

# Mathematica 11.3 Integration Test Results

Test results for the 218 problems in "8.2 Fresnel integral functions.m"

Problem 9: Unable to integrate problem.

$$\int \frac{\text{FresnelS}[b x]}{x} dx$$

Optimal (type 5, 73 leaves, 3 steps):

$$\frac{1}{2} i b x \text{HypergeometricPFQ}\left[\left\{\frac{1}{2}, \frac{1}{2}\right\}, \left\{\frac{3}{2}, \frac{3}{2}\right\}, -\frac{1}{2} i b^2 \pi x^2\right] - \frac{1}{2} i b x \text{HypergeometricPFQ}\left[\left\{\frac{1}{2}, \frac{1}{2}\right\}, \left\{\frac{3}{2}, \frac{3}{2}\right\}, \frac{1}{2} i b^2 \pi x^2\right]$$

Result (type 8, 10 leaves):

$$\int \frac{\text{FresnelS}[b x]}{x} dx$$

Problem 22: Result more than twice size of optimal antiderivative.

$$\int \text{FresnelS}[a + b x] dx$$

Optimal (type 4, 36 leaves, 1 step):

$$\frac{\cos\left[\frac{1}{2} \pi (a + b x)^2\right]}{b \pi} + \frac{(a + b x) \text{FresnelS}[a + b x]}{b}$$

Result (type 4, 89 leaves):

$$\frac{\cos\left[\frac{a^2 \pi}{2}\right] \cos\left[a b \pi x + \frac{1}{2} b^2 \pi x^2\right]}{b \pi} + \frac{a \text{FresnelS}[a + b x]}{b} + x \text{FresnelS}[a + b x] - \frac{\sin\left[\frac{a^2 \pi}{2}\right] \sin\left[a b \pi x + \frac{1}{2} b^2 \pi x^2\right]}{b \pi}$$

Problem 28: Result more than twice size of optimal antiderivative.

$$\int \text{FresnelS}[a + b x] dx$$

Optimal (type 4, 36 leaves, 1 step):

$$\frac{\cos\left[\frac{1}{2}\pi(a+bx)^2\right]}{b\pi} + \frac{(a+bx)\text{FresnelS}[a+bx]}{b}$$

Result (type 4, 89 leaves):

$$\frac{\cos\left[\frac{a^2\pi}{2}\right]\cos\left[ab\pi x + \frac{1}{2}b^2\pi x^2\right]}{b\pi} + \frac{a\text{FresnelS}[a+bx]}{b} +$$

$$x\text{FresnelS}[a+bx] - \frac{\sin\left[\frac{a^2\pi}{2}\right]\sin\left[ab\pi x + \frac{1}{2}b^2\pi x^2\right]}{b\pi}$$

Problem 31: Unable to integrate problem.

$$\int x^7 \text{FresnelS}[bx]^2 dx$$

Optimal (type 4, 253 leaves, 23 steps):

$$-\frac{105x^2}{16b^6\pi^4} + \frac{7x^6}{48b^2\pi^2} - \frac{55x^2\cos[b^2\pi x^2]}{16b^6\pi^4} + \frac{x^6\cos[b^2\pi x^2]}{16b^2\pi^2} -$$

$$\frac{35x^3\cos\left[\frac{1}{2}b^2\pi x^2\right]\text{FresnelS}[bx]}{4b^5\pi^3} + \frac{x^7\cos\left[\frac{1}{2}b^2\pi x^2\right]\text{FresnelS}[bx]}{4b\pi} -$$

$$\frac{105\text{FresnelS}[bx]^2}{8b^8\pi^4} + \frac{1}{8}x^8\text{FresnelS}[bx]^2 + \frac{105x\text{FresnelS}[bx]\sin\left[\frac{1}{2}b^2\pi x^2\right]}{4b^7\pi^4} -$$

$$\frac{7x^5\text{FresnelS}[bx]\sin\left[\frac{1}{2}b^2\pi x^2\right]}{4b^3\pi^2} + \frac{10\sin[b^2\pi x^2]}{b^8\pi^5} - \frac{5x^4\sin[b^2\pi x^2]}{8b^4\pi^3}$$

Result (type 8, 12 leaves):

$$\int x^7 \text{FresnelS}[bx]^2 dx$$

Problem 33: Unable to integrate problem.

$$\int x^5 \text{FresnelS}[bx]^2 dx$$

Optimal (type 5, 265 leaves, 16 steps):

$$\begin{aligned}
 & \frac{5 x^4}{24 b^2 \pi^2} - \frac{11 \operatorname{Cos}\left[b^2 \pi x^2\right]}{6 b^6 \pi^4} + \frac{x^4 \operatorname{Cos}\left[b^2 \pi x^2\right]}{12 b^2 \pi^2} - \frac{5 x \operatorname{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \operatorname{FresnelS}[b x]}{b^5 \pi^3} + \\
 & \frac{x^5 \operatorname{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \operatorname{FresnelS}[b x]}{3 b \pi} + \frac{5 \operatorname{FresnelC}[b x] \operatorname{FresnelS}[b x]}{2 b^6 \pi^3} + \\
 & \frac{1}{6} x^6 \operatorname{FresnelS}[b x]^2 - \frac{5 i x^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\},\left\{\frac{3}{2}, 2\right\},-\frac{1}{2} i b^2 \pi x^2\right]}{8 b^4 \pi^3} + \\
 & \frac{5 i x^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\},\left\{\frac{3}{2}, 2\right\},\frac{1}{2} i b^2 \pi x^2\right]}{8 b^4 \pi^3} - \\
 & \frac{5 x^3 \operatorname{FresnelS}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{3 b^3 \pi^2} - \frac{7 x^2 \operatorname{Sin}\left[b^2 \pi x^2\right]}{12 b^4 \pi^3}
 \end{aligned}$$

Result (type 8, 12 leaves):

$$\int x^5 \operatorname{FresnelS}[b x]^2 dx$$

**Problem 35: Unable to integrate problem.**

$$\int x^3 \operatorname{FresnelS}[b x]^2 dx$$

Optimal (type 4, 140 leaves, 10 steps):

$$\begin{aligned}
 & \frac{3 x^2}{8 b^2 \pi^2} + \frac{x^2 \operatorname{Cos}\left[b^2 \pi x^2\right]}{8 b^2 \pi^2} + \frac{x^3 \operatorname{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \operatorname{FresnelS}[b x]}{2 b \pi} + \frac{3 \operatorname{FresnelS}[b x]^2}{4 b^4 \pi^2} + \\
 & \frac{1}{4} x^4 \operatorname{FresnelS}[b x]^2 - \frac{3 x \operatorname{FresnelS}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{2 b^3 \pi^2} - \frac{\operatorname{Sin}\left[b^2 \pi x^2\right]}{2 b^4 \pi^3}
 \end{aligned}$$

Result (type 8, 12 leaves):

$$\int x^3 \operatorname{FresnelS}[b x]^2 dx$$

**Problem 37: Unable to integrate problem.**

$$\int x \operatorname{FresnelS}[b x]^2 dx$$

Optimal (type 5, 143 leaves, 5 steps):

$$\begin{aligned}
 & \frac{\operatorname{Cos}\left[b^2 \pi x^2\right]}{4 b^2 \pi^2} + \frac{x \operatorname{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \operatorname{FresnelS}[b x]}{b \pi} - \frac{\operatorname{FresnelC}[b x] \operatorname{FresnelS}[b x]}{2 b^2 \pi} + \\
 & \frac{1}{2} x^2 \operatorname{FresnelS}[b x]^2 + \frac{i x^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\},\left\{\frac{3}{2}, 2\right\},-\frac{1}{2} i b^2 \pi x^2\right]}{8 \pi} - \\
 & \frac{i x^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\},\left\{\frac{3}{2}, 2\right\},\frac{1}{2} i b^2 \pi x^2\right]}{8 \pi}
 \end{aligned}$$

Result (type 8, 10 leaves):

$$\int x \operatorname{FresnelS}[b x]^2 dx$$

**Problem 43: Unable to integrate problem.**

$$\int \frac{\operatorname{FresnelS}[b x]^2}{x^5} dx$$

Optimal (type 4, 127 leaves, 9 steps):

$$\begin{aligned} & -\frac{b^2}{24 x^2} + \frac{b^2 \operatorname{Cos}[b^2 \pi x^2]}{24 x^2} - \frac{b^3 \pi \operatorname{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \operatorname{FresnelS}[b x]}{6 x} - \frac{1}{12} b^4 \pi^2 \operatorname{FresnelS}[b x]^2 - \\ & \frac{\operatorname{FresnelS}[b x]^2}{4 x^4} - \frac{b \operatorname{FresnelS}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{6 x^3} + \frac{1}{12} b^4 \pi \operatorname{SinIntegral}[b^2 \pi x^2] \end{aligned}$$

Result (type 8, 12 leaves):

$$\int \frac{\operatorname{FresnelS}[b x]^2}{x^5} dx$$

**Problem 47: Unable to integrate problem.**

$$\int \frac{\operatorname{FresnelS}[b x]^2}{x^9} dx$$

Optimal (type 4, 242 leaves, 20 steps):

$$\begin{aligned} & -\frac{b^2}{336 x^6} + \frac{b^6 \pi^2}{1680 x^2} + \frac{b^2 \operatorname{Cos}[b^2 \pi x^2]}{336 x^6} - \frac{b^6 \pi^2 \operatorname{Cos}[b^2 \pi x^2]}{336 x^2} - \\ & \frac{b^3 \pi \operatorname{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \operatorname{FresnelS}[b x]}{140 x^5} + \frac{b^7 \pi^3 \operatorname{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \operatorname{FresnelS}[b x]}{420 x} + \\ & \frac{1}{840} b^8 \pi^4 \operatorname{FresnelS}[b x]^2 - \frac{\operatorname{FresnelS}[b x]^2}{8 x^8} - \frac{b \operatorname{FresnelS}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{28 x^7} + \\ & \frac{b^5 \pi^2 \operatorname{FresnelS}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{420 x^3} - \frac{b^4 \pi \operatorname{Sin}[b^2 \pi x^2]}{420 x^4} - \frac{1}{280} b^8 \pi^3 \operatorname{SinIntegral}[b^2 \pi x^2] \end{aligned}$$

Result (type 8, 12 leaves):

$$\int \frac{\operatorname{FresnelS}[b x]^2}{x^9} dx$$

**Problem 49: Unable to integrate problem.**

$$\int (c + d x)^2 \operatorname{FresnelS}[a + b x]^2 dx$$

Optimal (type 5, 497 leaves, 18 steps):

$$\begin{aligned}
 & \frac{2 d^2 x}{3 b^2 \pi^2} + \frac{d (b c - a d) \operatorname{Cos}\left[\pi (a + b x)^2\right]}{2 b^3 \pi^2} + \frac{d^2 (a + b x) \operatorname{Cos}\left[\pi (a + b x)^2\right]}{6 b^3 \pi^2} - \\
 & \frac{5 d^2 \operatorname{FresnelC}\left[\sqrt{2} (a + b x)\right]}{6 \sqrt{2} b^3 \pi^2} + \frac{2 (b c - a d)^2 \operatorname{Cos}\left[\frac{1}{2} \pi (a + b x)^2\right] \operatorname{FresnelS}[a + b x]}{b^3 \pi} + \\
 & \frac{2 d (b c - a d) (a + b x) \operatorname{Cos}\left[\frac{1}{2} \pi (a + b x)^2\right] \operatorname{FresnelS}[a + b x]}{b^3 \pi} + \\
 & \frac{2 d^2 (a + b x)^2 \operatorname{Cos}\left[\frac{1}{2} \pi (a + b x)^2\right] \operatorname{FresnelS}[a + b x]}{3 b^3 \pi} - \\
 & \frac{d (b c - a d) \operatorname{FresnelC}[a + b x] \operatorname{FresnelS}[a + b x]}{b^3 \pi} + \\
 & \frac{(b c - a d)^2 (a + b x) \operatorname{FresnelS}[a + b x]^2}{b^3} + \frac{d (b c - a d) (a + b x)^2 \operatorname{FresnelS}[a + b x]^2}{b^3} + \\
 & \frac{d^2 (a + b x)^3 \operatorname{FresnelS}[a + b x]^2}{3 b^3} - \frac{(b c - a d)^2 \operatorname{FresnelS}\left[\sqrt{2} (a + b x)\right]}{\sqrt{2} b^3 \pi} + \frac{1}{4 b^3 \pi} \\
 & i d (b c - a d) (a + b x)^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i \pi (a + b x)^2\right] - \\
 & \frac{1}{4 b^3 \pi} i d (b c - a d) (a + b x)^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} i \pi (a + b x)^2\right] - \\
 & \frac{4 d^2 \operatorname{FresnelS}[a + b x] \operatorname{Sin}\left[\frac{1}{2} \pi (a + b x)^2\right]}{3 b^3 \pi^2}
 \end{aligned}$$

Result (type 8, 18 leaves):

$$\int (c + d x)^2 \operatorname{FresnelS}[a + b x]^2 dx$$

**Problem 50: Unable to integrate problem.**

$$\int (c + d x) \operatorname{FresnelS}[a + b x]^2 dx$$

Optimal (type 5, 279 leaves, 10 steps):

$$\begin{aligned}
& \frac{d \operatorname{Cos}\left[\pi (a+b x)^2\right]}{4 b^2 \pi^2} + \frac{2 (b c-a d) \operatorname{Cos}\left[\frac{1}{2} \pi (a+b x)^2\right] \operatorname{FresnelS}[a+b x]}{b^2 \pi} + \\
& \frac{d (a+b x) \operatorname{Cos}\left[\frac{1}{2} \pi (a+b x)^2\right] \operatorname{FresnelS}[a+b x]}{b^2 \pi} - \\
& \frac{d \operatorname{FresnelC}[a+b x] \operatorname{FresnelS}[a+b x]}{2 b^2 \pi} + \frac{(b c-a d) (a+b x) \operatorname{FresnelS}[a+b x]^2}{b^2} + \\
& \frac{d (a+b x)^2 \operatorname{FresnelS}[a+b x]^2}{2 b^2} - \frac{(b c-a d) \operatorname{FresnelS}\left[\sqrt{2} (a+b x)\right]}{\sqrt{2} b^2 \pi} + \\
& \frac{i d (a+b x)^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\},\left\{\frac{3}{2}, 2\right\},-\frac{1}{2} i \pi (a+b x)^2\right]}{8 b^2 \pi} - \\
& \frac{i d (a+b x)^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\},\left\{\frac{3}{2}, 2\right\},\frac{1}{2} i \pi (a+b x)^2\right]}{8 b^2 \pi}
\end{aligned}$$

Result (type 8, 16 leaves):

$$\int (c+d x) \operatorname{FresnelS}[a+b x]^2 dx$$

**Problem 57: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{FresnelS}\left[d (a+b \operatorname{Log}[c x^n])\right]}{x} dx$$

Optimal (type 4, 65 leaves, 3 steps):

$$\frac{\operatorname{Cos}\left[\frac{1}{2} d^2 \pi (a+b \operatorname{Log}[c x^n])^2\right]}{b d n \pi} + \frac{\operatorname{FresnelS}\left[d (a+b \operatorname{Log}[c x^n])\right] (a+b \operatorname{Log}[c x^n])}{b n}$$

Result (type 4, 164 leaves):

$$\begin{aligned}
& \frac{\operatorname{Cos}\left[\frac{1}{2} a^2 d^2 \pi\right] \operatorname{Cos}\left[a b d^2 \pi \operatorname{Log}[c x^n] + \frac{1}{2} b^2 d^2 \pi \operatorname{Log}[c x^n]^2\right]}{b d n \pi} + \\
& \frac{a \operatorname{FresnelS}\left[d (a+b \operatorname{Log}[c x^n])\right]}{b n} + \frac{\operatorname{FresnelS}\left[d (a+b \operatorname{Log}[c x^n])\right] \operatorname{Log}[c x^n]}{n} - \\
& \frac{\operatorname{Sin}\left[\frac{1}{2} a^2 d^2 \pi\right] \operatorname{Sin}\left[a b d^2 \pi \operatorname{Log}[c x^n] + \frac{1}{2} b^2 d^2 \pi \operatorname{Log}[c x^n]^2\right]}{b d n \pi}
\end{aligned}$$

**Problem 61: Unable to integrate problem.**

$$\int e^{c+\frac{1}{2} i b^2 \pi x^2} \operatorname{FresnelS}[b x] dx$$

Optimal (type 5, 64 leaves, 4 steps):

$$-\frac{e^c \operatorname{Erfi}\left[\left(\frac{1}{2}+\frac{i}{2}\right) b \sqrt{\pi} x\right]^2}{8 b} + \frac{1}{4} i b e^c x^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\},\left\{\frac{3}{2}, 2\right\},\frac{1}{2} i b^2 \pi x^2\right]$$

Result (type 8, 24 leaves):

$$\int e^{c + \frac{1}{2} i b^2 \pi x^2} \text{FresnelS}[b x] dx$$

**Problem 62: Unable to integrate problem.**

$$\int e^{c - \frac{1}{2} i b^2 \pi x^2} \text{FresnelS}[b x] dx$$

Optimal (type 5, 64 leaves, 4 steps):

$$\frac{e^c \text{Erf}\left[\left(\frac{1}{2} + \frac{i}{2}\right) b \sqrt{\pi} x\right]^2}{8 b} - \frac{1}{4} i b e^c x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i b^2 \pi x^2\right]$$

Result (type 8, 24 leaves):

$$\int e^{c - \frac{1}{2} i b^2 \pi x^2} \text{FresnelS}[b x] dx$$

**Problem 63: Unable to integrate problem.**

$$\int \text{FresnelS}[b x] \text{Sin}\left[c + \frac{1}{2} b^2 \pi x^2\right] dx$$

Optimal (type 5, 101 leaves, 4 steps):

$$\frac{\text{Cos}[c] \text{FresnelS}[b x]^2}{2 b} + \frac{\text{FresnelC}[b x] \text{FresnelS}[b x] \text{Sin}[c]}{2 b} - \frac{1}{8} i b x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i b^2 \pi x^2\right] \text{Sin}[c] + \frac{1}{8} i b x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} i b^2 \pi x^2\right] \text{Sin}[c]$$

Result (type 8, 21 leaves):

$$\int \text{FresnelS}[b x] \text{Sin}\left[c + \frac{1}{2} b^2 \pi x^2\right] dx$$

**Problem 64: Unable to integrate problem.**

$$\int \text{Cos}\left[c + \frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x] dx$$

Optimal (type 5, 101 leaves, 4 steps):

$$\frac{\text{Cos}[c] \text{FresnelC}[b x] \text{FresnelS}[b x]}{2 b} - \frac{1}{8} i b x^2 \text{Cos}[c] \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i b^2 \pi x^2\right] + \frac{1}{8} i b x^2 \text{Cos}[c] \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} i b^2 \pi x^2\right] - \frac{\text{FresnelS}[b x]^2 \text{Sin}[c]}{2 b}$$

Result (type 8, 21 leaves):

$$\int \cos\left[c + \frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x] dx$$

### Problem 71: Unable to integrate problem.

$$\int x^8 \text{FresnelS}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right] dx$$

Optimal (type 4, 232 leaves, 22 steps):

$$\begin{aligned} & \frac{105 x^2}{4 b^7 \pi^4} - \frac{7 x^6}{12 b^3 \pi^2} + \frac{55 x^2 \cos[b^2 \pi x^2]}{4 b^7 \pi^4} - \frac{x^6 \cos[b^2 \pi x^2]}{4 b^3 \pi^2} + \frac{35 x^3 \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{b^6 \pi^3} - \\ & \frac{x^7 \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{b^2 \pi} + \frac{105 \text{FresnelS}[b x]^2}{2 b^9 \pi^4} - \frac{105 x \text{FresnelS}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{b^8 \pi^4} + \\ & \frac{7 x^5 \text{FresnelS}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{b^4 \pi^2} - \frac{40 \sin[b^2 \pi x^2]}{b^9 \pi^5} + \frac{5 x^4 \sin[b^2 \pi x^2]}{2 b^5 \pi^3} \end{aligned}$$

Result (type 8, 22 leaves):

$$\int x^8 \text{FresnelS}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right] dx$$

### Problem 73: Unable to integrate problem.

$$\int x^6 \text{FresnelS}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right] dx$$

Optimal (type 5, 248 leaves, 15 steps):

$$\begin{aligned} & -\frac{5 x^4}{8 b^3 \pi^2} + \frac{11 \cos[b^2 \pi x^2]}{2 b^7 \pi^4} - \frac{x^4 \cos[b^2 \pi x^2]}{4 b^3 \pi^2} + \frac{15 x \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{b^6 \pi^3} - \\ & \frac{x^5 \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{b^2 \pi} - \frac{15 \text{FresnelC}[b x] \text{FresnelS}[b x]}{2 b^7 \pi^3} + \\ & \frac{15 i x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i b^2 \pi x^2\right]}{8 b^5 \pi^3} - \\ & \frac{15 i x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} i b^2 \pi x^2\right]}{8 b^5 \pi^3} + \\ & \frac{5 x^3 \text{FresnelS}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{b^4 \pi^2} + \frac{7 x^2 \sin[b^2 \pi x^2]}{4 b^5 \pi^3} \end{aligned}$$

Result (type 8, 22 leaves):

$$\int x^6 \text{FresnelS}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right] dx$$



### Problem 75: Unable to integrate problem.

$$\int x^4 \text{FresnelS}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right] dx$$

Optimal (type 4, 120 leaves, 9 steps):

$$-\frac{3 x^2}{4 b^3 \pi^2} - \frac{x^2 \cos[b^2 \pi x^2]}{4 b^3 \pi^2} - \frac{x^3 \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{b^2 \pi} - \frac{3 \text{FresnelS}[b x]^2}{2 b^5 \pi^2} + \frac{3 x \text{FresnelS}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{b^4 \pi^2} + \frac{\sin[b^2 \pi x^2]}{b^5 \pi^3}$$

Result (type 8, 22 leaves):

$$\int x^4 \text{FresnelS}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right] dx$$

### Problem 77: Unable to integrate problem.

$$\int x^2 \text{FresnelS}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right] dx$$

Optimal (type 5, 137 leaves, 4 steps):

$$-\frac{\cos[b^2 \pi x^2]}{4 b^3 \pi^2} - \frac{x \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{b^2 \pi} + \frac{\text{FresnelC}[b x] \text{FresnelS}[b x]}{2 b^3 \pi} - \frac{i x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i b^2 \pi x^2\right]}{8 b \pi} + \frac{i x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} i b^2 \pi x^2\right]}{8 b \pi}$$

Result (type 8, 22 leaves):

$$\int x^2 \text{FresnelS}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right] dx$$

### Problem 83: Unable to integrate problem.

$$\int \frac{\text{FresnelS}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{x^4} dx$$

Optimal (type 4, 109 leaves, 8 steps):

$$-\frac{b}{12 x^2} + \frac{b \cos[b^2 \pi x^2]}{12 x^2} - \frac{b^2 \pi \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{3 x} - \frac{1}{6} b^3 \pi^2 \text{FresnelS}[b x]^2 - \frac{\text{FresnelS}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{3 x^3} + \frac{1}{6} b^3 \pi \text{SinIntegral}[b^2 \pi x^2]$$

Result (type 8, 22 leaves):

$$\int \frac{\text{FresnelS}[b x] \text{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{x^4} dx$$

Problem 87: Unable to integrate problem.

$$\int \frac{\text{FresnelS}[b x] \text{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{x^8} dx$$

Optimal (type 4, 224 leaves, 19 steps):

$$\begin{aligned} & -\frac{b}{84 x^6} + \frac{b^5 \pi^2}{420 x^2} + \frac{b \text{Cos}[b^2 \pi x^2]}{84 x^6} - \frac{b^5 \pi^2 \text{Cos}[b^2 \pi x^2]}{84 x^2} - \frac{b^2 \pi \text{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{35 x^5} + \\ & \frac{b^6 \pi^3 \text{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{105 x} + \frac{1}{210} b^7 \pi^4 \text{FresnelS}[b x]^2 - \frac{\text{FresnelS}[b x] \text{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{7 x^7} + \\ & \frac{b^4 \pi^2 \text{FresnelS}[b x] \text{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{105 x^3} - \frac{b^3 \pi \text{Sin}[b^2 \pi x^2]}{105 x^4} - \frac{1}{70} b^7 \pi^3 \text{SinIntegral}[b^2 \pi x^2] \end{aligned}$$

Result (type 8, 22 leaves):

$$\int \frac{\text{FresnelS}[b x] \text{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{x^8} dx$$

Problem 91: Unable to integrate problem.

$$\int x^8 \text{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x] dx$$

Optimal (type 5, 307 leaves, 23 steps):

$$\begin{aligned} & \frac{35 x^4}{8 b^5 \pi^3} - \frac{x^8}{16 b \pi} - \frac{40 \text{Cos}[b^2 \pi x^2]}{b^9 \pi^5} + \frac{5 x^4 \text{Cos}[b^2 \pi x^2]}{2 b^5 \pi^3} - \frac{105 x \text{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{b^8 \pi^4} + \\ & \frac{7 x^5 \text{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{b^4 \pi^2} + \frac{105 \text{FresnelC}[b x] \text{FresnelS}[b x]}{2 b^9 \pi^4} - \\ & \frac{105 \int x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} \int b^2 \pi x^2\right]}{8 b^7 \pi^4} + \\ & \frac{105 \int x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} \int b^2 \pi x^2\right]}{8 b^7 \pi^4} - \frac{35 x^3 \text{FresnelS}[b x] \text{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{b^6 \pi^3} + \\ & \frac{x^7 \text{FresnelS}[b x] \text{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{b^2 \pi} - \frac{55 x^2 \text{Sin}[b^2 \pi x^2]}{4 b^7 \pi^4} + \frac{x^6 \text{Sin}[b^2 \pi x^2]}{4 b^3 \pi^2} \end{aligned}$$

Result (type 8, 22 leaves):

$$\int x^8 \text{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x] dx$$

### Problem 93: Unable to integrate problem.

$$\int x^6 \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x] \, dx$$

Optimal (type 4, 184 leaves, 16 steps):

$$\begin{aligned} & \frac{15 x^2}{4 b^5 \pi^3} - \frac{x^6}{12 b \pi} + \frac{7 x^2 \cos[b^2 \pi x^2]}{4 b^5 \pi^3} + \frac{5 x^3 \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{b^4 \pi^2} + \\ & \frac{15 \text{FresnelS}[b x]^2}{2 b^7 \pi^3} - \frac{15 x \text{FresnelS}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{b^6 \pi^3} + \\ & \frac{x^5 \text{FresnelS}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{b^2 \pi} - \frac{11 \sin[b^2 \pi x^2]}{2 b^7 \pi^4} + \frac{x^4 \sin[b^2 \pi x^2]}{4 b^3 \pi^2} \end{aligned}$$

Result (type 8, 22 leaves):

$$\int x^6 \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x] \, dx$$

### Problem 95: Unable to integrate problem.

$$\int x^4 \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x] \, dx$$

Optimal (type 5, 195 leaves, 10 steps):

$$\begin{aligned} & -\frac{x^4}{8 b \pi} + \frac{\cos[b^2 \pi x^2]}{b^5 \pi^3} + \frac{3 x \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{b^4 \pi^2} - \\ & \frac{3 \text{FresnelC}[b x] \text{FresnelS}[b x]}{2 b^5 \pi^2} + \frac{3 i x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i b^2 \pi x^2\right]}{8 b^3 \pi^2} - \\ & \frac{3 i x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} i b^2 \pi x^2\right]}{8 b^3 \pi^2} + \\ & \frac{x^3 \text{FresnelS}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{b^2 \pi} + \frac{x^2 \sin[b^2 \pi x^2]}{4 b^3 \pi^2} \end{aligned}$$

Result (type 8, 22 leaves):

$$\int x^4 \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x] \, dx$$

### Problem 97: Unable to integrate problem.

$$\int x^2 \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x] \, dx$$

Optimal (type 4, 73 leaves, 5 steps):

$$-\frac{x^2}{4 b \pi} - \frac{\text{FresnelS}[b x]^2}{2 b^3 \pi} + \frac{x \text{FresnelS}[b x] \text{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{b^2 \pi} + \frac{\text{Sin}[b^2 \pi x^2]}{4 b^3 \pi^2}$$

Result (type 8, 22 leaves):

$$\int x^2 \text{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x] \, dx$$

**Problem 99: Unable to integrate problem.**

$$\int \text{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x] \, dx$$

Optimal (type 5, 80 leaves, 1 step):

$$\frac{\text{FresnelC}[b x] \text{FresnelS}[b x]}{2 b} - \frac{1}{8} i b x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i b^2 \pi x^2\right] + \frac{1}{8} i b x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} i b^2 \pi x^2\right]$$

Result (type 8, 19 leaves):

$$\int \text{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x] \, dx$$

**Problem 101: Unable to integrate problem.**

$$\int \frac{\text{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{x^2} \, dx$$

Optimal (type 4, 48 leaves, 4 steps):

$$-\frac{\text{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{x} - \frac{1}{2} b \pi \text{FresnelS}[b x]^2 + \frac{1}{4} b \text{SinIntegral}[b^2 \pi x^2]$$

Result (type 8, 22 leaves):

$$\int \frac{\text{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{x^2} \, dx$$

**Problem 105: Unable to integrate problem.**

$$\int \frac{\text{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{x^6} \, dx$$

Optimal (type 4, 163 leaves, 13 steps):

$$\frac{b^3 \pi}{60 x^2} - \frac{b^3 \pi \cos [b^2 \pi x^2]}{24 x^2} - \frac{\cos \left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{5 x^5} +$$

$$\frac{b^4 \pi^2 \cos \left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{15 x} + \frac{1}{30} b^5 \pi^3 \text{FresnelS}[b x]^2 +$$

$$\frac{b^2 \pi \text{FresnelS}[b x] \sin \left[\frac{1}{2} b^2 \pi x^2\right]}{15 x^3} - \frac{b \sin [b^2 \pi x^2]}{40 x^4} - \frac{7}{120} b^5 \pi^2 \text{SinIntegral}[b^2 \pi x^2]$$

Result (type 8, 22 leaves):

$$\int \frac{\cos \left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{x^6} dx$$

Problem 109: Unable to integrate problem.

$$\int \frac{\cos \left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{x^{10}} dx$$

Optimal (type 4, 278 leaves, 26 steps):

$$\frac{b^3 \pi}{756 x^6} - \frac{b^7 \pi^3}{3780 x^2} - \frac{11 b^3 \pi \cos [b^2 \pi x^2]}{3024 x^6} + \frac{5 b^7 \pi^3 \cos [b^2 \pi x^2]}{2016 x^2} - \frac{\cos \left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{9 x^9} +$$

$$\frac{b^4 \pi^2 \cos \left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{315 x^5} - \frac{b^8 \pi^4 \cos \left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{945 x} -$$

$$\frac{b^9 \pi^5 \text{FresnelS}[b x]^2}{1890} + \frac{b^2 \pi \text{FresnelS}[b x] \sin \left[\frac{1}{2} b^2 \pi x^2\right]}{63 x^7} - \frac{b^6 \pi^3 \text{FresnelS}[b x] \sin \left[\frac{1}{2} b^2 \pi x^2\right]}{945 x^3} -$$

$$\frac{b \sin [b^2 \pi x^2]}{144 x^8} + \frac{67 b^5 \pi^2 \sin [b^2 \pi x^2]}{30240 x^4} + \frac{83 b^9 \pi^4 \text{SinIntegral}[b^2 \pi x^2]}{30240}$$

Result (type 8, 22 leaves):

$$\int \frac{\cos \left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelS}[b x]}{x^{10}} dx$$

Problem 118: Unable to integrate problem.

$$\int \frac{\text{FresnelC}[b x]}{x} dx$$

Optimal (type 5, 69 leaves, 3 steps):

$$\frac{1}{2} b x \text{HypergeometricPFQ}\left[\left\{\frac{1}{2}, \frac{1}{2}\right\}, \left\{\frac{3}{2}, \frac{3}{2}\right\}, -\frac{1}{2} i b^2 \pi x^2\right] +$$

$$\frac{1}{2} b x \text{HypergeometricPFQ}\left[\left\{\frac{1}{2}, \frac{1}{2}\right\}, \left\{\frac{3}{2}, \frac{3}{2}\right\}, \frac{1}{2} i b^2 \pi x^2\right]$$

Result (type 8, 10 leaves):

$$\int \frac{\text{FresnelC}[b x]}{x} dx$$

**Problem 131: Result more than twice size of optimal antiderivative.**

$$\int \text{FresnelC}[a + b x] dx$$

Optimal (type 4, 37 leaves, 1 step):

$$\frac{(a + b x) \text{FresnelC}[a + b x]}{b} - \frac{\text{Sin}\left[\frac{1}{2} \pi (a + b x)^2\right]}{b \pi}$$

Result (type 4, 90 leaves):

$$\frac{a \text{FresnelC}[a + b x]}{b} + x \text{FresnelC}[a + b x] - \frac{\text{Cos}\left[a b \pi x + \frac{1}{2} b^2 \pi x^2\right] \text{Sin}\left[\frac{a^2 \pi}{2}\right]}{b \pi} - \frac{\text{Cos}\left[\frac{a^2 \pi}{2}\right] \text{Sin}\left[a b \pi x + \frac{1}{2} b^2 \pi x^2\right]}{b \pi}$$

**Problem 137: Result more than twice size of optimal antiderivative.**

$$\int \text{FresnelC}[a + b x] dx$$

Optimal (type 4, 37 leaves, 1 step):

$$\frac{(a + b x) \text{FresnelC}[a + b x]}{b} - \frac{\text{Sin}\left[\frac{1}{2} \pi (a + b x)^2\right]}{b \pi}$$

Result (type 4, 90 leaves):

$$\frac{a \text{FresnelC}[a + b x]}{b} + x \text{FresnelC}[a + b x] - \frac{\text{Cos}\left[a b \pi x + \frac{1}{2} b^2 \pi x^2\right] \text{Sin}\left[\frac{a^2 \pi}{2}\right]}{b \pi} - \frac{\text{Cos}\left[\frac{a^2 \pi}{2}\right] \text{Sin}\left[a b \pi x + \frac{1}{2} b^2 \pi x^2\right]}{b \pi}$$

**Problem 140: Unable to integrate problem.**

$$\int x^7 \text{FresnelC}[b x]^2 dx$$

Optimal (type 4, 253 leaves, 23 steps):

$$\begin{aligned}
 & -\frac{105 x^2}{16 b^6 \pi^4} + \frac{7 x^6}{48 b^2 \pi^2} + \frac{55 x^2 \operatorname{Cos}[b^2 \pi x^2]}{16 b^6 \pi^4} - \frac{x^6 \operatorname{Cos}[b^2 \pi x^2]}{16 b^2 \pi^2} + \\
 & \frac{105 x \operatorname{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \operatorname{FresnelC}[b x]}{4 b^7 \pi^4} - \frac{7 x^5 \operatorname{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \operatorname{FresnelC}[b x]}{4 b^3 \pi^2} - \\
 & \frac{105 \operatorname{FresnelC}[b x]^2}{8 b^8 \pi^4} + \frac{1}{8} x^8 \operatorname{FresnelC}[b x]^2 + \frac{35 x^3 \operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{4 b^5 \pi^3} - \\
 & \frac{x^7 \operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{4 b \pi} - \frac{10 \operatorname{Sin}[b^2 \pi x^2]}{b^8 \pi^5} + \frac{5 x^4 \operatorname{Sin}[b^2 \pi x^2]}{8 b^4 \pi^3}
 \end{aligned}$$

Result (type 8, 12 leaves):

$$\int x^7 \operatorname{FresnelC}[b x]^2 dx$$

**Problem 142: Unable to integrate problem.**

$$\int x^5 \operatorname{FresnelC}[b x]^2 dx$$

Optimal (type 5, 265 leaves, 16 steps):

$$\begin{aligned}
 & \frac{5 x^4}{24 b^2 \pi^2} + \frac{11 \operatorname{Cos}[b^2 \pi x^2]}{6 b^6 \pi^4} - \frac{x^4 \operatorname{Cos}[b^2 \pi x^2]}{12 b^2 \pi^2} - \frac{5 x^3 \operatorname{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \operatorname{FresnelC}[b x]}{3 b^3 \pi^2} + \\
 & \frac{1}{6} x^6 \operatorname{FresnelC}[b x]^2 - \frac{5 \operatorname{FresnelC}[b x] \operatorname{FresnelS}[b x]}{2 b^6 \pi^3} - \\
 & \frac{5 i x^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i b^2 \pi x^2\right]}{8 b^4 \pi^3} + \\
 & \frac{5 i x^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} i b^2 \pi x^2\right]}{8 b^4 \pi^3} + \\
 & \frac{5 x \operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{b^5 \pi^3} - \frac{x^5 \operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{3 b \pi} + \frac{7 x^2 \operatorname{Sin}[b^2 \pi x^2]}{12 b^4 \pi^3}
 \end{aligned}$$

Result (type 8, 12 leaves):

$$\int x^5 \operatorname{FresnelC}[b x]^2 dx$$

**Problem 144: Unable to integrate problem.**

$$\int x^3 \operatorname{FresnelC}[b x]^2 dx$$

Optimal (type 4, 140 leaves, 10 steps):

$$\frac{3 x^2}{8 b^2 \pi^2} - \frac{x^2 \operatorname{Cos}\left[b^2 \pi x^2\right]}{8 b^2 \pi^2} - \frac{3 x \operatorname{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \operatorname{FresnelC}[b x]}{2 b^3 \pi^2} + \frac{3 \operatorname{FresnelC}[b x]^2}{4 b^4 \pi^2} +$$

$$\frac{1}{4} x^4 \operatorname{FresnelC}[b x]^2 - \frac{x^3 \operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{2 b \pi} + \frac{\operatorname{Sin}\left[b^2 \pi x^2\right]}{2 b^4 \pi^3}$$

Result (type 8, 12 leaves):

$$\int x^3 \operatorname{FresnelC}[b x]^2 dx$$

### Problem 146: Unable to integrate problem.

$$\int x \operatorname{FresnelC}[b x]^2 dx$$

Optimal (type 5, 144 leaves, 5 steps):

$$-\frac{\operatorname{Cos}\left[b^2 \pi x^2\right]}{4 b^2 \pi^2} + \frac{1}{2} x^2 \operatorname{FresnelC}[b x]^2 + \frac{\operatorname{FresnelC}[b x] \operatorname{FresnelS}[b x]}{2 b^2 \pi} +$$

$$\frac{i x^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i b^2 \pi x^2\right]}{8 \pi} -$$

$$\frac{i x^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} i b^2 \pi x^2\right]}{8 \pi} - \frac{x \operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{b \pi}$$

Result (type 8, 10 leaves):

$$\int x \operatorname{FresnelC}[b x]^2 dx$$

### Problem 152: Unable to integrate problem.

$$\int \frac{\operatorname{FresnelC}[b x]^2}{x^5} dx$$

Optimal (type 4, 127 leaves, 9 steps):

$$-\frac{b^2}{24 x^2} - \frac{b^2 \operatorname{Cos}\left[b^2 \pi x^2\right]}{24 x^2} - \frac{b \operatorname{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \operatorname{FresnelC}[b x]}{6 x^3} - \frac{1}{12} b^4 \pi^2 \operatorname{FresnelC}[b x]^2 -$$

$$\frac{\operatorname{FresnelC}[b x]^2}{4 x^4} + \frac{b^3 \pi \operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{6 x} - \frac{1}{12} b^4 \pi \operatorname{SinIntegral}\left[b^2 \pi x^2\right]$$

Result (type 8, 12 leaves):

$$\int \frac{\operatorname{FresnelC}[b x]^2}{x^5} dx$$



### Problem 156: Unable to integrate problem.

$$\int \frac{\text{FresnelC}[b x]^2}{x^9} dx$$

Optimal (type 4, 242 leaves, 20 steps):

$$\begin{aligned} & -\frac{b^2}{336 x^6} + \frac{b^6 \pi^2}{1680 x^2} - \frac{b^2 \text{Cos}[b^2 \pi x^2]}{336 x^6} + \frac{b^6 \pi^2 \text{Cos}[b^2 \pi x^2]}{336 x^2} - \\ & \frac{b \text{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelC}[b x]}{28 x^7} + \frac{b^5 \pi^2 \text{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelC}[b x]}{420 x^3} + \\ & \frac{1}{840} b^8 \pi^4 \text{FresnelC}[b x]^2 - \frac{\text{FresnelC}[b x]^2}{8 x^8} + \frac{b^3 \pi \text{FresnelC}[b x] \text{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{140 x^5} - \\ & \frac{b^7 \pi^3 \text{FresnelC}[b x] \text{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{420 x} + \frac{b^4 \pi \text{Sin}[b^2 \pi x^2]}{420 x^4} + \frac{1}{280} b^8 \pi^3 \text{SinIntegral}[b^2 \pi x^2] \end{aligned}$$

Result (type 8, 12 leaves):

$$\int \frac{\text{FresnelC}[b x]^2}{x^9} dx$$

### Problem 158: Unable to integrate problem.

$$\int (c + d x)^2 \text{FresnelC}[a + b x]^2 dx$$

Optimal (type 5, 495 leaves, 18 steps):

$$\begin{aligned}
 & \frac{2 d^2 x}{3 b^2 \pi^2} - \frac{d (b c - a d) \operatorname{Cos}\left[\pi (a + b x)^2\right]}{2 b^3 \pi^2} - \\
 & \frac{d^2 (a + b x) \operatorname{Cos}\left[\pi (a + b x)^2\right]}{6 b^3 \pi^2} - \frac{4 d^2 \operatorname{Cos}\left[\frac{1}{2} \pi (a + b x)^2\right] \operatorname{FresnelC}[a + b x]}{3 b^3 \pi^2} + \\
 & \frac{(b c - a d)^2 (a + b x) \operatorname{FresnelC}[a + b x]^2}{b^3} + \frac{d (b c - a d) (a + b x)^2 \operatorname{FresnelC}[a + b x]^2}{b^3} + \\
 & \frac{d^2 (a + b x)^3 \operatorname{FresnelC}[a + b x]^2}{3 b^3} + \frac{5 d^2 \operatorname{FresnelC}\left[\sqrt{2} (a + b x)\right]}{6 \sqrt{2} b^3 \pi^2} + \\
 & \frac{d (b c - a d) \operatorname{FresnelC}[a + b x] \operatorname{FresnelS}[a + b x]}{b^3 \pi} + \frac{(b c - a d)^2 \operatorname{FresnelS}\left[\sqrt{2} (a + b x)\right]}{\sqrt{2} b^3 \pi} + \\
 & \frac{1}{4 b^3 \pi} i d (b c - a d) (a + b x)^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i \pi (a + b x)^2\right] - \\
 & \frac{1}{4 b^3 \pi} i d (b c - a d) (a + b x)^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} i \pi (a + b x)^2\right] - \\
 & \frac{2 (b c - a d)^2 \operatorname{FresnelC}[a + b x] \operatorname{Sin}\left[\frac{1}{2} \pi (a + b x)^2\right]}{b^3 \pi} - \\
 & \frac{2 d (b c - a d) (a + b x) \operatorname{FresnelC}[a + b x] \operatorname{Sin}\left[\frac{1}{2} \pi (a + b x)^2\right]}{b^3 \pi} - \\
 & \frac{2 d^2 (a + b x)^2 \operatorname{FresnelC}[a + b x] \operatorname{Sin}\left[\frac{1}{2} \pi (a + b x)^2\right]}{3 b^3 \pi}
 \end{aligned}$$

Result (type 8, 18 leaves):

$$\int (c + d x)^2 \operatorname{FresnelC}[a + b x]^2 dx$$

Problem 159: Unable to integrate problem.

$$\int (c + d x) \operatorname{FresnelC}[a + b x]^2 dx$$

Optimal (type 5, 279 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{d \operatorname{Cos}[\pi (a + b x)^2]}{4 b^2 \pi^2} + \frac{(b c - a d) (a + b x) \operatorname{FresnelC}[a + b x]^2}{b^2} + \frac{d (a + b x)^2 \operatorname{FresnelC}[a + b x]^2}{2 b^2} + \\
 & \frac{d \operatorname{FresnelC}[a + b x] \operatorname{FresnelS}[a + b x]}{2 b^2 \pi} + \frac{(b c - a d) \operatorname{FresnelS}[\sqrt{2} (a + b x)]}{\sqrt{2} b^2 \pi} + \\
 & \frac{i d (a + b x)^2 \operatorname{HypergeometricPFQ}[\{1, 1\}, \{\frac{3}{2}, 2\}, -\frac{1}{2} i \pi (a + b x)^2]}{8 b^2 \pi} - \\
 & \frac{i d (a + b x)^2 \operatorname{HypergeometricPFQ}[\{1, 1\}, \{\frac{3}{2}, 2\}, \frac{1}{2} i \pi (a + b x)^2]}{8 b^2 \pi} - \\
 & \frac{2 (b c - a d) \operatorname{FresnelC}[a + b x] \operatorname{Sin}[\frac{1}{2} \pi (a + b x)^2]}{b^2 \pi} - \frac{d (a + b x) \operatorname{FresnelC}[a + b x] \operatorname{Sin}[\frac{1}{2} \pi (a + b x)^2]}{b^2 \pi}
 \end{aligned}$$

Result (type 8, 16 leaves):

$$\int (c + d x) \operatorname{FresnelC}[a + b x]^2 dx$$

**Problem 166: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{FresnelC}[d (a + b \operatorname{Log}[c x^n])]}{x} dx$$

Optimal (type 4, 66 leaves, 3 steps):

$$\frac{\operatorname{FresnelC}[d (a + b \operatorname{Log}[c x^n])]}{b n} - \frac{\operatorname{Sin}[\frac{1}{2} d^2 \pi (a + b \operatorname{Log}[c x^n])^2]}{b d n \pi}$$

Result (type 4, 165 leaves):

$$\begin{aligned}
 & \frac{a \operatorname{FresnelC}[d (a + b \operatorname{Log}[c x^n])]}{b n} + \frac{\operatorname{FresnelC}[d (a + b \operatorname{Log}[c x^n])] \operatorname{Log}[c x^n]}{n} - \\
 & \frac{\operatorname{Cos}[a b d^2 \pi \operatorname{Log}[c x^n] + \frac{1}{2} b^2 d^2 \pi \operatorname{Log}[c x^n]^2] \operatorname{Sin}[\frac{1}{2} a^2 d^2 \pi]}{b d n \pi} - \\
 & \frac{\operatorname{Cos}[\frac{1}{2} a^2 d^2 \pi] \operatorname{Sin}[a b d^2 \pi \operatorname{Log}[c x^n] + \frac{1}{2} b^2 d^2 \pi \operatorname{Log}[c x^n]^2]}{b d n \pi}
 \end{aligned}$$

**Problem 170: Unable to integrate problem.**

$$\int e^{c + \frac{1}{2} i b^2 \pi x^2} \operatorname{FresnelC}[b x] dx$$

Optimal (type 5, 64 leaves, 4 steps):

$$- \frac{i e^c \operatorname{Erfi}\left[\left(\frac{1}{2} + \frac{i}{2}\right) b \sqrt{\pi} x\right]^2}{8 b} + \frac{1}{4} b e^c x^2 \operatorname{HypergeometricPFQ}[\{1, 1\}, \{\frac{3}{2}, 2\}, \frac{1}{2} i b^2 \pi x^2]$$

Result (type 8, 24 leaves):

$$\int e^{c + \frac{1}{2} i b^2 \pi x^2} \text{FresnelC}[b x] dx$$

**Problem 171: Unable to integrate problem.**

$$\int e^{c - \frac{1}{2} i b^2 \pi x^2} \text{FresnelC}[b x] dx$$

Optimal (type 5, 64 leaves, 4 steps):

$$-\frac{i e^c \text{Erf}\left[\left(\frac{1}{2} + \frac{i}{2}\right) b \sqrt{\pi} x\right]^2}{8 b} + \frac{1}{4} b e^c x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i b^2 \pi x^2\right]$$

Result (type 8, 24 leaves):

$$\int e^{c - \frac{1}{2} i b^2 \pi x^2} \text{FresnelC}[b x] dx$$

**Problem 172: Unable to integrate problem.**

$$\int \text{FresnelC}[b x] \text{Sin}\left[c + \frac{1}{2} b^2 \pi x^2\right] dx$$

Optimal (type 5, 101 leaves, 4 steps):

$$\frac{\text{Cos}[c] \text{FresnelC}[b x] \text{FresnelS}[b x]}{2 b} + \frac{1}{8} i b x^2 \text{Cos}[c] \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i b^2 \pi x^2\right] - \frac{1}{8} i b x^2 \text{Cos}[c] \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} i b^2 \pi x^2\right] + \frac{\text{FresnelC}[b x]^2 \text{Sin}[c]}{2 b}$$

Result (type 8, 21 leaves):

$$\int \text{FresnelC}[b x] \text{Sin}\left[c + \frac{1}{2} b^2 \pi x^2\right] dx$$

**Problem 173: Unable to integrate problem.**

$$\int \text{Cos}\left[c + \frac{1}{2} b^2 \pi x^2\right] \text{FresnelC}[b x] dx$$

Optimal (type 5, 101 leaves, 4 steps):

$$\frac{\text{Cos}[c] \text{FresnelC}[b x]^2}{2 b} - \frac{\text{FresnelC}[b x] \text{FresnelS}[b x] \text{Sin}[c]}{2 b} - \frac{1}{8} i b x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i b^2 \pi x^2\right] \text{Sin}[c] + \frac{1}{8} i b x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} i b^2 \pi x^2\right] \text{Sin}[c]$$

Result (type 8, 21 leaves):

$$\int \cos \left[ c + \frac{1}{2} b^2 \pi x^2 \right] \text{FresnelC}[b x] \, dx$$

**Problem 180: Unable to integrate problem.**

$$\int x^8 \cos \left[ \frac{1}{2} b^2 \pi x^2 \right] \text{FresnelC}[b x] \, dx$$

Optimal (type 4, 231 leaves, 22 steps):

$$\begin{aligned} & \frac{105 x^2}{4 b^7 \pi^4} - \frac{7 x^6}{12 b^3 \pi^2} - \frac{55 x^2 \cos [b^2 \pi x^2]}{4 b^7 \pi^4} + \frac{x^6 \cos [b^2 \pi x^2]}{4 b^3 \pi^2} - \frac{105 x \cos \left[ \frac{1}{2} b^2 \pi x^2 \right] \text{FresnelC}[b x]}{b^8 \pi^4} + \\ & \frac{7 x^5 \cos \left[ \frac{1}{2} b^2 \pi x^2 \right] \text{FresnelC}[b x]}{b^4 \pi^2} + \frac{105 \text{FresnelC}[b x]^2}{2 b^9 \pi^4} - \frac{35 x^3 \text{FresnelC}[b x] \sin \left[ \frac{1}{2} b^2 \pi x^2 \right]}{b^6 \pi^3} + \\ & \frac{x^7 \text{FresnelC}[b x] \sin \left[ \frac{1}{2} b^2 \pi x^2 \right]}{b^2 \pi} + \frac{40 \sin [b^2 \pi x^2]}{b^9 \pi^5} - \frac{5 x^4 \sin [b^2 \pi x^2]}{2 b^5 \pi^3} \end{aligned}$$

Result (type 8, 22 leaves):

$$\int x^8 \cos \left[ \frac{1}{2} b^2 \pi x^2 \right] \text{FresnelC}[b x] \, dx$$

**Problem 182: Unable to integrate problem.**

$$\int x^6 \cos \left[ \frac{1}{2} b^2 \pi x^2 \right] \text{FresnelC}[b x] \, dx$$

Optimal (type 5, 247 leaves, 15 steps):

$$\begin{aligned} & -\frac{5 x^4}{8 b^3 \pi^2} - \frac{11 \cos [b^2 \pi x^2]}{2 b^7 \pi^4} + \frac{x^4 \cos [b^2 \pi x^2]}{4 b^3 \pi^2} + \frac{5 x^3 \cos \left[ \frac{1}{2} b^2 \pi x^2 \right] \text{FresnelC}[b x]}{b^4 \pi^2} + \\ & \frac{15 \text{FresnelC}[b x] \text{FresnelS}[b x]}{2 b^7 \pi^3} + \frac{15 i x^2 \text{HypergeometricPFQ}[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i b^2 \pi x^2]}{8 b^5 \pi^3} - \\ & \frac{15 i x^2 \text{HypergeometricPFQ}[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} i b^2 \pi x^2]}{8 b^5 \pi^3} - \\ & \frac{15 x \text{FresnelC}[b x] \sin \left[ \frac{1}{2} b^2 \pi x^2 \right]}{b^6 \pi^3} + \frac{x^5 \text{FresnelC}[b x] \sin \left[ \frac{1}{2} b^2 \pi x^2 \right]}{b^2 \pi} - \frac{7 x^2 \sin [b^2 \pi x^2]}{4 b^5 \pi^3} \end{aligned}$$

Result (type 8, 22 leaves):

$$\int x^6 \cos \left[ \frac{1}{2} b^2 \pi x^2 \right] \text{FresnelC}[b x] \, dx$$

**Problem 184: Unable to integrate problem.**

$$\int x^4 \cos \left[ \frac{1}{2} b^2 \pi x^2 \right] \text{FresnelC}[b x] \, dx$$

Optimal (type 4, 120 leaves, 9 steps):

$$-\frac{3x^2}{4b^3\pi^2} + \frac{x^2 \operatorname{Cos}\left[\frac{1}{2}b^2\pi x^2\right]}{4b^3\pi^2} + \frac{3x \operatorname{Cos}\left[\frac{1}{2}b^2\pi x^2\right] \operatorname{FresnelC}[bx]}{b^4\pi^2} - \frac{3 \operatorname{FresnelC}[bx]^2}{2b^5\pi^2} + \frac{x^3 \operatorname{FresnelC}[bx] \operatorname{Sin}\left[\frac{1}{2}b^2\pi x^2\right]}{b^2\pi} - \frac{\operatorname{Sin}\left[b^2\pi x^2\right]}{b^5\pi^3}$$

Result (type 8, 22 leaves):

$$\int x^4 \operatorname{Cos}\left[\frac{1}{2}b^2\pi x^2\right] \operatorname{FresnelC}[bx] \, dx$$

### Problem 186: Unable to integrate problem.

$$\int x^2 \operatorname{Cos}\left[\frac{1}{2}b^2\pi x^2\right] \operatorname{FresnelC}[bx] \, dx$$

Optimal (type 5, 136 leaves, 4 steps):

$$\frac{\operatorname{Cos}\left[b^2\pi x^2\right]}{4b^3\pi^2} - \frac{\operatorname{FresnelC}[bx] \operatorname{FresnelS}[bx]}{2b^3\pi} - \frac{i x^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i b^2\pi x^2\right]}{8b\pi} + \frac{i x^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} i b^2\pi x^2\right]}{8b\pi} + \frac{x \operatorname{FresnelC}[bx] \operatorname{Sin}\left[\frac{1}{2}b^2\pi x^2\right]}{b^2\pi}$$

Result (type 8, 22 leaves):

$$\int x^2 \operatorname{Cos}\left[\frac{1}{2}b^2\pi x^2\right] \operatorname{FresnelC}[bx] \, dx$$

### Problem 192: Unable to integrate problem.

$$\int \frac{\operatorname{Cos}\left[\frac{1}{2}b^2\pi x^2\right] \operatorname{FresnelC}[bx]}{x^4} \, dx$$

Optimal (type 4, 109 leaves, 8 steps):

$$-\frac{b}{12x^2} - \frac{b \operatorname{Cos}\left[b^2\pi x^2\right]}{12x^2} - \frac{\operatorname{Cos}\left[\frac{1}{2}b^2\pi x^2\right] \operatorname{FresnelC}[bx]}{3x^3} - \frac{1}{6} b^3\pi^2 \operatorname{FresnelC}[bx]^2 + \frac{b^2\pi \operatorname{FresnelC}[bx] \operatorname{Sin}\left[\frac{1}{2}b^2\pi x^2\right]}{3x} - \frac{1}{6} b^3\pi \operatorname{SinIntegral}\left[b^2\pi x^2\right]$$

Result (type 8, 22 leaves):

$$\int \frac{\operatorname{Cos}\left[\frac{1}{2}b^2\pi x^2\right] \operatorname{FresnelC}[bx]}{x^4} \, dx$$

### Problem 196: Unable to integrate problem.

$$\int \frac{\cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelC}[b x]}{x^8} dx$$

Optimal (type 4, 224 leaves, 19 steps):

$$\begin{aligned} & -\frac{b}{84 x^6} + \frac{b^5 \pi^2}{420 x^2} - \frac{b \cos[b^2 \pi x^2]}{84 x^6} + \frac{b^5 \pi^2 \cos[b^2 \pi x^2]}{84 x^2} - \frac{\cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelC}[b x]}{7 x^7} + \\ & \frac{b^4 \pi^2 \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelC}[b x]}{105 x^3} + \frac{1}{210} b^7 \pi^4 \text{FresnelC}[b x]^2 + \frac{b^2 \pi \text{FresnelC}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{35 x^5} - \\ & \frac{b^6 \pi^3 \text{FresnelC}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{105 x} + \frac{b^3 \pi \sin[b^2 \pi x^2]}{105 x^4} + \frac{1}{70} b^7 \pi^3 \text{SinIntegral}[b^2 \pi x^2] \end{aligned}$$

Result (type 8, 22 leaves):

$$\int \frac{\cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelC}[b x]}{x^8} dx$$

### Problem 200: Unable to integrate problem.

$$\int x^8 \text{FresnelC}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right] dx$$

Optimal (type 5, 308 leaves, 23 steps):

$$\begin{aligned} & -\frac{35 x^4}{8 b^5 \pi^3} + \frac{x^8}{16 b \pi} - \frac{40 \cos[b^2 \pi x^2]}{b^9 \pi^5} + \frac{5 x^4 \cos[b^2 \pi x^2]}{2 b^5 \pi^3} + \\ & \frac{35 x^3 \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelC}[b x]}{b^6 \pi^3} - \frac{x^7 \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelC}[b x]}{b^2 \pi} + \\ & \frac{105 \text{FresnelC}[b x] \text{FresnelS}[b x]}{2 b^9 \pi^4} + \frac{105 i x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i b^2 \pi x^2\right]}{8 b^7 \pi^4} - \\ & \frac{105 i x^2 \text{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} i b^2 \pi x^2\right]}{8 b^7 \pi^4} - \frac{105 x \text{FresnelC}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{b^8 \pi^4} + \\ & \frac{7 x^5 \text{FresnelC}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{b^4 \pi^2} - \frac{55 x^2 \sin[b^2 \pi x^2]}{4 b^7 \pi^4} + \frac{x^6 \sin[b^2 \pi x^2]}{4 b^3 \pi^2} \end{aligned}$$

Result (type 8, 22 leaves):

$$\int x^8 \text{FresnelC}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right] dx$$

### Problem 202: Unable to integrate problem.

$$\int x^6 \operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right] dx$$

Optimal (type 4, 185 leaves, 16 steps):

$$\begin{aligned} & -\frac{15 x^2}{4 b^5 \pi^3} + \frac{x^6}{12 b \pi} + \frac{7 x^2 \operatorname{Cos}\left[b^2 \pi x^2\right]}{4 b^5 \pi^3} + \frac{15 x \operatorname{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \operatorname{FresnelC}[b x]}{b^6 \pi^3} - \\ & \frac{x^5 \operatorname{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \operatorname{FresnelC}[b x]}{b^2 \pi} - \frac{15 \operatorname{FresnelC}[b x]^2}{2 b^7 \pi^3} + \\ & \frac{5 x^3 \operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{b^4 \pi^2} - \frac{11 \operatorname{Sin}\left[b^2 \pi x^2\right]}{2 b^7 \pi^4} + \frac{x^4 \operatorname{Sin}\left[b^2 \pi x^2\right]}{4 b^3 \pi^2} \end{aligned}$$

Result (type 8, 22 leaves):

$$\int x^6 \operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right] dx$$

### Problem 204: Unable to integrate problem.

$$\int x^4 \operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right] dx$$

Optimal (type 5, 196 leaves, 10 steps):

$$\begin{aligned} & \frac{x^4}{8 b \pi} + \frac{\operatorname{Cos}\left[b^2 \pi x^2\right]}{b^5 \pi^3} - \frac{x^3 \operatorname{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \operatorname{FresnelC}[b x]}{b^2 \pi} - \\ & \frac{3 \operatorname{FresnelC}[b x] \operatorname{FresnelS}[b x]}{2 b^5 \pi^2} - \frac{3 i x^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i b^2 \pi x^2\right]}{8 b^3 \pi^2} + \\ & \frac{3 i x^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} i b^2 \pi x^2\right]}{8 b^3 \pi^2} + \\ & \frac{3 x \operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{b^4 \pi^2} + \frac{x^2 \operatorname{Sin}\left[b^2 \pi x^2\right]}{4 b^3 \pi^2} \end{aligned}$$

Result (type 8, 22 leaves):

$$\int x^4 \operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right] dx$$

### Problem 206: Unable to integrate problem.

$$\int x^2 \operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right] dx$$

Optimal (type 4, 74 leaves, 5 steps):



$$\frac{x^2}{4 b \pi} - \frac{x \operatorname{Cos}\left[\frac{1}{2} b^2 \pi x^2\right] \operatorname{FresnelC}[b x]}{b^2 \pi} + \frac{\operatorname{FresnelC}[b x]^2}{2 b^3 \pi} + \frac{\operatorname{Sin}\left[b^2 \pi x^2\right]}{4 b^3 \pi^2}$$

Result (type 8, 22 leaves):

$$\int x^2 \operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right] dx$$

**Problem 208: Unable to integrate problem.**

$$\int \operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right] dx$$

Optimal (type 5, 80 leaves, 1 step):

$$\frac{\operatorname{FresnelC}[b x] \operatorname{FresnelS}[b x]}{2 b} + \frac{1}{8} i b x^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, -\frac{1}{2} i b^2 \pi x^2\right] - \frac{1}{8} i b x^2 \operatorname{HypergeometricPFQ}\left[\{1, 1\}, \left\{\frac{3}{2}, 2\right\}, \frac{1}{2} i b^2 \pi x^2\right]$$

Result (type 8, 19 leaves):

$$\int \operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right] dx$$

**Problem 210: Unable to integrate problem.**

$$\int \frac{\operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{x^2} dx$$

Optimal (type 4, 48 leaves, 4 steps):

$$\frac{1}{2} b \pi \operatorname{FresnelC}[b x]^2 - \frac{\operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{x} + \frac{1}{4} b \operatorname{SinIntegral}\left[b^2 \pi x^2\right]$$

Result (type 8, 22 leaves):

$$\int \frac{\operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{x^2} dx$$

**Problem 214: Unable to integrate problem.**

$$\int \frac{\operatorname{FresnelC}[b x] \operatorname{Sin}\left[\frac{1}{2} b^2 \pi x^2\right]}{x^6} dx$$

Optimal (type 4, 163 leaves, 13 steps):

$$\begin{aligned}
& - \frac{b^3 \pi}{60 x^2} - \frac{b^3 \pi \cos[b^2 \pi x^2]}{24 x^2} - \frac{b^2 \pi \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelC}[b x]}{15 x^3} - \\
& \frac{1}{30} b^5 \pi^3 \text{FresnelC}[b x]^2 - \frac{\text{FresnelC}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{5 x^5} + \\
& \frac{b^4 \pi^2 \text{FresnelC}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{15 x} - \frac{b \sin[b^2 \pi x^2]}{40 x^4} - \frac{7}{120} b^5 \pi^2 \text{SinIntegral}[b^2 \pi x^2]
\end{aligned}$$

Result (type 8, 22 leaves):

$$\int \frac{\text{FresnelC}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{x^6} dx$$

Problem 218: Unable to integrate problem.

$$\int \frac{\text{FresnelC}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{x^{10}} dx$$

Optimal (type 4, 278 leaves, 26 steps):

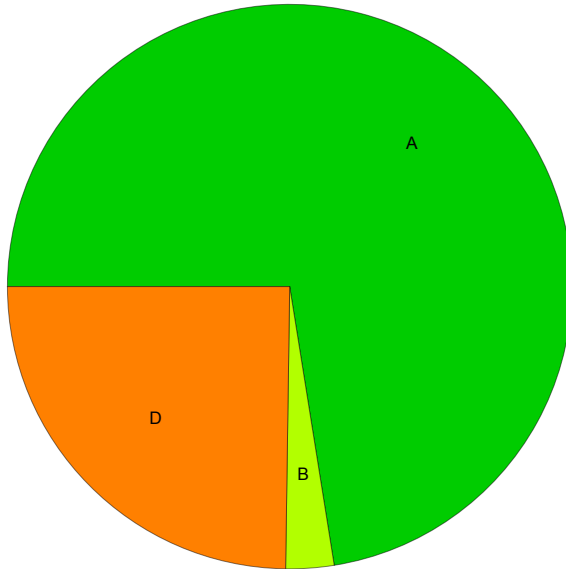
$$\begin{aligned}
& - \frac{b^3 \pi}{756 x^6} + \frac{b^7 \pi^3}{3780 x^2} - \frac{11 b^3 \pi \cos[b^2 \pi x^2]}{3024 x^6} + \frac{5 b^7 \pi^3 \cos[b^2 \pi x^2]}{2016 x^2} - \frac{b^2 \pi \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelC}[b x]}{63 x^7} + \\
& \frac{b^6 \pi^3 \cos\left[\frac{1}{2} b^2 \pi x^2\right] \text{FresnelC}[b x]}{945 x^3} + \frac{b^9 \pi^5 \text{FresnelC}[b x]^2}{1890} - \frac{\text{FresnelC}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{9 x^9} + \\
& \frac{b^4 \pi^2 \text{FresnelC}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{315 x^5} - \frac{b^8 \pi^4 \text{FresnelC}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{945 x} - \\
& \frac{b \sin[b^2 \pi x^2]}{144 x^8} + \frac{67 b^5 \pi^2 \sin[b^2 \pi x^2]}{30240 x^4} + \frac{83 b^9 \pi^4 \text{SinIntegral}[b^2 \pi x^2]}{30240}
\end{aligned}$$

Result (type 8, 22 leaves):

$$\int \frac{\text{FresnelC}[b x] \sin\left[\frac{1}{2} b^2 \pi x^2\right]}{x^{10}} dx$$

## Summary of Integration Test Results

218 integration problems



A - 158 optimal antiderivatives

B - 6 more than twice size of optimal antiderivatives

C - 0 unnecessarily complex antiderivatives

D - 54 unable to integrate problems

E - 0 integration timeouts