frac{e - c^2 e x^2}{c^2 d + e}, 1 - c^2 x^2\right] \right) \right) \right) + \frac{\sqrt{d + e x^2} (a + b \operatorname{ArcSec}[c x])}{e}$$

Problem 139: Unable to integrate problem.

$$\int \frac{a + b \operatorname{ArcSec}[c x]}{x^4 \sqrt{d + e x^2}} dx$$

Optimal (type 4, 362 leaves, 11 steps):

$$\frac{b c (2 c^2 d - 5 e) \sqrt{-1 + c^2 x^2} \sqrt{d + e x^2}}{9 d^2 \sqrt{c^2 x^2}} + \frac{b c \sqrt{-1 + c^2 x^2} \sqrt{d + e x^2}}{9 d x^2 \sqrt{c^2 x^2}} -$$

$$\frac{\sqrt{d + e x^2} (a + b \operatorname{ArcSec}[c x])}{3 d x^3} + \frac{2 e \sqrt{d + e x^2} (a + b \operatorname{ArcSec}[c x])}{3 d^2 x} -$$

$$\left(b c^2 (2 c^2 d - 5 e) x \sqrt{1 - c^2 x^2} \sqrt{d + e x^2} \operatorname{EllipticE}[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}] \right) /$$

$$\left(9 d^2 \sqrt{c^2 x^2} \sqrt{-1 + c^2 x^2} \sqrt{1 + \frac{e x^2}{d}} \right) +$$

$$\left(2 b (c^2 d - 3 e) (c^2 d + e) x \sqrt{1 - c^2 x^2} \sqrt{1 + \frac{e x^2}{d}} \operatorname{EllipticF}[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}] \right) /$$

$$\left(9 d^2 \sqrt{c^2 x^2} \sqrt{-1 + c^2 x^2} \sqrt{d + e x^2} \right)$$

Result (type 8, 25 leaves):

$$\int \frac{a + b \operatorname{ArcSec}[c x]}{x^4 \sqrt{d + e x^2}} dx$$

Problem 140: Unable to integrate problem.

$$\int \frac{a + b \operatorname{ArcSec}[c x]}{x^6 \sqrt{d + e x^2}} dx$$

Optimal (type 4, 1006 leaves, 32 steps):

$$\begin{aligned}
 & \frac{8 b c e^2 \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}{15 d^3 \sqrt{c^2 x^2}} - \frac{4 b c e (2 c^2 d+e) \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}{45 d^3 \sqrt{c^2 x^2}} + \\
 & \frac{b c (8 c^4 d^2+3 c^2 d e-2 e^2) \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}{75 d^3 \sqrt{c^2 x^2}} + \\
 & \frac{b c \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}{25 d x^4 \sqrt{c^2 x^2}} - \frac{4 b c e \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}{45 d^2 x^2 \sqrt{c^2 x^2}} + \\
 & \frac{b c (4 c^2 d+e) \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}{75 d^2 x^2 \sqrt{c^2 x^2}} - \frac{\sqrt{d+e x^2} (a+b \operatorname{ArcSec}[c x])}{5 d x^5} + \\
 & \frac{4 e \sqrt{d+e x^2} (a+b \operatorname{ArcSec}[c x])}{15 d^2 x^3} - \frac{8 e^2 \sqrt{d+e x^2} (a+b \operatorname{ArcSec}[c x])}{15 d^3 x} - \\
 & \frac{8 b c^2 e^2 x \sqrt{1-c^2 x^2} \sqrt{d+e x^2} \operatorname{EllipticE}[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}]}{15 d^3 \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{1+\frac{e x^2}{d}}} + \\
 & \left(4 b c^2 e (2 c^2 d+e) x \sqrt{1-c^2 x^2} \sqrt{d+e x^2} \operatorname{EllipticE}[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}] \right) / \\
 & \left(45 d^3 \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{1+\frac{e x^2}{d}} \right) - \\
 & \left(b c^2 (8 c^4 d^2+3 c^2 d e-2 e^2) x \sqrt{1-c^2 x^2} \sqrt{d+e x^2} \operatorname{EllipticE}[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}] \right) / \\
 & \left(75 d^3 \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{1+\frac{e x^2}{d}} \right) + \\
 & \left(b c^2 (8 c^2 d-e) (c^2 d+e) x \sqrt{1-c^2 x^2} \sqrt{1+\frac{e x^2}{d}} \operatorname{EllipticF}[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}] \right) / \\
 & \left(75 d^2 \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{d+e x^2} \right) - \\
 & \left(8 b c^2 e (c^2 d+e) x \sqrt{1-c^2 x^2} \sqrt{1+\frac{e x^2}{d}} \operatorname{EllipticF}[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}] \right) / \\
 & \left(45 d^2 \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{d+e x^2} \right) + \\
 & \left(8 b e^2 (c^2 d+e) x \sqrt{1-c^2 x^2} \sqrt{1+\frac{e x^2}{d}} \operatorname{EllipticF}[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}] \right) / \\
 & \left(15 d^3 \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{d+e x^2} \right)
 \end{aligned}$$

Result (type 8, 25 leaves):

$$\int \frac{a + b \operatorname{ArcSec}[c x]}{x^6 \sqrt{d + e x^2}} dx$$

Problem 141: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{x^5 (a + b \operatorname{ArcSec}[c x])}{(d + e x^2)^{3/2}} dx$$

Optimal (type 3, 252 leaves, 10 steps):

$$\begin{aligned} & -\frac{b x \sqrt{-1 + c^2 x^2} \sqrt{d + e x^2}}{6 c e^2 \sqrt{c^2 x^2}} - \frac{d^2 (a + b \operatorname{ArcSec}[c x])}{e^3 \sqrt{d + e x^2}} - \\ & \frac{2 d \sqrt{d + e x^2} (a + b \operatorname{ArcSec}[c x])}{e^3} + \frac{(d + e x^2)^{3/2} (a + b \operatorname{ArcSec}[c x])}{3 e^3} - \\ & \frac{8 b c d^{3/2} x \operatorname{ArcTan}\left[\frac{\sqrt{d + e x^2}}{\sqrt{d} \sqrt{-1 + c^2 x^2}}\right]}{3 e^3 \sqrt{c^2 x^2}} + \frac{b (9 c^2 d - e) x \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{-1 + c^2 x^2}}{c \sqrt{d + e x^2}}\right]}{6 c^2 e^{5/2} \sqrt{c^2 x^2}} \end{aligned}$$

Result (type 6, 587 leaves):

$$\begin{aligned}
 & \left(b d \sqrt{1 - \frac{1}{c^2 x^2}} x^3 \right. \\
 & \quad \left((9 c^2 d - e) \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right] \left(c^2 d \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] - \right. \right. \\
 & \quad \left. \left. e \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] \right) + 4 \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] \right. \\
 & \quad \left((c^2 e^2 x^2 + c^4 d (16 d - 9 e x^2)) \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right] + 4 c^4 d x^2 \left(-e \operatorname{AppellF1}\left[\right. \right. \right. \\
 & \quad \left. \left. \left. 2, \frac{1}{2}, \frac{3}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] + c^2 d \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] \right) \right) \left. \right) / \\
 & \quad \left(3 c e^2 (-1 + c^2 x^2) \sqrt{d + e x^2} \left(-4 c^2 e x^2 \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] + \right. \right. \\
 & \quad \left. \left. c^2 d \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] - e \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2}\right] \right) \right. \\
 & \quad \left(4 d \operatorname{AppellF1}\left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d}\right] + \right. \\
 & \quad \left. x^2 \left(-e \operatorname{AppellF1}\left[2, \frac{1}{2}, \frac{3}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] + c^2 d \operatorname{AppellF1}\left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d}\right] \right) \right) \left. \right) + \\
 & \quad \frac{1}{6 c e^3 \sqrt{d + e x^2}} \left(-b e \sqrt{1 - \frac{1}{c^2 x^2}} x (d + e x^2) - 2 a c (8 d^2 + 4 d e x^2 - e^2 x^4) - \right. \\
 & \quad \left. 2 b c (8 d^2 + 4 d e x^2 - e^2 x^4) \operatorname{ArcSec}[c x] \right)
 \end{aligned}$$

Problem 142: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{x^3 (a + b \operatorname{ArcSec}[c x])}{(d + e x^2)^{3/2}} dx$$

Optimal (type 3, 157 leaves, 9 steps):

$$\frac{d (a + b \operatorname{ArcSec}[c x])}{e^2 \sqrt{d + e x^2}} + \frac{\sqrt{d + e x^2} (a + b \operatorname{ArcSec}[c x])}{e^2} + \\
 \frac{2 b c \sqrt{d} x \operatorname{ArcTan}\left[\frac{\sqrt{d + e x^2}}{\sqrt{d} \sqrt{-1 + c^2 x^2}}\right]}{e^2 \sqrt{c^2 x^2}} - \frac{b x \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{-1 + c^2 x^2}}{c \sqrt{d + e x^2}}\right]}{e^{3/2} \sqrt{c^2 x^2}}$$

Result (type 6, 326 leaves):

$$\begin{aligned}
 & - \left(\left(2 b c d \sqrt{1 - \frac{1}{c^2 x^2}} x^3 \right. \right. \\
 & \quad \left. \left(\left(\left(2 c^2 \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] \right) / \left(4 c^2 e x^2 \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] - c^2 d \operatorname{AppellF1} \left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] + \right. \right. \\
 & \quad \left. \left. \left. e \operatorname{AppellF1} \left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] \right) \right) + \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d} \right] / \right. \\
 & \quad \left. \left(4 d \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d} \right] + x^2 \left(-e \operatorname{AppellF1} \left[2, \frac{1}{2}, \frac{3}{2}, 3, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. c^2 x^2, -\frac{e x^2}{d} \right] + c^2 d \operatorname{AppellF1} \left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d} \right] \right) \right) \right) / \\
 & \quad \left. \left(e (-1 + c^2 x^2) \sqrt{d + e x^2} \right) \right) + \frac{(2 d + e x^2) (a + b \operatorname{ArcSec}[c x])}{e^2 \sqrt{d + e x^2}}
 \end{aligned}$$

Problem 143: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{x (a + b \operatorname{ArcSec}[c x])}{(d + e x^2)^{3/2}} dx$$

Optimal (type 3, 80 leaves, 4 steps):

$$\frac{a + b \operatorname{ArcSec}[c x]}{e \sqrt{d + e x^2}} - \frac{b c x \operatorname{ArcTan} \left[\frac{\sqrt{d + e x^2}}{\sqrt{d} \sqrt{-1 + c^2 x^2}} \right]}{\sqrt{d} e \sqrt{c^2 x^2}}$$

Result (type 6, 190 leaves):

$$\begin{aligned}
 & - \left(\left(2 b c^3 \sqrt{1 - \frac{1}{c^2 x^2}} x^3 \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] \right) / \right. \\
 & \quad \left((-1 + c^2 x^2) \sqrt{d + e x^2} \left(4 c^2 e x^2 \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] - c^2 d \operatorname{AppellF1} \left[2, \frac{1}{2}, \frac{3}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] + e \operatorname{AppellF1} \left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] \right) \right) \right) - \frac{a + b \operatorname{ArcSec}[c x]}{e \sqrt{d + e x^2}}
 \end{aligned}$$

Problem 149: Unable to integrate problem.

$$\int \frac{a + b \operatorname{ArcSec}[c x]}{x^2 (d + e x^2)^{3/2}} dx$$

Optimal (type 4, 274 leaves, 10 steps):

$$\frac{b c \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}{d^2 \sqrt{c^2 x^2}} - \frac{a+b \operatorname{ArcSec}[c x]}{d x \sqrt{d+e x^2}} - \frac{2 e x (a+b \operatorname{ArcSec}[c x])}{d^2 \sqrt{d+e x^2}} -$$

$$\frac{b c^2 x \sqrt{1-c^2 x^2} \sqrt{d+e x^2} \operatorname{EllipticE}[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}]}{d^2 \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{1+\frac{e x^2}{d}}} +$$

$$\frac{b (c^2 d+2 e) x \sqrt{1-c^2 x^2} \sqrt{1+\frac{e x^2}{d}} \operatorname{EllipticF}[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}]}{d^2 \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}$$

Result (type 8, 25 leaves):

$$\int \frac{a+b \operatorname{ArcSec}[c x]}{x^2 (d+e x^2)^{3/2}} dx$$

Problem 150: Unable to integrate problem.

$$\int \frac{a+b \operatorname{ArcSec}[c x]}{x^4 (d+e x^2)^{3/2}} dx$$

Optimal (type 4, 701 leaves, 25 steps):

$$\frac{2 b c\left(c^2 d-e\right) \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}{9 d^3 \sqrt{c^2 x^2}}-\frac{4 b c e \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}{3 d^3 \sqrt{c^2 x^2}}+\frac{b c \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}{9 d^2 x^2 \sqrt{c^2 x^2}}-\frac{a+b \operatorname{ArcSec}[c x]}{3 d x^3 \sqrt{d+e x^2}}+\frac{4 e(a+b \operatorname{ArcSec}[c x])}{3 d^2 x \sqrt{d+e x^2}}+\frac{8 e^2 x(a+b \operatorname{ArcSec}[c x])}{3 d^3 \sqrt{d+e x^2}}-\left(2 b c^2\left(c^2 d-e\right) x \sqrt{1-c^2 x^2} \sqrt{d+e x^2} \operatorname{EllipticE}\left[\operatorname{ArcSin}[c x],-\frac{e}{c^2 d}\right]\right) / \left(9 d^3 \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{1+\frac{e x^2}{d}}\right)+\frac{4 b c^2 e x \sqrt{1-c^2 x^2} \sqrt{d+e x^2} \operatorname{EllipticE}\left[\operatorname{ArcSin}[c x],-\frac{e}{c^2 d}\right]}{3 d^3 \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{1+\frac{e x^2}{d}}}+\left(b c^2\left(2 c^2 d-e\right) x \sqrt{1-c^2 x^2} \sqrt{1+\frac{e x^2}{d}} \operatorname{EllipticF}\left[\operatorname{ArcSin}[c x],-\frac{e}{c^2 d}\right]\right) / \left(9 d^2 \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}\right)-\frac{4 b c^2 e x \sqrt{1-c^2 x^2} \sqrt{1+\frac{e x^2}{d}} \operatorname{EllipticF}\left[\operatorname{ArcSin}[c x],-\frac{e}{c^2 d}\right]}{3 d^2 \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}-\frac{8 b e^2 x \sqrt{1-c^2 x^2} \sqrt{1+\frac{e x^2}{d}} \operatorname{EllipticF}\left[\operatorname{ArcSin}[c x],-\frac{e}{c^2 d}\right]}{3 d^3 \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}$$

Result (type 8, 25 leaves):

$$\int \frac{a+b \operatorname{ArcSec}[c x]}{x^4(d+e x^2)^{3 / 2}} d x$$

Problem 151: Result unnecessarily involves higher level functions.

$$\int \frac{x^5(a+b \operatorname{ArcSec}[c x])}{(d+e x^2)^{5 / 2}} d x$$

Optimal (type 3, 244 leaves, 10 steps):

$$-\frac{b c d x \sqrt{-1+c^2 x^2}}{3 e^2\left(c^2 d+e\right) \sqrt{c^2 x^2} \sqrt{d+e x^2}}-\frac{d^2(a+b \operatorname{ArcSec}[c x])}{3 e^3(d+e x^2)^{3 / 2}}+\frac{2 d(a+b \operatorname{ArcSec}[c x])}{e^3 \sqrt{d+e x^2}}+\frac{\sqrt{d+e x^2}(a+b \operatorname{ArcSec}[c x])}{e^3}+\frac{8 b c \sqrt{d} x \operatorname{ArcTan}\left[\frac{\sqrt{d+e x^2}}{\sqrt{d} \sqrt{-1+c^2 x^2}}\right]}{3 e^3 \sqrt{c^2 x^2}}-\frac{b x \operatorname{ArcTanh}\left[\frac{\sqrt{e} \sqrt{-1+c^2 x^2}}{c \sqrt{d+e x^2}}\right]}{e^{5 / 2} \sqrt{c^2 x^2}}$$

Result (type 6, 417 leaves):

$$\begin{aligned}
 & \left(2 b c d \sqrt{1 - \frac{1}{c^2 x^2}} x^3 \right. \\
 & \quad \left(\left(8 c^2 \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] \right) / \left(4 c^2 e x^2 \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] - \right. \right. \\
 & \quad \left. \left. c^2 d \operatorname{AppellF1} \left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] + e \operatorname{AppellF1} \left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] \right) - \right. \\
 & \quad \left(3 \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d} \right] \right) / \left(4 d \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, c^2 x^2, -\frac{e x^2}{d} \right] + \right. \\
 & \quad \left. x^2 \left(-e \operatorname{AppellF1} \left[2, \frac{1}{2}, \frac{3}{2}, 3, c^2 x^2, -\frac{e x^2}{d} \right] + \right. \right. \\
 & \quad \left. \left. c^2 d \operatorname{AppellF1} \left[2, \frac{3}{2}, \frac{1}{2}, 3, c^2 x^2, -\frac{e x^2}{d} \right] \right) \right) / \left(3 e^2 (-1 + c^2 x^2) \sqrt{d + e x^2} \right) + \\
 & \left(-b c d e \sqrt{1 - \frac{1}{c^2 x^2}} x (d + e x^2) + a (c^2 d + e) (8 d^2 + 12 d e x^2 + 3 e^2 x^4) + \right. \\
 & \quad \left. b (c^2 d + e) (8 d^2 + 12 d e x^2 + 3 e^2 x^4) \operatorname{ArcSec}[c x] \right) / \\
 & \quad \left(3 e^3 (c^2 d + e) (d + e x^2)^{3/2} \right)
 \end{aligned}$$

Problem 152: Result unnecessarily involves higher level functions.

$$\int \frac{x^3 (a + b \operatorname{ArcSec}[c x])}{(d + e x^2)^{5/2}} dx$$

Optimal (type 3, 163 leaves, 7 steps):

$$\begin{aligned}
 & \frac{b c x \sqrt{-1 + c^2 x^2}}{3 e (c^2 d + e) \sqrt{c^2 x^2} \sqrt{d + e x^2}} + \frac{d (a + b \operatorname{ArcSec}[c x])}{3 e^2 (d + e x^2)^{3/2}} - \\
 & \frac{a + b \operatorname{ArcSec}[c x]}{e^2 \sqrt{d + e x^2}} - \frac{2 b c x \operatorname{ArcTan} \left[\frac{\sqrt{d + e x^2}}{\sqrt{d} \sqrt{-1 + c^2 x^2}} \right]}{3 \sqrt{d} e^2 \sqrt{c^2 x^2}}
 \end{aligned}$$

Result (type 6, 269 leaves):

$$\begin{aligned}
 & - \left(\left(4 b c^3 \sqrt{1 - \frac{1}{c^2 x^2}} x^3 \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] \right) / \right. \\
 & \quad \left. \left(3 e (-1 + c^2 x^2) \sqrt{d + e x^2} \left(4 c^2 e x^2 \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] - \right. \right. \right. \\
 & \quad \quad \left. \left. \left. c^2 d \operatorname{AppellF1} \left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] + e \operatorname{AppellF1} \left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] \right) \right) \right) + \\
 & \left(b c e \sqrt{1 - \frac{1}{c^2 x^2}} x (d + e x^2) - a (c^2 d + e) (2 d + 3 e x^2) - b (c^2 d + e) (2 d + 3 e x^2) \operatorname{ArcSec}[c x] \right) / \\
 & \quad \left(3 e^2 (c^2 d + e) (d + e x^2)^{3/2} \right)
 \end{aligned}$$

Problem 153: Result unnecessarily involves higher level functions.

$$\int \frac{x (a + b \operatorname{ArcSec}[c x])}{(d + e x^2)^{5/2}} dx$$

Optimal (type 3, 138 leaves, 5 steps):

$$- \frac{b c x \sqrt{-1 + c^2 x^2}}{3 d (c^2 d + e) \sqrt{c^2 x^2} \sqrt{d + e x^2}} - \frac{a + b \operatorname{ArcSec}[c x]}{3 e (d + e x^2)^{3/2}} - \frac{b c x \operatorname{ArcTan} \left[\frac{\sqrt{d + e x^2}}{\sqrt{d} \sqrt{-1 + c^2 x^2}} \right]}{3 d^{3/2} e \sqrt{c^2 x^2}}$$

Result (type 6, 255 leaves):

$$\begin{aligned}
 & - \left(\left(2 b c^3 \sqrt{1 - \frac{1}{c^2 x^2}} x^3 \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] \right) / \right. \\
 & \quad \left. \left(3 d (-1 + c^2 x^2) \sqrt{d + e x^2} \left(4 c^2 e x^2 \operatorname{AppellF1} \left[1, \frac{1}{2}, \frac{1}{2}, 2, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] - \right. \right. \right. \\
 & \quad \quad \left. \left. \left. c^2 d \operatorname{AppellF1} \left[2, \frac{1}{2}, \frac{3}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] + e \operatorname{AppellF1} \left[2, \frac{3}{2}, \frac{1}{2}, 3, \frac{1}{c^2 x^2}, -\frac{d}{e x^2} \right] \right) \right) \right) + \\
 & \left(-a d (c^2 d + e) - b c e \sqrt{1 - \frac{1}{c^2 x^2}} x (d + e x^2) - b d (c^2 d + e) \operatorname{ArcSec}[c x] \right) / \\
 & \quad \left(3 d e (c^2 d + e) (d + e x^2)^{3/2} \right)
 \end{aligned}$$

Problem 159: Unable to integrate problem.

$$\int \frac{a + b \operatorname{ArcSec}[c x]}{(d + e x^2)^{5/2}} dx$$

Optimal (type 4, 296 leaves, 10 steps):

$$\frac{b c e x^2 \sqrt{-1+c^2 x^2}}{3 d^2 (c^2 d+e) \sqrt{c^2 x^2} \sqrt{d+e x^2}} + \frac{x (a+b \operatorname{ArcSec}[c x])}{3 d (d+e x^2)^{3/2}} +$$

$$\frac{2 x (a+b \operatorname{ArcSec}[c x])}{3 d^2 \sqrt{d+e x^2}} - \frac{b c^2 x \sqrt{1-c^2 x^2} \sqrt{d+e x^2} \operatorname{EllipticE}[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}]}{3 d^2 (c^2 d+e) \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{1+\frac{e x^2}{d}}}$$

$$\frac{2 b x \sqrt{1-c^2 x^2} \sqrt{1+\frac{e x^2}{d}} \operatorname{EllipticF}[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}]}{3 d^2 \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}$$

Result (type 8, 22 leaves):

$$\int \frac{a+b \operatorname{ArcSec}[c x]}{(d+e x^2)^{5/2}} dx$$

Problem 160: Unable to integrate problem.

$$\int \frac{a+b \operatorname{ArcSec}[c x]}{x^2 (d+e x^2)^{5/2}} dx$$

Optimal (type 4, 631 leaves, 26 steps):

$$-\frac{b c e \sqrt{-1+c^2 x^2}}{d^2 (c^2 d+e) \sqrt{c^2 x^2} \sqrt{d+e x^2}} - \frac{4 b c e^2 x^2 \sqrt{-1+c^2 x^2}}{3 d^3 (c^2 d+e) \sqrt{c^2 x^2} \sqrt{d+e x^2}} +$$

$$\frac{b c (c^2 d+2 e) \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}{d^3 (c^2 d+e) \sqrt{c^2 x^2}} - \frac{a+b \operatorname{ArcSec}[c x]}{d x (d+e x^2)^{3/2}} - \frac{4 e x (a+b \operatorname{ArcSec}[c x])}{3 d^2 (d+e x^2)^{3/2}} -$$

$$\frac{8 e x (a+b \operatorname{ArcSec}[c x])}{3 d^3 \sqrt{d+e x^2}} + \frac{4 b c^2 e x \sqrt{1-c^2 x^2} \sqrt{d+e x^2} \operatorname{EllipticE}[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}]}{3 d^3 (c^2 d+e) \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{1+\frac{e x^2}{d}}}$$

$$\left(b c^2 (c^2 d+2 e) x \sqrt{1-c^2 x^2} \sqrt{d+e x^2} \operatorname{EllipticE}[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}] \right) /$$

$$\left(d^3 (c^2 d+e) \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{1+\frac{e x^2}{d}} \right) +$$

$$\frac{b c^2 x \sqrt{1-c^2 x^2} \sqrt{1+\frac{e x^2}{d}} \operatorname{EllipticF}[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}]}{d^2 \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}} +$$

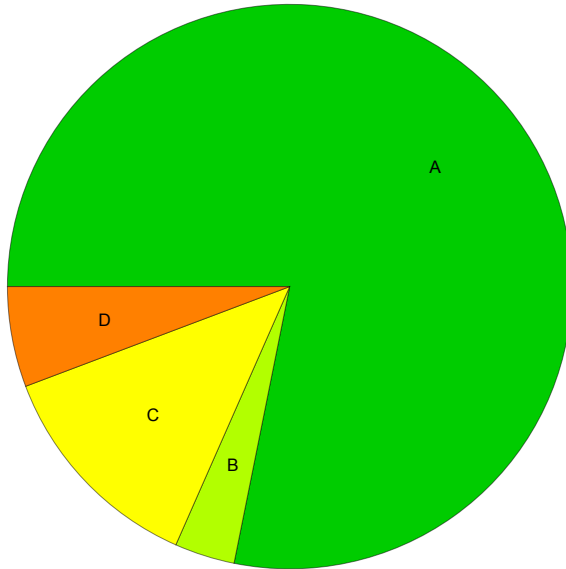
$$\frac{8 b e x \sqrt{1-c^2 x^2} \sqrt{1+\frac{e x^2}{d}} \operatorname{EllipticF}[\operatorname{ArcSin}[c x], -\frac{e}{c^2 d}]}{3 d^3 \sqrt{c^2 x^2} \sqrt{-1+c^2 x^2} \sqrt{d+e x^2}}$$

Result (type 8, 25 leaves):

$$\int \frac{a + b \operatorname{ArcSec}[c x]}{x^2 (d + e x^2)^{5/2}} dx$$

Summary of Integration Test Results

174 integration problems



A - 136 optimal antiderivatives

B - 6 more than twice size of optimal antiderivatives

C - 22 unnecessarily complex antiderivatives

D - 10 unable to integrate problems

E - 0 integration timeouts